Precise Cosmological Constraints from BOSS Galaxy Clustering using the Wavelet Scattering Transform



Georgios Valogiannis University of Chicago

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Based on arXiv: 2310.16116, 2204.13717 & 2108.07821 in collaboration with **Cora Dvorkin & Sandy Yuan**

Background from Millennium Simulation, 2005

Challenges in the era of precision cosmology

- Large-Scale Structure (LSS) of the universe a powerful probe of fundamental physics
 - Dark energy
 - Dark matter
 - Massive neutrinos
 - Gravity
- Will soon be mapped precisely by:
 - Dark Energy Scientific Instrument (DESI)
 - V. Rubin Observatory LSST
 - Euclid
 - Nancy Grace Roman Space Telescope
 - SPHEREx
 - + Synergies with CMB
- How do we optimally extract information from the LSS??









F. Villaescusa-Navaro et al. (2019)



2-point correlation function/Power Spectrum



F. Villaescusa-Navaro et al. (2019)



Physical Information





2-point correlation function/Power Spectrum (Incomplete)





Power Spectrum information saturates in nonlinear regime. Inadequate! (Carron 2011,2012)

M. Neyrinck et al. (2009)





Power spectrum + Higher order statistics (expensive)





F. Villaescusa-

Navaro et al. (2019)



• Attempts to describe the information encoded in the 3D cosmic density field



Marked power spectrum, log. transform, skew spectrum Nearest neighbor distributions, density split, etc



Physical Information

Massara et al 2020





Power spectrum + Higher order statistics

Marked power spectrum, log. transform, skew spectrum Nearest neighbor distributions, density split, etc

Physical Information

F. Villaescusa-Navaro et al. (2019)









Artificial Intelligence (e.g. CNNs)

AI in Science The Wavelet Scattering Transform (WST)



"Scattering Network" image by G. Exarchakis (2018)



AI in Science The Wavelet Scattering Transform (WST)

Physical interpretation of WST coefficients

• $S_0 = \langle |I_0|
angle$: Mean field

•
$$S_1^{j_1,l_1} = \langle \left| I_0 \star \psi^{j_1,l_1} \right| \rangle : \sim P(k). \text{ In fact, } P(k) \longrightarrow \langle \left| I \star e^{-ikx} \right|^2 \rangle$$

• $S_2^{j_1,l_1,j_2,l_2} = \langle ||I_0 \star \psi^{j_1,l_1}| \star \psi^{j_2,l_2}| \rangle$: Non-Gaussian information (up to 2² = 4pcf, for n=2)

- Basis $S_0 + S_1 + S_2$ reflects clustering properties of target field $I_0(x)$
- Retaining all desirable properties of regular P(k) ✓ Mallat (2012)

+

- Compactness
 ✓
 (Anden & Mallat, 2011,2014, Bruna & Mallat, 2013) & Robustness/Stability
 ✓
 (Carron 2011,2012, Cheng & Menard 2021b)
- A CNN with fixed weights, but interpretable! (Bruna & Mallat 2013)
 - Performance on par with a CNN in WL applications! (Cheng et al. 2020b, Cheng & Menard 2021a)
- WST exceeds performance of traditional P(k) in 3D LSS studies (Valogiannis & Dvorkin 2022a)
 - Also overperforms marked P(k) (Massara et al., PRL 126, 011301 (2021))



WST application on weak lensing

- Fisher information obtained from 2D simulated WL shear maps
- Performance on par with a state-of-the-art CNN!





WST application on weak lensing



scattering transform power spectrum similar different input Cosmology 1 Cosmology 2 $\log k^2 P(k)$ $i_1 = 1, i_2 = 3$ Gaussian Field $j_1 = 1, j_2 = 3$ $\log k^{-1}$ $\langle I_2 \rangle_{l_1,l_2}$ I_0

Cheng et al. (2020)

non-Gaussianity increases

• WST coefficients efficiently identify non-Gaussianity in WL shear maps





• 3-dimensional WST implementation with 'solid harmonic' wavelets (Eickenberg et al. (2018))

$$S_{0} = \langle |I(\vec{x})|^{q} \rangle,$$

$$S_{1}(j_{1}, l_{1}) = \left\langle \left(\sum_{m=-l_{1}}^{m=l_{1}} |I(\vec{x}) * \psi_{j_{1}, l_{1}}^{m}(\vec{x})|^{2} \right)^{\frac{q}{2}} \right\rangle,$$

$$S_{2}(j_{2}, j_{1}, l_{1}) = \left\langle \left(\sum_{m=1}^{m=l_{1}} |U_{1}(j_{1}, l_{1})(\vec{x}) * \psi_{j_{2}, l_{1}}^{m}(\vec{x})|^{2} \right)^{\frac{q}{2}} \right\rangle$$

$$U_{1}(j_{1}, l_{1})(\mathbf{x}) = \left(\sum_{m=-l_{1}}^{m=l_{1}} |I(\mathbf{x}) * \psi_{j_{1}, l_{1}}^{m}(\mathbf{x})|^{2} \right)^{\frac{1}{2}}$$

• Implemented in KYMATIO package (Andreux et al. 2019)

$$\psi_l^m(\mathbf{x}) = \frac{1}{(2\pi)^{3/2}} e^{-|\mathbf{x}|^2/2\sigma^2} |\mathbf{x}|^l Y_l^m\left(\frac{\mathbf{x}}{|\mathbf{x}|}\right)$$

Gaussian
envelope
Solid Harmonics

• Dilated by dyadic scales 2^{j_1}

 $\psi_{j_1,l_1}^m(\mathbf{x}) = 2^{-3j_1} \psi_{l_1}^{m_1}(2^{-j_1}\mathbf{x})$

- Wavelets in the literature
 - Bump steerable wavelets (Eickenberg et al, 2022, Allys et al, 2020)
 - Morlet wavelets (Cheng et al. 2020b, Cheng & Menard 2021a)
 - Equivariant wavelets (Saydjari & Finkbeiner, 2021)



- CatSci - cutta latur
- 3-dimensional WST implementation with 'solid harmonic' wavelets (Eickenberg et al. (2018))



• Implemented in KYMATIO package (Andreux et al. 2019)



• Dilated by dyadic scales 2^{j_1}

$$\psi_{j_1,l_1}^m(\mathbf{x}) = 2^{-3j_1} \psi_{l_1}^{m_1}(2^{-j_1}\mathbf{x})$$

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 - Equivariant wavelets (Saydjari & Finkbeiner, 2021)



First WST application on 3D LSS



• First WST application on 3D matter density field! (Valogiannis & Dvorkin, 2022a)

$$I(\vec{x}) \equiv \delta_m(\vec{x}) = rac{
ho_m(\vec{x})}{ar{
ho}_m} - 1.0$$
 , resolution $N_{grid} = 256^3$

- Evaluated from the Quijote simulations (F. Villaescusa-Navaro et al., 2019)
- Fiducial cosmology

$$\Omega_{\rm m} = 0.3175, \ \Omega_{\rm b} = 0.049, \ h = 0.6711$$

 $n_s = 0.9624, \ \sigma_8 = 0.834, \ M_{\nu} = 0.0 \ {\rm eV}, \ {\rm and} \ w = -1$
Box L=1.0 Gpc/h

- In presence of massive neutrinos, trace both:
- $\delta_m = \delta_{CDM} + \delta_b + \delta_{\nu}$ Total 'm' field
- $\delta_{cb} = \delta_{CDM} + \delta_b$ 'cb' field





Fisher forecast



Fisher forecasting

- 15,000 realizations for fiducial cosmology
- 7,000 for linear derivatives in parameters

$$\begin{split} F_{\alpha\beta} &= \frac{\partial O_i}{\partial \theta_{\alpha}} C_{ij}^{-1} \frac{\partial O_j^T}{\partial \theta_{\beta}} \\ \bullet \text{ Marginalized } \sigma_{\alpha} &= \sqrt{(F^{-1})_{\alpha\alpha}} \\ \text{for } \theta_{\alpha} &= \left\{ \Omega_m, \Omega_b, H_0, n_s, \sigma_8, M_\nu \right\} \end{bmatrix} \text{, z=0} \end{split}$$

Comparing 3 observables O_i :

- Power spectrum P(k)
- Marked power spectrum M(k)
- $S_0 + S_1 + S_2 = 76$ **WST** coefficients Using J=5 scales and L=5 orientations



WST coefficients - correlation matrix Valogiannis & Dvorkin 2022a



• Marked correlation function generalizes 2-point function

Marked Power Spectrum

$$\mathcal{M}(r) = \frac{1}{n(r)\bar{m}^2} \sum_{ij} \delta_D(|\mathbf{x}_i - \mathbf{x}_j| - r) m_i m_j = \frac{1 + W(r)}{1 + \xi(r)}$$

• Each galaxy weighted by mark 'm'

AI in Science

A program of SCHMIDT FUTURES

• Inverse density weighted mark (highlights voids)

$$m[\mathbf{x}, R, \delta_s, p] = \left(\frac{1+\delta_s}{1+\delta_s+\delta_R(\mathbf{x})}\right)^R$$

- Can constrain modified gravity (M. White 2016, Valogiannis & Bean 2018, Alam et al., 2021) m(x)
- Can constrain neutrino mass (Massara et al, PRL 2020)
- Contains info beyond 2-point function (Philxcox et al., 2020)



Massara et al 2020



WST sensitivity to neutrino mass

- Raising modulus to powers q<1 emphasizes on cosmic voids (lower overdensity regions)
- Very sensitive to neutrino mass!

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$$S_{0} = \langle |I(\vec{x})|^{q} \rangle,$$

$$S_{1}(j_{1}, l_{1}) = \left\langle \left(\sum_{m=-l_{1}}^{m=l_{1}} |I(\vec{x}) * \psi_{j_{1}, l_{1}}^{m}(\vec{x})|^{2} \right)^{q} \right\rangle,$$

$$S_{2}(j_{2}, j_{1}, l_{1}) = \left\langle \left(\sum_{m=1}^{m=l_{1}} |U_{1}(j_{1}, l_{1})(\vec{x}) * \psi_{j_{2}, l_{1}}^{m}(\vec{x})|^{2} \right)^{q} \right\rangle$$

• $\underline{q=0.8}$ found to be optimal



Valogiannis & Dvorkin 2022a

AI in Science Great improvement over matter P(k)!





- WST delivers **significant** improvement in the 1- σ errors for all parameters!
- ~1.2-4x tighter errors than from 'cb' P(k)!
- Constrains on <u>neutrino mass:</u>
 - ~4x tighter than 'cb' P(k)!
 - ~1.6x tighter than 'cb' M(k)!
- ~3x100x tighter errors than from 'm' P(k)

Matter type	ʻm'			'cb'			
Statistic	P(k)	M(k)	WST	P(k)	M(k)	WST	
$\sigma(\Omega_m)$	0.076	0.013	0.014	0.040	0.016	0.016	
$\sigma(\Omega_b)$	0.033	0.010	0.012	0.015	0.009	0.012	
$\sigma(\sigma_8)$	0.01	0.002	0.001	0.067	0.026	0.017	
$\sigma(n_s)$	0.39	0.044	0.031	0.088	0.035	0.029	
$\sigma(H_0) [\mathrm{km/s/Mpc}]$	40.62	9.50	10.34	14.42	8.28	10.32	
$\sigma(M_{\nu}) [eV]$	0.72	0.016	0.008	1.17	0.45	0.29	

Valogiannis & Dvorkin 2022a



Upcoming MG application





- New WST application on MG in the works, Quijote-MG
- f(R) Hu-Sawicki model application + 6 ΛCDM
- Constrains on <u>MG parameter</u> $Y=f_{R_0}^{\log_2 10}$:
 - ~5x tighter than 'cb' P(k)!
- Follows and exceeds neutrino mass trend
 - Parallels between scale-dependent growth in both scenarios
- In collaboration with <u>Francisco Villaescusa-</u> <u>Navarro & Marco Baldi</u>

New column showing contraints on deviations from GR (Y->0)

Valogiannis et al., in prep.



Realistic galaxy survey data

However

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• We perform likelihood analysis, sampling from Gaussian likelihood

$$\log \mathcal{L}(\theta | \mathbf{d}) \propto -\frac{1}{2} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]^{\mathrm{T}} C^{-1} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]$$





- First WST application on 3D redshift-space galaxy density field! (Valogiannis & Dvorkin 2022b)
 - Working with BOSS CMASS DR12 sample at 0.46<z<0.57
 - Northern + Southern Galactic Cap
- For survey data, fundamental quantity of interest is
- the FKP field (Feldman, Kaiser, Peacock et al., 1994) :

$$F(\mathbf{r}) = \frac{w_{\text{FKP}}(\mathbf{r})}{I_2^{1/2}} \begin{bmatrix} w_c(\mathbf{r})n_g(\mathbf{r}) - \alpha_r n_s(\mathbf{r}) \end{bmatrix}$$

Galaxies Randoms

• Systematic + FKP weights

 $w_c(\mathbf{r}) = (w_{\rm rf}(\mathbf{r}) + w_{\rm fc}(\mathbf{r}) - 1.0) w_{\rm sys}(\mathbf{r})$ $w_{\rm FKP}(\mathbf{r}) = [1 + \bar{n}_g(\mathbf{r})P_0]^{-1}$

- Serves as input into WST network
 - With $N_{grid} = 270^3$ and $L_{Box} = 2700 Mpc/h$



SDSS <u>https://blog.sdss.org/</u>





• <u>Data</u>

$$\log \mathcal{L}(\theta | \mathbf{d}) \propto -\frac{1}{2} \left(\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right)^{\mathrm{T}} C^{-1} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]$$

- Use vector of WST coefficients as observable
- Extracted from BOSS CMASS FKP field, using
- J=5 scales and L=5 orientations
- $S_0 + S_1 + S_2 = 76$ WST coefficients
- Also, use galaxy 2-point correlation function multipoles $\xi_{l=0,2}(r)$ ($r_{min} = 8$ Mpc/h) as benchmark



SDSS <u>https://blog.sdss.org/</u>





• Theory model

$$\log \mathcal{L}(\theta | \mathbf{d}) \propto -\frac{1}{2} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]^{\mathrm{T}} C^{-1} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]$$

Capture cosmological dependence using

Abacus Summit simulations (Maksimova et al. 2021, Garrison et al. 2019&2021) HOD tuned to BOSS CMASS at 0.46<z<0.60 with AbacusHOD (**Yuan et al. 2021**) Box L=2000 Mpc/h, $N_{grid} = 200^3$

- Fiducial cosmology from Planck 2018 $\{\omega_b, \omega_c, n_s, \sigma_8\} = \{0.02237, 0.120, 0.9649, 0.8114\}$
- + Fixed angular size of sound horizon at last scattering. $100\theta_{\star} = 1.041533$
- + 7 HOD model parameters (vanilla HOD + velocity bias)

 $\{\alpha, \alpha_{\rm c}, \alpha_{\rm s}, \kappa, \log M_1, \log M_{\rm cut}, \sigma\} = \{0.9022, 0.2499, 1.1807, 0.3288, 14.313, 12.8881, 0.02084\}$

- We cut Abacus cubic boxes into actual CMASS geometry
 - Using 'make survey' (White et al., 2013)





















• Covariance matrix obtained from N=2048 PATCHY mocks (S. A. Rodriguez-Torres et al., 2016)

$$\log \mathcal{L}(\theta | \mathbf{d}) \propto -\frac{1}{2} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]^{\mathsf{T}} C^{-1} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]$$

-1.0 70 - 0.8 60 WST coefficient order -0.6 -0.4 -0.2 -0.0 -0.210 -0.40 50 60 70 10 20 30 40 WST coefficient order







• We perform likelihood analysis, sampling from Gaussian likelihood

$$\log \mathcal{L}(\theta | \mathbf{d}) \propto -\frac{1}{2} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]^{\mathrm{T}} C^{-1} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]$$







Hold-out tests on Abacus mocks



- Tests against out-sample test set of mocks
- Successful parameter recovery in all 40 hold-out tests!!
- Confirms tight 1- σ errors using full likelihood/MCMC!
- Marginalized over 7 HOD nuisance parameters
- In agreement with conclusions of (Valogiannis & Dvorkin, 2022b) !

Example of successful parameter recovery from a test mock with low σ_8



AI in Science A program of SCHMIDT FUTURES

Hold-out tests on Abacus mocks











AI in Science A program of SCHMIDT FUTURES Hold-out tests on external Uchuu mock









WST Constraints from BOSS CMASS data!



	2-point c.f.		WST		Joint 2-point c.f.+WST	
	Best-fit	$Mean \pm \sigma$	Best-fit	$Mean \pm \sigma$	Best-fit	$Mean \pm \sigma$
ω_b	0.02261	$0.02270^{+0.00037}_{-0.00037}$	0.02274	$0.02277^{+0.00038}_{-0.00038}$	0.0225	$0.02262^{+0.00029}_{-0.00029}$
ω_c	0.1201	$0.1222^{+0.0040}_{-0.0063}$	0.1239	$0.1244_{-0.0015}^{+0.0015}$	0.1238	$0.1241^{+0.0011}_{-0.0011}$
n_s	0.925	$0.922_{-0.037}^{+0.037}$	0.961	$0.951^{+0.023}_{-0.023}$	0.927	$0.924_{-0.01}^{+0.01}$
σ_8	0.742	$0.746^{+0.051}_{-0.051}$	0.860	$0.834_{-0.039}^{+0.058}$	0.793	$0.795^{+0.019}_{-0.019}$
h	0.677	$0.677^{+0.022}_{-0.015}$	0.67	$0.669^{+0.0059}_{-0.0059}$	0.668	$0.669^{+0.0049}_{-0.0049}$

- WST 1 σ errors on $\omega_c \& n_s$ 4.2x & 1.6x tighter than $\xi(r)$
- Joint WST+ξ(r) analysis improves 1σ errors by 2.5-6x compared to ξ(r)-only!
- Joint WST+ ξ (r) analysis improves 1 σ errors by 1.4-2.5x compared to WST-only
- Competitive 0.9%, 2.3% & 1% determination of ω_c , σ_8 & n_s
- 0.7% determination of H_0 , as a derived parameter from fixed θ_*



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Competitive Constraints on Structure Growth!







WST Constraints from BOSS CMASS data!



	2-point c.f.		WST		Joint 2-point c.f.+WST		
	Best-fit	$\mathrm{Mean} \pm \sigma$	Best-fit	$Mean \pm \sigma$	Best-fit	$Mean \pm \sigma$	
ω_b	0.02261	$0.02270\substack{+0.00037\\-0.00037}$	0.02274	$0.02277\substack{+0.00038\\-0.00038}$	0.0225	$0.02262^{+0.00029}_{-0.00029}$	
ω_c	0.1201	$0.1222^{+0.0040}_{-0.0063}$	0.1239	$0.1244_{-0.0015}^{+0.0015}$	0.1238	$0.1241\substack{+0.0011\\-0.0011}$	
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h	0.677	$0.677^{+0.022}_{-0.015}$	0.67	$0.669^{+0.0059}_{-0.0059}$	0.668	$0.669^{+0.0049}_{-0.0049}$	





Constraints on ACDM extensions



- Joint WST+ $\xi(r)$ analysis allows simultaneous constraints on 4 extensions to ΛCDM
- 1σ consistency with Λ CDM limits

$$w_0 = -1, w_a = 0, a_{\text{run}} = 0, N_{\text{eff}} = 3.046$$

	Joint 2-p	Joint 2-point c.f.+WST				
	Best-fit	$Mean \pm \sigma$				
ω_b	0.02280	$0.02273^{+0.00036}_{-0.00036}$				
ω_c	0.1227	$0.1239^{+0.0056}_{-0.0056}$				
σ_8	0.748	$0.751_{-0.040}^{+0.034}$				
n_s	0.928	$0.953^{+0.022}_{-0.030}$				
h	0.675	$0.671^{+0.021}_{-0.021}$				
$a_{ m run}$	0.002	$0.004\substack{+0.019\\-0.012}$				
$N_{ m eff}$	3.048	$3.23_{-0.26}^{+0.26}$				
w_0	-1.039	$-0.995^{+0.061}_{-0.073}$				
w_a	0.29	$0.17^{+0.24}_{-0.21}$				



WST Constraints from DESI Y1 data!





Dark Energy Spectroscopic Instrument (DESI)

Alternative Summary Statistics in DESI

- Wavelet scattering transform
- Void-galaxy cross-correlation function
- DT spheres/voids
- Void size function
- kNN statistics
- Lensing Cumulants
- Minkowski functionals
- Density-split clustering
- Linear point distance scale
- Void lensing
 Etc



Two-point correlation functions of DESI tracers from DESI Y1 blinded catalogs (without reconstruction). The circle indicates the location of the BAO features. (Credits to by Ashley Ross & DESI collaboration)







- <u>Wavelet Scattering Transform</u>: a novel statistic that efficiently extracts non-Gaussian information from physical fields. *Ideal* middle ground between CNN and traditional estimators
- First WST application to actual spectroscopic data (Valogiannis et al., 2023, <u>arXiv: 2310.16116</u>, Valogiannis & Dvorkin, <u>arXiv: 2204.13717</u>, <u>Phys. Rev. D 105, 103534</u>, 2022)
 - Worked with BOSS CMASS galaxy sample at 0.46<z<0.57
 - Substantial improvement in the 1σ errors over traditional galaxy $\xi(r)$ multipoles
- Ongoing & future improvements (in progress)
 - Can more accurately capture lightcone evolution, fiber collision/systematic effects in galaxy mocks (Eg. see Yuan et al. 2022c)
 - Design wavelets tailored for cosmological/RSD applications (public package under construction!)
 - Blind mock challenges
- Future applications
 - Application to DESI Project #255 (& Euclid)
 - Constrain neutrino mass (Eg. as in Valogiannis & Dvorkin, <u>arXiv: 2108.07821</u>, <u>Phys. Rev. D 105, 103534</u>, 2022)
 - Constrain fundamental physics (theories of gravity, primordial non-Gaussianity, parity violation)
 - Weak lensing & cross-correlations (DES, future applications to Rubin LSST & Euclid, DESI-II)
 - Recent applications also to Lyman-a, 21cm cosmology, axion string-induced effects





2.0

1.5

0.5

0.0

0

20

<u>|</u>θ^{emn}| 1.0

WST emulator



- Quantify emulator error using test Abacus mocks •
 - Test c001-c004 cosmologies
 - 1000 hod configurations for each, 4x1000=4000 test mocks
- Obtain total WST covariance





modeled fields with high order statistics (800 steps)









modeled fields with scattering statistics (200 steps)













Cheng et al. (2023)





• WST coefficients can also be used to generate fields with similar properties/texture



Weak Lensing map

Cheng & Benard (2021a)





• Application to various physical fields



Input

Generated

Cheng et al. (2023)





• Application to various physical fields





Generated



Cheng & Benard (2021b)



Constraints on full set of parameters, including HOD

- WST able to constrain HOD parameters
- Evidence of non-zero velocity bias

 α_s

	WST		Joint 2-point c.f.+WST		
	Best-fit	$\mathrm{Mean} \pm \sigma$	Best-fit	$Mean \pm \sigma$	
$\log M_{\rm cut}$	12.681	$12.668^{+0.068}_{-0.068}$	12.608	$12.613_{-0.060}^{+0.045}$	
$\log M_1$	13.34	$13.33_{-0.13}^{+0.13}$	13.252	$13.25^{+0.11}_{-0.11}$	
$\log \sigma$	-0.783	$-0.823^{+0.11}_{-0.097}$	-0.829	$-0.87^{+0.25}_{-0.25}$	
α	0.921	$0.934_{-0.054}^{+0.064}$	0.943	$0.944_{-0.049}^{+0.077}$	
κ	1.336	$1.36^{+0.32}_{-0.32}$	1.236	$1.22^{+0.28}_{-0.28}$	
$lpha_{ m c}$	0.322	$0.34_{-0.20}^{+0.17}$	0.367	$0.32^{+0.16}_{-0.22}$	
$lpha_{ m s}$	0.306	$0.32^{+0.12}_{-0.11}$	0.411	$0.408\substack{+0.099\\-0.049}$	





WST Constraints from BOSS CMASS data!







• Covariance matrix obtained from N=2048 PATCHY mocks (S. A. Rodriguez-Torres et al., 2016)











- Addition of emulator error increases 1σ errors disproportionally for WST (vs ξ(r))
- In some cases (e.g. σ_8) this effect almost completely masks the gains compared to $\xi(\mathbf{r})$



Impact of ω_b prior





• Joint analysis results robust against choice of ω_b prior !



Sensitivity to small scales









Effect of n(z) on wst estimator



- BOSS CMASS sample has varied n(z)
- Clustering approximated using Abacus mock of constant $n(z) = 2.9x10^{-4} \frac{h^3}{Mpc^3}$.
- Good enough approximation for 2-point function Yuan et al., 2022b)
- Not sure for WST, density-dependent/field-level statistic
- Downsample to match constant $n(z) = 2.9 \times 10^{-4} \frac{h^3}{Mpc^3}$









• <u>Theory model</u>

$$\log \mathcal{L}(\theta | \mathbf{d}) \propto -\frac{1}{2} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]^{\mathrm{T}} C^{-1} \left[\mathbf{X}_{\mathbf{d}} - \mathbf{X}_{t}(\theta) \right]$$

• To model WST (and P(k)) cosmological dependence, we use the approximation:

$\mathbf{X}_t(\theta) = \mathbf{X}_t(\theta_{\text{fid}}) + (\theta - \theta_{\text{fid}}) \nabla_{\theta} \mathbf{X}$			ω_c	n_s	σ_8
4		0.02237	0.1200	0.9649	0.8114
Prediction for fiducial	Constructed from 'Linear derivative grid' of cosmologies	0.02282	0.1200	0.9649	0.8114
cosmology		0.02193	0.1200	0.9649	0.8114
		0.02237	0.1240	0.9649	0.8114
 + Additional derivative steps in the 7 HOD parameters 			0.1161	0.9649	0.8114
			0.1200	1.0249	0.8114
			0.1200	0.9049	0.8114
			0.1200	0.9649	0.8698
	Valogiannis & Dvorkin 2022k	0.02237	0.1200	0.9649	0.7532



Physical explanation of results

Why does the WST work so well??

WST key physical properties

- Successive WST layers pick up information >2-point function
 - Known to encode additional information (eg. Hahn et al. 2020 & 2021)
 - +
- Choice of q<1 highlights cosmic voids (under-densities)
 - Sensitive cosmological probe (eg. Massara et al, 2020)

Enhanced cosmological information

• Parallels to marked M(k) (Massara et al, 2020)



Convergence



Valogiannis & Dvorkin 2022



Advantages of low-order statistics



moment approach: amplifying the tail



Cheng & Menard, 2021



Localized Wavelets



Cheng & Menard, 2021