

# The Impact of Galaxy Formation on Galaxy Biasing, and Informative Priors for Primordial non-Gaussianity Constraints

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[arxiv.org/abs/2602.04987](https://arxiv.org/abs/2602.04987)




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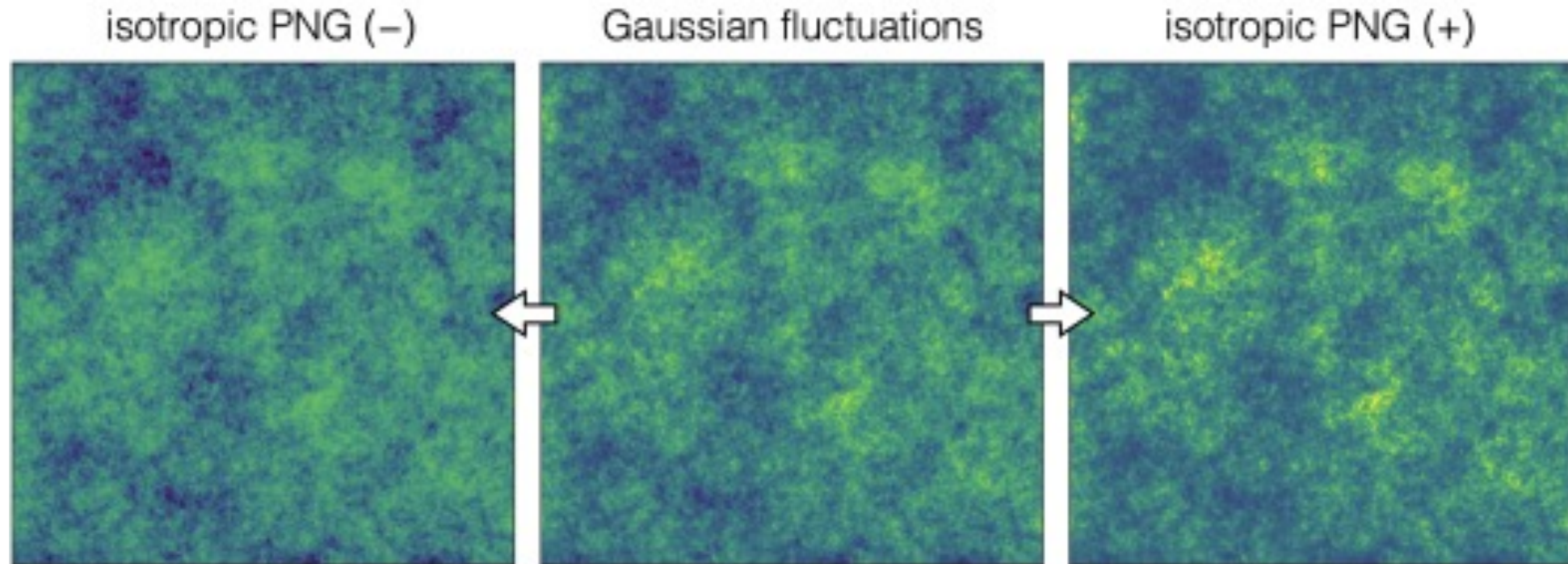
better galaxies =  
better cosmology

# How non-Gaussian were the primordial energy fluctuations? How did inflation occur?

Single-field inflation:  $\phi = \phi_G$



Not single-field inflation:  $\phi \stackrel{L.O.}{=} \phi_G + f_{NL}(\phi_G^2 - \langle \phi_G \rangle^2)$

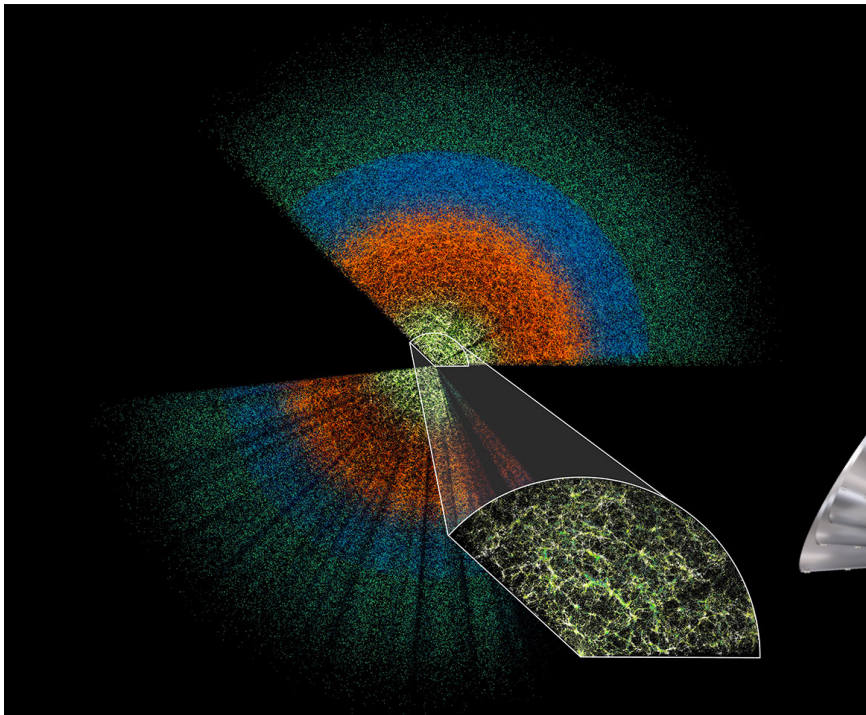
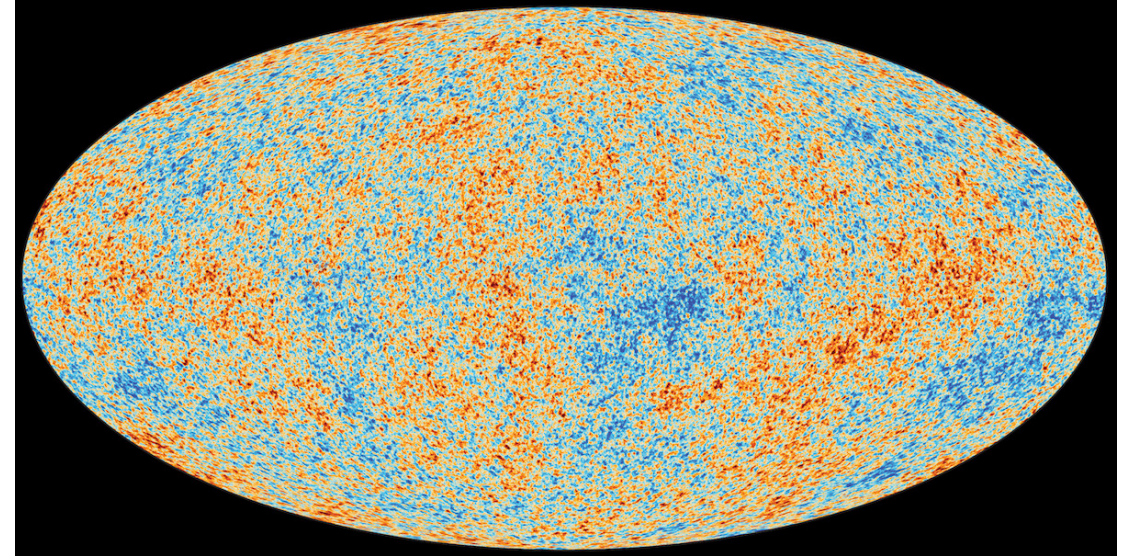


# $f_{NL}$ measures local primordial non-Gaussianity

Measuring non-zero  $f_{NL}$  helps constrain the process of inflation

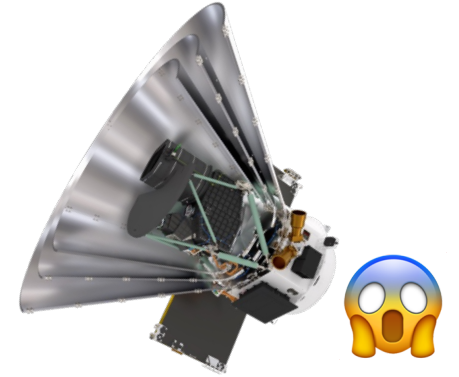
$$f_{NL} = -0.9 \pm 5.1 \text{ (68\%)}$$

but I can't go past  $k \sim 0.05 \text{ h}^{-1} \text{ Mpc}$   
and I'm nearing my cosmic  
variance limit ☹️



That's okay—I'll use galaxy  
clustering past  $k > 0.3 \text{ h}^{-1} \text{ Mpc}$   
and reduce that error bar to  
within  $\pm 1$ !

$f_{\text{NL}}$  is completely degenerate with galaxy bias parameters in analyses of galaxy clustering!



$$\delta_g(\vec{k}, z) \stackrel{\text{l.o.}}{=} b_1(z) \delta_m(\vec{k}, z) + b_\phi(z) f_{\text{NL}}^{\text{loc}} \phi(\vec{k}, z) + \epsilon(z)$$

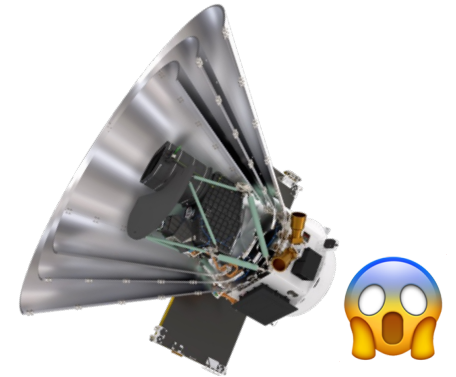
galaxy density contrast

matter density contrast

primordial gravitational potential

random noise

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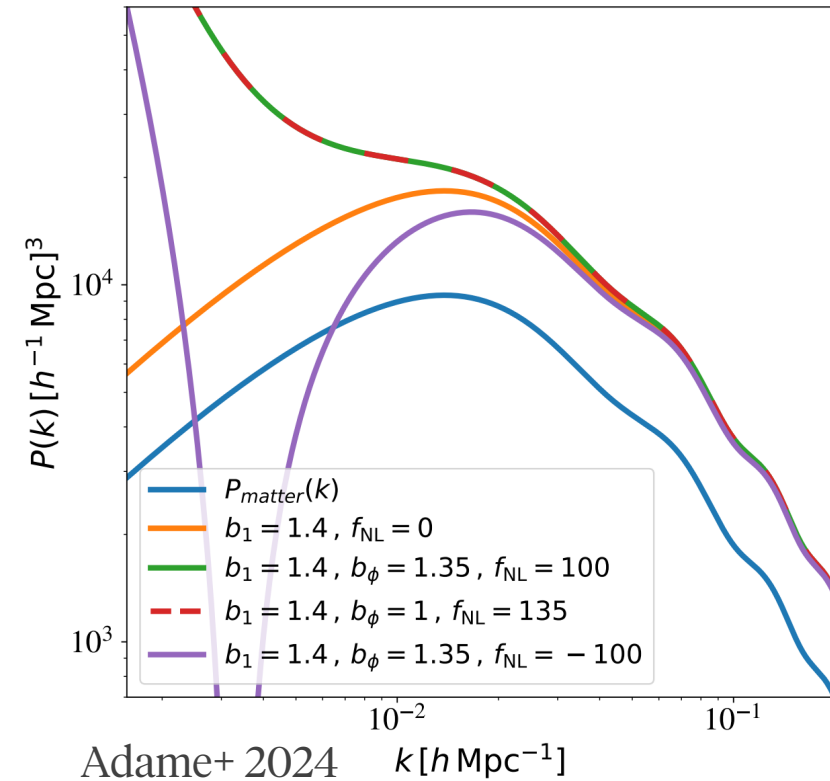
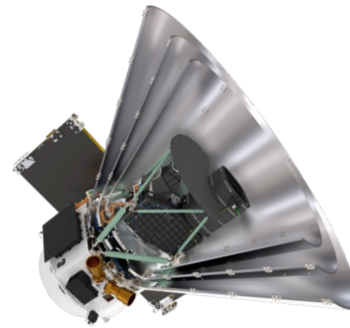
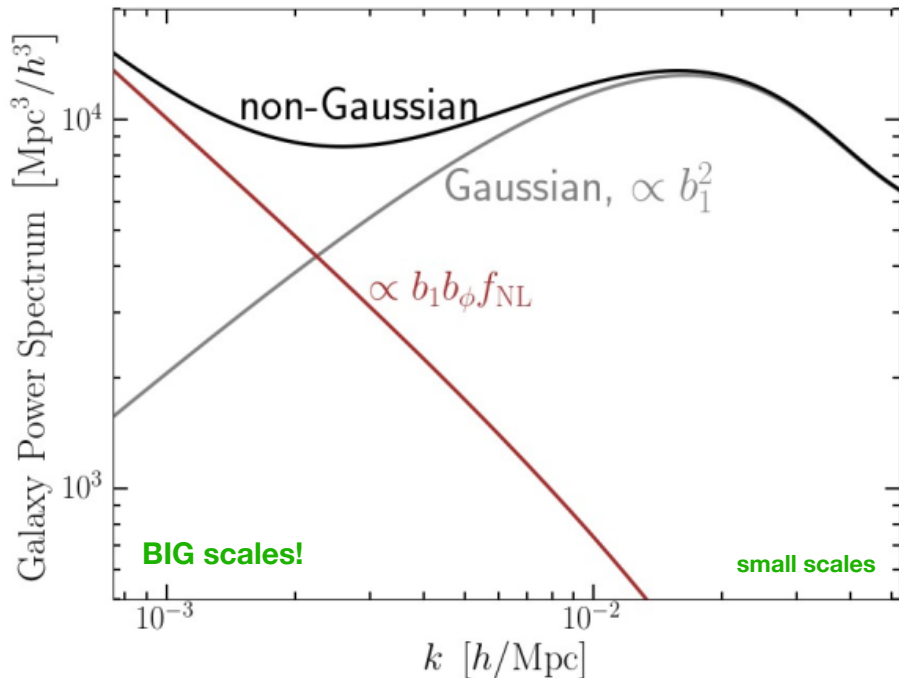
galaxy density contrast      matter density contrast      primordial gravitational potential      random noise

$$\hookrightarrow \delta_g(\vec{k}, z) \equiv \frac{n_g(\vec{k}, z)}{\bar{n}_g(\vec{k}, z)} - 1; \quad \frac{\text{local mean}}{\text{comoving galaxy densities}}$$

# $f_{\text{NL}}$ is completely degenerate with galaxy bias parameters in analyses of galaxy clustering!

$$P_{gg}(\vec{k}, z) \stackrel{\text{L.O.}}{=} P_{mm}(\vec{k}, z) \left\{ b_1^2 + \frac{2b_1 b_\phi f_{\text{NL}}}{\mathcal{M}(\vec{k}, z)} + \frac{b_\phi^2 f_{\text{NL}}^2}{\mathcal{M}(\vec{k}, z)^2} \right\} + P_{\epsilon\epsilon}$$

galaxy power spectrum      matter power spectrum



Can we get around the degeneracy of  $b_1$   $b_\phi$   $f_{\text{NL}}$  ? 

Let's try what works for halos:

“universality relation”

$$b_\phi(z) = 2\delta_c ( b_1(z) - 1 )$$

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*Issue 1:* not perfect for simulated halos

*Issue 2:* priors on  $b_1$  and  $b_\phi$  are supremely important for your final  $f_{\text{NL}}$  constraint

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## Can we actually constrain $f_{\text{NL}}$ using the scale-dependent bias effect?

An illustration of the impact of galaxy bias uncertainties using the BOSS DR12 galaxy power spectrum

Alexandre Barreira<sup>a,b</sup>

<sup>a</sup>Excellence Cluster ORIGINS, Boltzmannstraße 2, 85748 Garching, Germany

<sup>b</sup>Ludwig-Maximilians-Universität, Schellingstraße 4, 80799 München, Germany

Same BOSS galaxy data,  
different priors for  $b_\phi$  and  $b_1$

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$$f_{\text{NL}} = 16 \pm 16 \text{ or}$$

$$f_{\text{NL}} = 230 \pm 226$$

# Can we get around the degeneracy of $b_1$ $b_\phi$ $f_{NL}$ ?



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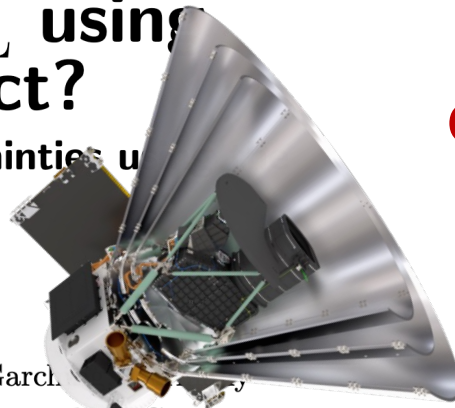
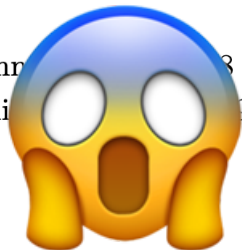
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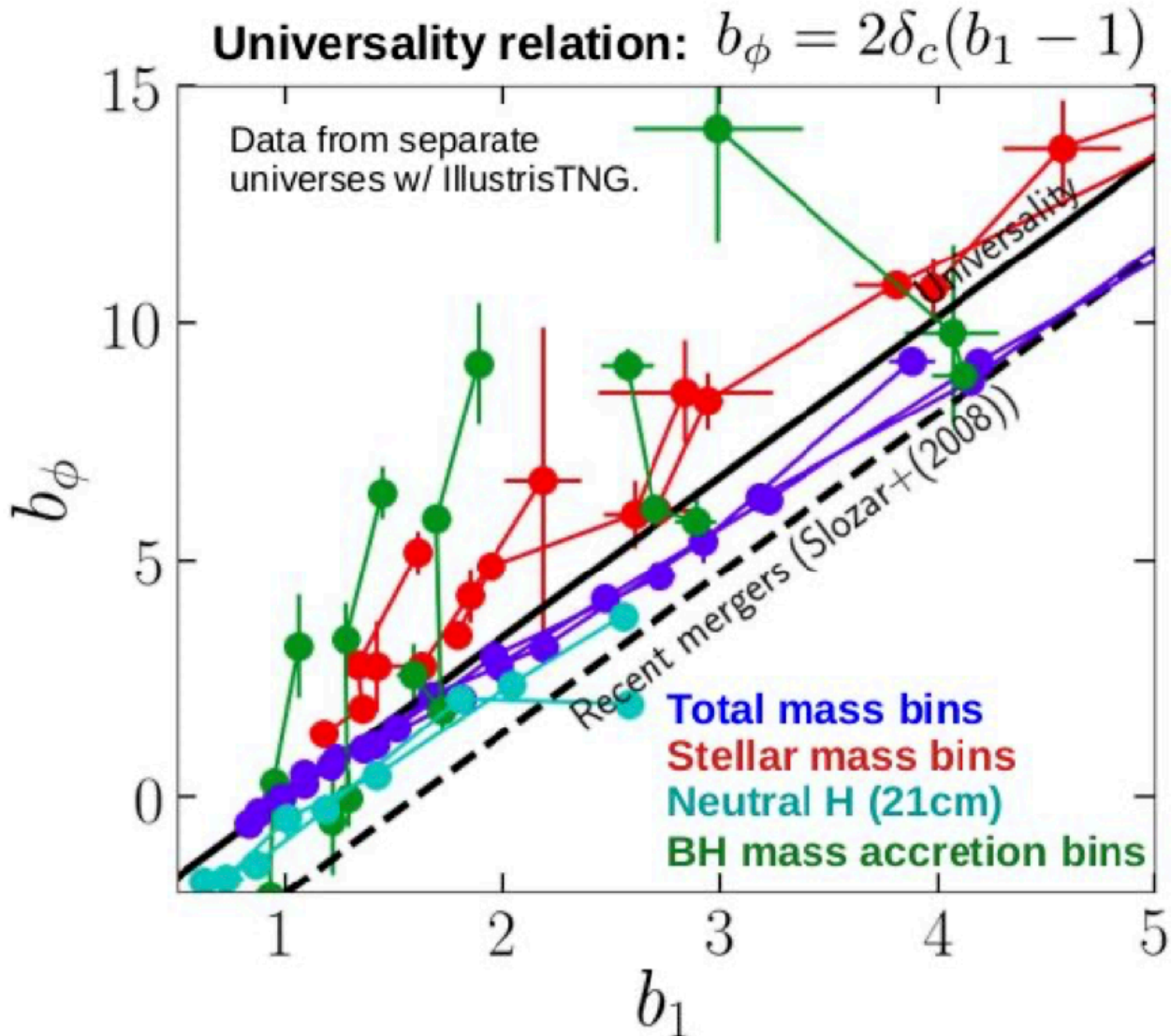


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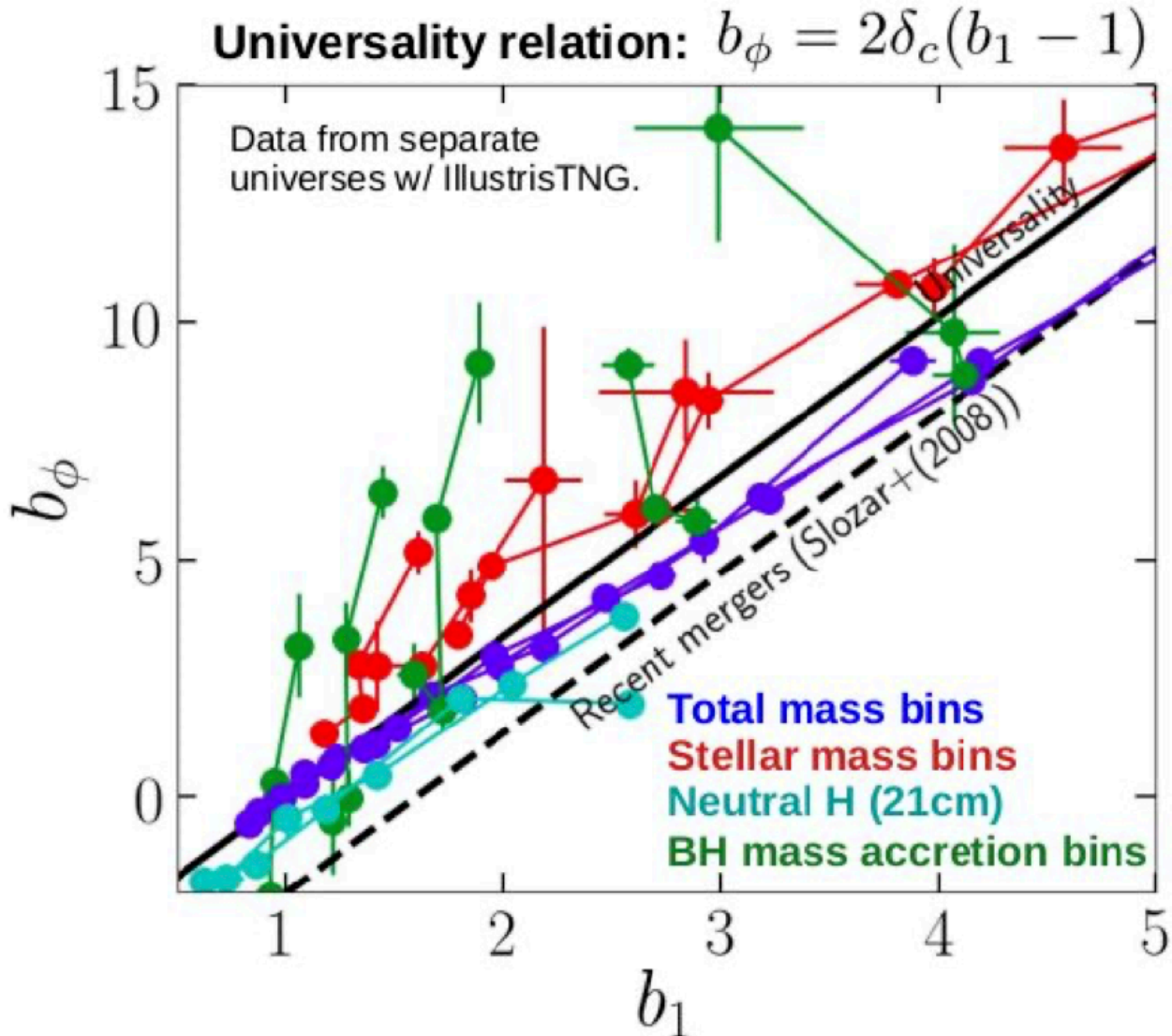


$$f_{NL} = 16 \pm 16 \text{ or}$$
$$f_{NL} = 230 \pm 226$$

# Can galaxy simulations help?



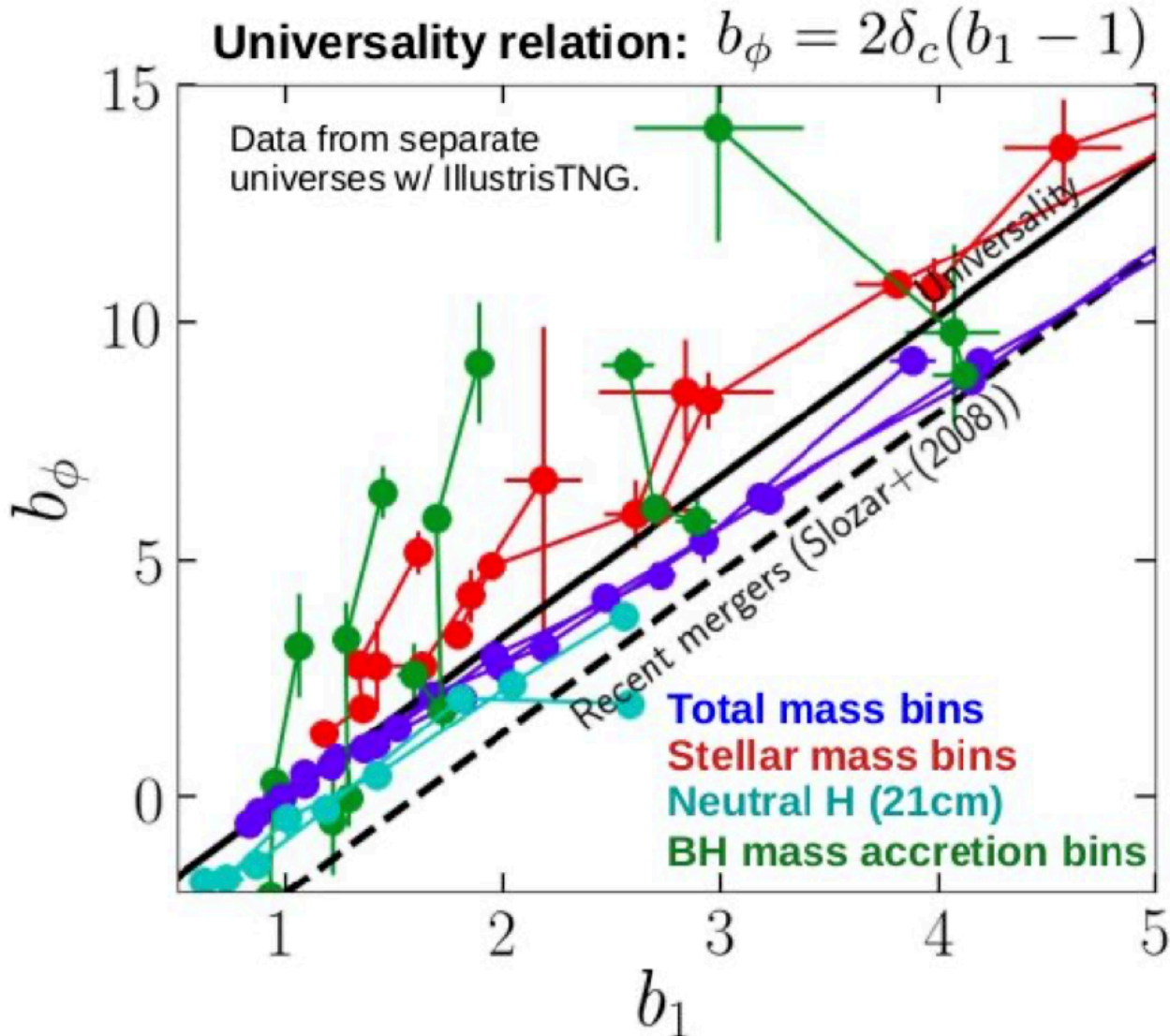
# Can galaxy simulations help?



What about different parameters within the same galaxy model?

What about other galaxy models?

# Can galaxy simulations help?



What about different parameters within the same galaxy model?

What about other galaxy models?

*How much better could our cosmology be if we quantify our ignorance around galaxy formation?*

# Let's pin down $b_\phi$ with the Santa Cruz Semi-Analytic Model for Galaxy Formation

Separate Universe  
simulations to  
measure  $b_\phi$

$(205 h^{-1} \text{cMpc})^3$ ,  $N=1280^3$ , same  
initial conditions, different  $\sigma_8$



Several dozen unique  
runs of the SC-SAM

Vary 3 parameters for SN & AGN  
feedback (see Perez, Genel, + 2023)

# Separate Universes method for measuring galaxy bias

$$\delta_g(\vec{k}, z) \stackrel{\text{l.o.}}{=} \underbrace{b_1(z)}_{\text{red wavy}} \delta_m(\vec{k}, z) + \underbrace{b_\phi(z)}_{\text{blue wavy}} \underbrace{f_{NL}^{\text{loc}}}_{\text{yellow}} \phi(\vec{k}, z)$$

$$\hookrightarrow \delta_g(\vec{k}, z) \equiv \frac{n_g(\vec{k}, z)}{\bar{n}_g(\vec{k}, z)} - 1; \quad \begin{array}{l} \text{local} \\ \text{mean} \end{array} \begin{array}{l} \text{comoving galaxy} \\ \text{densities} \end{array}$$

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*The local structure formation response to long-wavelength perturbations is equivalent to structure formation in a different cosmology*

# Separate Universes method for measuring galaxy bias

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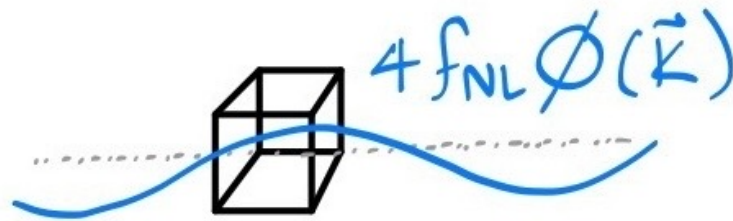
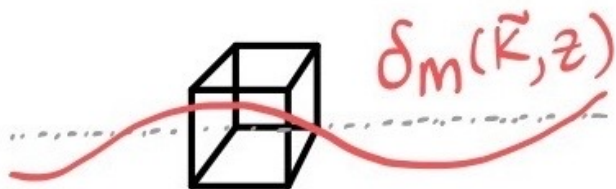
$$b_{\perp} \equiv \frac{d \ln(n_g(z))}{d \delta_L(z)}$$

$$b_{\phi} \equiv 4 \frac{d \ln(n_g(z))}{d \delta_{As}}$$

The local structure formation response to long-wavelength perturbations is equivalent to structure formation in a different cosmology

Bias  $\rightarrow$  the response of galaxy density to a different cosmology!

a.k.a. "Separate Universes"  
(from the peak background split)



# Let's pin down $b_\phi$ with the Santa Cruz Semi-Analytic Model for Galaxy Formation

Separate Universe simulations to measure  $b_\phi$

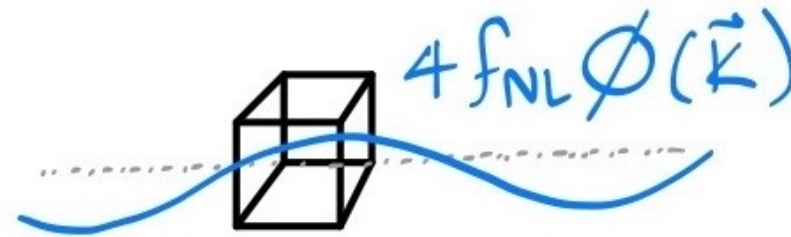
$(205 h^{-1} \text{cMpc})^3$ ,  $N=1280^3$ , same initial conditions, different  $\sigma_8$



Several dozen unique runs of the SC-SAM

Vary 3 parameters for SN & AGN feedback (see Perez, Genel, + 2023)

$$b_\phi \equiv 4 \frac{d \ln (n_g(z))}{d \delta A_s} \rightarrow 4 f_{\text{NL}} \phi_L$$



$b_\phi \rightarrow$  how galaxy counts/density respond to changing the primordial power spectrum ( $A_s$  or  $\sigma_8$ )

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$$\dot{m}_{\text{out}} = \epsilon_{\text{SN}} \left( \frac{V_0}{V_c} \right)^{\alpha_{\text{rh}}} \dot{m}_* + A_{\text{SN2}}$$

- ↑ mass outflow rate due to SN & massive stars
- ↓ mass ejected by an AGN in radio jets

$$\dot{m}_{\text{radio}} = \kappa_{\text{radio}} \left[ \frac{kT}{\Lambda(T, Z_h)} \right] \left( \frac{M_{\text{BH}}}{10^8 M_\odot} \right)$$

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Understand how  $b_\phi$  and  $b_\phi (b_1)$  varies  
with galaxy selection across  
different parametrizations of one  
galaxy formation model

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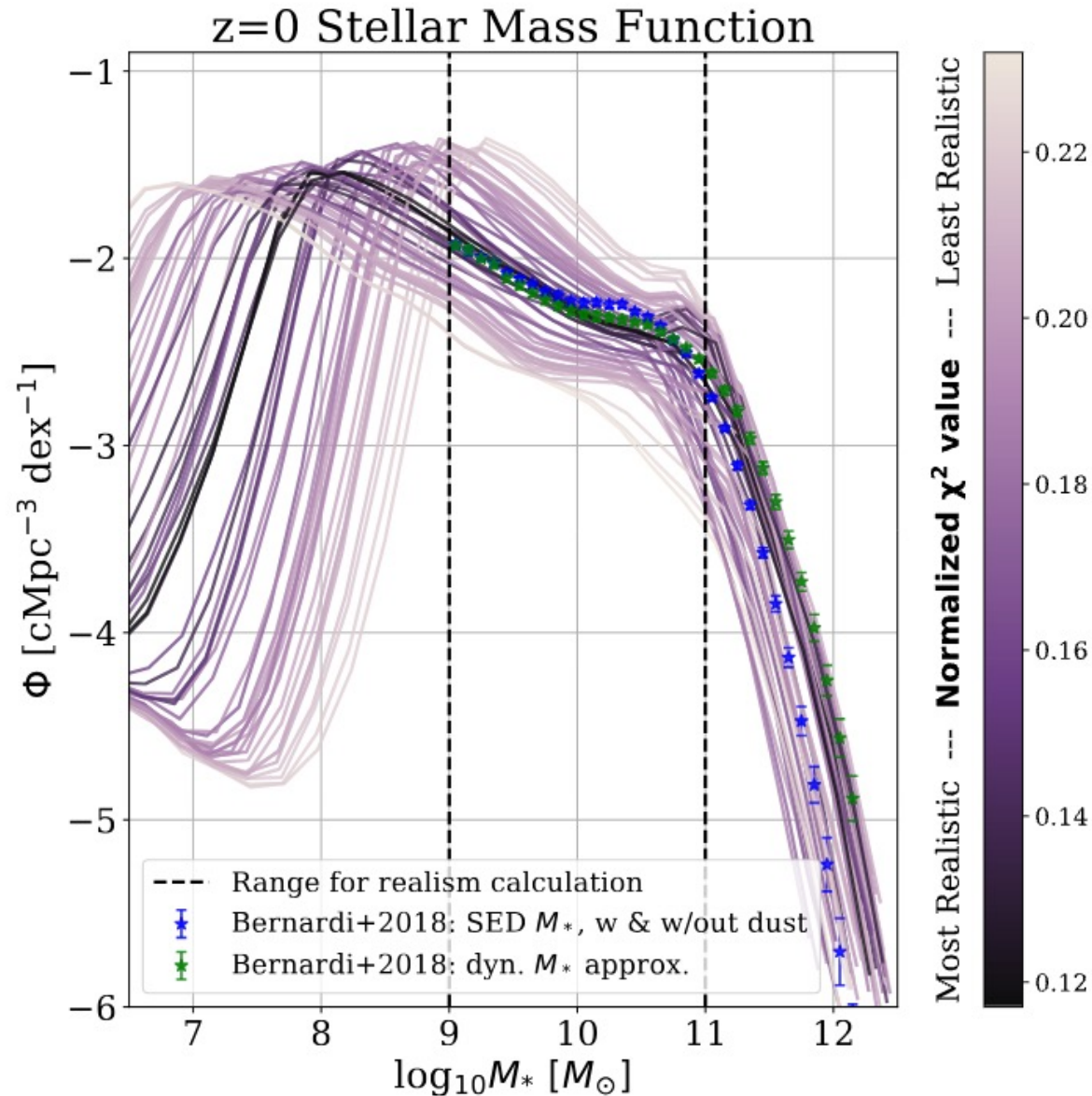


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Do we agree with the IllustrisTNG findings, and  
the few others measured for SAMs? Let's get  
physically-motivated  $b_\phi$  priors for  $f_{\text{NL}}$  analyses?

# How “realistic” is a given SAM parametrization?



Here, we compare to z=0 stellar mass function between  $9 < \log_{10}(M_{\text{star}}) < 11$

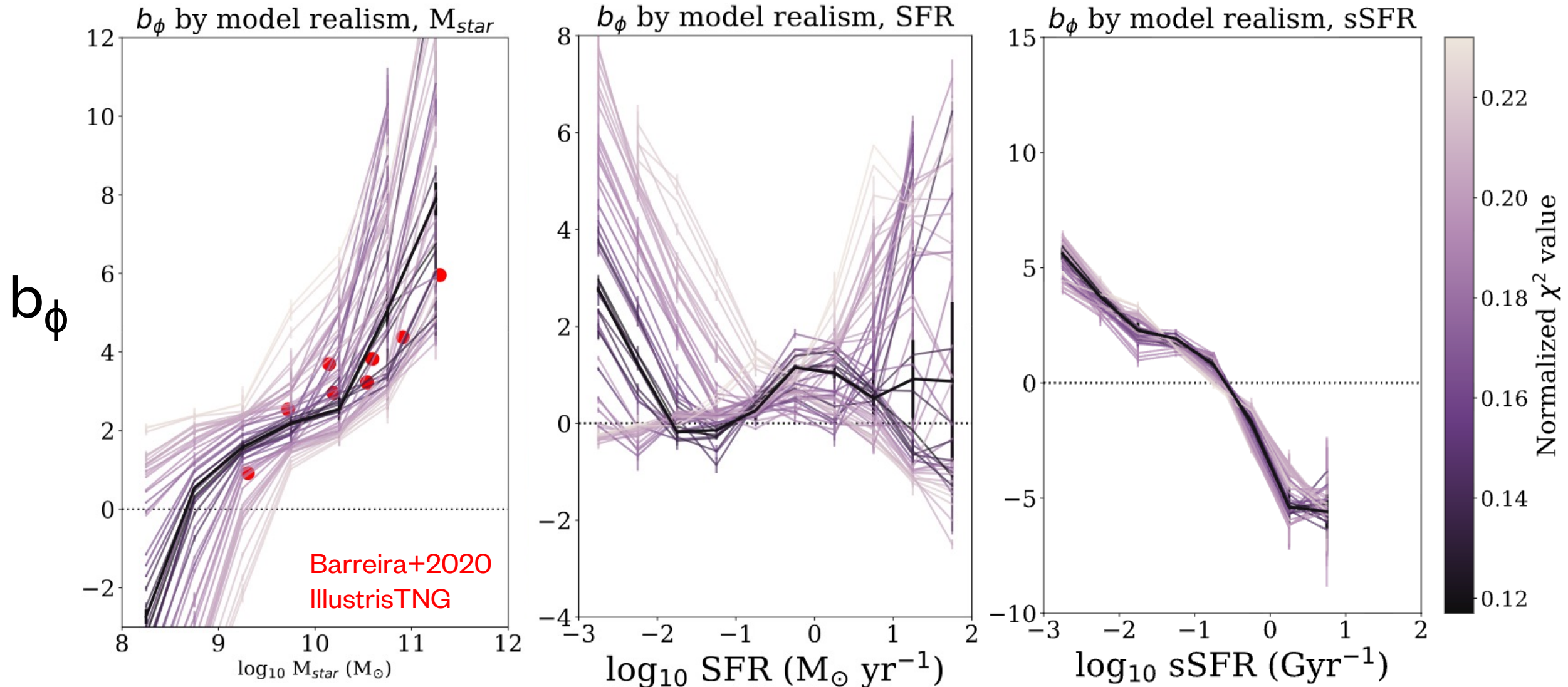
Light- to-stellar mass is hard science

Black → beige is most to least ‘realistic’

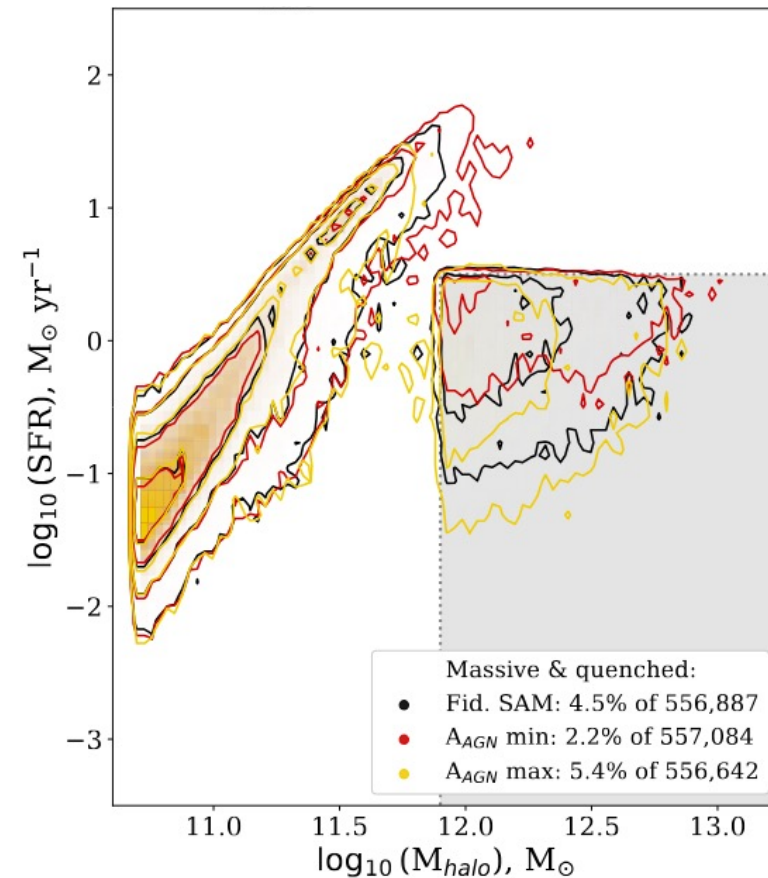
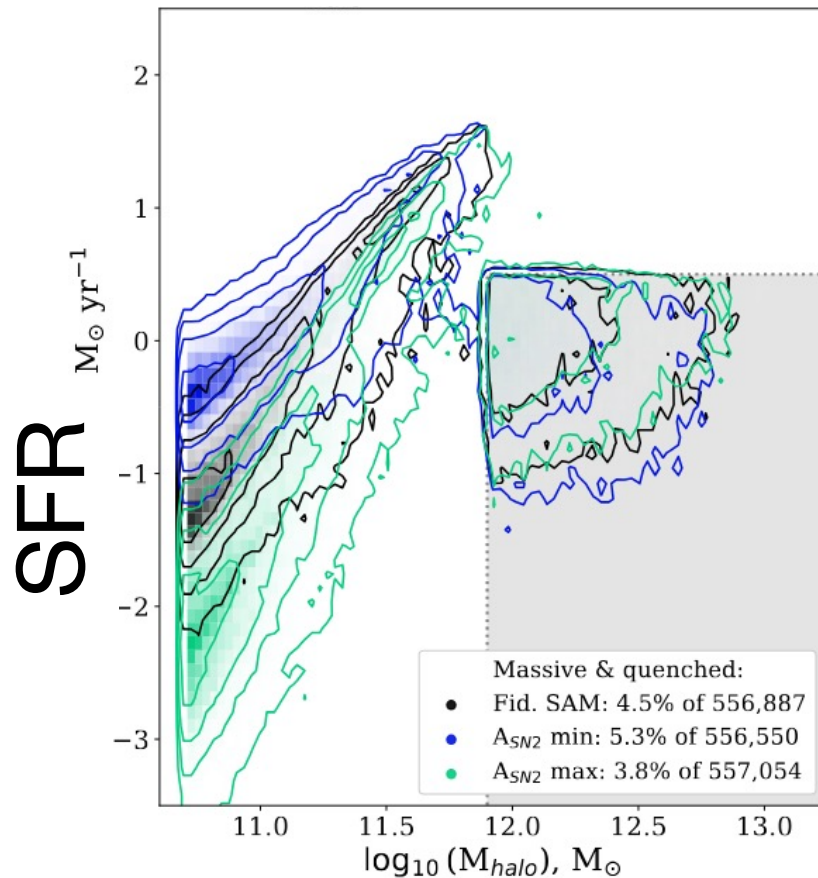
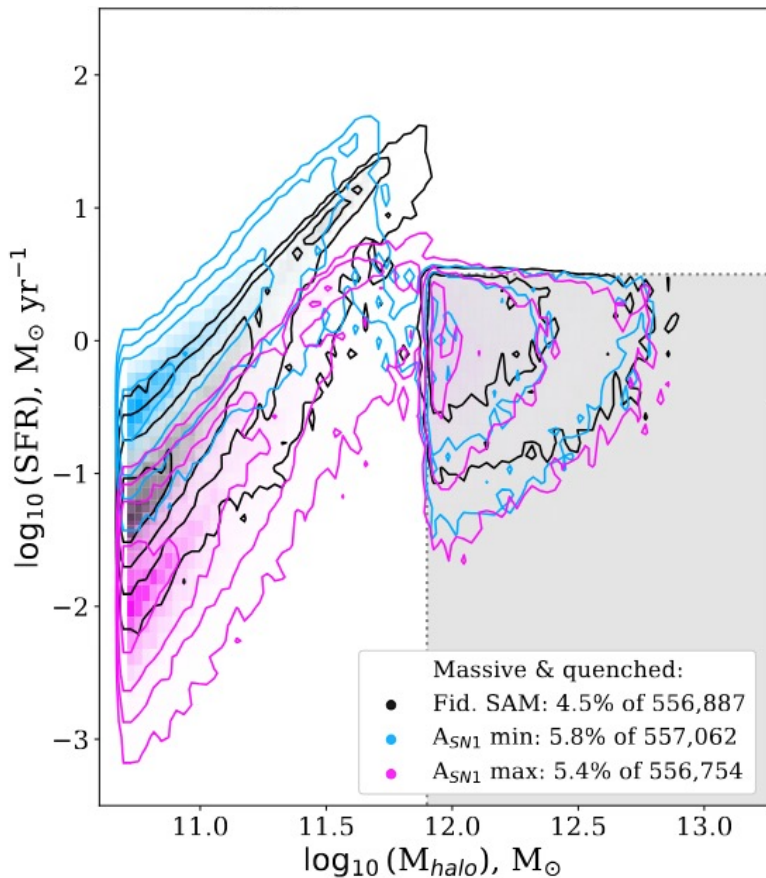
Even extreme parameters can yield realistic SMFs in unique combinations!

# $b_\phi$ different galaxy selections, $z=1$

$b_\phi \rightarrow$  how galaxy counts/density respond to changing the primordial power spectrum ( $A_s$  or  $\sigma_8$ )



# Why? The galaxy-halo connection!



## Halo Mass

$$\dot{m}_{\text{out}} = \epsilon_{\text{SN}} \left( \frac{V_0}{V_c} \right)^{\alpha_{\text{rh}}} \dot{m}_* + A_{\text{SN2}}$$

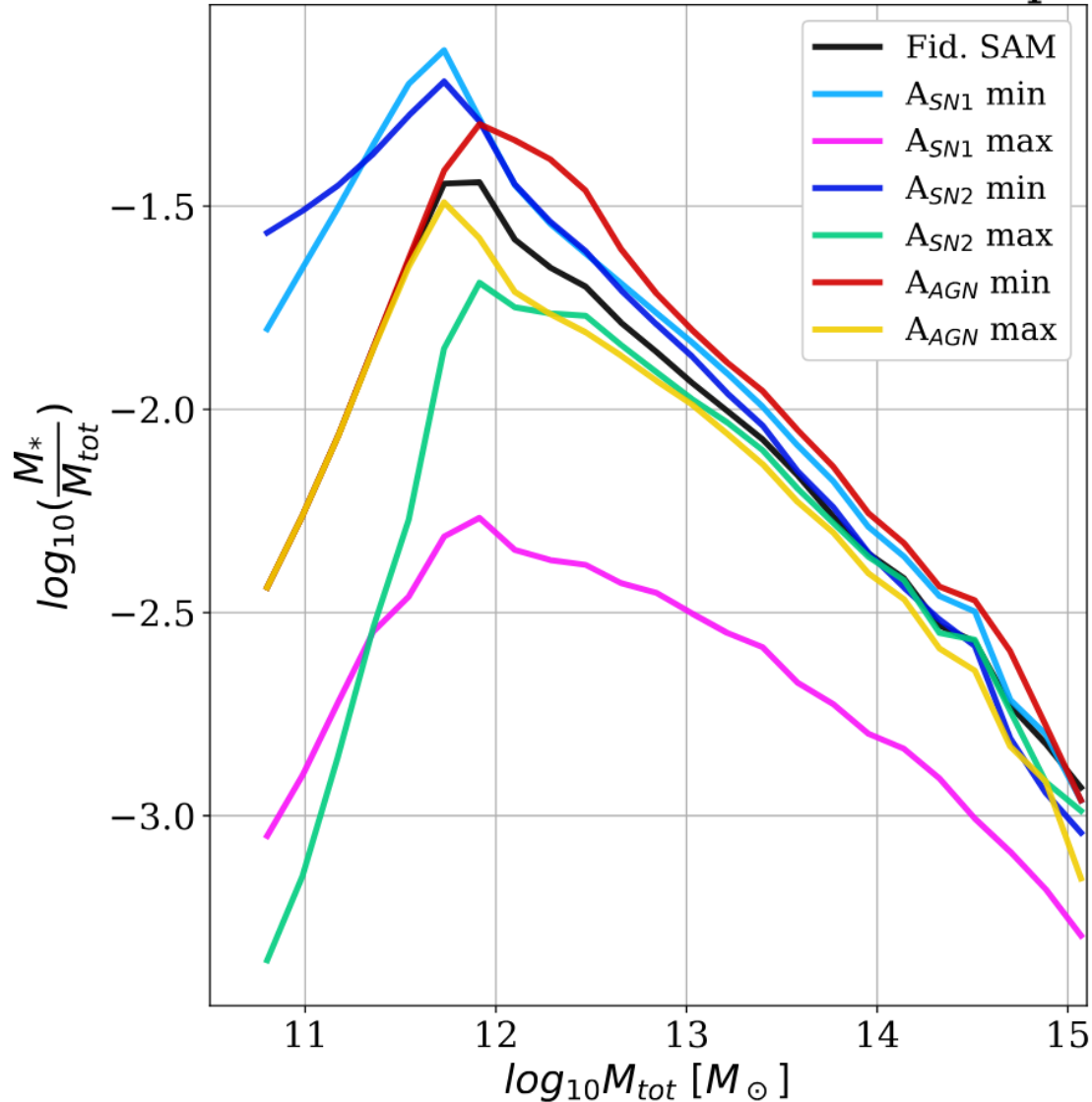
↑ mass outflow rate due to SN & massive stars

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$$\dot{m}_{\text{radio}} = \kappa_{\text{radio}} \left[ \frac{kT}{\Lambda(T, Z_h)} \right] \left( \frac{M_{\text{BH}}}{10^8 M_{\odot}} \right)$$

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Stellar-Halo Mass Relationship



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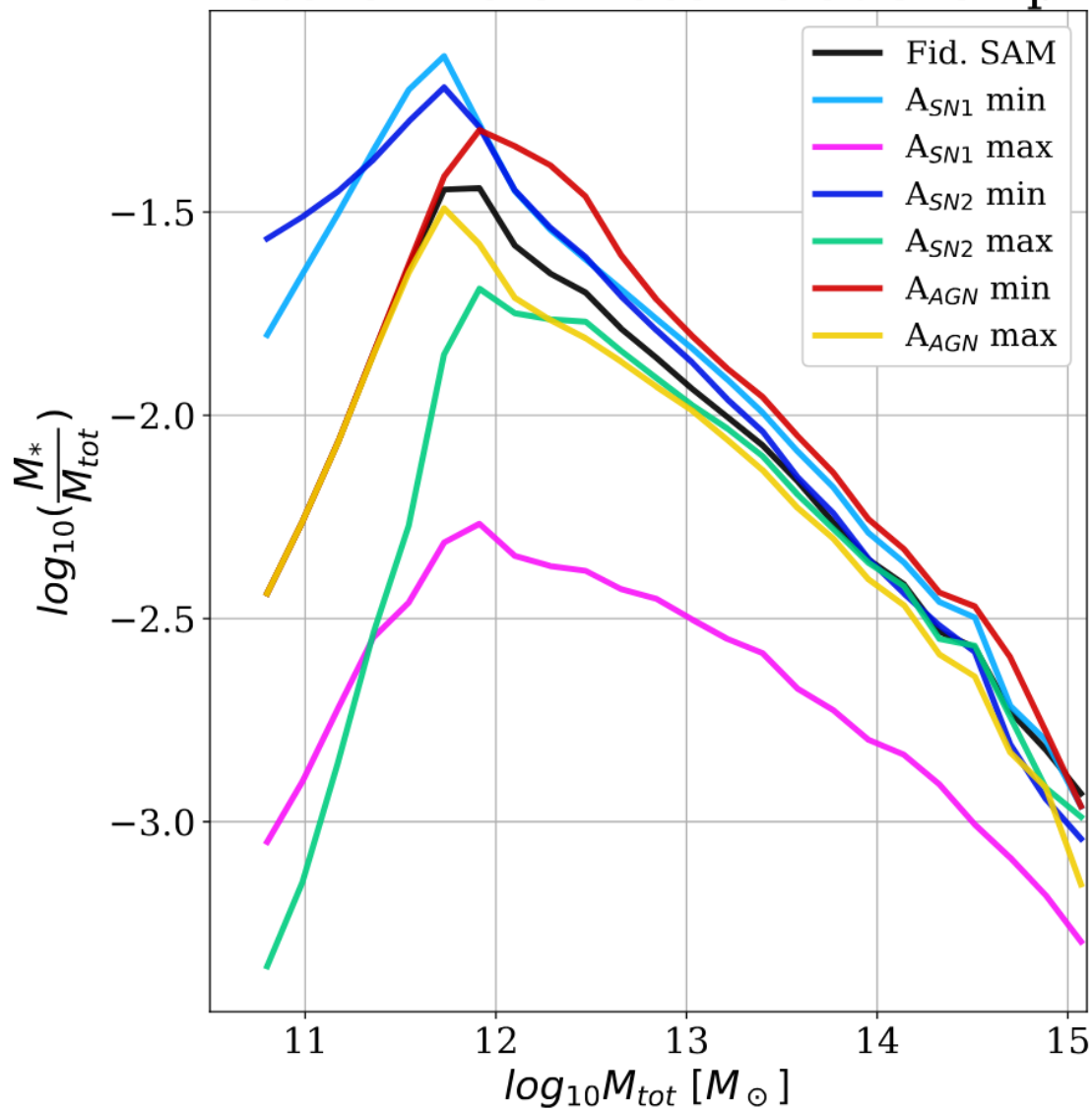
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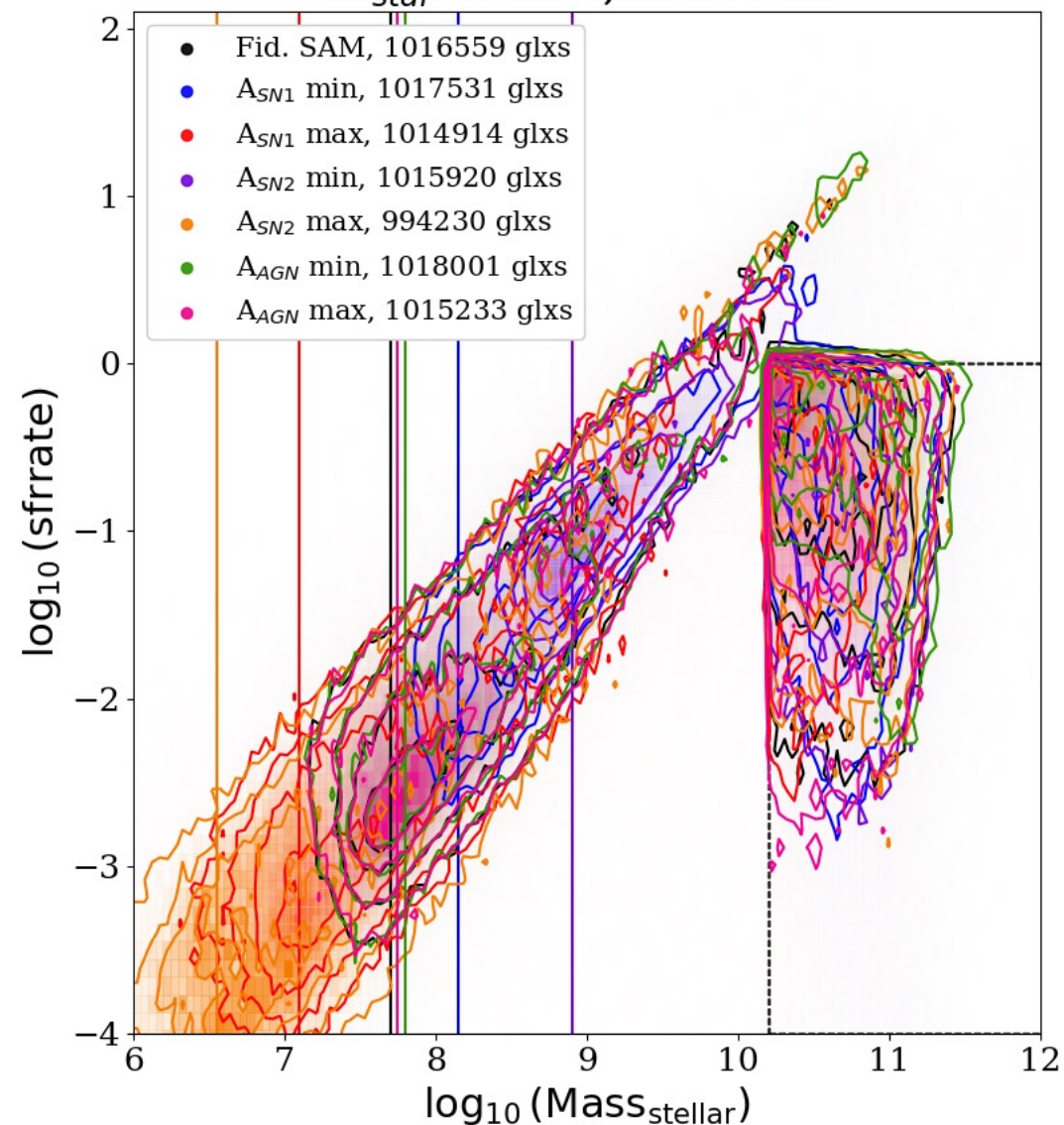
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## Stellar-Halo Mass Relationship



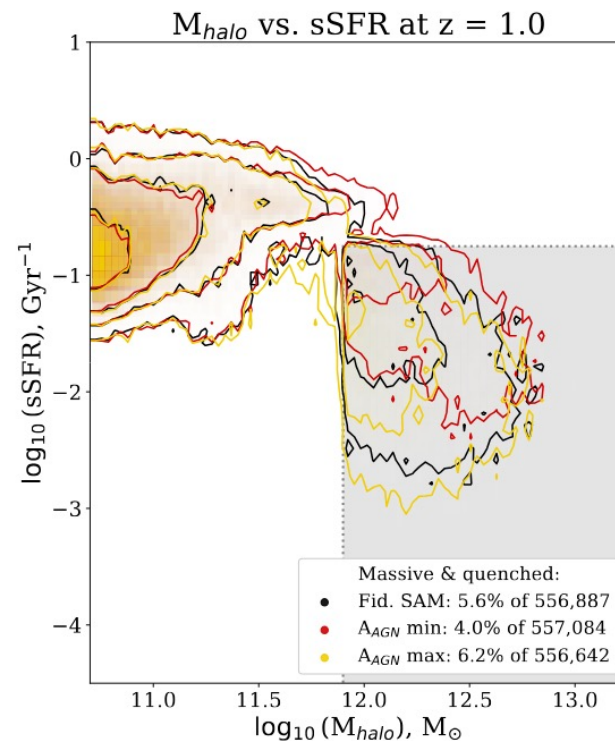
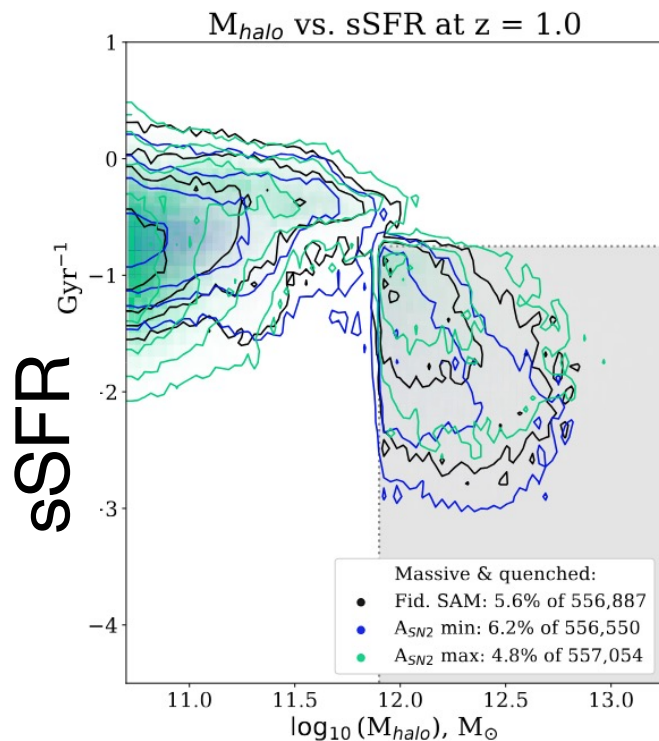
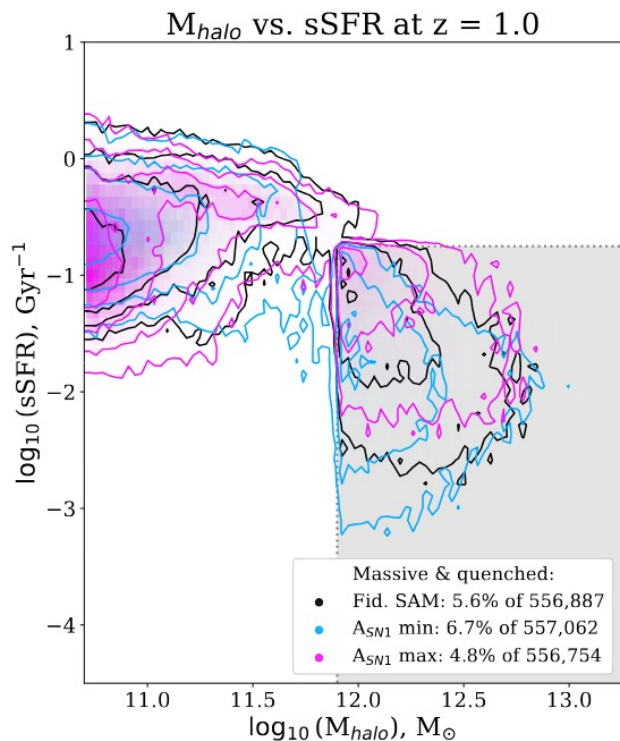
## $M_{star}$ vs SFR, at $z = 0.0$



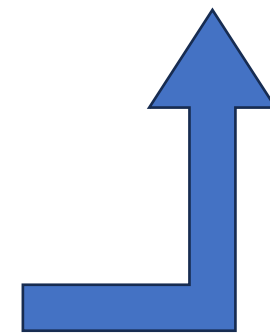
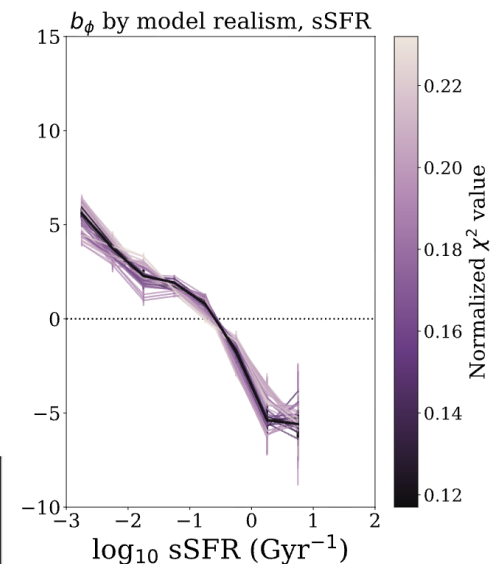
# Why? The galaxy-halo connection!

Regulated sSFR-  $M_{\text{halo}}$  makes  $b_{\phi}$ (sSFR) standard

sSFR vs.  $M_{\text{halo}}$   $z = 1$  'Main Sequence': one-parameter-at-a-time models

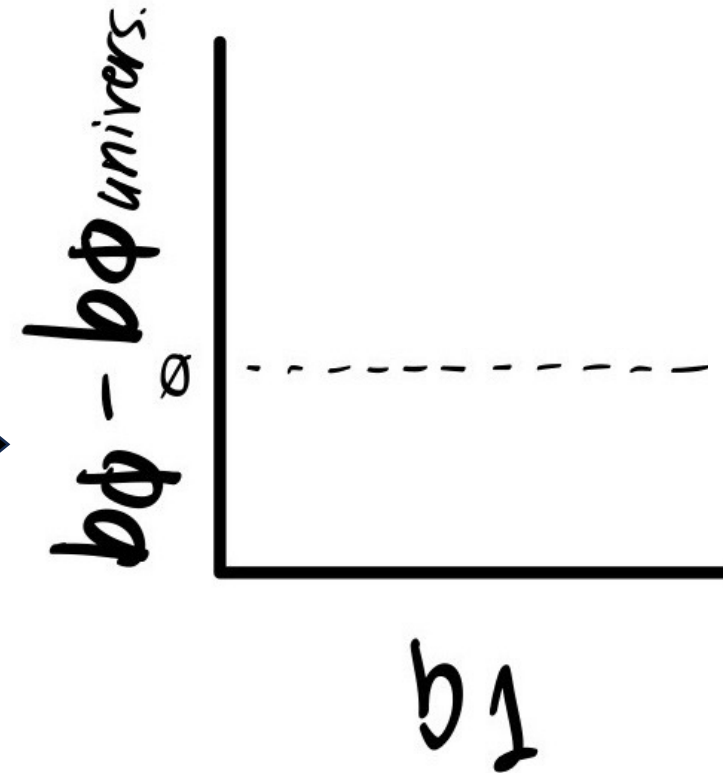
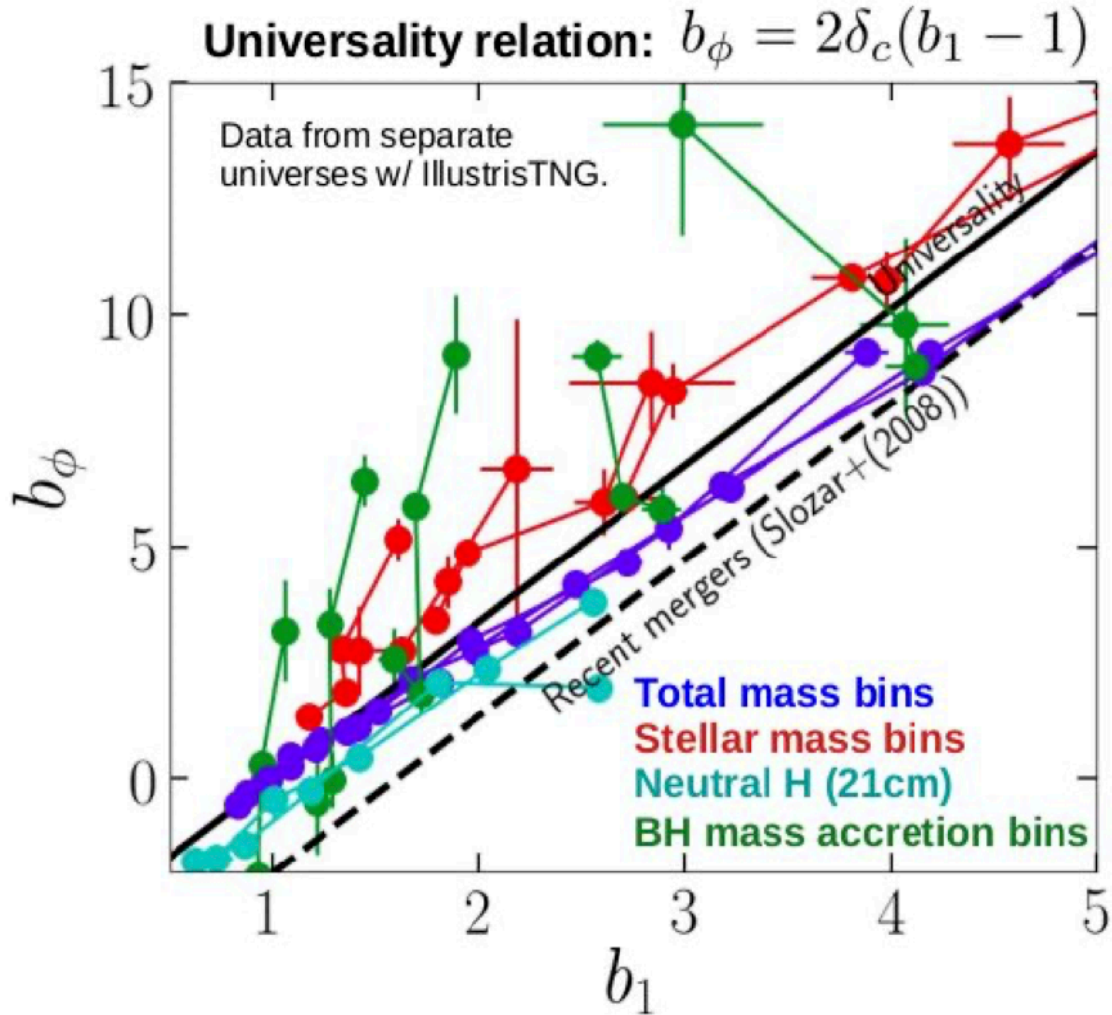


Halo Mass



(The SC-SAM is correctly regulating star formation even as the parameters go wild)

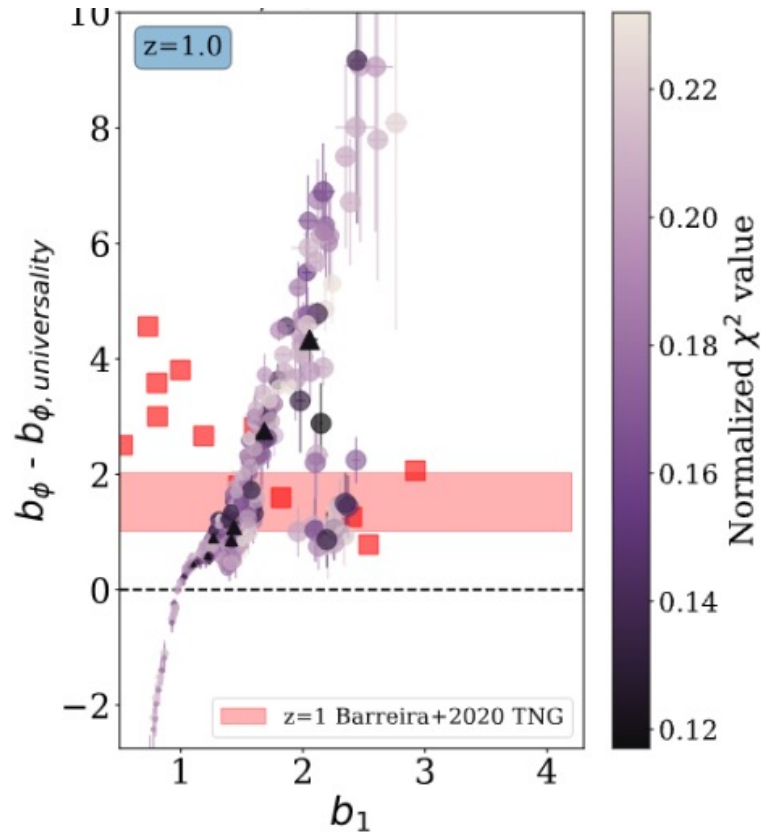
# $(b_\phi - b_{\phi, \text{universality}})$ vs. $b_1$



If universality describes well,  
points will clump near 0!

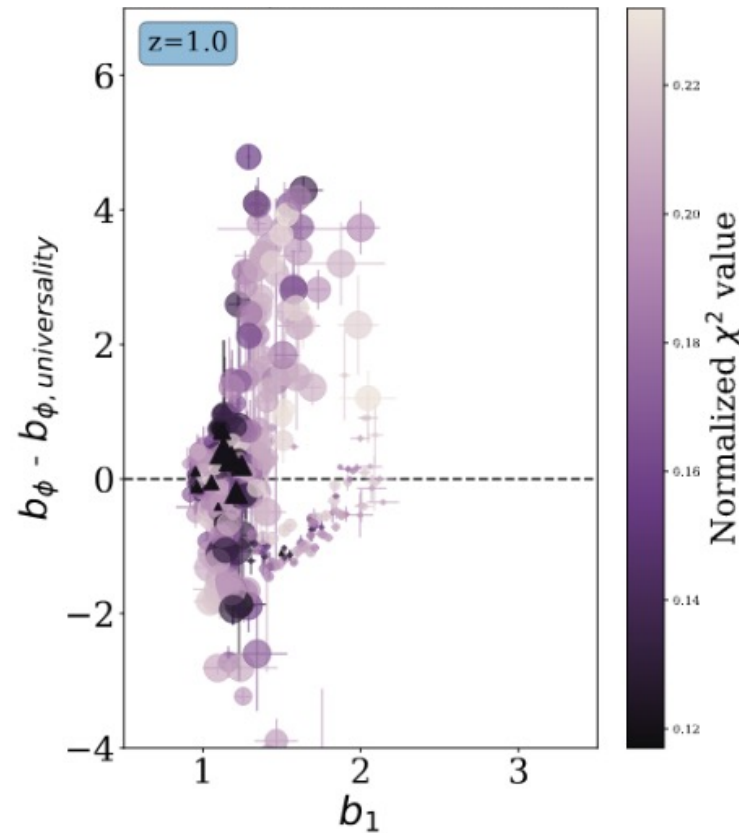
# $b_\phi$ vs. $b_1$ for $M_{\text{star}}$ , SFR, sSFR

## Stellar Mass selections



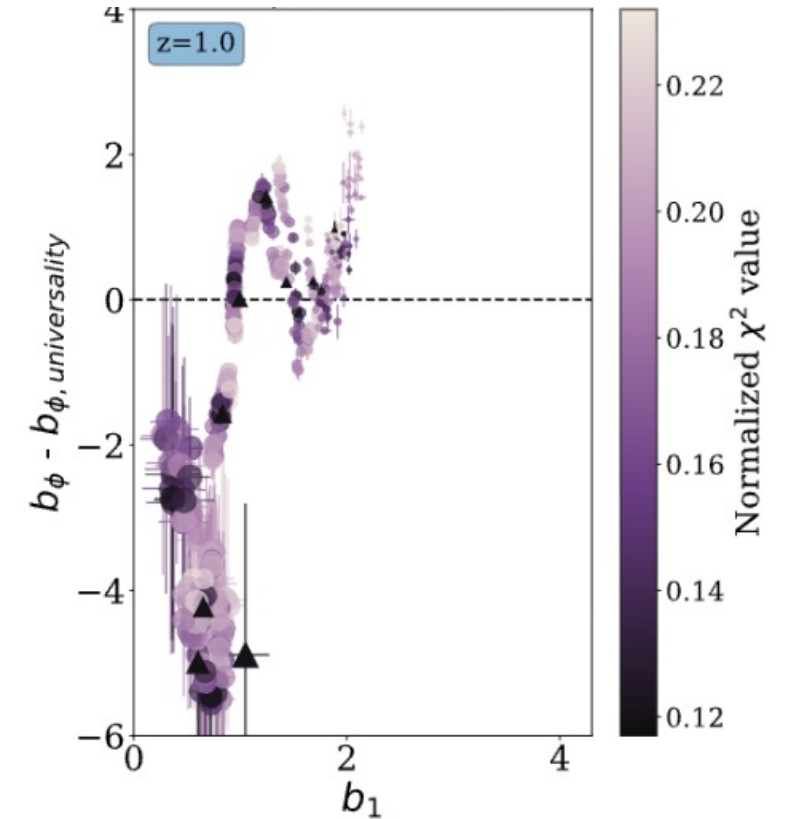
- Universality:  $2\delta_c(b_1 - 1)$
- +  $8.0 < M_*, \log_{10} M_\odot < 8.5$
- $12.5 < M_*, \log_{10} M_\odot < 13.0$
- ▲ Fid. SC-SAM

## Instan. SFR selections



- Universality:  $2\delta_c(b_1 - 1)$
- +  $-3.0 < \text{SFR}, M_\odot \text{yr}^{-1} < -2.5$
- $1.5 < \text{SFR}, M_\odot \text{yr}^{-1} < 2.0$
- ▲ Fid. SC-SAM

## Specific SFR selections

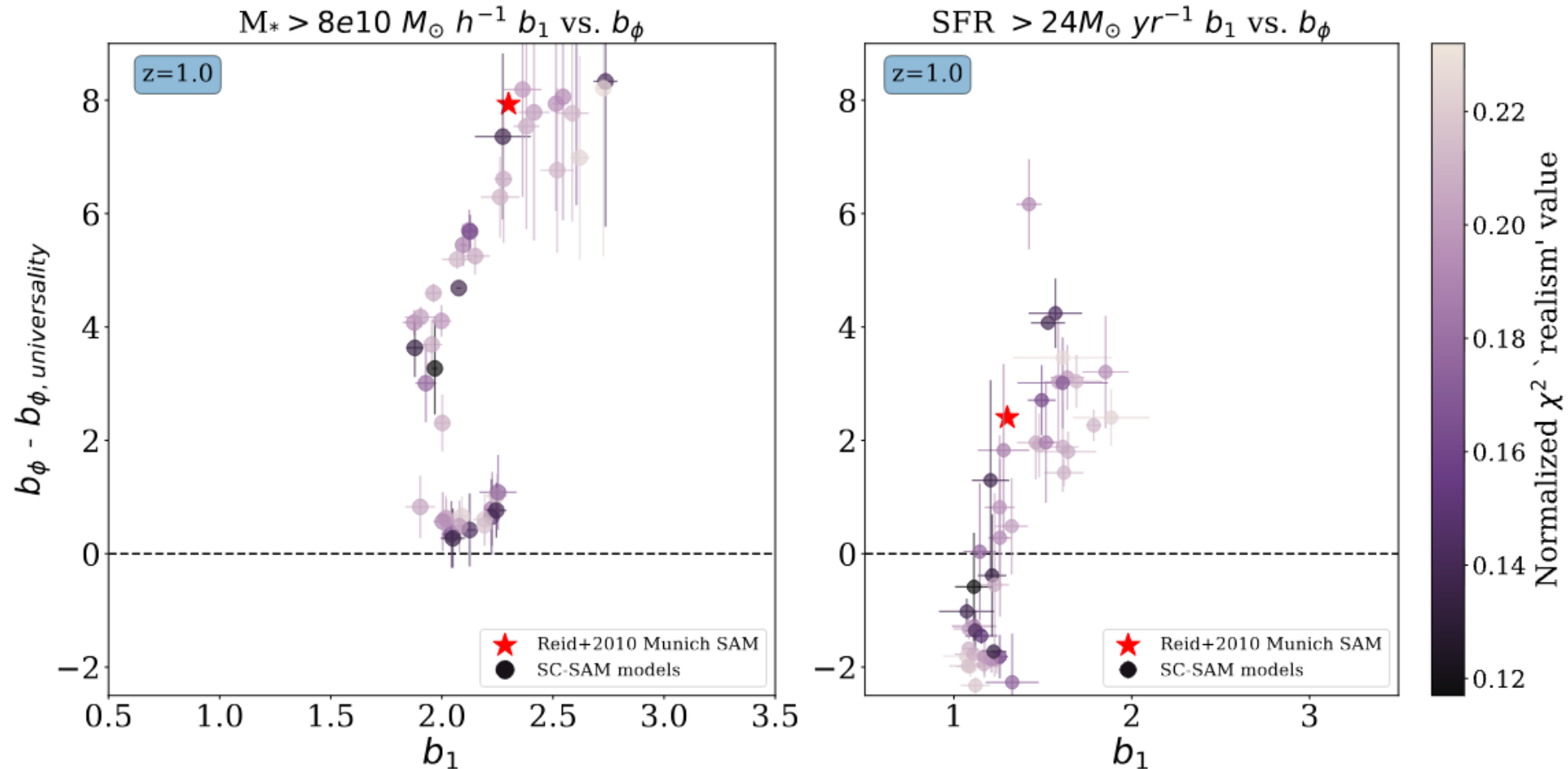


- Universality
- +  $-3.0 < \text{sSFR } \log_{10} \text{Gyr}^{-1} < -2.5$
- $1.5 < \text{sSFR } \log_{10} \text{Gyr}^{-1} < 2.0$
- ▲ Fid. SC-SAM

# What about other galaxy models?

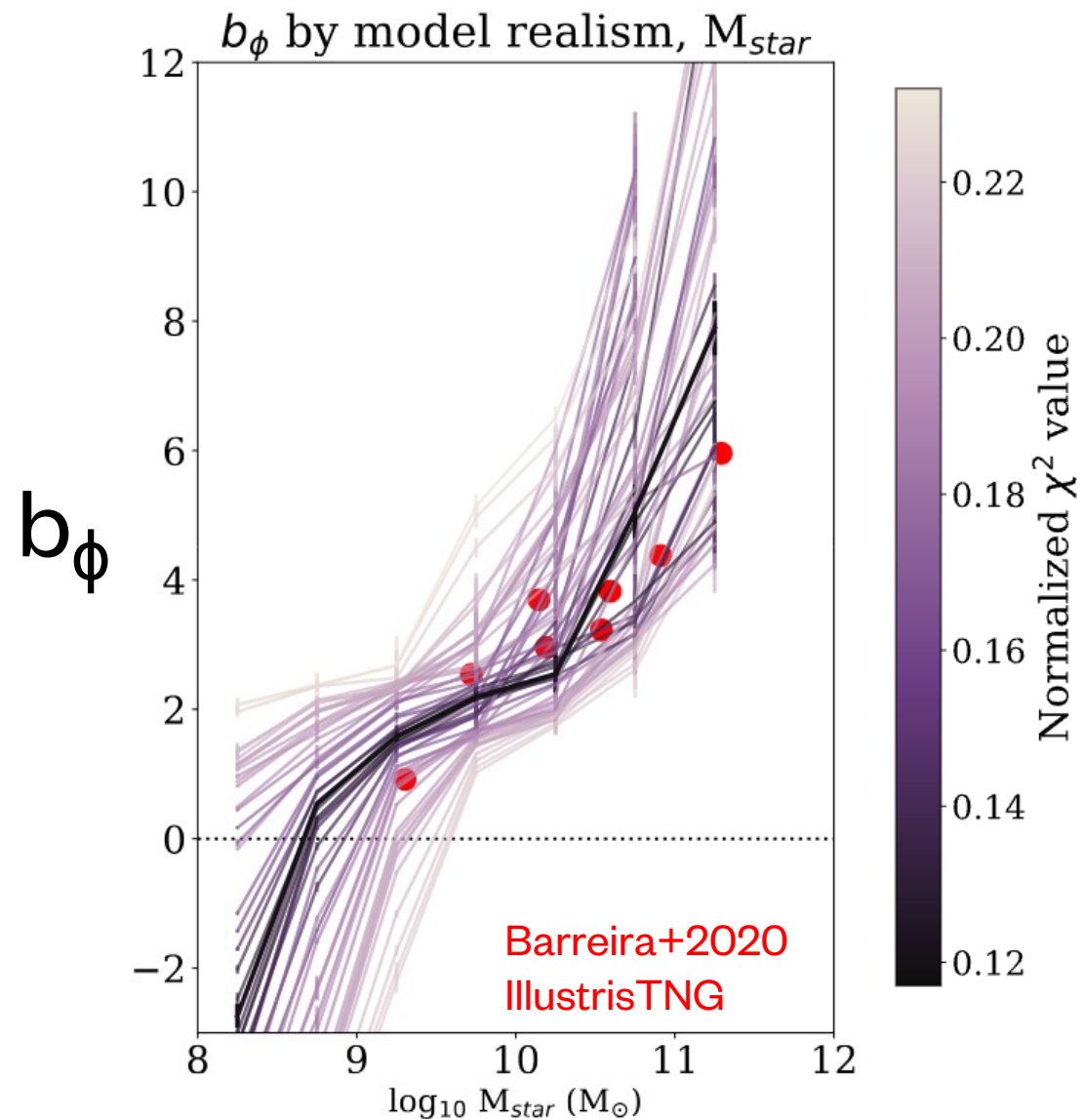
High mass galaxies

Strongly star forming galaxies

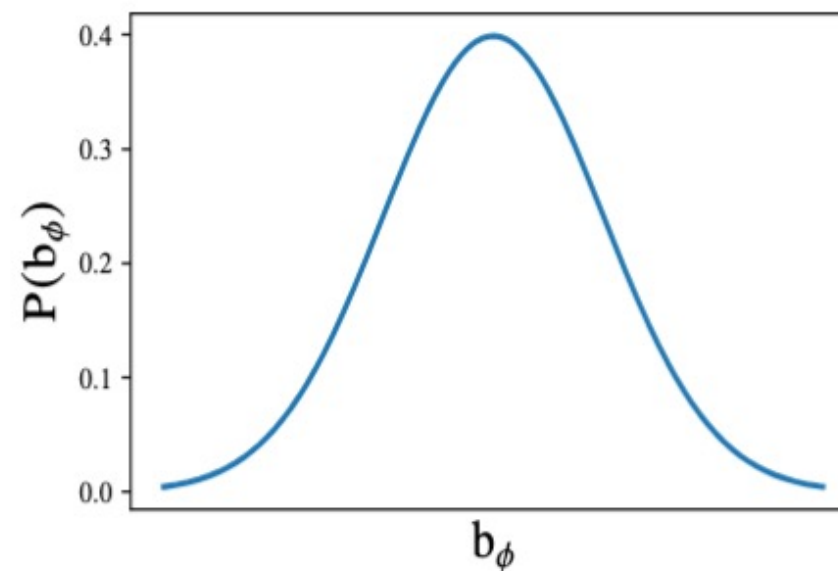
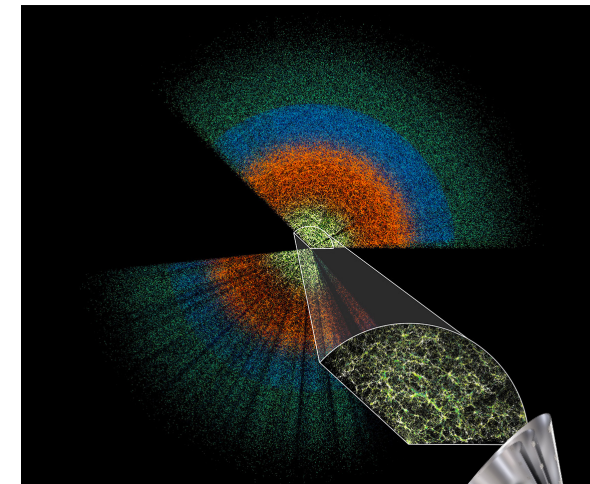


Reid et al. (2010) measure non-Gaussian assembly bias in the Munich SAM

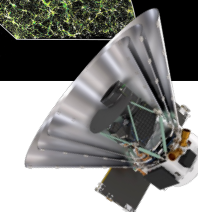
# Next: get useful priors for $f_{\text{NL}}$ studies



*But not all those models are realistic!  
The prior should reflect that.*



*Galaxies selected by e.g. high stellar mass or SFR*



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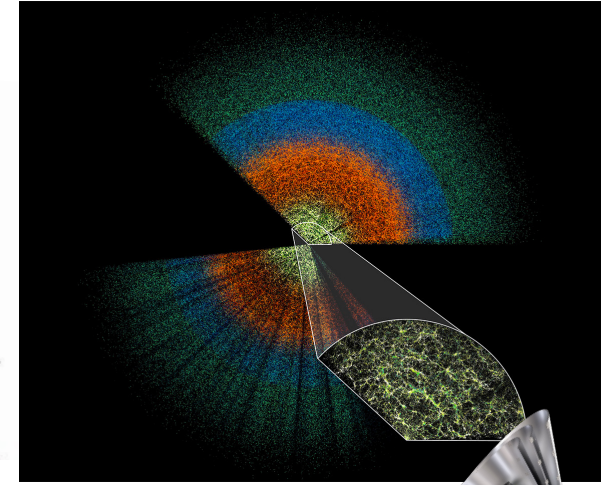
$$p(b_\phi | \text{obs}) = \int d\theta_{\text{GF}} p(b_\phi | \theta_{\text{GF}}) p(\theta_{\text{GF}} | \text{obs})$$

prior on  $b_\phi$ , for some selection, given a comparison observation

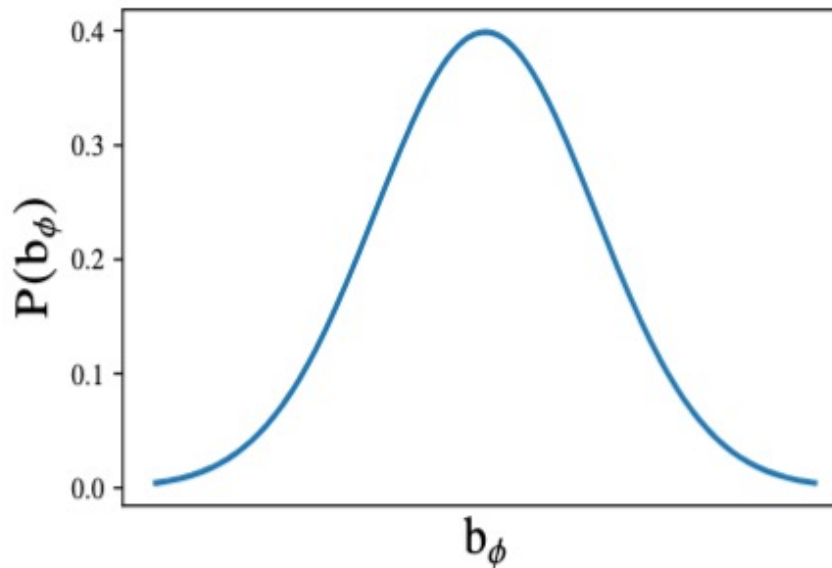
galaxy formation parameters

$b_\phi$  for some set of params

realism of a set of params conditioned on some observable



Led by Annie Moore, U of AZ PhD candidate



Galaxies selected by e.g. high stellar mass or SFR

# Next: get useful priors for $f_{\text{NL}}$ studies:

$$p(b_\phi | \text{obs}) = \int d\theta_{\text{GF}} p(b_\phi | \theta_{\text{GF}}) p(\theta_{\text{GF}} | \text{obs})$$

prior on  $b_\phi$ , for some selection, given a comparison observation

galaxy formation parameters

$b_\phi$  for some set of params

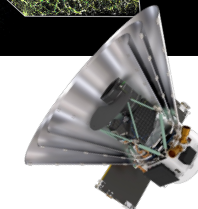
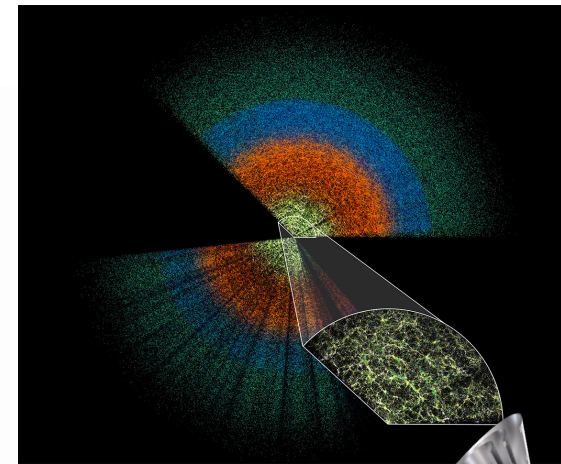
realism of a set of params conditioned on some observable



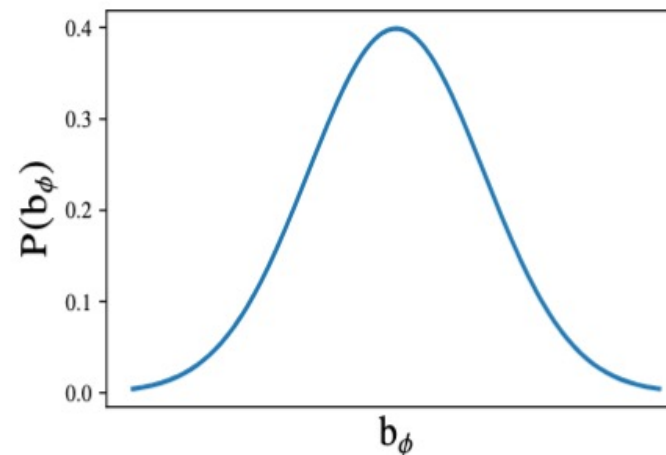
use separate universe SC-SAM simulations +  $b_\phi$ 's



use full CAMELS-SAM  $L=100 h^{-1}\text{Mpc}$  suite of 1000 sims (marginalize over cosmology)



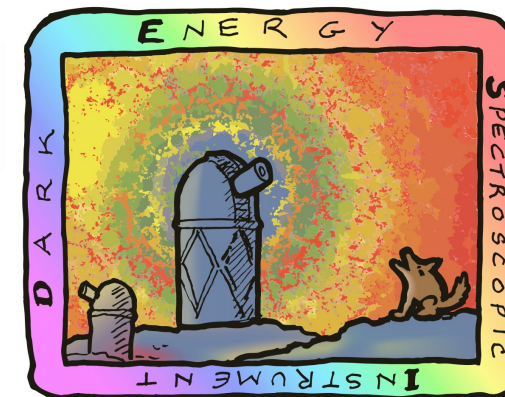
Galaxies selected by e.g. high stellar mass or SFR



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# Next: get useful priors for $f_{NL}$ studies:

$$\rho(b_\phi | Obs) = \int d\theta_{GF} \rho(b_\phi | \theta_{GF}) \rho(\theta_{GF} | Obs)$$

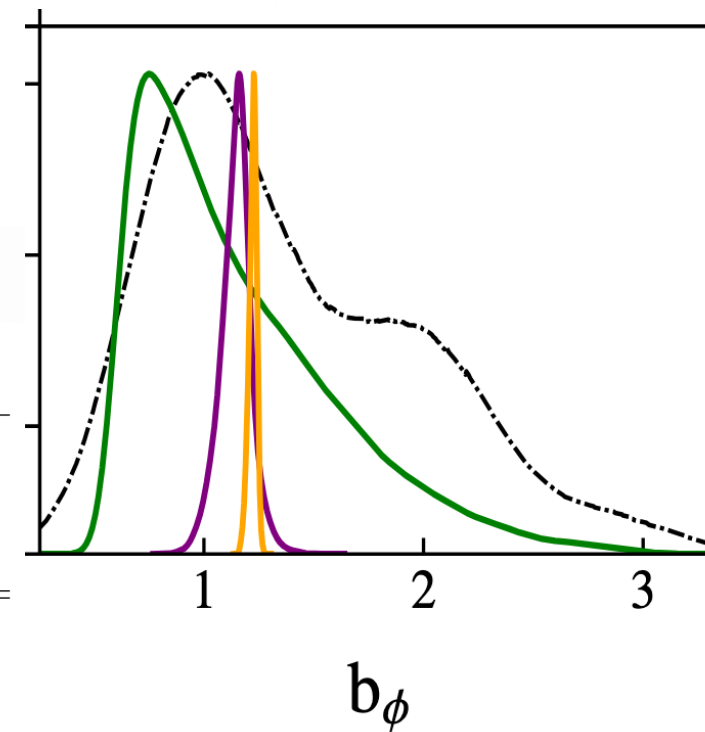
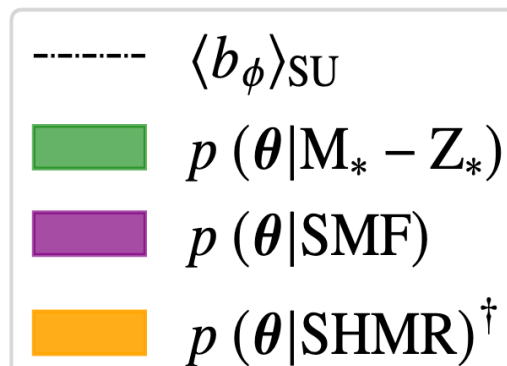


Preliminary results: this leads to significant narrowing in the  $b_\phi$  prior,

$\sigma_{b_\phi}$  reduced by ~90%!

But it depends on the observable, limited by the fewer Sep. Univ. SC-SAMs

DESI ELG-like selection in stellar mass and specific SFR



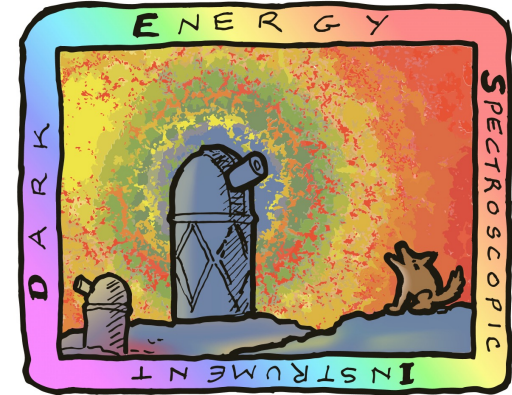
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$b_\phi$  Priors Conditioned on Observed Data

Metric	$\langle b_\phi \rangle_{SU}$	$\langle b_\phi \rangle_{\chi^2_{\{Obs\}}}$			$p(b_\phi   \{Obs\})$		
		SMF	SHMR	$M_* - Z_*$	SMF	SHMR <sup>†</sup>	$M_* - Z_*$
$\langle b_\phi \rangle$	1.43	1.20	1.41	1.39	1.15	1.25	1.15
$\sigma_{b_\phi}$	0.69	0.48	0.58	0.62	0.08	0.02	0.45

# Next: get useful priors for $f_{NL}$ studies:

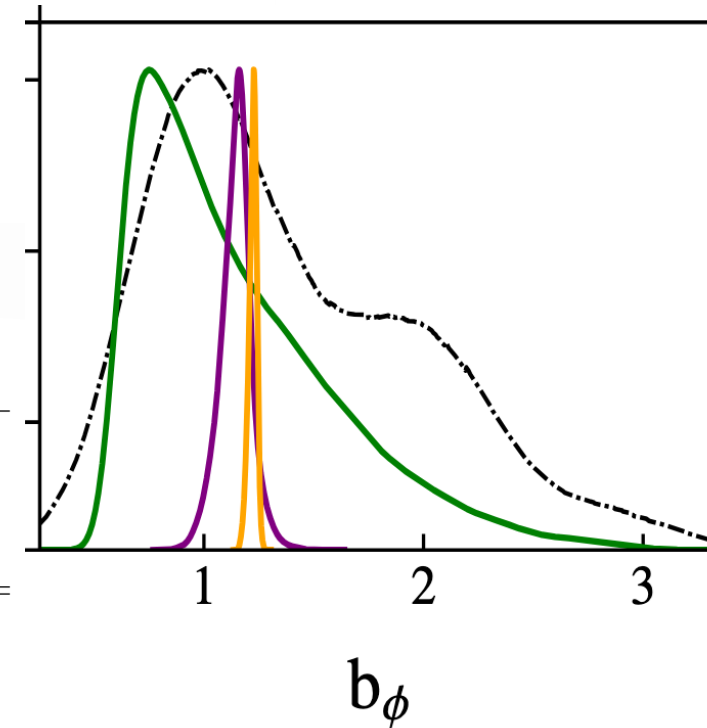
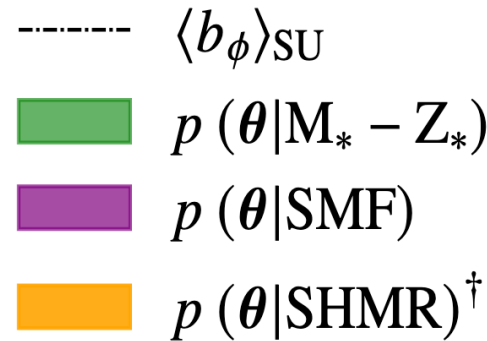
$$\rho(b_\phi | \text{Obs}) = \int d\theta_{GF} \rho(b_\phi | \theta_{GF}) \rho(\theta_{GF} | \text{Obs})$$



Preliminary results: this leads to significant narrowing in the  $b_\phi$  prior,  $\sigma_{b_\phi}$  reduced by ~90%!

*2026arXiv260421790M*

DESI ELG-like selection in stellar mass and specific SFR



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# Summary & Takeaways: [arxiv.org/abs/2602.04987](https://arxiv.org/abs/2602.04987)



- $f_{\text{NL}}$  will not be well constrained until we better understand how galaxy formation affects galaxy bias parameters!
- With separate universe simulations and the Santa Cruz SAM, we measure non-Gaussian galaxy bias  $b_\phi$  across several dozen parametrizations varying SN and AGN feedback
- All selections strongly diverge from the universality relation:
  - Our stellar mass findings aligns well with previous IllustrisTNG  $b_\phi$  measurements, but diverge a bit in  $b_\phi(b_1)$
  - SFR selections yield chaotic  $b_\phi$  and  $b_\phi(b_1)$
  - sSFR seems robust to galaxy formation parameterizations, likely due to regulated star formation in the SC-SAM
- We agree with the  $b_\phi(b_1)$  measured in the Munich SAM—but we need more galaxy formation models!
- We can get much narrower priors for  $b_\phi$  by conditioning on how realistic a particular SC-SAM parametrization is given some observable (Moore, LAP, & Krause in final prep)

Redshift evolution of  $b_\phi$ ?  
Effect of individual parameters?

