

Cosmology with kSZ

Mathew Madhavacheril

with Nick Battaglia, Colin Hill, Simone Ferraro, Utkarsh Giri, Moritz Munchmeyer,
Matt Johnson, Emmanuel Schaan, Jon Sievers, Kendrick Smith

1. What does kSZ measure?
2. Bispectrum formalism
3. Applications
 - a. Primordial Non-Gaussianity
 - b. Cosmic growth w/ FRBs
 - c. Feedback and lensing

Smith, MM, Ferraro ++ 2018 arXiv:1810.13423

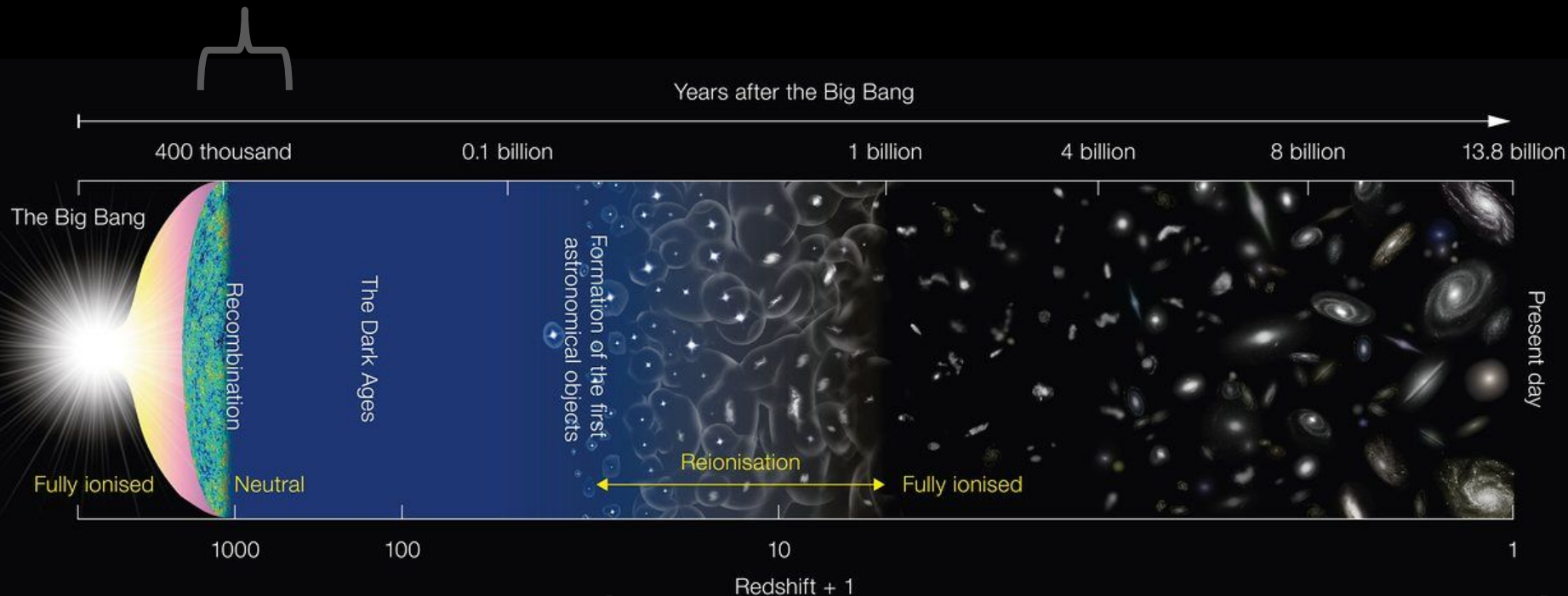
Munchmeyer, MM, Ferraro ++ 2018 arXiv:1810.13424

MM, Battaglia, Smith, Sievers 2019 arXiv:1901.02418

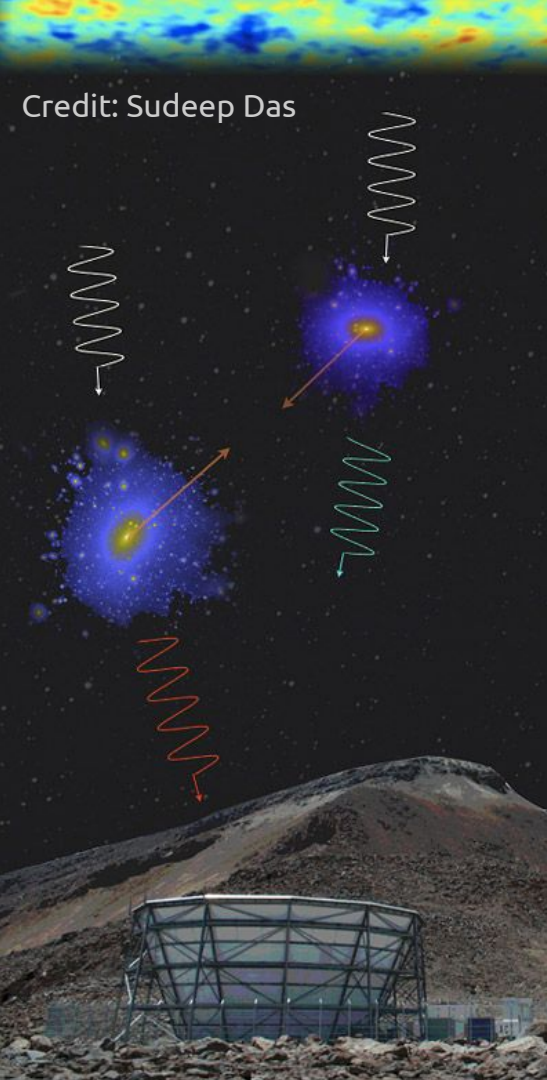
(work in progress with Schaan, Battaglia, Ferraro, Hill, ++)

CMB backlight

"I've been ionized, but I'm OK now." -- Dr. Buckaroo Banzai



Lots of (moving) free electrons



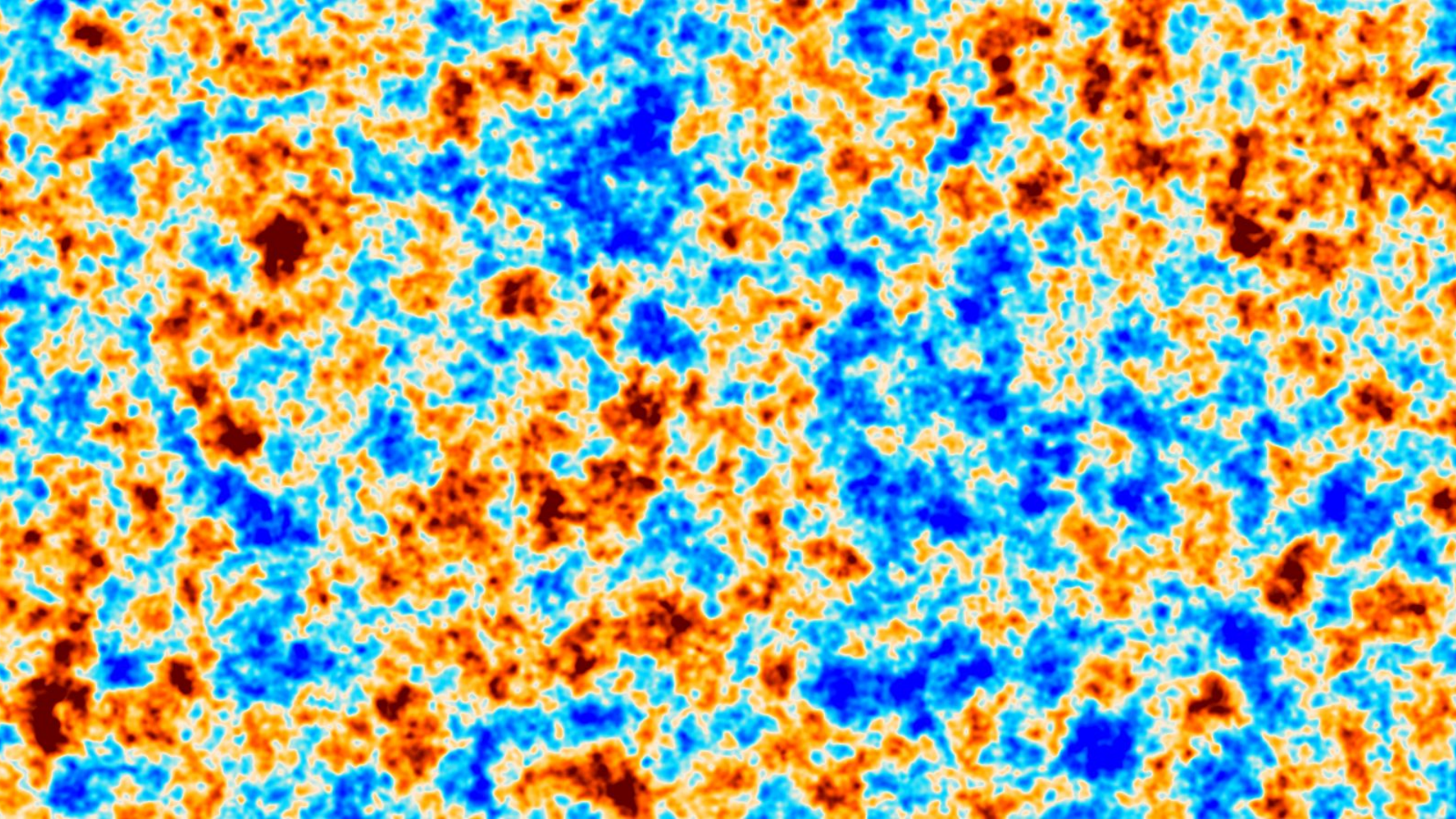
Credit: Sudeep Das

kSZ: Doppler shift of CMB photons scattering off electrons with bulk velocity

$$\frac{\Delta T_{\text{kSZ}}(\vec{\mathbf{n}})}{T_{\text{CMB}}} \sim \int d\chi e^{-\tau(z)} v_r \delta_e(\vec{\mathbf{n}}, \chi)$$

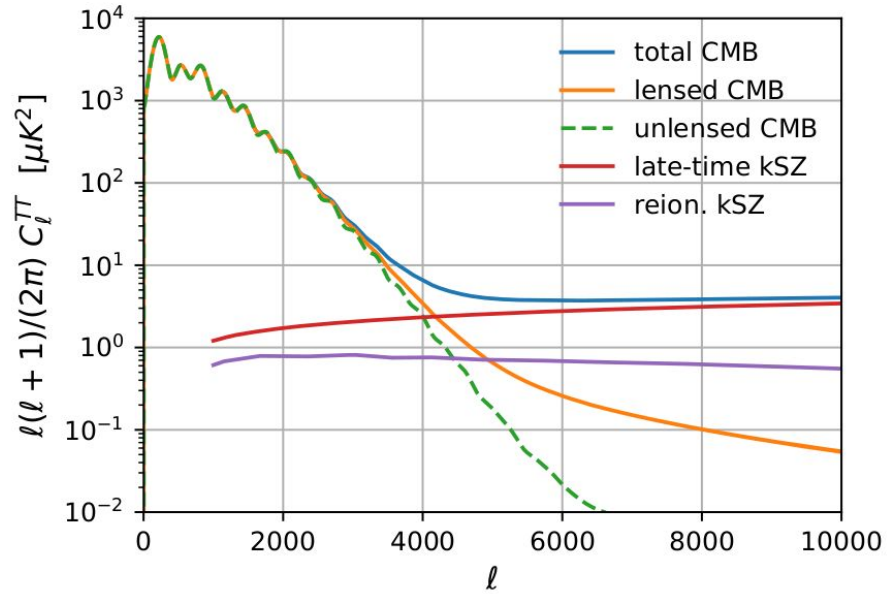
Contributions from

1. Reionization (from first stars) $6 < z < 20$
2. **Ionized gas in and between clusters $0 < z < 6$**



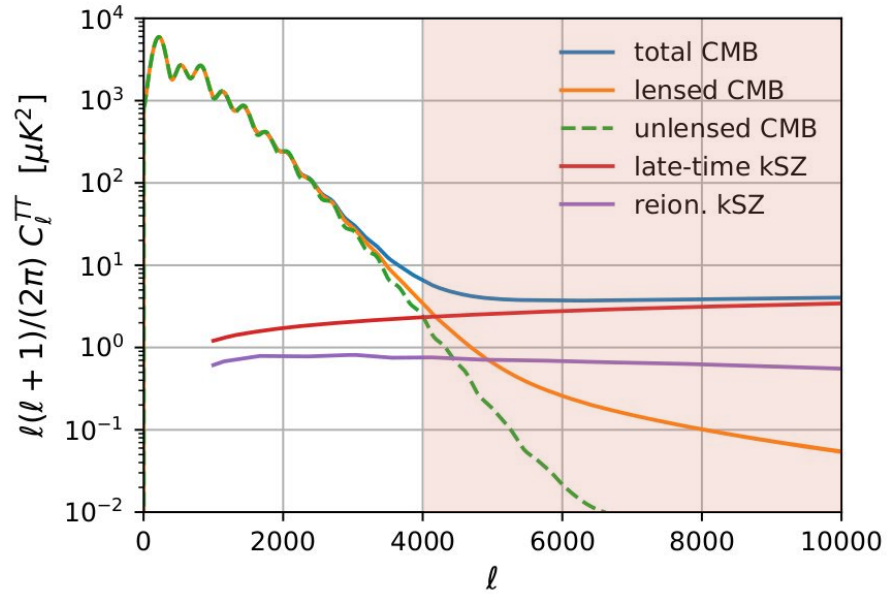
The image shows a vast field of simulated stars, likely from a WebSky simulation. The stars are represented as small, semi-transparent dots in various colors, including blue, orange, red, and yellow, scattered across a light blue background. The distribution is dense and somewhat irregular, with some larger, more prominent stars and many smaller ones. The overall appearance is that of a rich stellar population.

WebSky simulations
(George Stein, Marcelo Alvarez, Dick Bond)



kSZ dominates CMB at $l > 4000$

Can in fact bias CMB lensing: see **Ferraro, Hill 2017**

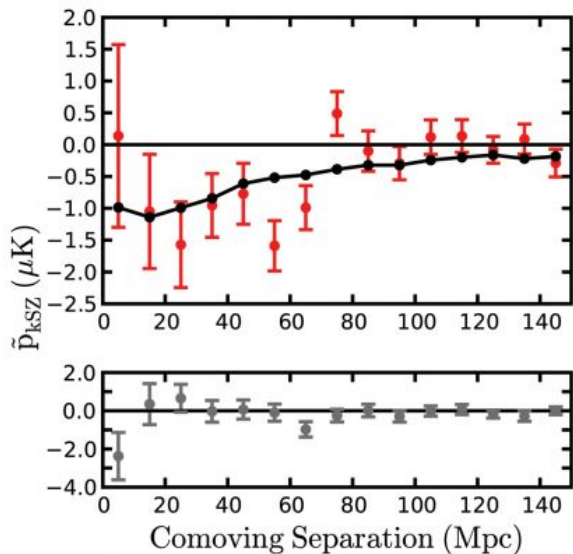


kSZ dominates CMB at $\ell > 4000$

Can in fact bias CMB lensing: see **Ferraro, Hill 2017**

Modes to be explored by AdvACT, SPT-3G, Simons Observatory, CMB-S4

ACT x BOSS, Hand++ '12



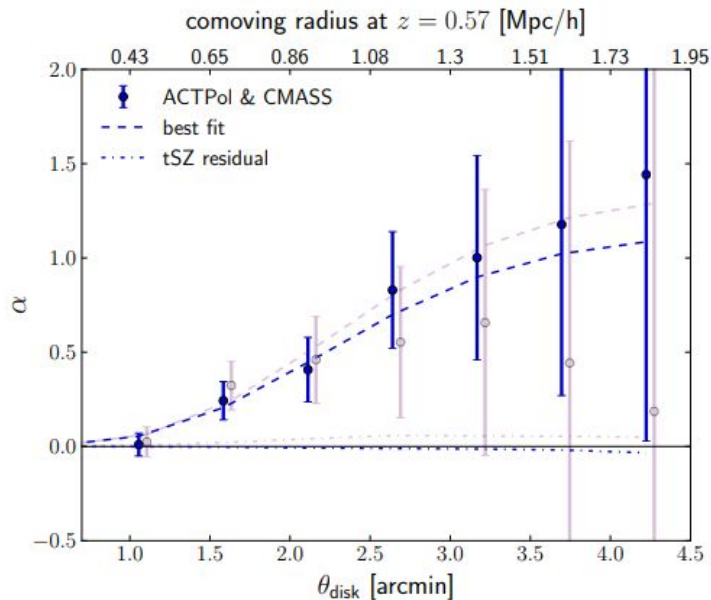
Also:

ACT x redMaPPer, de Bernardis++ '16

SPT x DES, Soergel++ '16

Planck x SDSS, '15

ACT x BOSS, Schaun++ '15



See also: Planck x WISE, Hill++ '16

Currently detected only at the <5 sigma level

But expected to improve quickly with (deeper) CMB x galaxy overlap!

SNR $O(100-1000)$ expected!

What can we learn with the kSZ effect?

$$\frac{\Delta T_{\text{kSZ}}(\mathbf{n})}{T_{\text{CMB}}} \sim \int d\chi e^{-\tau(z)} \delta_e(\mathbf{n}, \chi) v_r$$

Reionization

(Smith+ '17, Ferraro+ '18)

Missing baryons

(Lim+ '17, Hernández-Monteagudo+ '15)

Halo energetics and feedback

(Battaglia+ '18)

Astrophysics

Large scale anomalies

(e.g. Terrana+ '16)

Growth of structure?

Growth rate?

(e.g. Alonso+ '16)

Neutrino mass?

(Mueller+ '14)

Dark energy?

(Mueller+ '13)

+++ ...?

Cosmology?

What cosmology can kSZ potentially constrain?

$$\frac{\Delta T_{\text{kSZ}}(\mathbf{n})}{T_{\text{CMB}}} \sim \int d\chi e^{-\tau(z)} \delta_e(\mathbf{n}, \chi) v_r$$

- **Unbiased density modes** inferred from velocities

$$v \approx \frac{f a H}{k} \delta_m$$

- Velocities respond to **growth rate f** -> neutrino mass, dark energy, modified gravity

E.g Mueller+ '14
Alonso+ '16

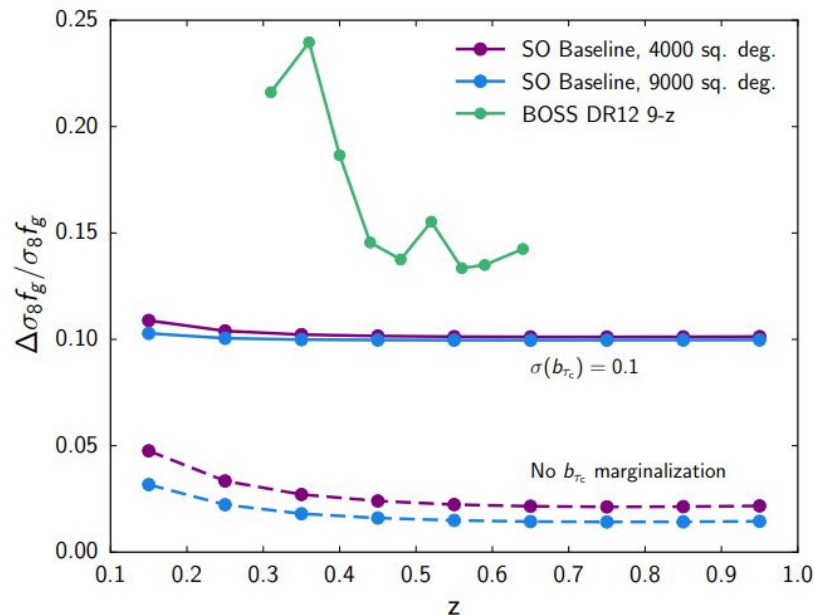
Astrophysics complicates this a bit

- Notorious “cluster optical depth”
- A catch-all term that includes our uncertainty about
 - Number density of electrons in halos associated with galaxies
 - Shape of the electron profile

$$\frac{\Delta T_{\text{kSZ}}(\mathbf{n})}{T_{\text{CMB}}} \sim \int d\chi e^{-\tau(z)} \delta_e(\mathbf{n}, \chi) v_r$$

But I'll show that this does **not** make it impossible to do interesting cosmology with kSZ!

arXiv:1808.07445 SO Collab. produced by **Victoria Calafut**



Unifying Framework: Bispectrum

Smith, MM ++ 2018 arXiv:1810.13423

Kendrick
Smith



Simone
Ferarro



Utkarsh
Giri



Moritz
Munchmeyer



Matt
Johnson



Proposed estimators for kSZ have one of these forms:

- $\langle ggT \rangle$ kSZ tomography: includes

- **pairwise momentum (4)**

- **template method (1)**

- velocity matched filter

- velocity reconstruction

- $\langle gTT \rangle$ **Projected kSZ (1)**

- $\langle TTTT \rangle$ patchy reionization kSZ

Hand++, de Bernardis++, Soergel++, Planck++

Schaan++ 2016

Li++ '17

Deutsch++ '17, Smith,MM,Ferraro++ arxiv:1810.13423

Hill++ '16, Ferraro++ '16

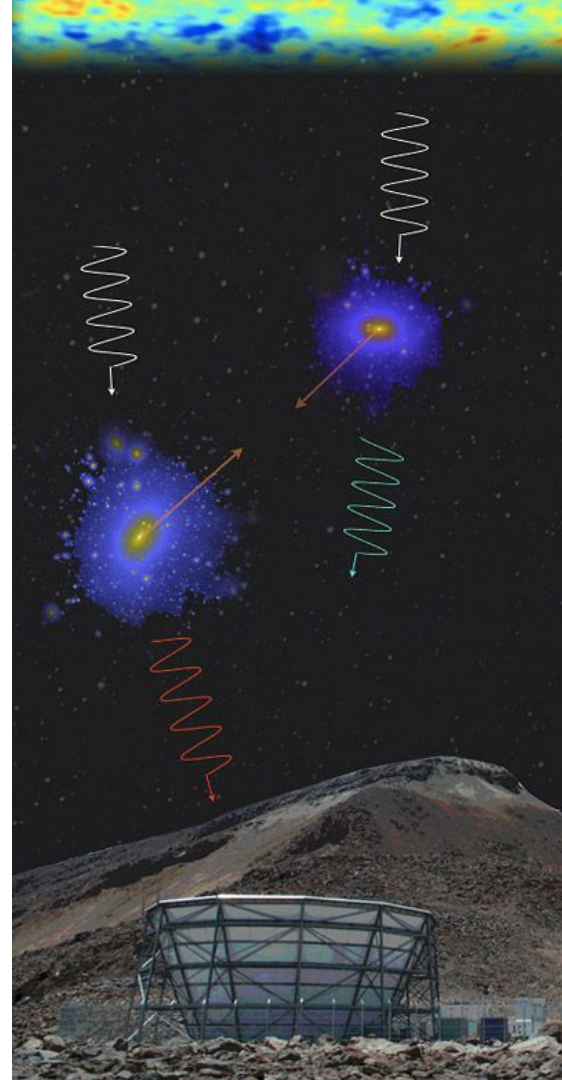
Smith++ '17, Ferraro++ '18

- $\langle ggT \rangle$ **kSZ tomography**: includes
 - pairwise momentum
 - template method
 - velocity matched filter
 - velocity reconstruction

These involve “cross-correlating” a CMB survey and a galaxy survey but effectively 3-point function since 2-pt cross-correlation is zero for halos equally likely to move towards or away

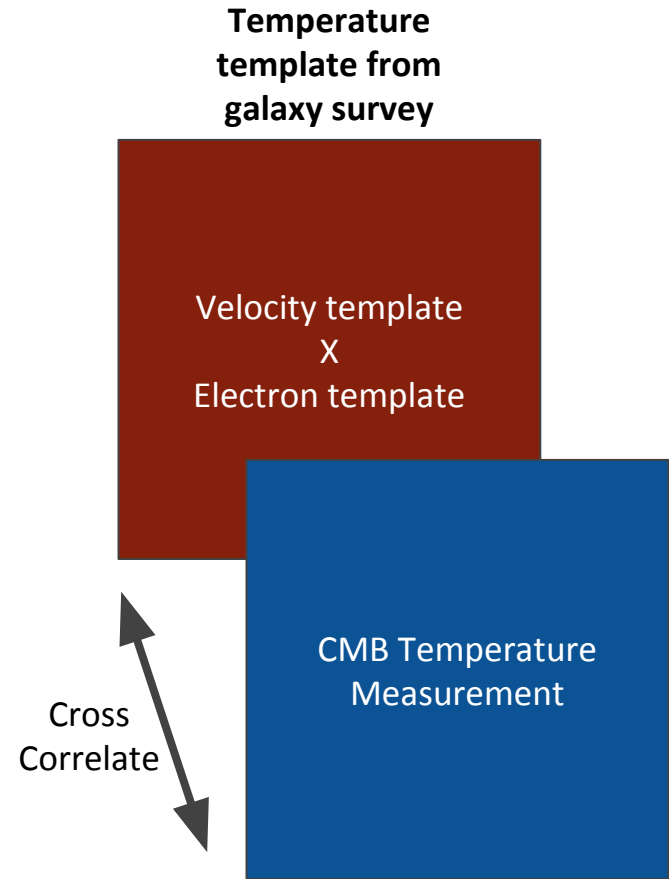
- $\langle ggT \rangle$ kSZ tomography: includes
 - **pairwise momentum**
 - template method
 - velocity matched filter
 - velocity reconstruction

e.g Hand++, de Bernardis++,
Soergel++, Planck++

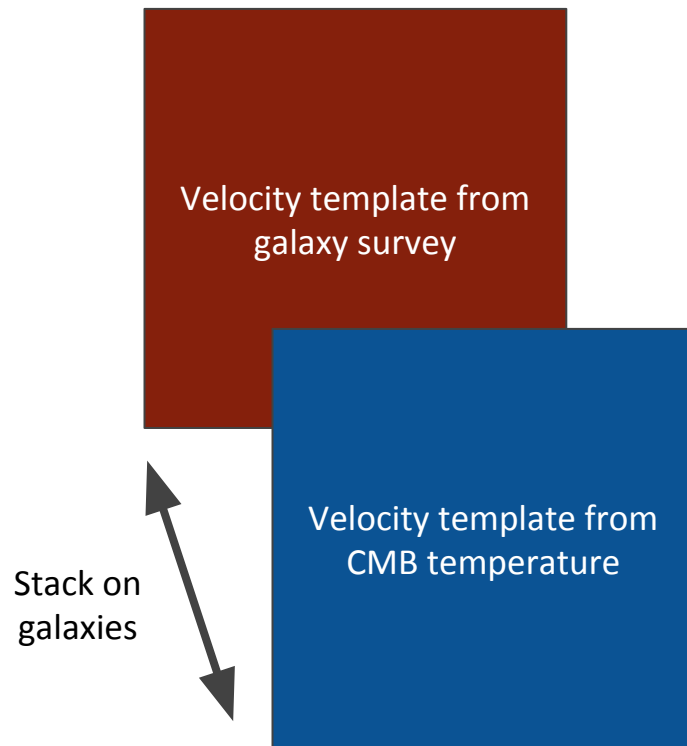


- $\langle ggT \rangle$ kSZ tomography: includes
 - pairwise momentum
 - **template method**
 - velocity matched filter
 - velocity reconstruction

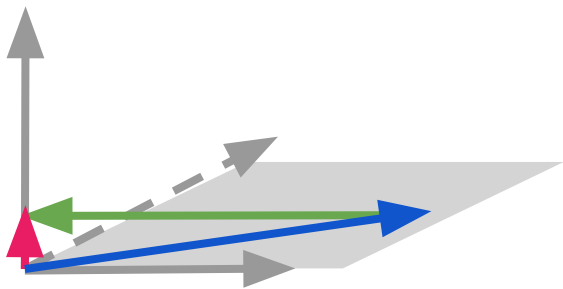
e.g. Schaan++



- $\langle ggT \rangle$ kSZ tomography: includes
 - pairwise momentum
 - template method
 - **velocity matched filter**
 - velocity reconstruction



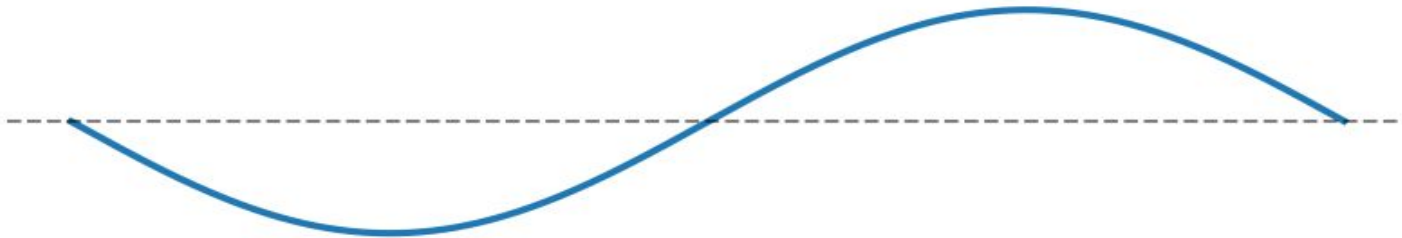
- $\langle ggT \rangle$ kSZ tomography: includes
 - pairwise momentum
 - template method
 - velocity matched filter
 - **velocity reconstruction**



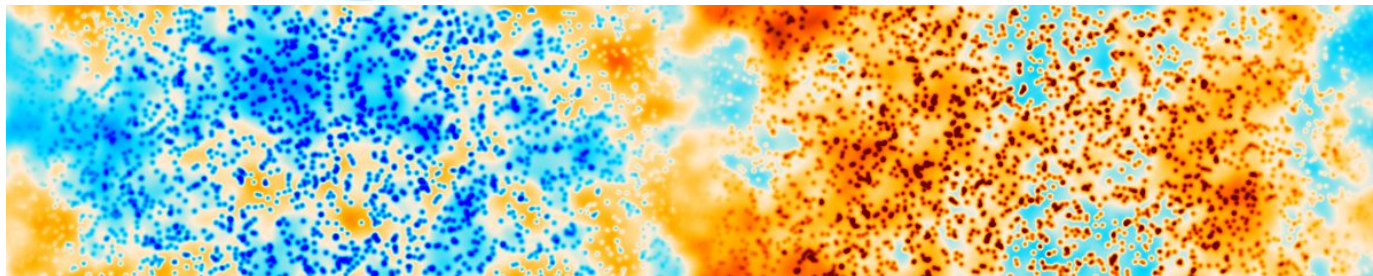
- An especially illuminating framework for cosmology is **velocity reconstruction**
- Cosmic velocity extracted from quadratic combination of galaxy positions (from BOSS, DESI, LSST) together with CMB temperature $v \sim \langle gT \rangle$
- 3D Velocity reconstruction then auto-correlated and cross-correlated with galaxy survey
- The cross-correlation with the galaxy survey $\langle vg \rangle$ realizes one possible projection of the bispectrum $\langle gv \rangle \rightarrow \langle ggT \rangle$

Squeezed bispectrum cartoon: kSZ

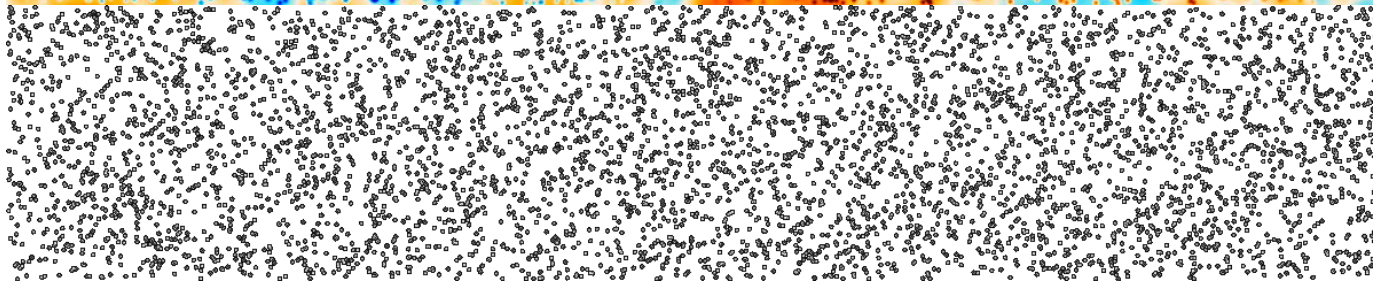
Cosmic
velocity
mode



CMB
temperature



Galaxy
positions



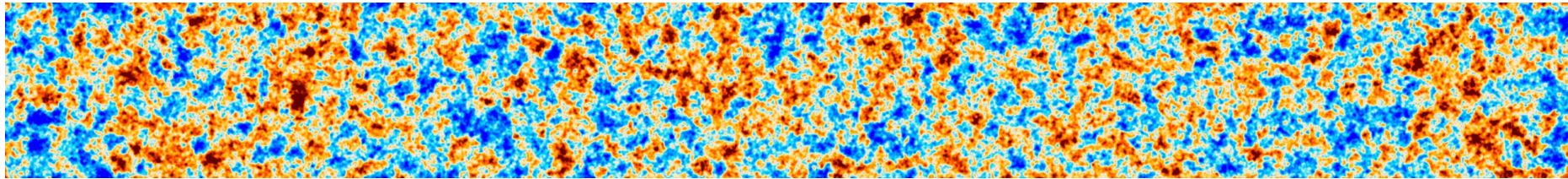
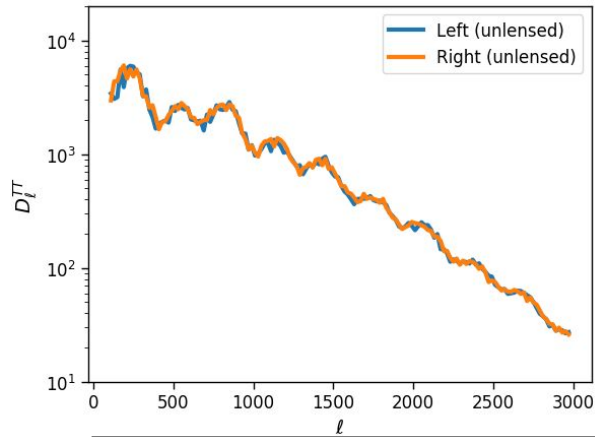
Velocities from modulation of late-time patchy kSZ cross-power with galaxies

The image displays a vast field of simulated stars, likely from a galaxy simulation. The stars are represented as small, circular points of light in various colors, including blue, orange, red, and yellow. The background is a light blue color, suggesting a deep sky or a specific spectral filter. The stars are distributed across the entire frame, with some appearing larger and brighter than others, indicating different stellar populations or distances. The overall appearance is that of a rich, multi-colored stellar population.

WebSky/CITA simulations

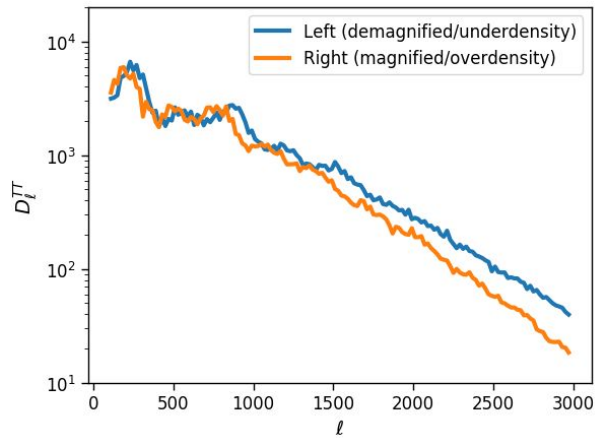
Squeezed bispectrum cartoon: **lensing**

Matter overdensity mode
(zero)

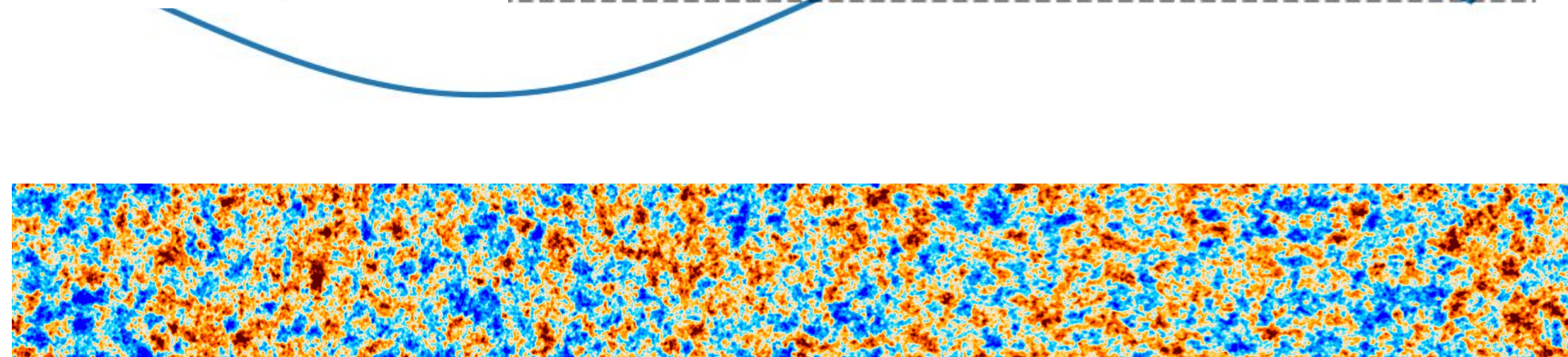


Unlensed CMB
temperature

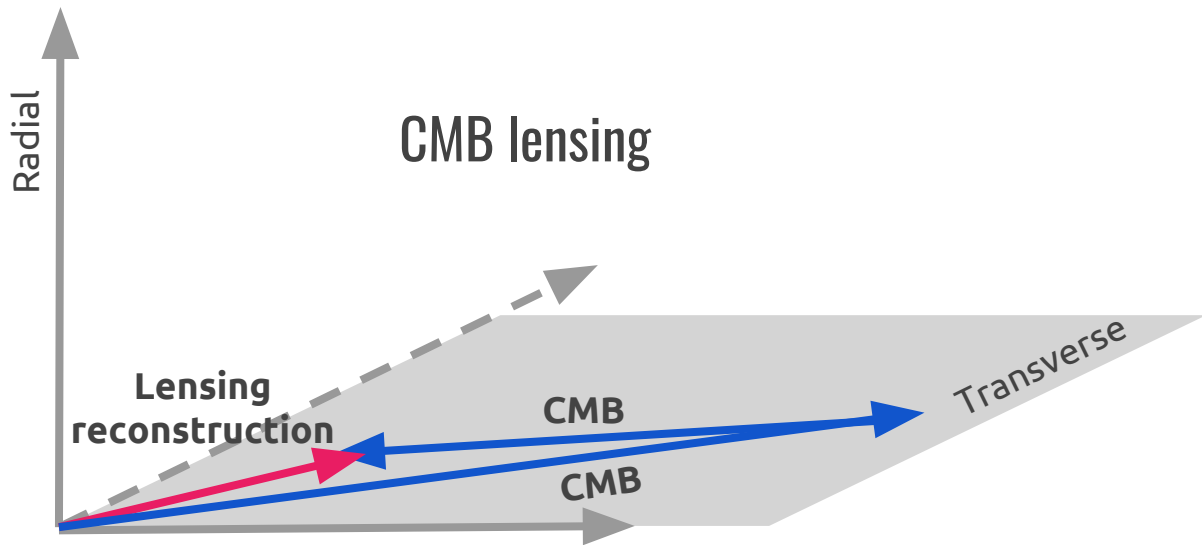
Squeezed bispectrum cartoon: **lensing**



Matter overdensity mode



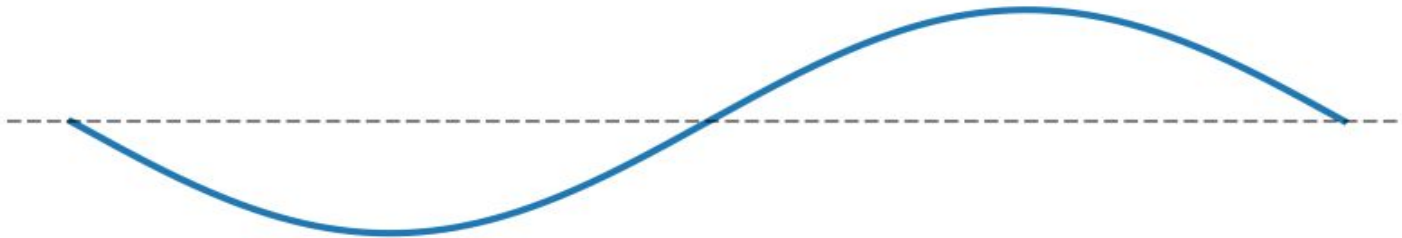
Lensed CMB
temperature



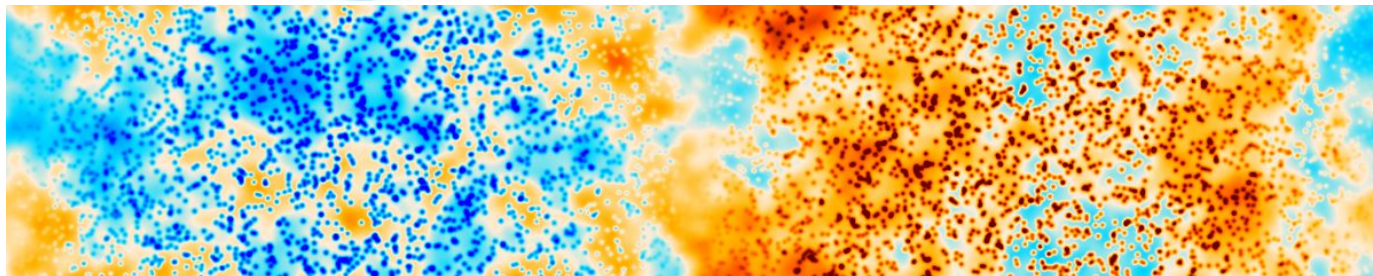
$$\hat{\phi}(L) = \langle TT \rangle_{\ell}$$

Squeezed bispectrum cartoon: kSZ

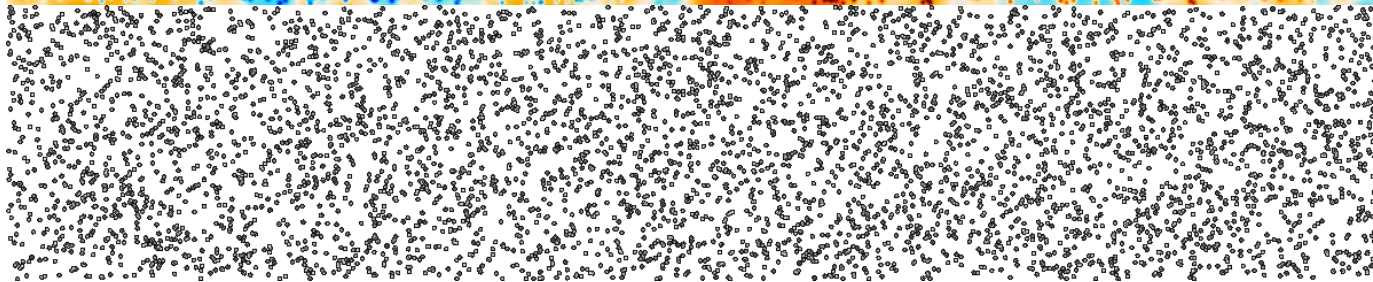
Cosmic
velocity
mode



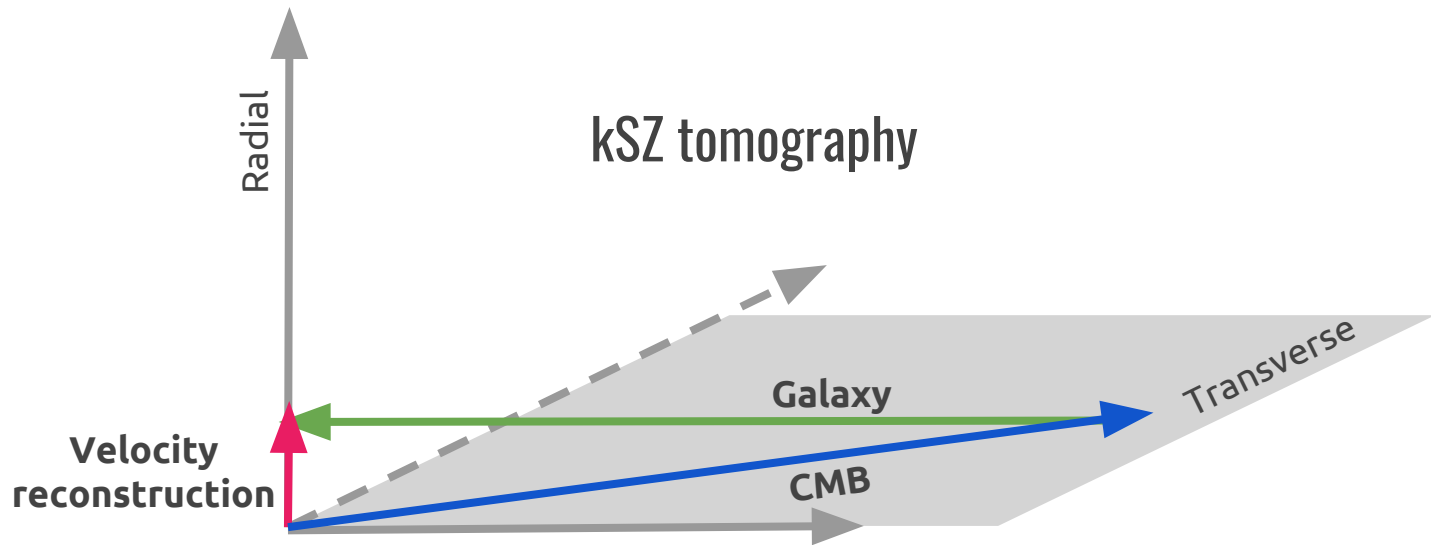
CMB
temperature



Galaxy
positions



Velocities from modulation of late-time patchy kSZ cross-power with galaxies



Step 1: get reconstructed velocity

$$\hat{v}_{\text{rec}}(k_L) \sim \langle gT \rangle k_S$$

Velocity Reconstruction Framework

- Average over quadratic pairs of modes -- effectively look for modulation of galaxy x CMB temperature power

$$\begin{aligned}\hat{v}_{\text{rec}}(k_L) &\sim \langle \delta_g T \rangle_{k_S} \\ &\sim \langle \delta_g(k_S) [\delta_e(k_S) v(k_L)] \rangle_{k_S} \\ &\sim \langle \delta_g(k_S) \delta_e(k_S) \rangle_{k_S} v(k_L)\end{aligned}$$

$$\left(T_{\text{KSZ}} \sim \delta_e v \right)$$

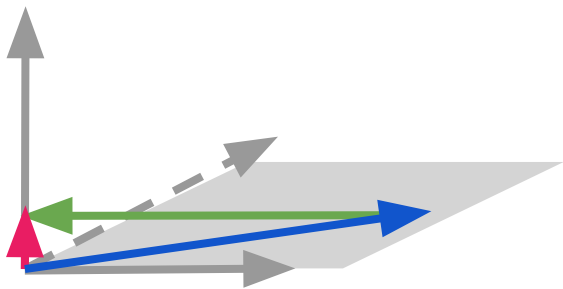
$$\sim v(k_L) \int dk_S P_{ge}(k_S)$$

Cosmology

Astrophysics

Scale-independent
number \mathbf{b}_v

- $\langle ggT \rangle$ kSZ tomography: includes
 - pairwise momentum
 - template method
 - velocity matched filter
 - **velocity reconstruction**



- An especially illuminating framework for cosmology is **velocity reconstruction**
- Cosmic velocity extracted from quadratic combination of galaxy positions (from BOSS, DESI, LSST) together with CMB temperature $v \sim \langle gT \rangle$
- 3D Velocity reconstruction then auto-correlated and cross-correlated with galaxy survey
- The cross-correlation with the galaxy survey $\langle vg \rangle$ realizes one possible projection of the bispectrum $\langle gv \rangle \rightarrow \langle ggT \rangle$

After velocity reconstruction, we have two probes of matter density

$$v = \frac{b_v f a H}{k} \delta_m$$

With some
reconstruction noise

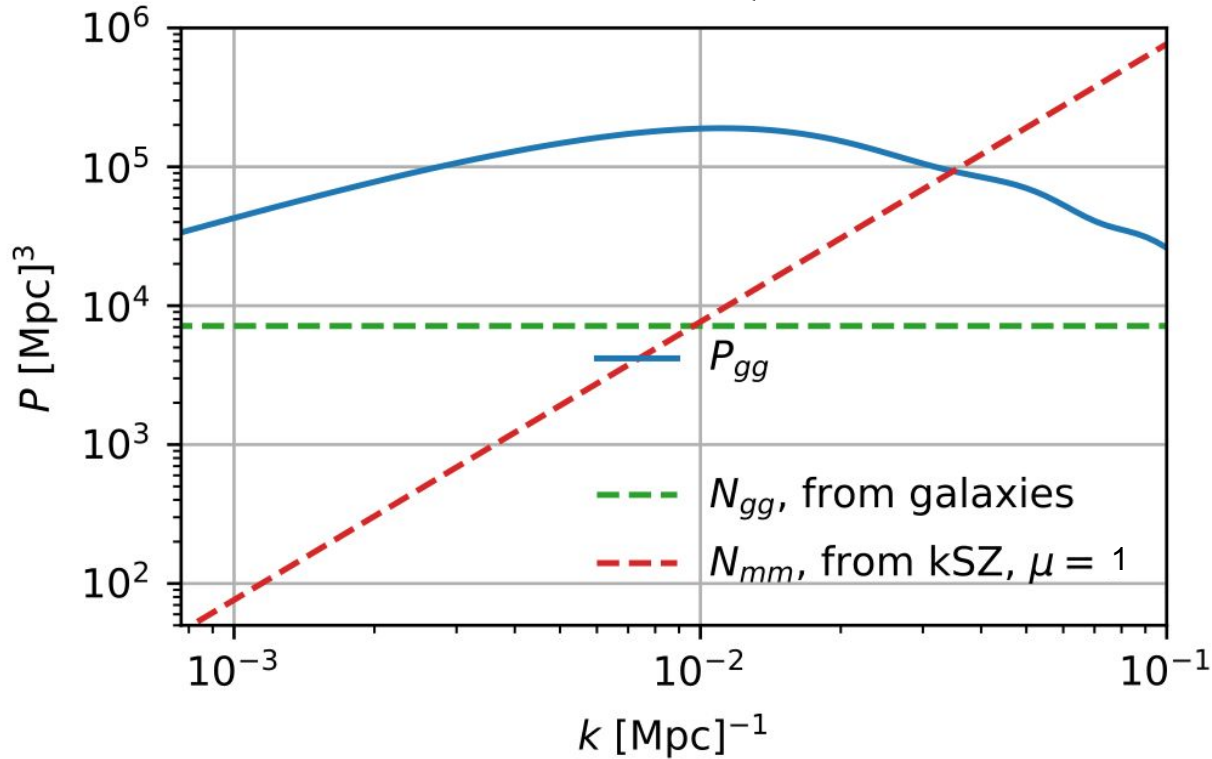
$$\delta_g = b_g \delta_m$$

With some shot noise

How does the noise compare between velocities and galaxies?

Squeezed limit noise is white

Convert noise on velocity to noise on matter density with k^2



$$\delta_g = b_g \delta_m$$

$$v = \frac{faH}{k} \delta_m$$

kSZ Velocities outperform galaxy clustering at large scales!

Recap!

kSZ tomography measures the **largest scale density modes**

Up to an unknown **scale-independent** normalization (“tau”)

With much lower noise than galaxy surveys!

Both galaxy and velocity surveys are signal dominated and hence **sample variance limited** at large scales.

New application: primordial non-Gaussianity (f_{NL})

Munchmeyer, MM++ 2018 arXiv:1810.13424

Moritz
Munchmeyer



Simone
Ferarro



Matt
Johnson



Kendrick
Smith



f_{NL}

Amplitude of non-gaussianity predicted generally in multi-field inflation models to be $O(1)$

$$\Phi_{\text{NG}} = \Phi_{\text{L}} + f_{\text{NL}}\Phi_{\text{L}}^2$$

Current best constraints:

$\sigma(f_{\text{NL}}) \sim 5$ from Planck CMB

Exhausted by sample variance

f_{NL} from scale-dependent galaxy bias b_g

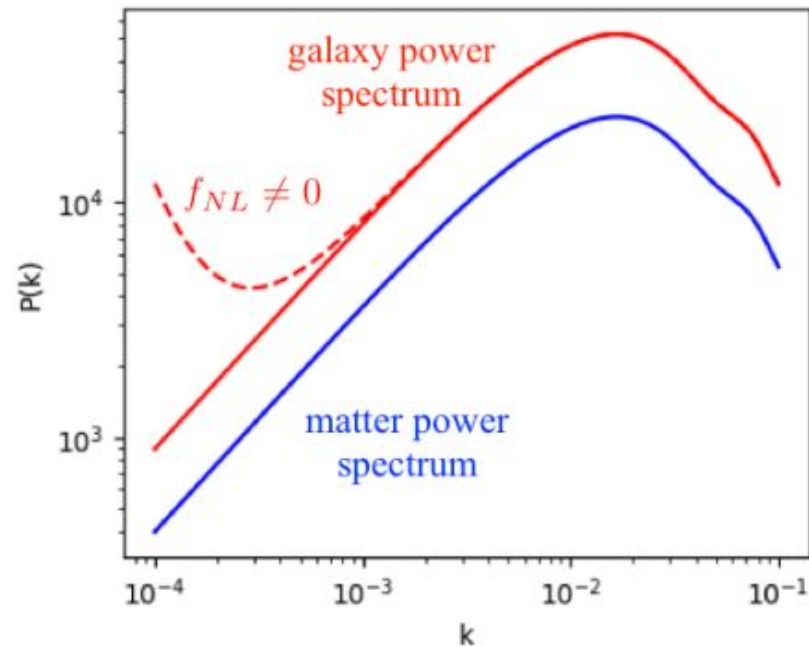
Another physical effect: **excess galaxy clustering** at large scales (Dalal++ 2008)

Galaxy surveys hope to measure bias at large scales

But constraints limited by sample variance (few modes at large scales)

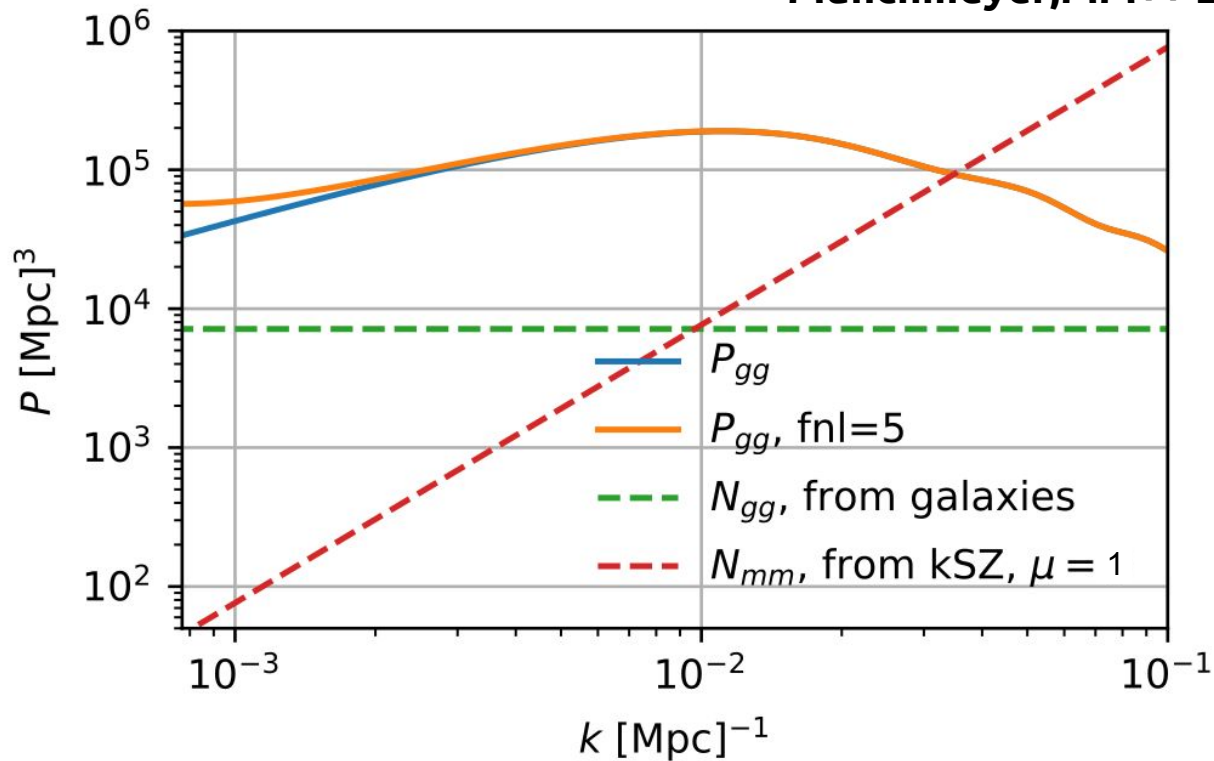
$\sigma(f_{NL}) \sim 1.5$ forecast for LSST

$\sigma(f_{NL}) < 1$ interesting models ruled out



Clustering of galaxies is scale-dependent on large scales in certain multi-field models of inflation, parameterized by f_{NL}

Munchmeyer, MM++ 2018



$$\delta_g = b_g \delta_m$$

$$v = \frac{b_v f a H}{k} \delta_m$$

Idea: ratio of (kSZ-)velocities and galaxies contains no matter field

$$v = \frac{b_v f a H}{k} \delta_m$$

With some
reconstruction noise

$$\delta_g = b_g(f_{\text{NL}}, k) \delta_m$$

With some shot noise

- Sample variance cancelled! Can measure bias **without sample variance**.
- Arbitrary improvement with CMB and galaxy survey noise improvement.
- Effectively done by measuring all auto and cross-correlations: **P_{gg}, P_{gv}, P_{vv}**
- **Not affected by scale-independent astrophysics (τ) marginalization!**

3x improvement in f_{NL} from CMB-S4 kSZ + LSST

Galaxy clustering (LSST)	Galaxy clustering + kSZ velocities
P_{gg}	$P_{\text{gg}}, P_{\text{gv}}, P_{\text{vv}}$
$\sigma(f_{\text{NL}}) = 1.5$	$\sigma(f_{\text{NL}}) = 1.0$
	$\sigma(f_{\text{NL}}) = 0.5$

Simons
Observatory

CMB-S4

Larger improvement than similar method from CMB lensing (Schmittful, Seljak 2016) due to better correlation

3x improvement in f_{NL} from CMB-S4 kSZ + LSST

Galaxy clustering (LSST)	Galaxy clustering + kSZ velocities
P_{gg}	$P_{\text{gg}}, P_{\text{gv}}, P_{\text{vv}}$
$\sigma(f_{\text{NL}}) = 1.5$	$\sigma(f_{\text{NL}}) = 1.0$
	$\sigma(f_{\text{NL}}) = 0.5$

Simons
Observatory

CMB-S4

Extremely robust measurement possible -- does not need galaxy auto!

Growth rate? (f)

MM++ 2019 arXiv:1901.02418

Nick
Battaglia



Kendrick
Smith



Jon
Sievers



What about the growth rate f ?

$f(k,z)$ constrains neutrino mass, dark energy, modified gravity

Amplitude $f(z)$ is degenerate with “optical depth” amplitude

$$v = \frac{b_v f a H}{k} \delta_m \quad b_v \sim \int dk_S w(k_S) P_{ge}(k_S)$$

Breaking this degeneracy requires an external measurement of **P_{ge}**

Breaking tau degeneracy requires predicting P_{ge}

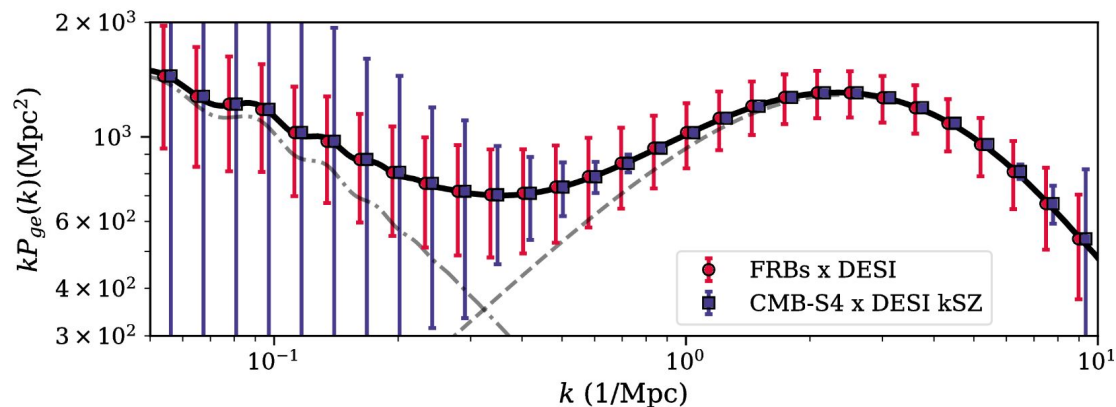
A data driven approach is to look for other effects that depend on **free electron density** and cross-correlate with the kSZ galaxy sample

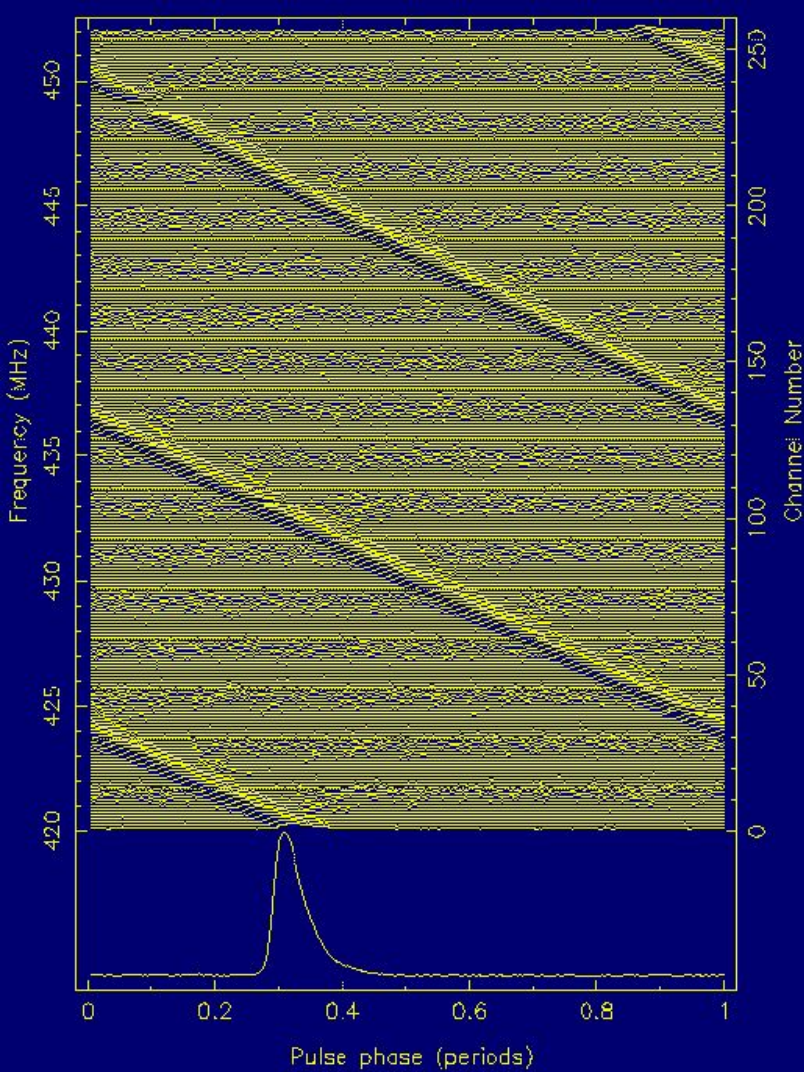
Breaking tau degeneracy requires predicting P_{ge}

A data driven approach is to look for other effects that depend on **free electron density** and cross-correlate with the kSZ galaxy sample

An ambitious possibility is:

Dispersion measures of Fast Radio Bursts (FRBs)



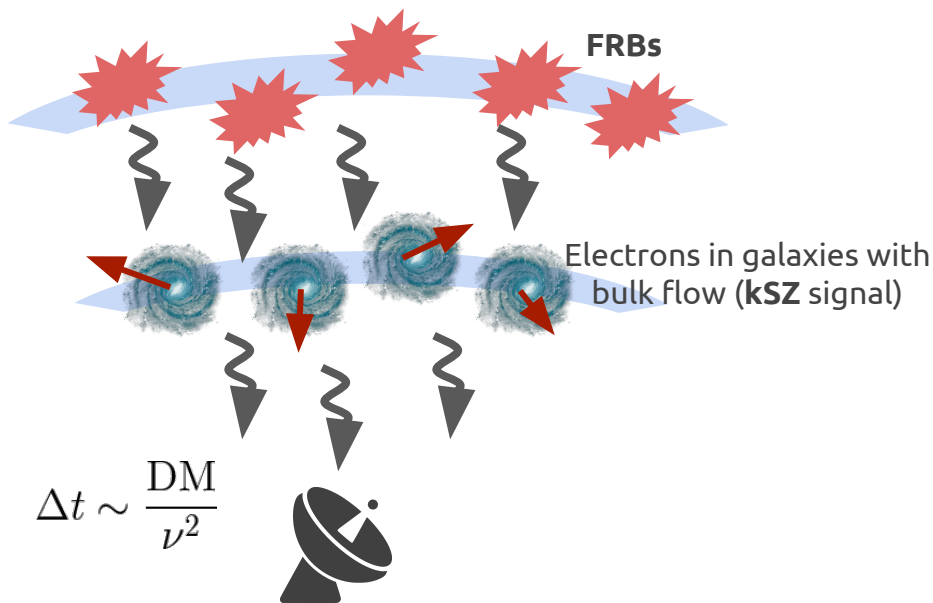


Radio waves from energetic sources interact with intervening ionized matter and undergo dispersion

$$\Delta t \sim \frac{DM}{\nu^2}$$

Higher frequencies push past free electrons and arrive earlier

Potentially **large number** of energetic sources at cosmological distances - **FRBs**



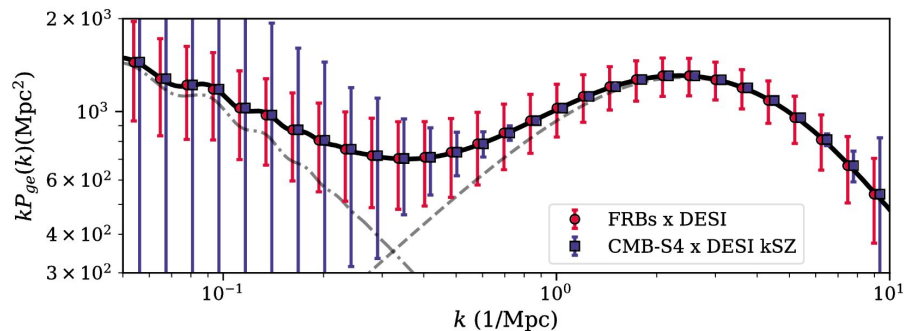
$$DM(\vec{n}) = \int_0^{\chi_f} d\chi (1+z) \delta_e(\vec{n}, z)$$

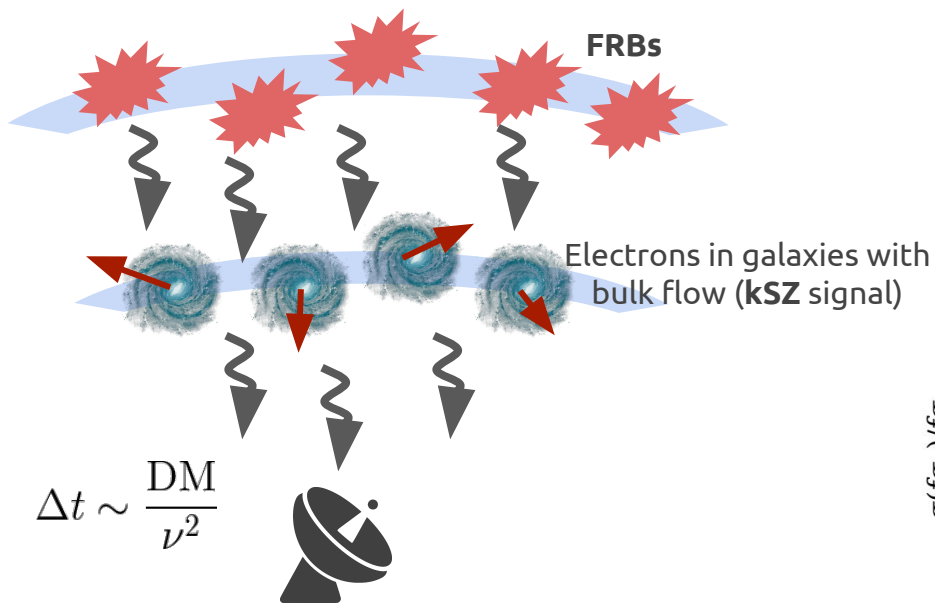
$$DM(\vec{n}) \times \delta_g(\vec{n}) \sim P_{ge}(k_S)$$

Breaking tau with FRBs

MM, Battaglia, Smith, Sievers arxiv:1901.02418

- FRB frequency-dependence of time delay depends on intervening electron density
- One contribution is electrons in galaxies whose “optical depth” we want to measure (apart from host galaxy and Milky Way)
- Cross-correlate DMs with galaxies used in kSZ estimator

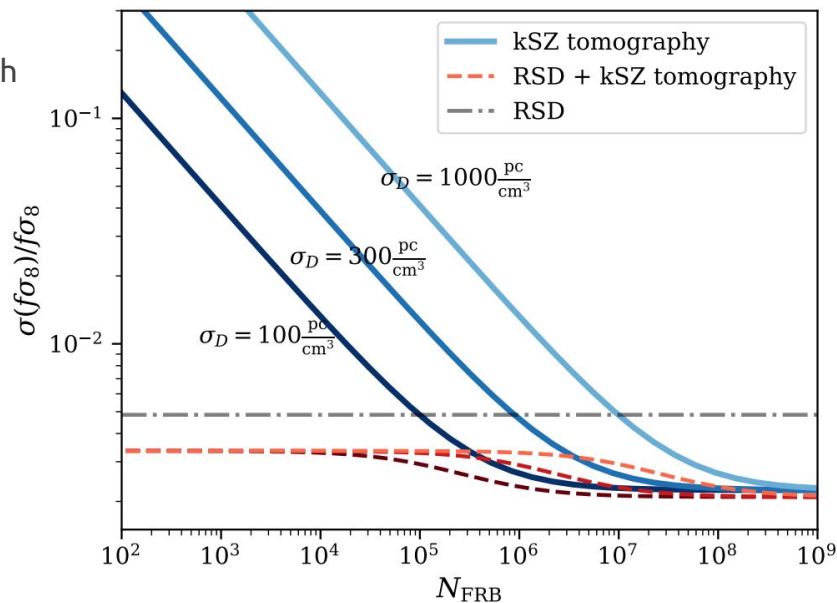




$$DM(\vec{n}) = \int_0^{\chi_f} d\chi (1+z) \delta_e(\vec{n}, z)$$

$$DM(\vec{n}) \times \delta_g(\vec{n}) \sim P_{ge}(k_S)$$

Breaking tau with FRBs



MM, Battaglia, Smith, Sievers arxiv:1901.02418

Feedback and lensing

(work in progress)

Emmanuel
Schaan



Nick
Battaglia



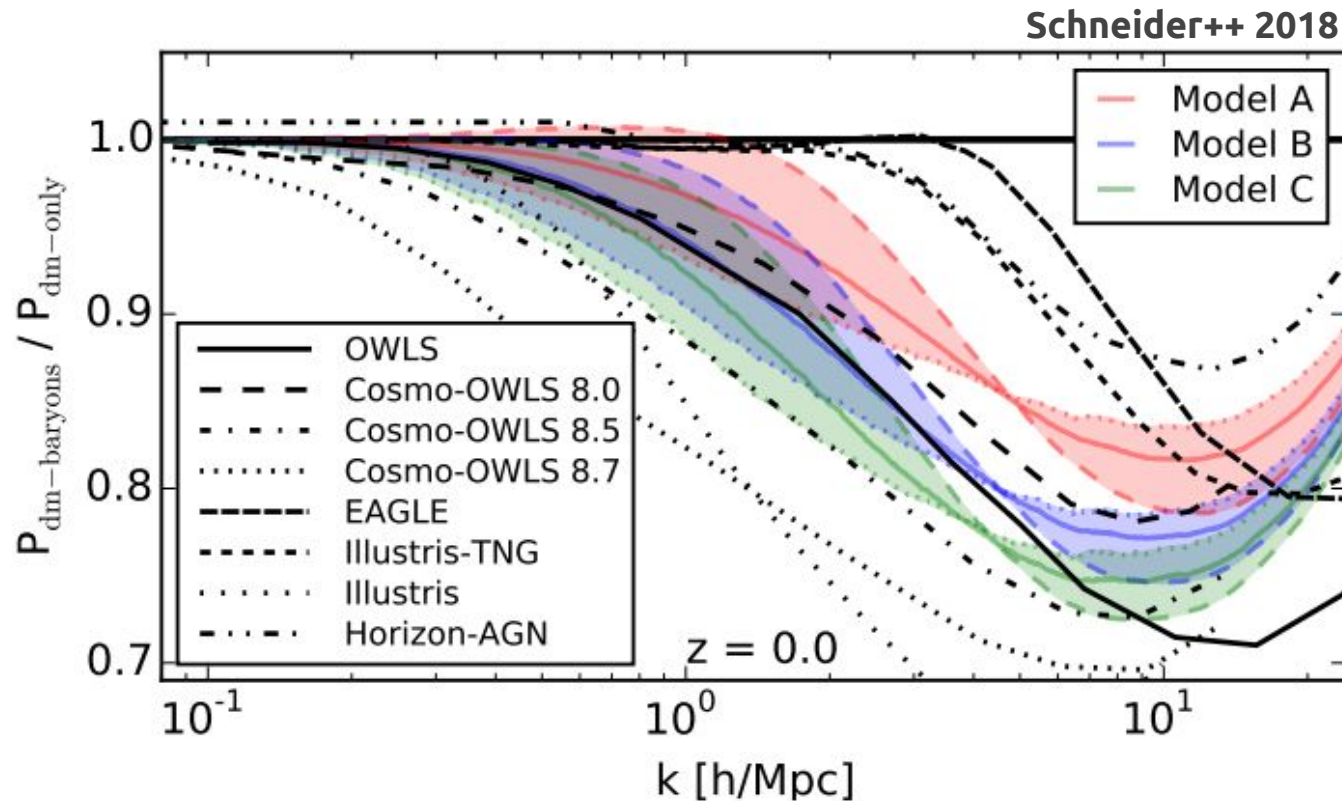
Simone
Ferro



Colin Hill

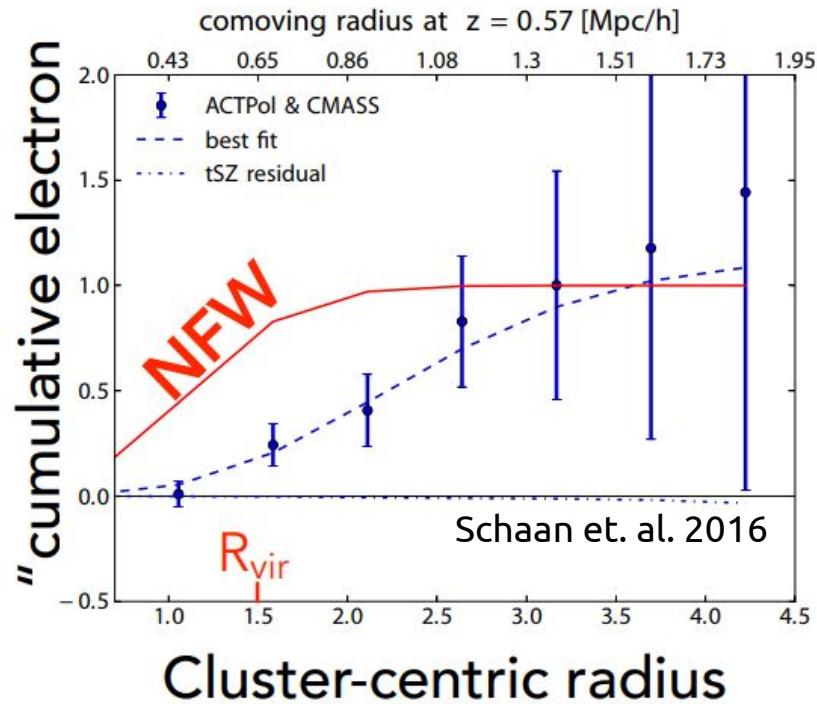


Matter power spectrum impacted by baryonic feedback



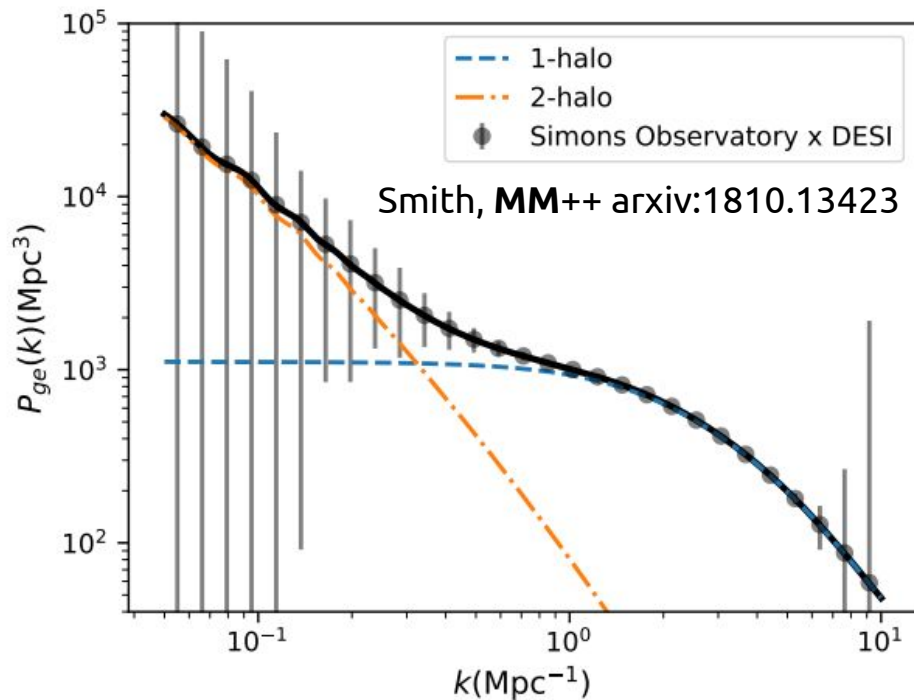
$$\delta_m = \delta_{\text{cdm}} \frac{\Omega_{\text{cdm}}}{\Omega_m} + \delta_{\text{gas}} \frac{\Omega_{\text{gas}}}{\Omega_m} + \delta_s \frac{\Omega_s}{\Omega_m}$$

Puffiness of gas seen in kSZ measurements

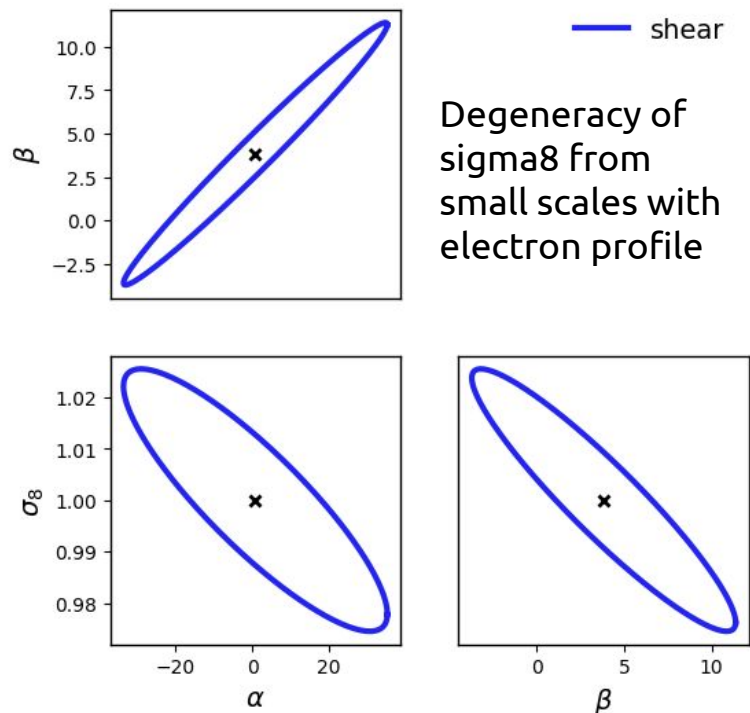


Plot from **Emmanuel Schaan** (kSZ detection)

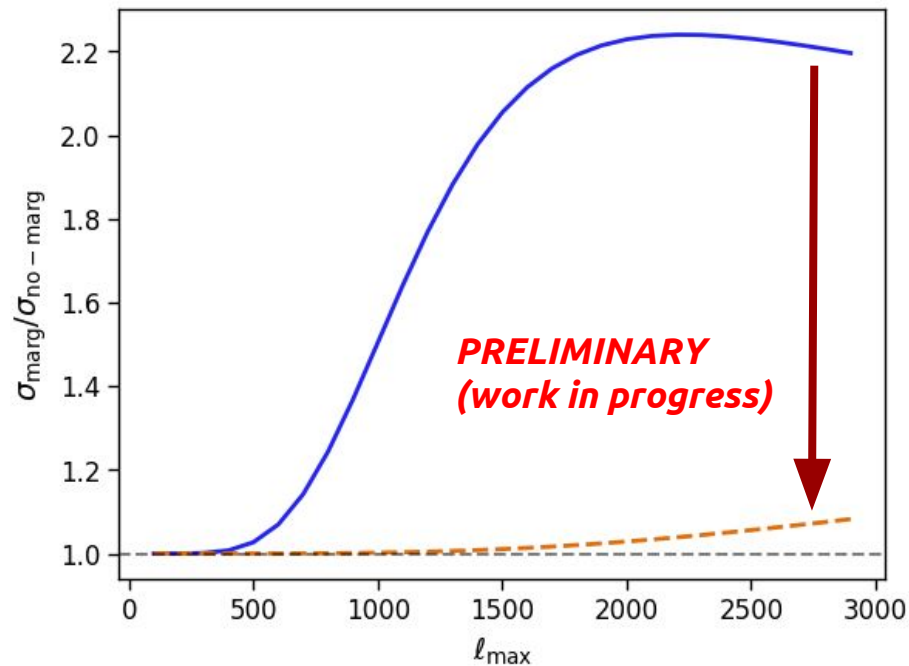
kSZ will constrain the gas (electron) profile



Which can translate to improvements on cosmology



with Emmanuel Schaan, Nick Battaglia, Simone Ferraro, Colin Hill



Improvement on σ_8 from 5% constraint on electron profile parameters

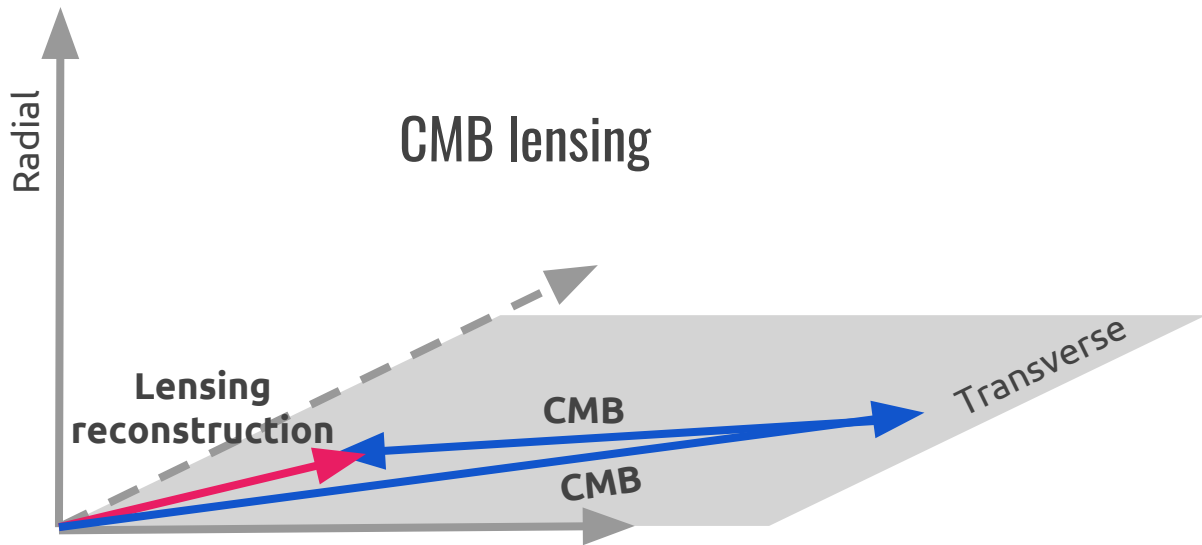
Conclusion

— — —

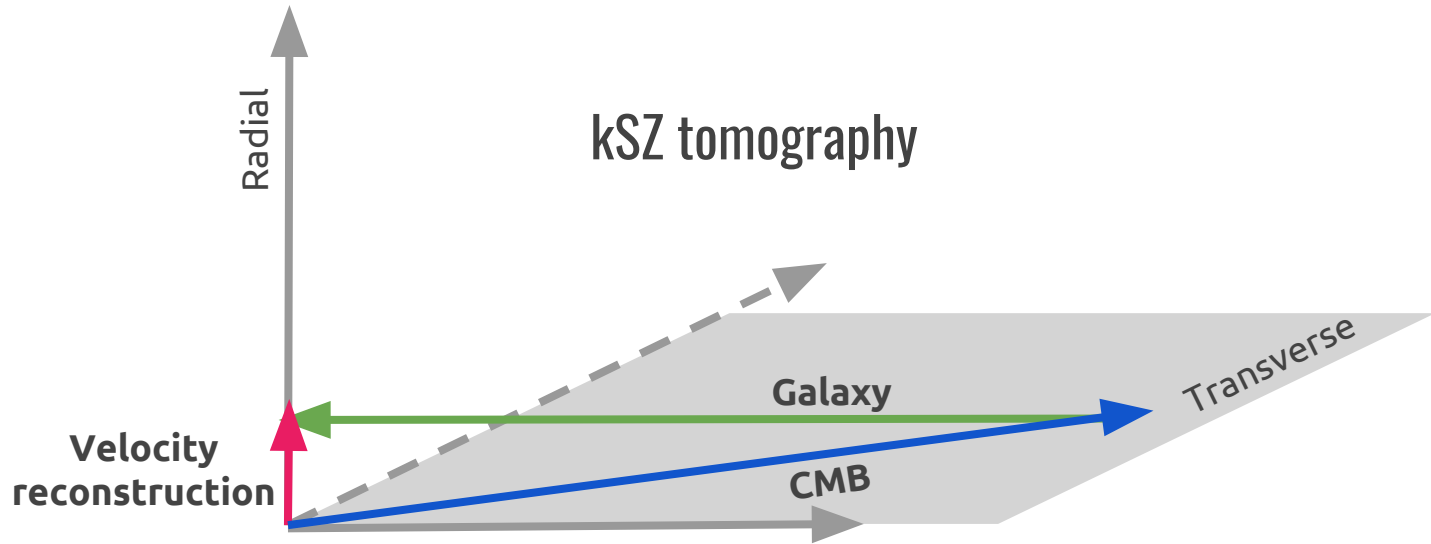
- Optical depth (τ) factors out as **scale-independent** uncertain amplitude
- kSZ velocity reconstruction does better than clustering at large scales
- Cosmological applications
 - Improves non-Gaussianity σ_8 through **scale-dependent bias** by 3x for CMB-S4 + LSST probing multi-field inflation
 - **Amplitude of growth** rate is perfectly degenerate with τ , but degeneracy can potentially be broken with localized **FRB** dispersion measures
 - Robustly include smaller scales in **cosmic shear** and galaxy-galaxy lensing with kSZ measurements of electron profile

Thank you!

Bonus slides

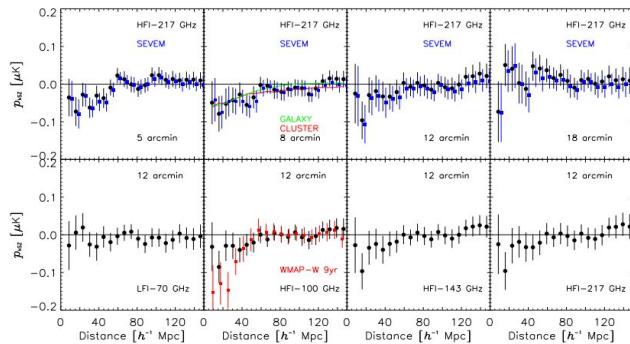
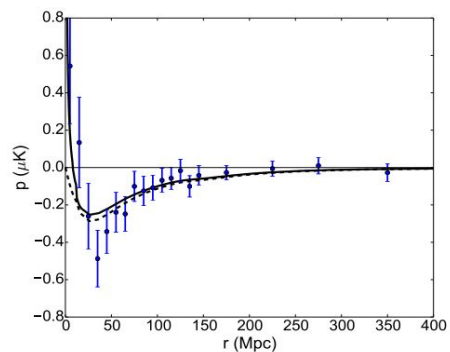
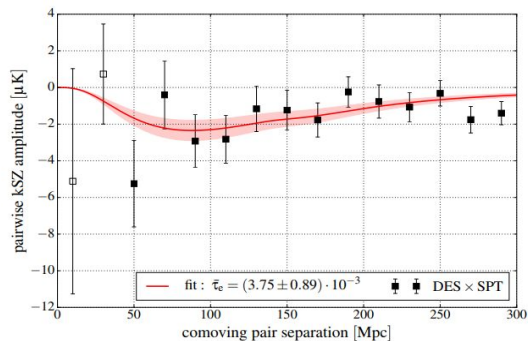
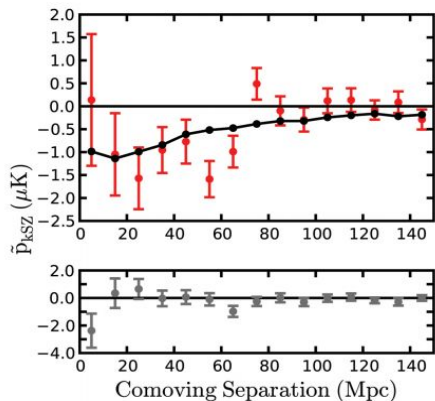


$$\hat{\phi}(L) = \langle TT \rangle_{\ell}$$



$$\langle v(k_L) \delta_g(k_S) T(\ell) \rangle$$

Bonus slide: pairwise kSZ detections



Step 2: cross-correlate velocity with galaxy pos.

$$\langle \hat{v} \delta_g \rangle = \langle \langle \delta_g T \rangle_{k_S} \delta_g \rangle \sim \langle \langle \delta_g (v \delta_e) \rangle_{k_S} \delta_g \rangle$$

$$\sim \underbrace{P_{gv}(k_L)}_{\text{Cosmology}} \int \underbrace{dk_S P_{ge}(k_S)}_{\text{Astrophysics}}$$

Astrophysics
Scale-independent
number

