# Cosmic Structure in the Age of Machine Learning: Rethinking Hydrodynamical Simulations

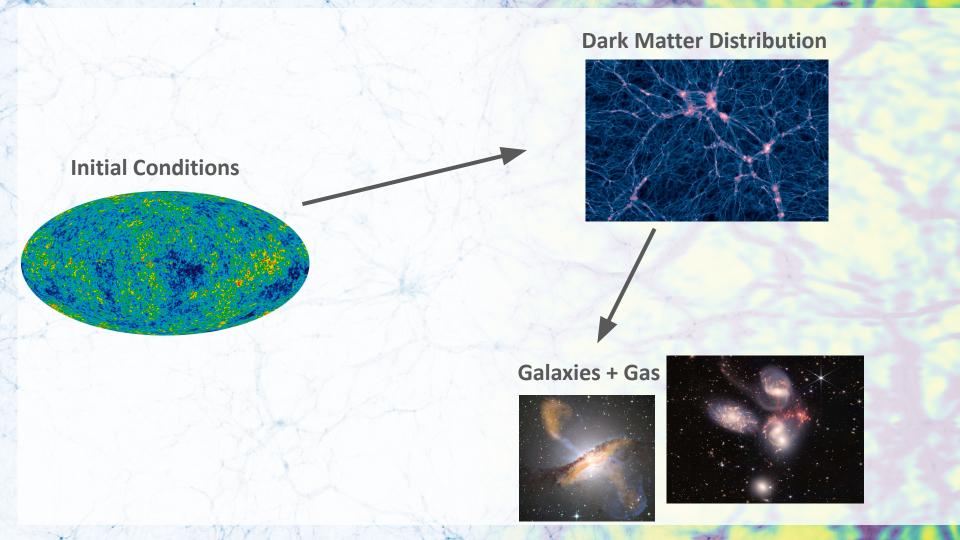
Benjamin Horowitz

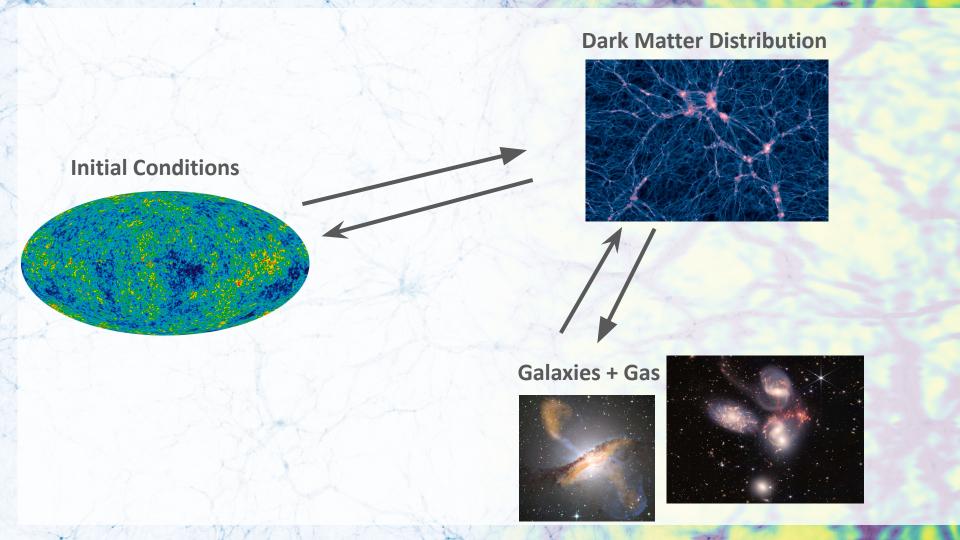
Kavli Fellow IPMU

View online with animations here



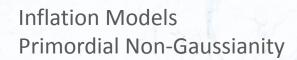




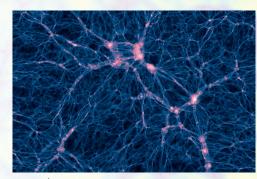


### Dark Energy Nature/Evolution General Relativity

### **Initial Conditions**



### **Dark Matter Distribution**



Galaxy Evolution/Formation
Thermal History of Gas







### **Outline**

1) Large-Scale Structure and Baryons: A high-z (Lyman-a)and low-z example (tSZ)

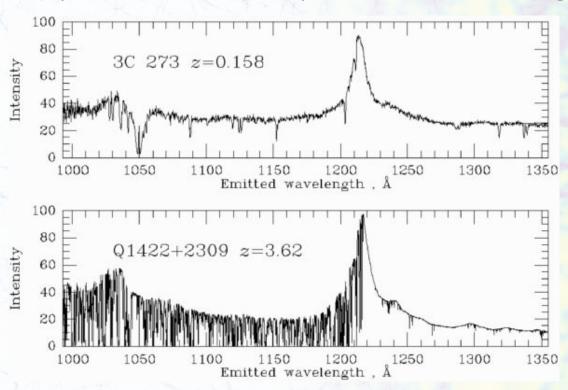
2) Cosmological Hydrodynamical Simulations

3) Machine Learning as a New Computational Paradigm

4) Unifying ML and Hydrodynamical Simulations with a Field Level Approach

### A High Redshift Example: Lyman-a Forest

Nearby (low-z) quasars have fewer absorption lines than distant (high-z) quasars

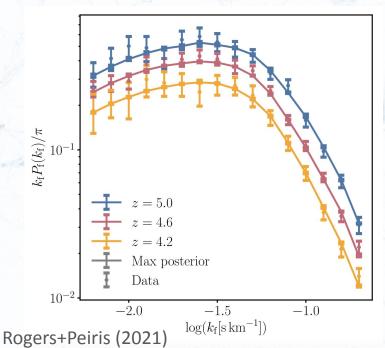




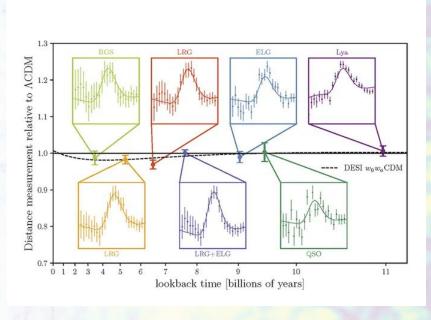
### Lyman Alpha as a Cosmological Probe

If neutral hydrogen/flux is a function of density, can use absorption as a tracer of clustering → constrain physics which effects clustering

### **Warm Dark Matter**



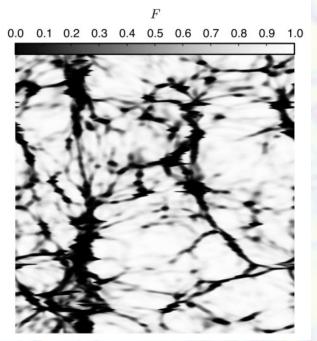
### **Cosmic Expansion**



**DESI** (2024)

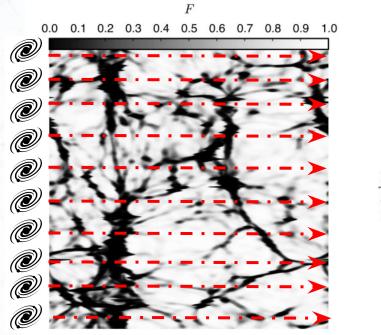
# Lyman Alpha Tomography: Unique Probe of z~2 Universe

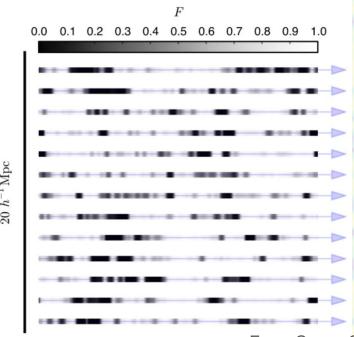
Basic Idea: Observe lots of lines of sight in small area and then interpolate/extrapolate between absorptions on various of lines of sight. (Pichon+2001, Caucci+2008, Lee+2014)



### Lyman Alpha Tomography: Unique Probe of z~2 Universe

Basic Idea: Observe lots of lines of sight in small area and then interpolate/extrapolate between absorptions on various of lines of sight. (Pichon+2001. Caucci+2008. Lee+2014)

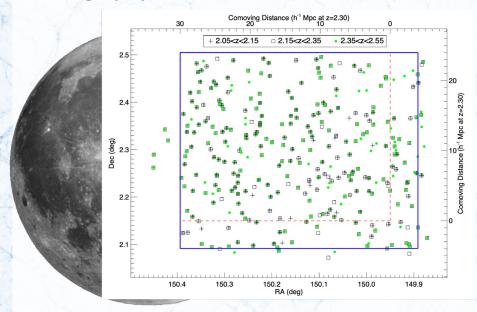




From Casey Stark

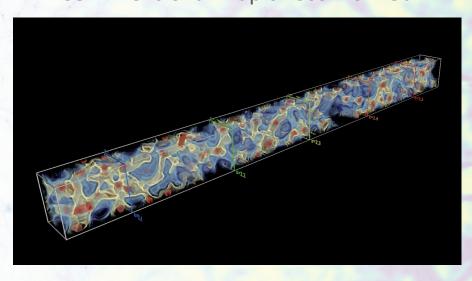
### **Applied to Data: COSMOS Field**

COSMOS Lyman Alpha Mapping and Tomography Observations (CLAMATO)

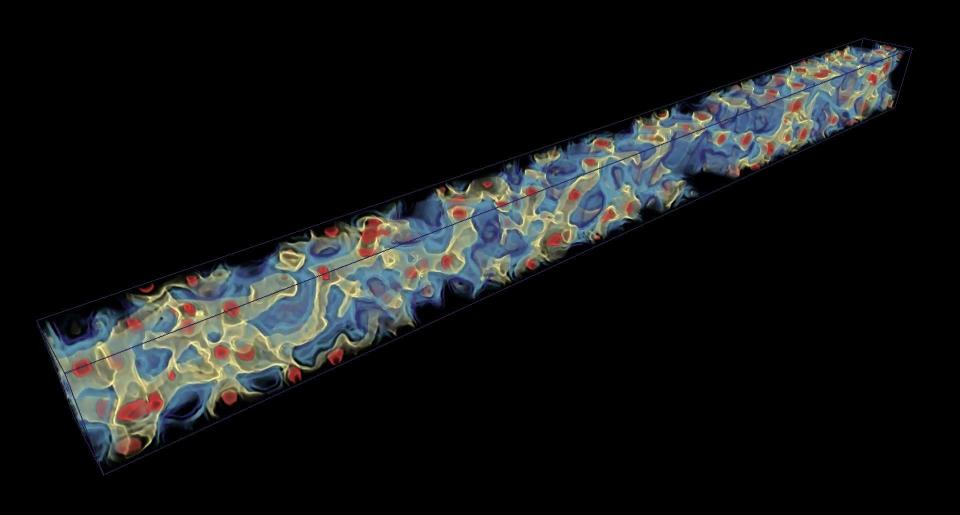


320 background sources in COSMOS field

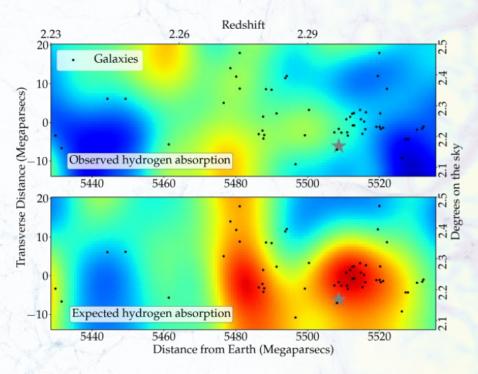
Three Dimensional Map of Cosmic Web



Lee et al. (2016), BH et al. (2023)

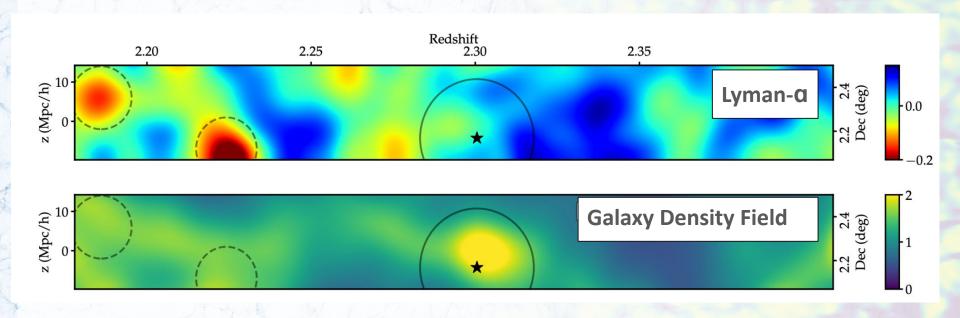


### Discrepancy between Galaxy Fields and Flux Fields



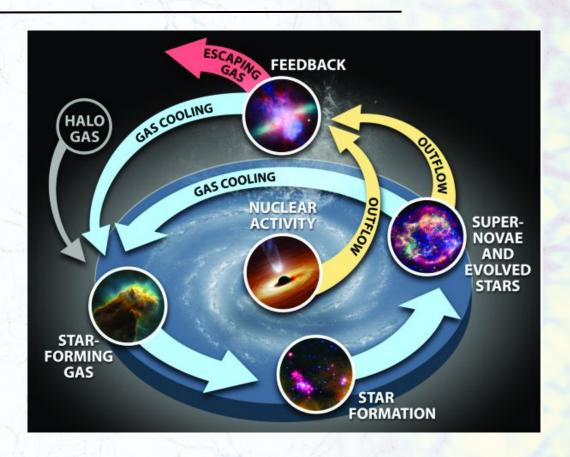
There exist a lot of clusters which appear in either galaxy or Lyman-a, but not both!

### Discrepancy between Galaxy Fields and Flux Fields



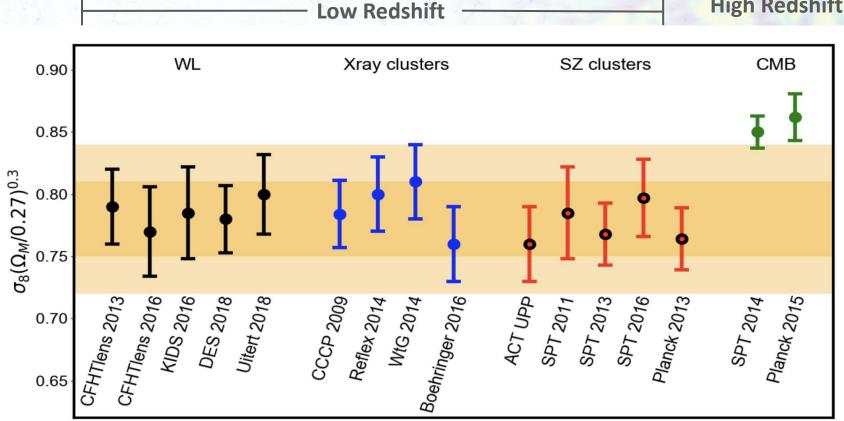
There exist a lot of clusters which appear in either galaxy or Lyman-a, but not both!

### **Feedback and Baryon Cycle**

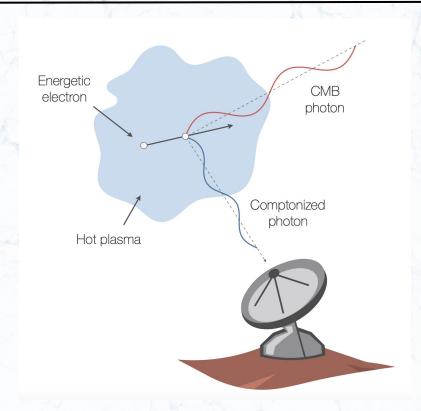


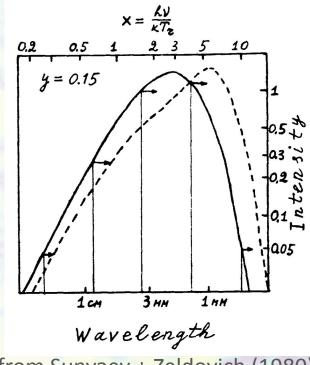
### A low-z Example: Sigma 8 Tension and tSZ

Inferred from High Redshift



### One Example: Thermal Sunyaev Zeldovich Effect





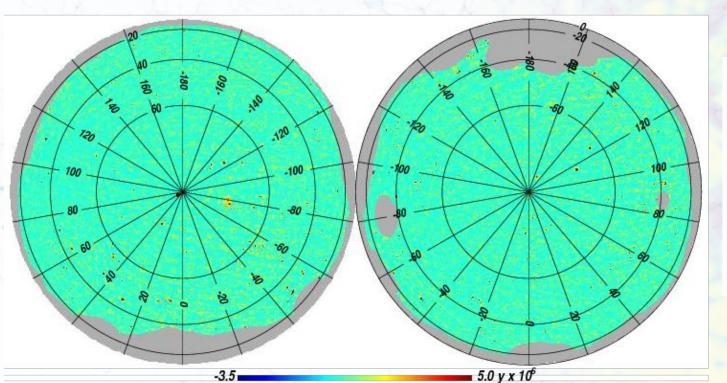
from Sunyaev + Zeldovich (1980)

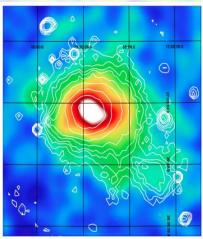
Mroczkowski, Nagai, Basu, Chluba et al. (2019)

### tSZ Effect: Compton y-map

NILC tSZ map

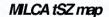
Planck 2015 (Aghanim, et al.)

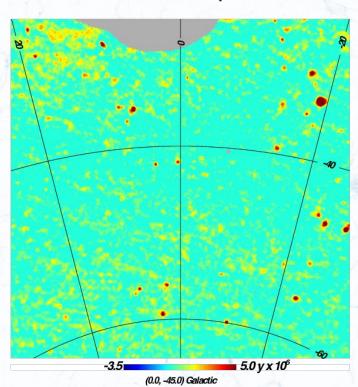




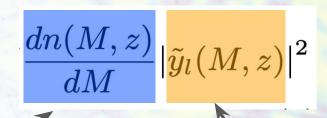
Coma Cluster tSZ

### **Thermal Sunyaev Zeldovich Effect: Halo Model**



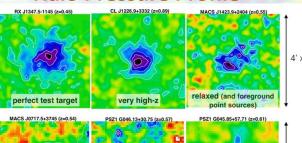


Total "power" of tSZ comes from clusters across different masses at different redshifts:



Halo Mass Function (Cosmology)

### **Halo Pressure Profile**



Planck SZ-discovered: follow-up

4' x 4

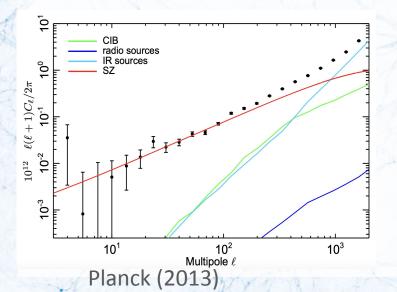
NIKA (Macías-Pérez et al. 2019)

### **Thermal Sunyaev Zeldovich Effect: Power Spectra**

Add up all halos across all redshifts and mass ranges, weighted by pressure/geometry

$$C_l^{1-halo} = \int_{z_{low}}^{z_{max}} dz \frac{d^2V}{d\Omega dz} \int_{M_{min}}^{M_{max}} dM \frac{dn(M,z)}{dM} |\tilde{y}_l(M,z)|^2$$

**Volume Factor (Geometry)** 



Halo Mass Function (Cosmology)

Halo Pressure Profile (Baryon Physics)

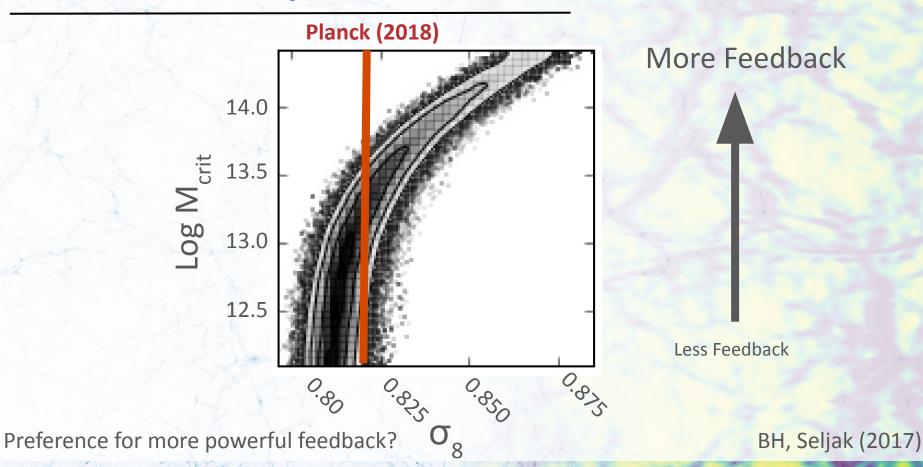
Modelling Pressure Profile with Feedback:

$$y_l^{\text{new}}(x, r_{\text{vir}}) = f_{\text{gas}} y_l^0(x) + (1 - f_{\text{gas}}) y_l^{\text{feedback}}(x, r_{\text{vir}})$$

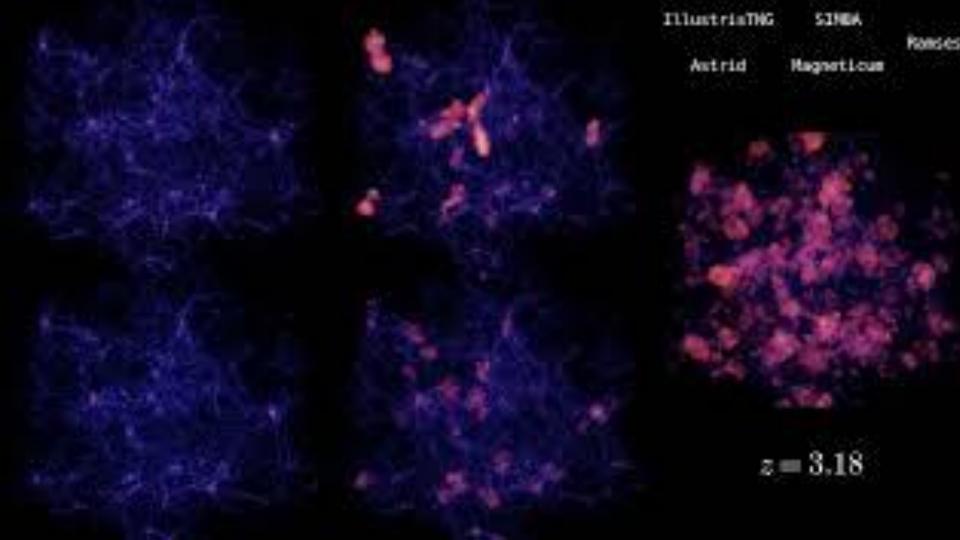
Parametrization:

$$f_{\text{gas}}(M_{halo}, M_{crit}) = \frac{1}{1 + \left(\frac{M_{crit}}{M_{halo}}\right)^2}$$

# tSZ: Likelihood analysis with Planck Data



# Can simulations provide insight?



# **Components of a Hydrodynamical Simulation**

1) Dark Matter evolution

2) Gas evolution

3) "Subgrid Physics" (i.e. anything not in Navier-Stokes Equations)

### **Dark Matter Evolution**

Collisionless Boltzmann Equation/Vlasov Equation for phase space distribution (f):

$$\frac{\partial f}{\partial t} + \frac{1}{ma^2} \mathbf{p} \cdot \nabla f - m \nabla \phi \cdot \frac{\partial f}{\partial \mathbf{p}} = 0$$

Can solve this numerically by sampling phase space and using Hamilton's Equations:

Position: 
$$\frac{d\mathbf{x}_i}{dt} = \frac{1}{a}\mathbf{u}_i$$
 Velocity: 
$$\frac{d(a\mathbf{u}_i)}{dt} = \mathbf{g}_i$$

Lots of tricks to calculate g efficiently (particle-mesh, octotree, etc.)



### **Hydrodynamics**

### **Euler Equations:**

(Comoving coordinates, single energy formalism)

$$\begin{aligned} & \mathcal{D}^{ensity} \frac{\partial \rho_b}{\partial t} = -\frac{1}{a} \nabla \cdot (\rho_b U) \\ & \mathcal{D}^{ensity} \frac{\partial (a \rho_b U)}{\partial t} = -\nabla \cdot (\rho_b U U) - \nabla p + \rho_b \mathbf{g} \end{aligned}$$

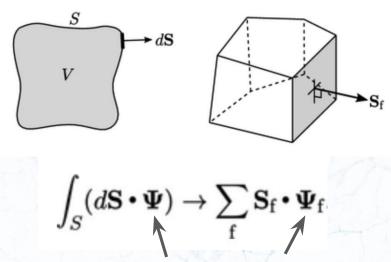
$$= -\nabla \cdot (\rho_b U U) - \nabla p + \rho_b \mathbf{g}$$

$$= -a \nabla \cdot (\rho_b U E + p U) + a(\rho_b U \cdot \mathbf{g})$$

Describes the change in density, pressure/internal energy, and momenta of a gas

### **Discretize and Solve (Eulerian)**

### Break up domain into discrete blocks:



State Vector (Density, Momentum, Energy)

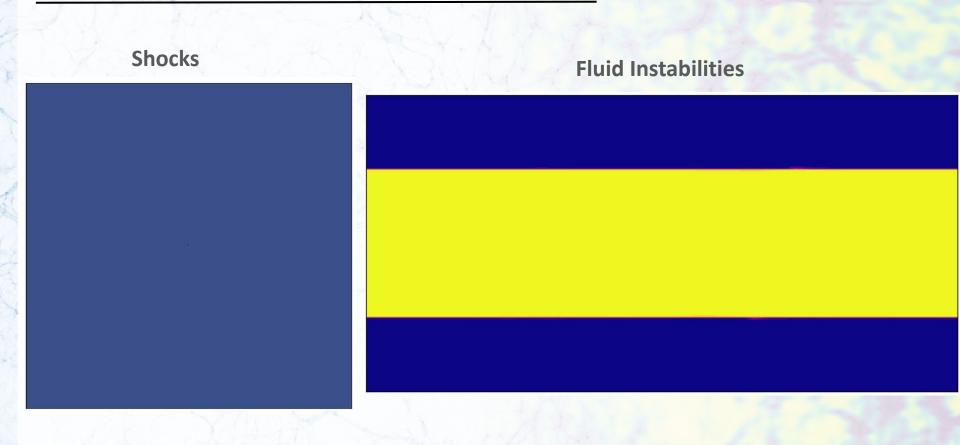
Turns every timestep into a series of linear operations:

$$\frac{\partial \mathbf{\Psi}}{\partial t} + \nabla \cdot (\mathbf{u}\mathbf{\Psi}) + \nabla \cdot (\Gamma \nabla \mathbf{\Psi}) = S_{\mathbf{\Psi}}$$

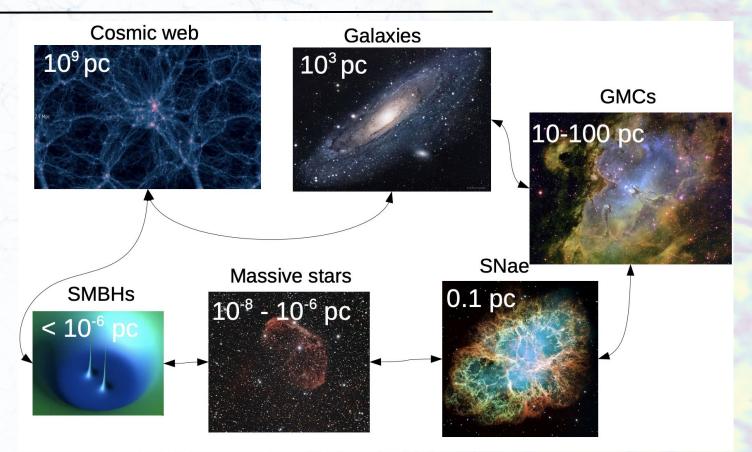
$$\begin{bmatrix} \star \star \star \star \star \\ \star \star \star \star \star \\ \star \star \star \star \end{bmatrix} \begin{bmatrix} \mathbf{\Psi} \end{bmatrix} = \begin{bmatrix} \star \\ \star \\ \star \end{bmatrix}$$

Actual choices of how to best break up these terms are quite complex...

# **Hydrodynamics**



# **Subgrid Physics**



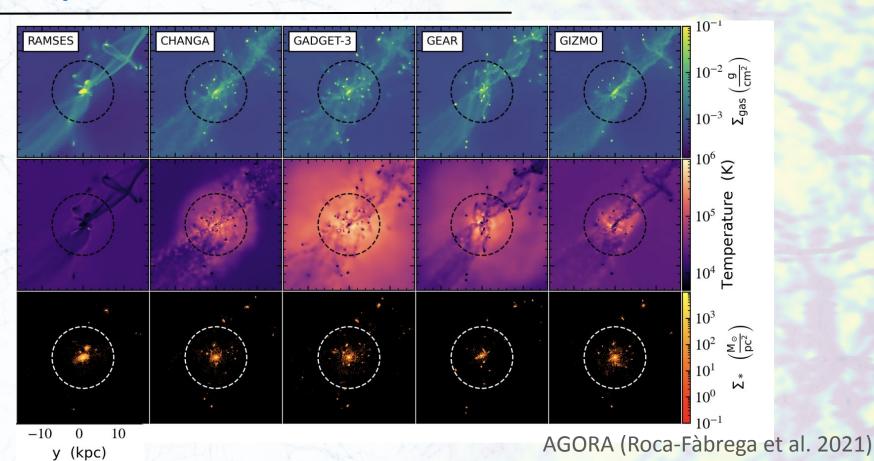
# **Subgrid Physics**

Lots of possible subgrid physics to include:

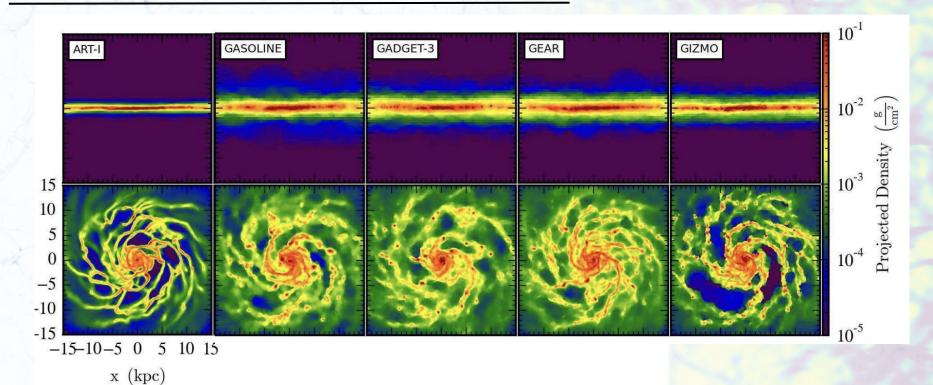
- Metal heating/cooling
- 2) Star Formation
- 3) Active Galactic Nuclei
- 4) MHD
- 5) Cosmic Rays
- 6) Galactic Inflow/Outflow
- 7) Subgrid turbulence

Many others...

### **Hydrodynamical Simulations: Inconsistencies at Small Scales**



# **Hydrodynamical Simulations: Inconsistencies at Small Scales**

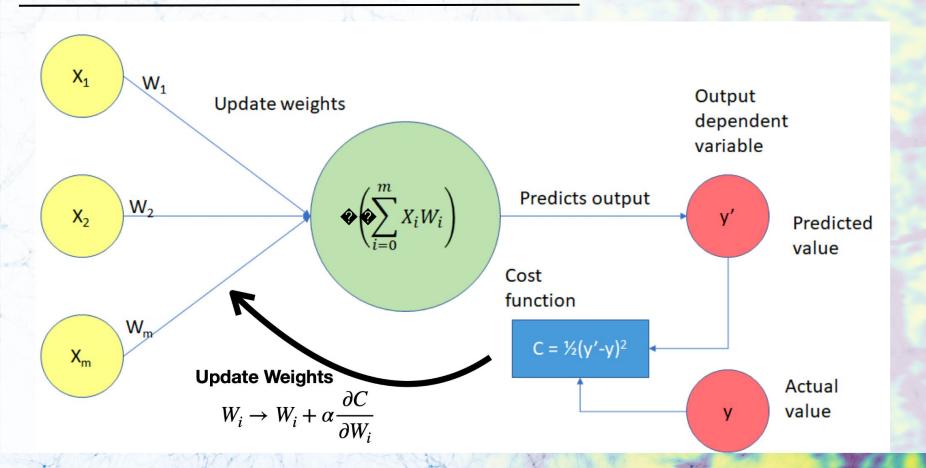


# Can machine learning help?

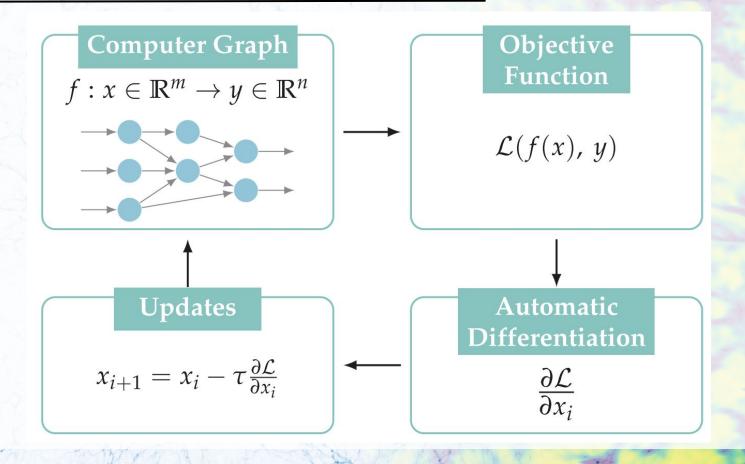
# **Machine Learning Revolution**

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### **Neural Network : Training a Regression Model**



### More Broadly: Differentiable Programming



### Role of (Deep) ML in Simulation-Based Cosmology

- Direct Regression/Inference: Train models on existing simulations and apply directly to data.
  - Models don't know what they aren't trained on... need to know systematics EXACTLY (see BH, Melchior 2022)

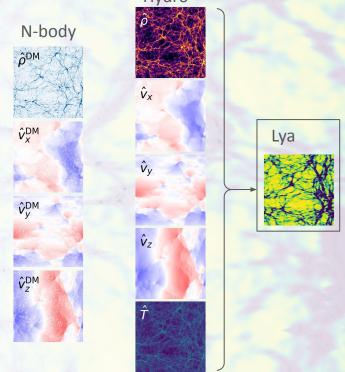
2) **Generation/Surrogate Modelling**: Use ML tools to generate additional simulations to apply "traditional" techniques.

3) **Integrated Approach**: Leverage ML tools within traditional simulations to allow new types of inference.

# **Surrogate Model Approach**

Finding a reliable method to reconstruct hydrodynamic quantities from N-body simulations has been a long-standing research goal

Hydro

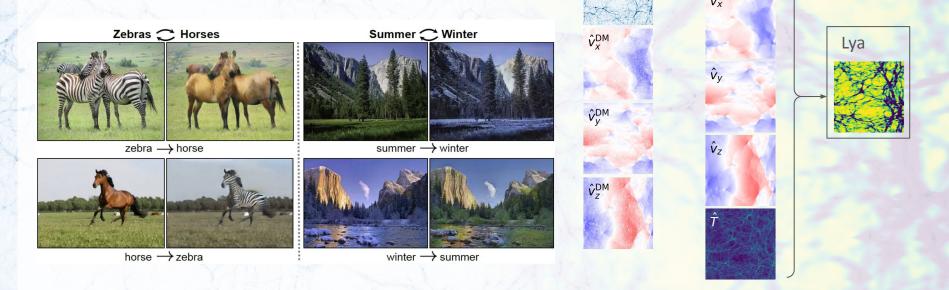


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Hydro

Do it with neural networks of course!

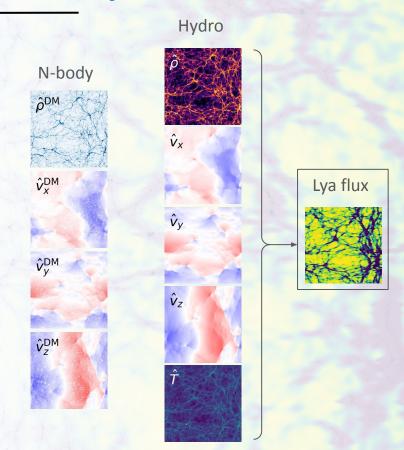
Image translation models are great candidates



N-body

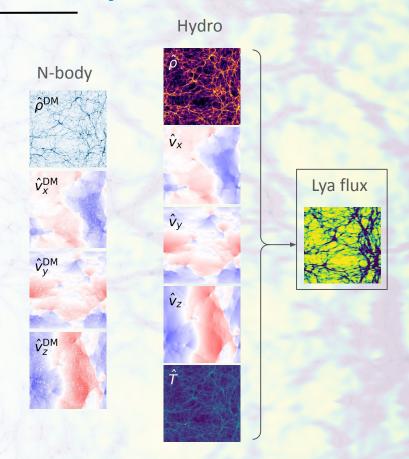
### Three approaches:

1. Adversarial U-Net: deterministic approach
Reconstruct hydro fields, focus on accuracy in Lya
(Harrington ++ BH, 2021)



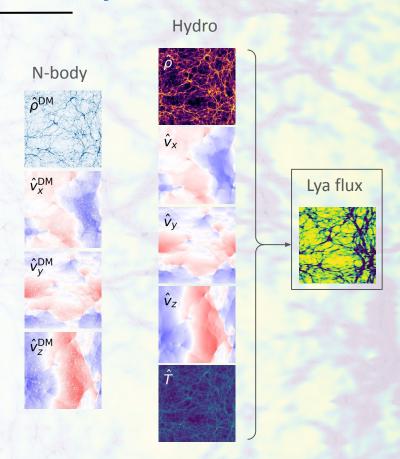
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### Three approaches:

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- 2. HyPhy: variational approach with a CVAE
  Reconstruct posterior over hydro fields, allowing for uncertainty quantification in mapping
  (BH+ 2022)
- Stochastic Interpolants Model
   Uncertainty estimation + better reconstruction fidelity
   (BH + 2025)

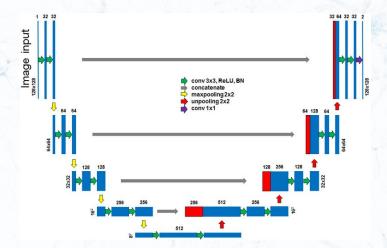


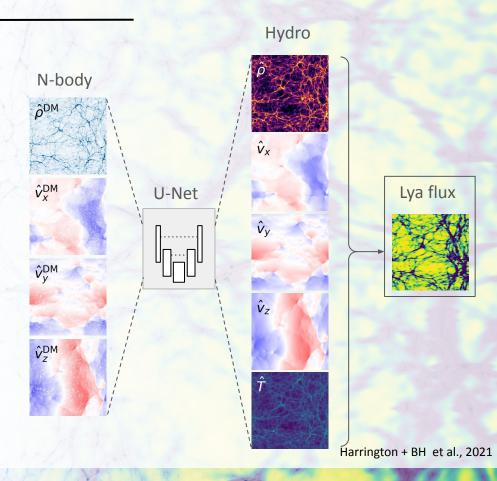
### N-body → Hydro

### **Generative modeling task:**

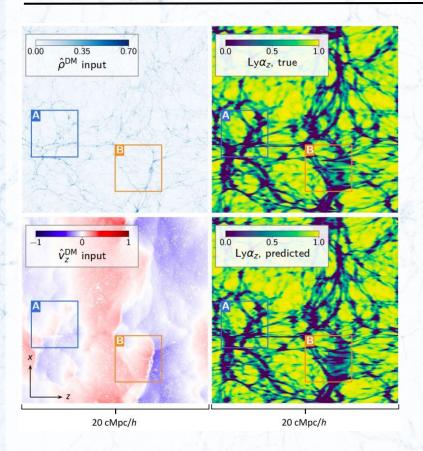
Accurately reproduce Lya flux from N-body simulation

Following <u>pix2pix</u> design, generation of output fields handled by U-Net architecture:

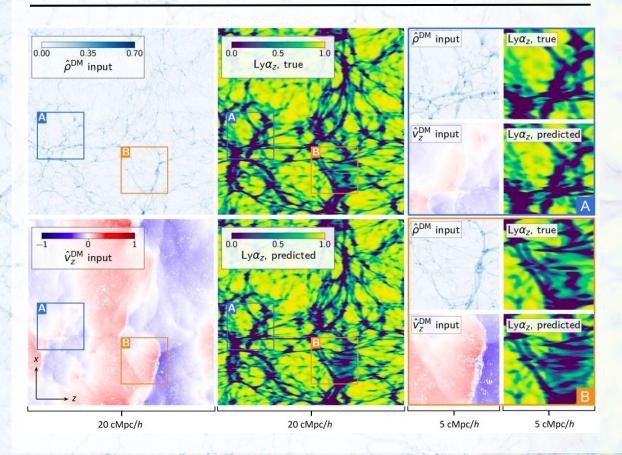




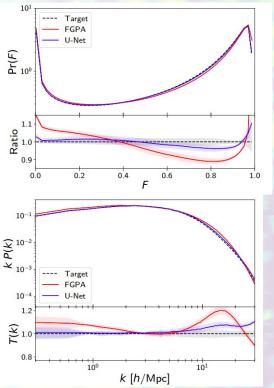
### N-body → Hydro: Lya reconstructions



### N-body → Hydro: Lya reconstructions

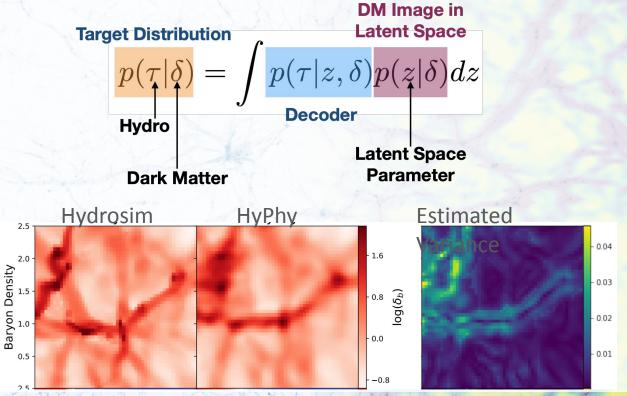


### **Summary Statistics**

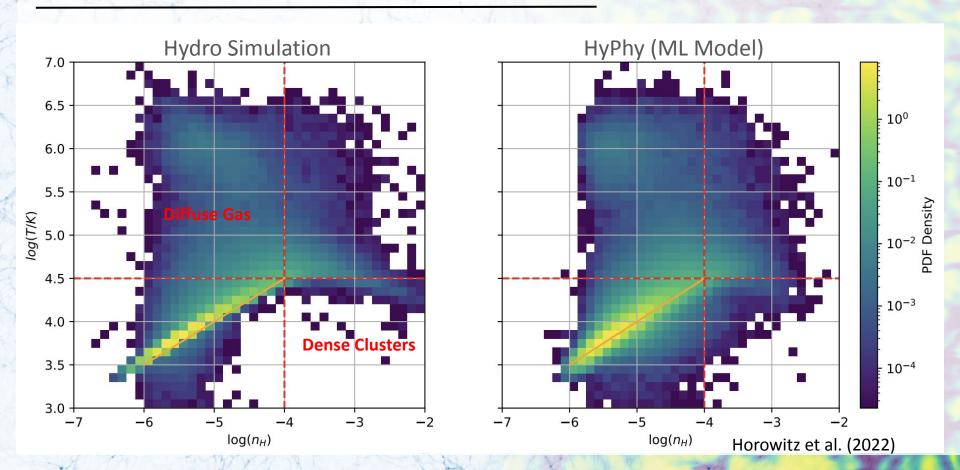


### **Extend to Include Uncertainty Estimation: HyPhy**

Can implement latent space implementation in variational auto-encoder or diffusion model approach.

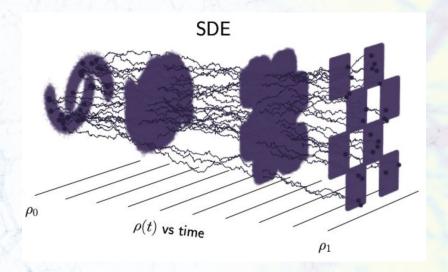


### **Uncertainty Quantification Allows Diffuse Gas Recon**



### The Future: Stochastic Interpolants with Score-Based Diffusion

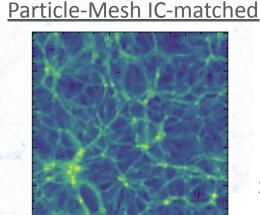
Learn the solution to a stochastic differential equation mapping from an input to a target distribution.

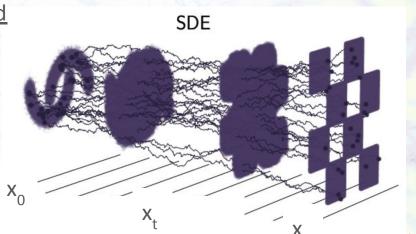


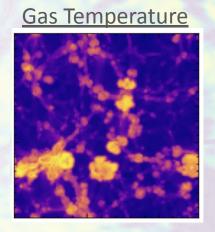
### **BaryonBridge: Stochastic Interpolants**

Learn the solution to a stochastic differential equation mapping from an input to a target distribution.

We will map to fully hydrodynamic CAMELS simulations from particle-mesh realizations generated from same ICs. Conditional on cosmological and astrophysical parameters.







Random/latent variables

$$x_t = (1 - t)x_0 + tx_1 + \sqrt{2t(1 - t)}z^{t}$$

ICML2025: ML4Astro

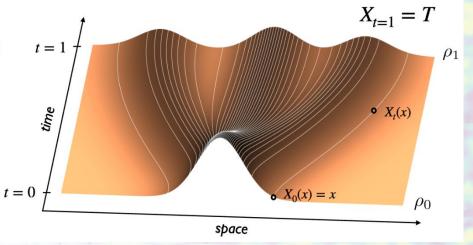
w/ Omar Yehia (IPMU), Carolina Cuesta (MIT)

### **Continuous Transport Realizations**

 $X_t$  flow map given by velocity field b(t,x)

$$X_{t=0}(x) = x \in \mathbb{R}^d$$

$$\dot{X}_t(x) = b(t, X_t(x))$$



Transport equation

$$\partial_t \rho(t, x) + \nabla \cdot (b(t, x)\rho(t, x)) = 0, \quad \rho(t = 0, \cdot) = \rho_0$$

If 
$$\rho(t)$$
 solves TE, then  $\rho(t=1,\cdot)=\rho_1$ 

Stochastic case generalizes to Fokker-Planck Equation

### **Interpolant Function**

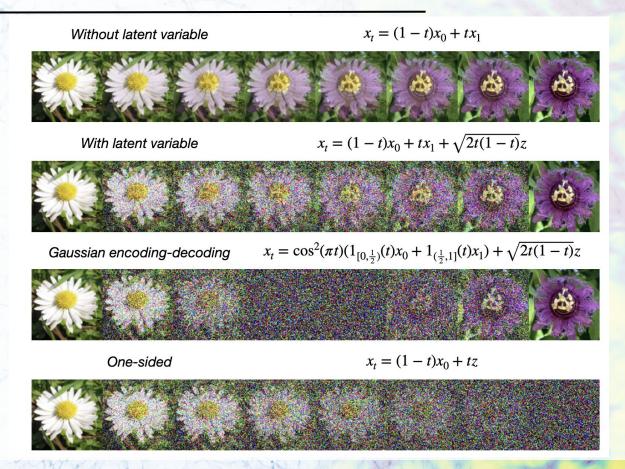
### **Interpolant** Function $I(t, x_0, x_1)$

- A function of  $x_0$ ,  $x_1$ , and time t with b.c.'s:  $I_{t=0} = x_0$  and  $I_{t=1} = x_1$
- Example:  $I(t, x_0, x_1) = (1 t)x_0 + tx_1$

If  $x_0$ ,  $x_1$  drawn independently, then  $I(t, x_0, x_1)$  is a stochastic process which samples  $x_t \sim \rho(t, x)$ 

$$\rho(t,x) = \mathbb{E}_{\rho_0,\rho_1} \left[ \delta \big( x - I(t,x_0,x_1) \big) \right]$$
 Interpolant Density

### **Interpolant Function**



### **Training Interpolant Functions**

The PDF  $\rho(t,x)$  satisfying the continuity equation has a velocity field b(t,x) which is the minimizer of a simple quadratic objective

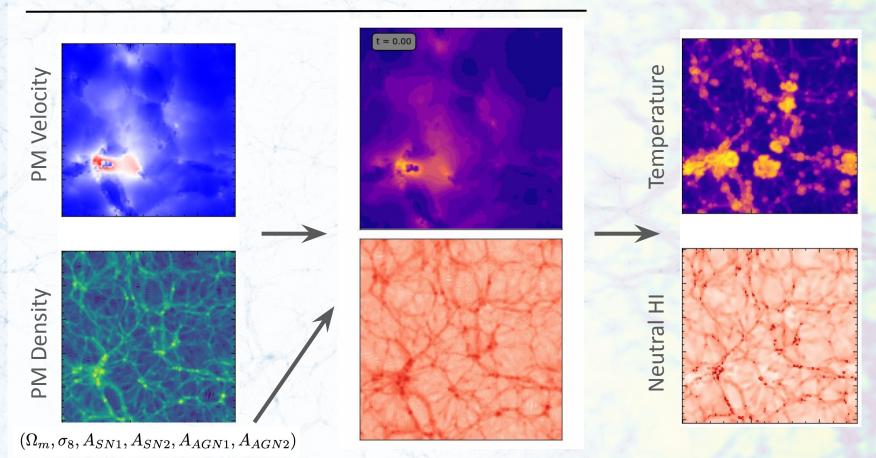
$$L[\hat{b}] = \min_{\hat{b}(t,x)} \int_{0}^{1} \mathbb{E}\left[|\hat{b}(t,x_{t}) - \partial_{t}I(t,x_{0},x_{1})|^{2}\right] dt$$

$$= \left(|\hat{b}(t,x_{t})|^{2} - 2\partial_{t}I(t,x_{0},x_{1}) \cdot \hat{b}(t,x_{t})\right) dt + \text{const}$$

where  $x_t = I(t, x_0, x_1)$ .

- Loss is directly estimable over  $\rho_0, \rho_1$
- Likelihood and sampling available via fast ODE integrators

## Stochastic Interpolation Model: Conditional with CAMELS sims nary

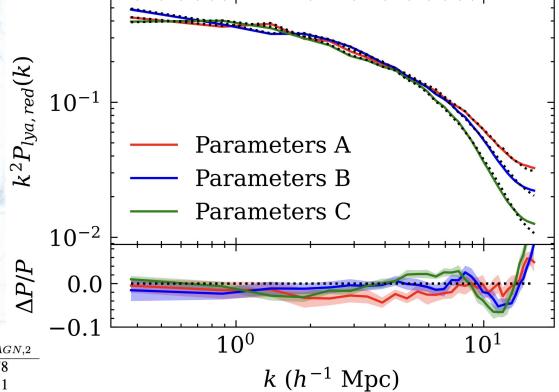


## Preliminary

### **Generalized Across Cosmology/Astrophysics**

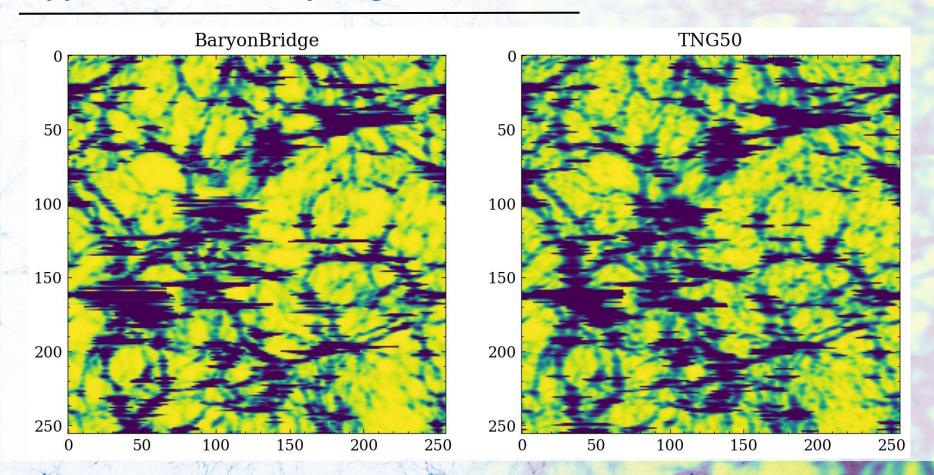
Map to 3d Lyman Alpha Forest w/ THALAS (Ding, BH, Lukic (2024))

Can also be used for field level inference, since ML model is differentiable...

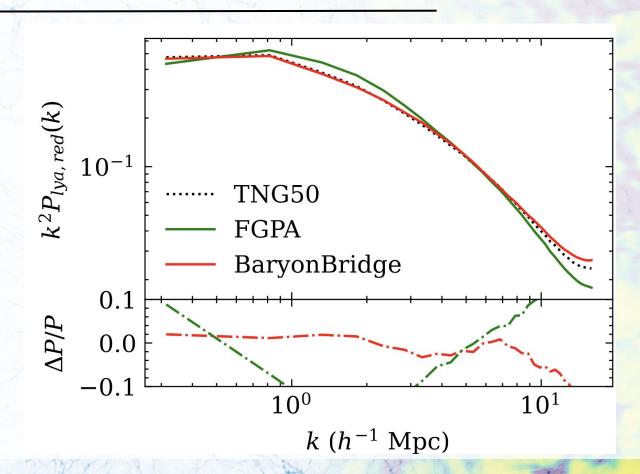


	$\Omega_m$	$\sigma_8$	$A_{SN,1}$	$A_{SN,2}$	$A_{AGN,1}$	$A_{AGN}$
Parameters A	0.46	0.87	3.81	0.70	1.50	1.78
Parameters B	0.22	0.79	0.82	0.27	0.55	1.11
Parameters A Parameters B Parameters C	0.14	0.68	2.34	2.83	0.79	0.54

### **Applied to Arbitrarily Large Volumes: CAMELS -> TNG50**

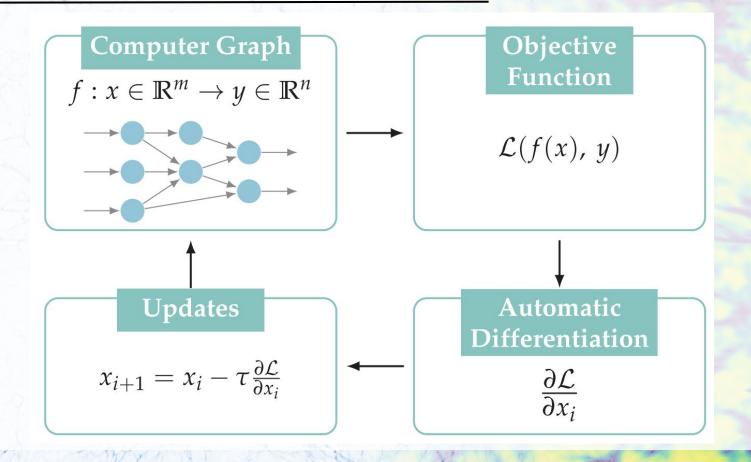


### Power Spectrum on TNG50 (large separate hydrosim)



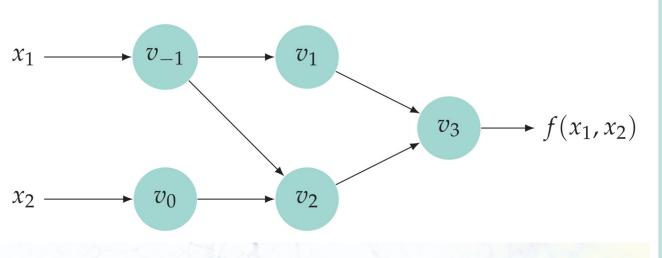
# Field Level Inference w/ Differentiable Programming

### **Differentiable Programming**



### **Automatic Differentiation**

Computational graph for simple function:  $y = f(x_1, x_2) = \sin(x_1) + x_1x_2$ 



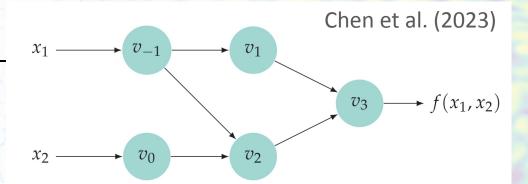
# Forward primal trace $v_{-1} = x_1 = 2$ $v_0 = x_2 = 1$ $v_1 = \sin v_{-1} = \sin 2$ $v_2 = v_{-1} \times v_0 = 2 \times 1$ $v_3 = v_1 + v_2 = 0.909 + 2$

 $= v_{3}$ 

= 2.909

### **Automatic Differentiation**

$$f(x_1, x_2) = \sin(x_1) + x_1 x_2$$



### Forward primal trace

$$v_{-1} = x_1 = 2$$

$$v_0 = x_2 = 1$$

$$v_1 = \sin v_{-1} = \sin 2$$

$$v_2 = v_{-1} \times v_0 = 2 \times 1$$

$$v_3 = v_1 + v_2 = 0.909 + 2$$

$$y = v_3 = 2.909$$

### Reverse derivative trace

$$\bar{x}_1 = \bar{v}_{-1}$$

$$\bar{v}_{-1}$$

$$\bar{x}_2 = \bar{v}_0$$

$$= 0.584$$

$$\bar{v}_{-1} = \bar{v}_1 \frac{\partial v_1}{\partial v_{-1}} + \bar{v}_2 \frac{\partial v_2}{\partial v_{-1}} = \bar{v}_1 \cos(v_{-1}) + \bar{v}_0 = 0.584$$

$$\bar{v}_0 = \bar{v}_2 \frac{\partial v_2}{\partial v_0} = \bar{v}_2 v_{-1}$$

$$= \bar{v}_2 v_{-1}$$

$$\bar{v}_1 = \bar{v}_3 \frac{\partial v_3}{\partial v_1} = \bar{v}_3 \times 1$$

$$=1$$

$$\bar{v}_2 = \bar{v}_3 \frac{\partial v_3}{\partial v_2}$$

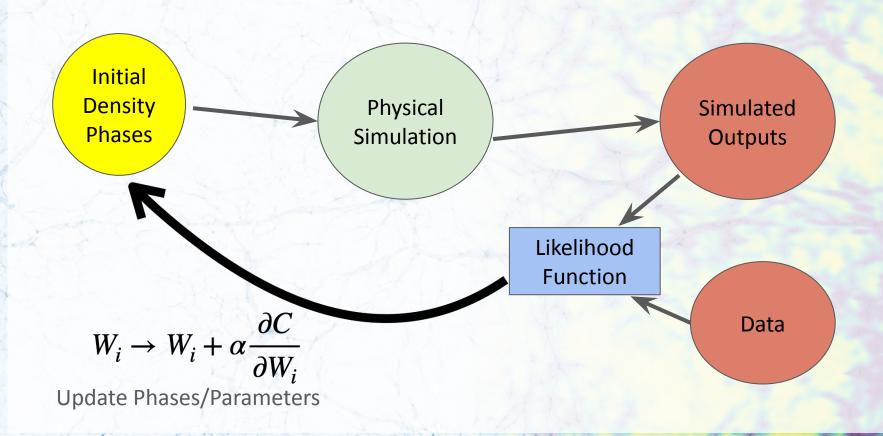
$$= \bar{v}_3 \times 1$$

$$= 1$$

$$\bar{v}_3 = \bar{y}$$

$$=1$$

### **Differentiable Cosmological Simulations**



### **Differentiable Dark Matter Evolution**

Small industry has developed for differentiable particle mesh codes:

code	OSS	gradient	mem efficient	hardware	2
BORG		analytic		CPU	 (Jas <mark>che &amp; Wandel</mark> t 2013)
ELUCID		analytic		CPU	(Wang et al. 2014,)
FastPM-vmad	$\checkmark$	AD		CPU	(Feng et al. 2016,)
FlowPM	$\checkmark$	AD		GPU/CPU	J (Modi et al. 2020)
pmwd	$\checkmark$	adjoint	$\checkmark$	GPU/CPU	J (Li et al. 2022)

Particle Mesh codes are lots of linear operations (including fast fourier transforms), so straightforward to differentiate.

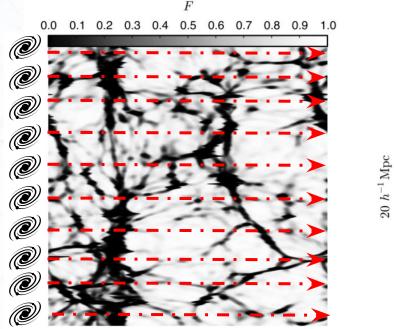
From Li et al. (2022)

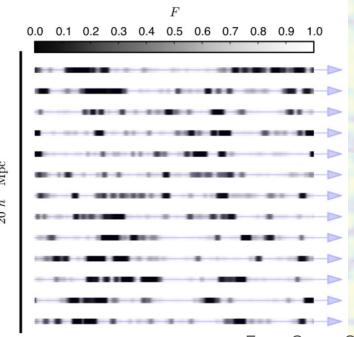
### **Differentiable Particle Mesh Dark Matter**

```
import tensorflow as tf
import numpy as np
import flowpm
cosmo = flowpm.cosmology.Planck15()
stages = np.linspace(0.1, 1.0, 10, endpoint=True)
100,
                                              # Physical size of the cube
                                              # Initial power spectrum
                                   ipklin,
                                   batch size=16)
# Sample particles
state = flowpm.lpt init(cosmo, initial conditions, a0=0.1)
# Evolve particles down to z=0
final state = flowpm.nbody(cosmo, state, stages, 32)
# Retrieve final density field
final_field = flowpm.cic_paint(tf.zeros_like(initial_conditions), final_state[0])
```

### Lyman Alpha Tomography: Unique Probe of z~2 Universe

Basic Idea: Observe lots of lines of sight in small area and then interpolate/extrapolate between absorptions on various of lines of sight. (Pichon+2001. Caucci+2008. Lee+2014)

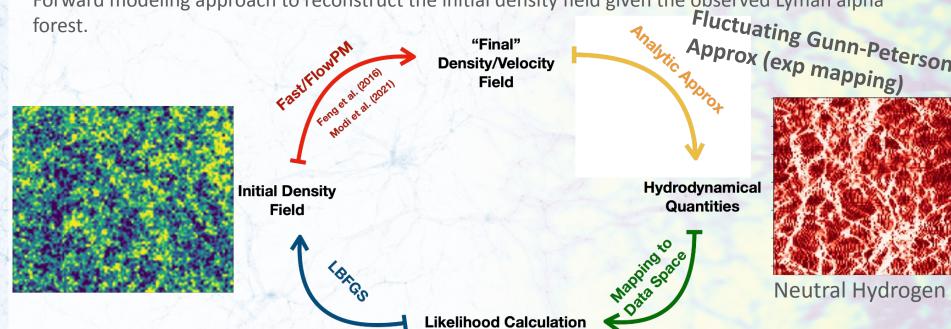




### **Tomographic Absorption Density Inference Scheme (TARDIS)**

Forward modeling approach to reconstruct the initial density field given the observed Lyman alpha

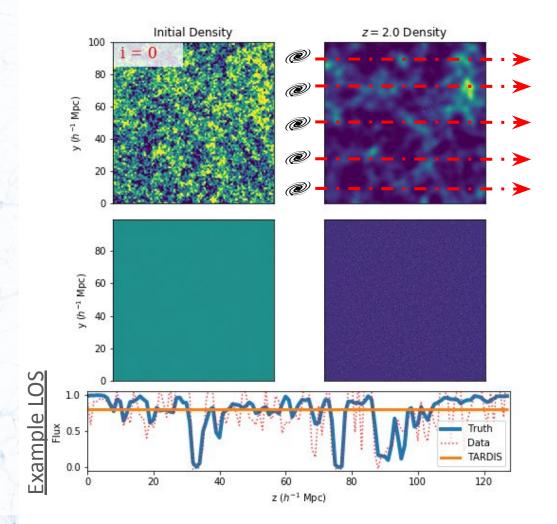
forest.



$$\mathcal{L}_{ ext{Ly}lpha}(\delta_i|\delta_{ ext{Ly}lpha, ext{obs}}) = \sum_n rac{(\delta_{ ext{Ly}lpha,obs}(n) - \delta_{\delta_{ ext{Ly}lpha,rec}}(n))^2}{\sigma_{obs}(n)^2}$$

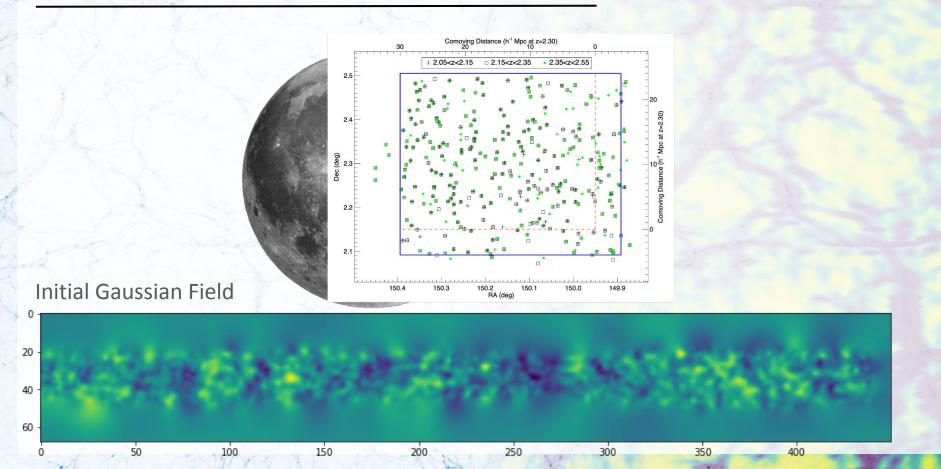
BH et al. (2019, 2020)

**Data to Initial Conditions** 

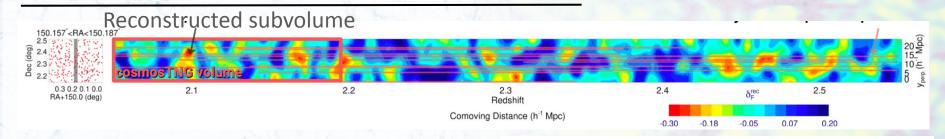


BH et al. (2019, 2020)

### **Applied to Data: COSMOS Field**



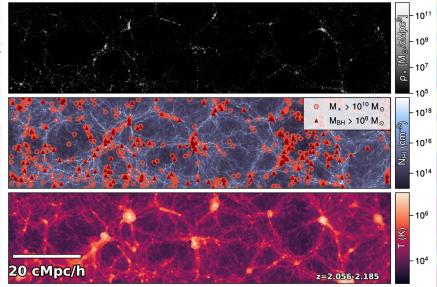
### Run Illustris With Same Initial Conditions: cosmosTNG



Design a constrained simulation in the COSMOS field at z~2 using the AREPO code + TNG galaxy formation model

Good qualitative match between field level observations and constrained hydrosim run

Lots of limitations, particularly in centers of massive clusters... Can we plug in AREPO/TNG to TARDIS?



Byrohl ++ BH (2024)

# **Fully Differentiable Hydrodynamics**

### **Fully Differentiable Hydrodynamical Simulations**

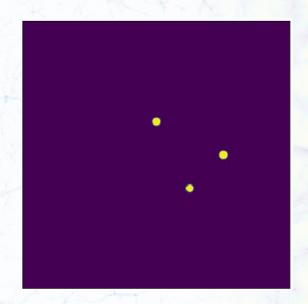
### Toy Example: Taylor-von Neumann-Sedov blast waves in 2D

### Euler Eq.

$$\frac{D\rho}{Dt} = -\rho\nabla \cdot \mathbf{u}$$

$$rac{D\mathbf{u}}{Dt} = -rac{
abla p}{
ho} + \mathbf{g}$$

$$rac{De}{Dt} = -rac{p}{
ho}
abla\cdot\mathbf{u}$$



No gravity, constant medium

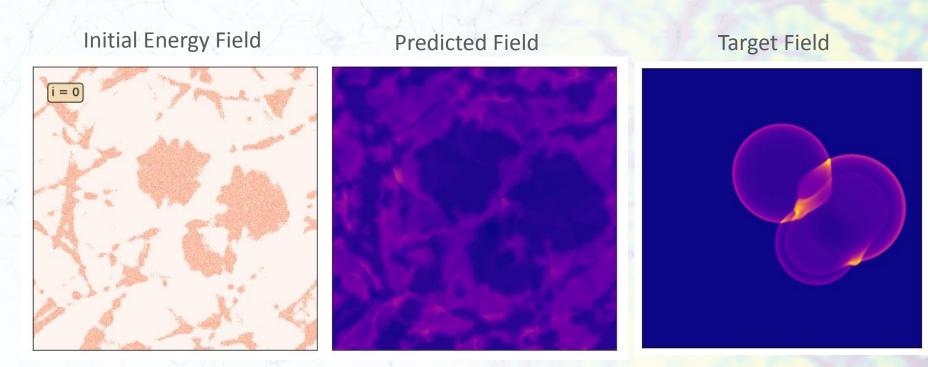
2nd order TVD scheme

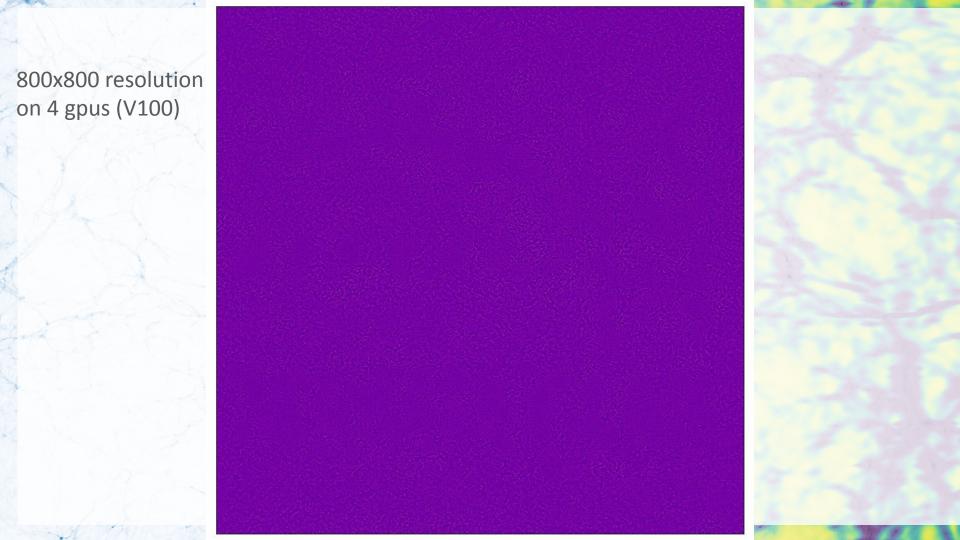
Based on fortran code from Trac & Pen (2003)

- In some cases can just import a different library to get automatic differentiability (i.e. JAX vs numpy).
- Care needed for full hydro-sims for memory reasons; can't save all states!
  - Adjoint method: Pontryagin (1962), McNamara et al. (2004), Li et al. (2022)

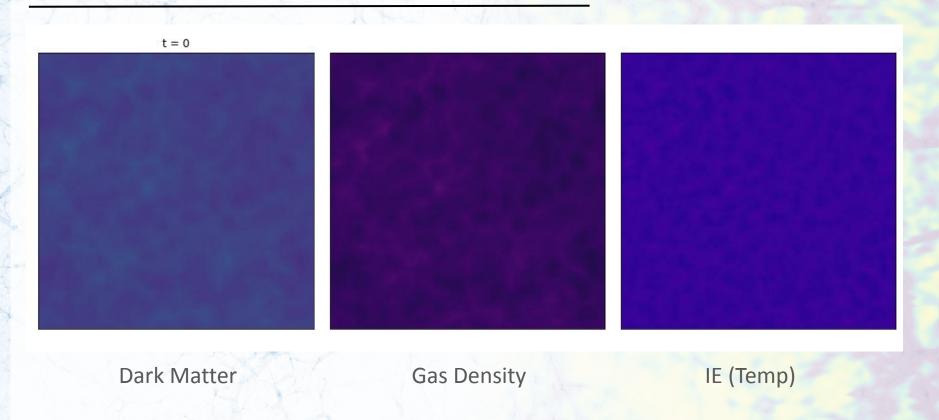
### The Future? Fully Differentiable Hydrodynamical Simulations

Toy Example: Taylor-von Neumann-Sedov blast wave in 2D Optimization!





### **Couple Dark Matter to Hydro Gravitationally**

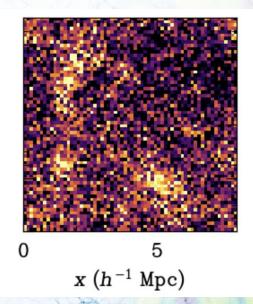


BH + Lukic (2025)

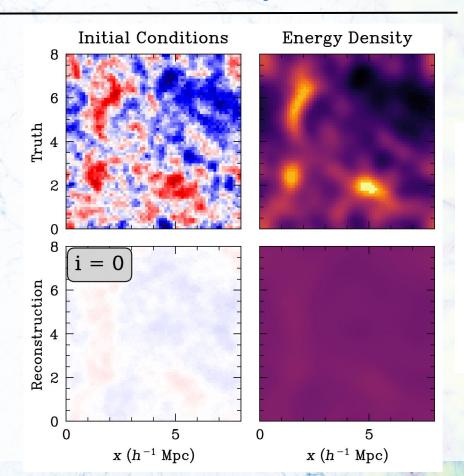
### **Field Level Inference through Hydrosims**

Mock observable inspired by thermal SZ: Noisy 3d map of thermal pressure 64<sup>3</sup> box, 8 h<sup>-1</sup> Mpc, evolved till z=2.98 (240 timesteps of hydrosim)

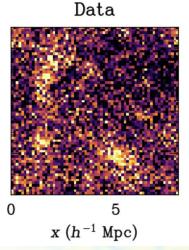
### **Mock Data Slice**



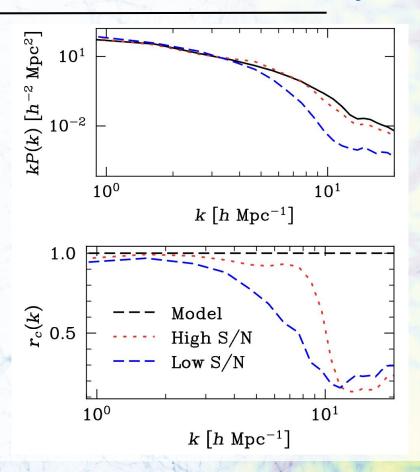
### Field Level Inference: Baryons + Dark Matter



Joint optimization of initial dark matter + baryon distribution!



### **Field Level Inference: Recovered Summary Statistics**



### **Applications**

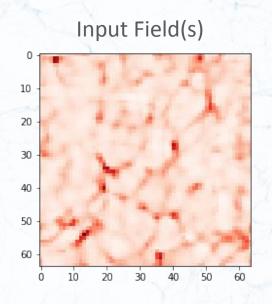
 The Dream: Full field level inverse modelling including galaxy formation down to z=0, marginalizing over all possible subgrid physics, including all CMB secondaries, etc.

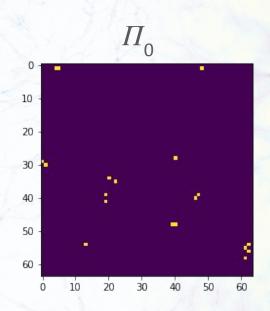
• The near-term: Map hydrodynamical fields and work in summary statistic space, optimizing for cosmology/subgrid/bias jointly. (i.e. Lanzieri+ (BH) (2022) for weak lensing)

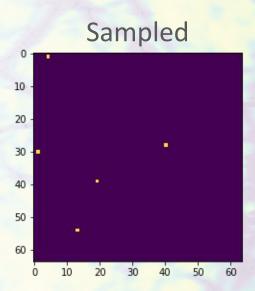
In either case, could also use some tricks like MUSE (BH+2018, Millea+Seljak 2022) to avoid sampling.

### Subgrid physics modelling example: Supernova feedback

A simple model: Stochastic formation of a star particle with probability  $\Pi_0$  if T < T<sub>c</sub>, and the density  $\delta > \delta_c$ . Stars release energy, E<sub>0</sub>, at once.





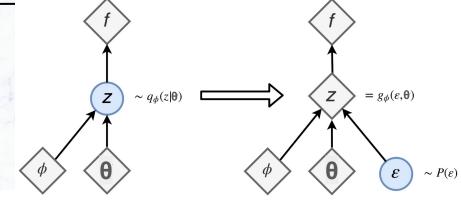


### **Dealing with Stochasticity and Discreteness**

Taking derivatives through random variables

$$z = f(\theta, \epsilon)$$
 with  $\epsilon \sim \mathbb{P}_{\epsilon}$ 

Reparametrization Trick... Common with VAEs



From F. Errica

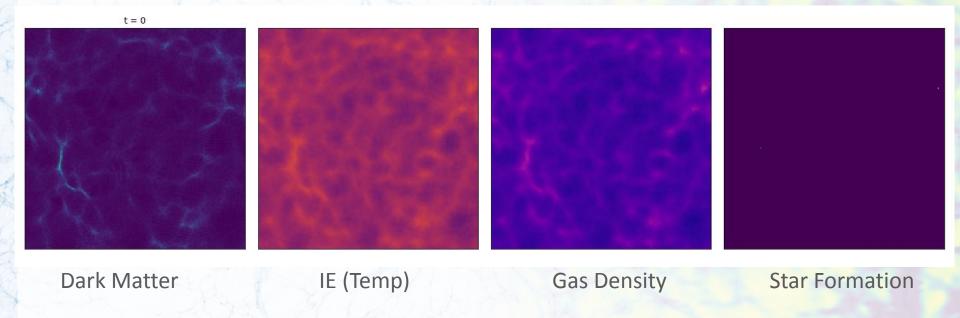
$$\frac{\partial}{\partial \theta} \mathbb{E}_{z \sim p_{\theta}} [h(z)] = \mathbb{E}_{\epsilon \sim p_{\epsilon}} \left[ \frac{\partial}{\partial \theta} h(f(\theta, \epsilon)) \right]$$

Gumbel Softmax (Maddison+2016, Jang+2016): Introduce a temperature parameter to control "discreteness" w/ one-hot encoding

$$z = \frac{1}{1 + \exp(-(\log \pi + \epsilon)/\tau)} \text{ with } \epsilon \sim \text{Logistic}(0, 1)$$

Same technique for Differentiable Halo Occupancy Distribution in BH+ (2022)

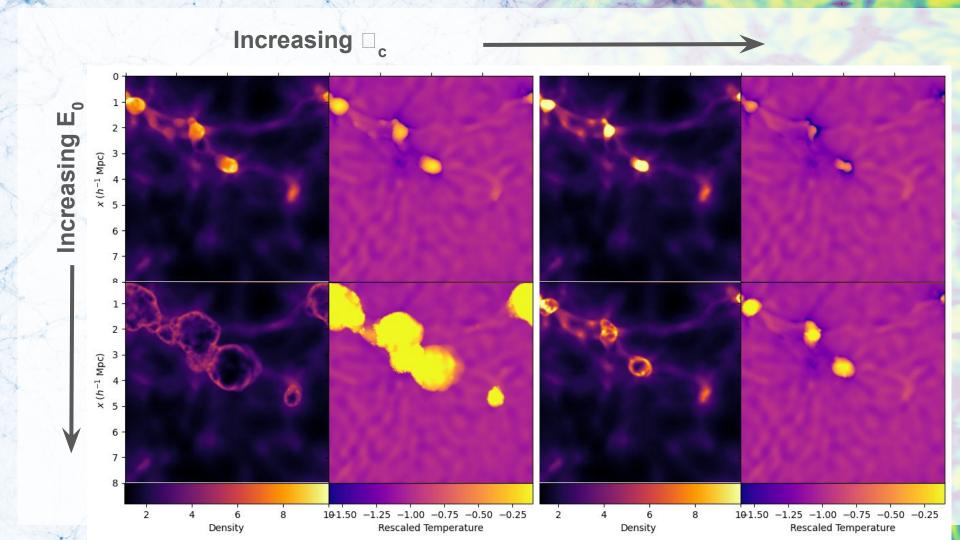
### **Subgrid Physics in Motion**



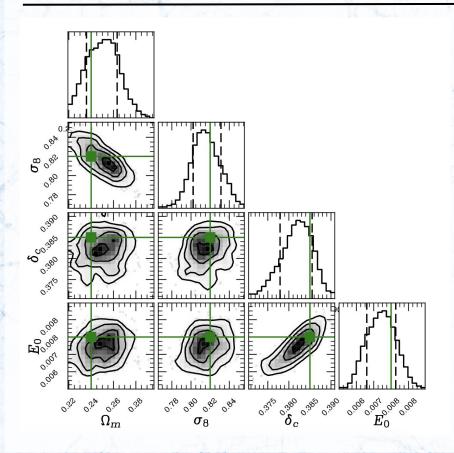
### **More Realistic Simulation**

Simplifying assumption, track stellar particles with dark matter particles.





### **Parameter Constraints via Hamiltonian Monte Carlo**



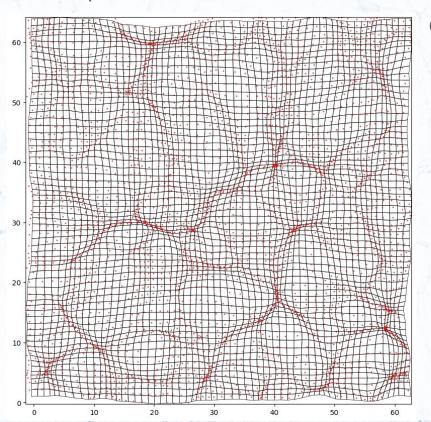
Rapidly explore combined parameter space based on mock power spectra data!

- HMC highly efficient, 500 samples with effective sample size of 6000!

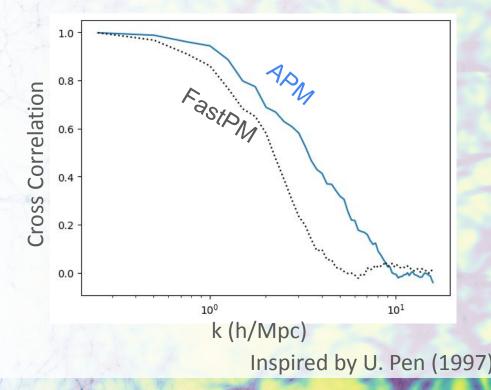
# Going to Smaller Scales/Faster Sims

## Going Beyond Standard Particle Mesh: Adaptive Approach Particle Mesh: Adaptive Approach

Use adaptive mesh which maintains same rectangular topology (easy for GPU, easy for autodiff)



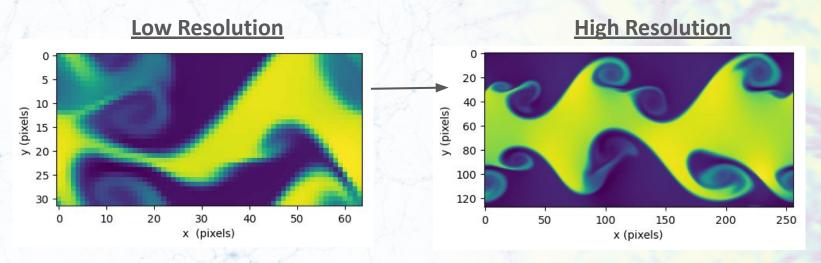
Can't use standard FFTs, instead directly solve for potential



### The Future... Solver-in-Loop Models

Best of both worlds?

Speed/accuracy of ML models with the generalizability of hydrodynamical simulations!



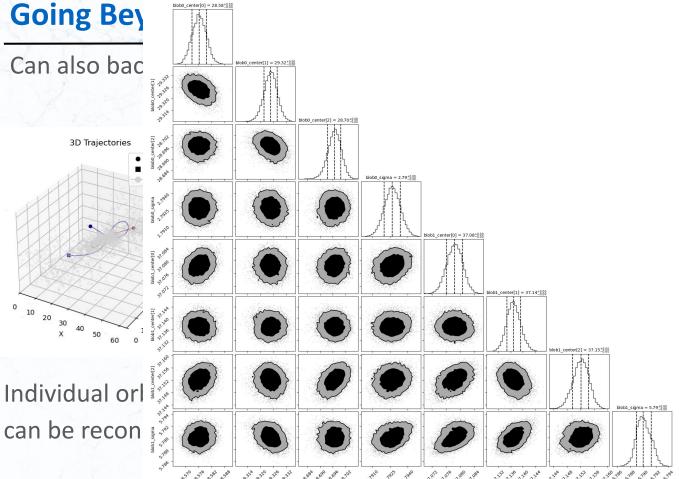
"Resolution" could mean many things... (mesh size, adaptive mesh refinement, memory intensive Riemann solvers, larger timesteps, additional (subgrid) physics, etc.)



n.



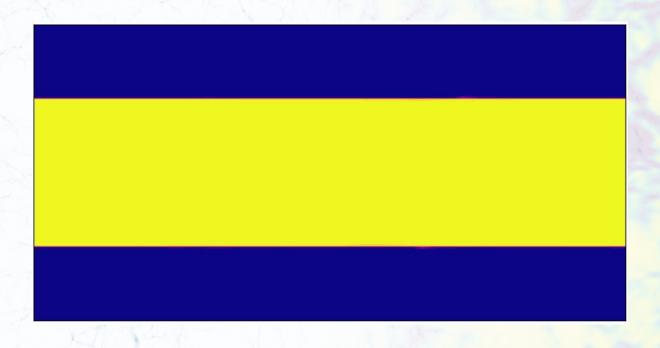
w/ Lucas Mebille



ibles (i.e. halos)

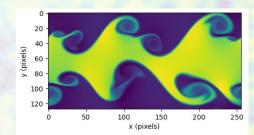
### The Future... Solver-in-Loop Models

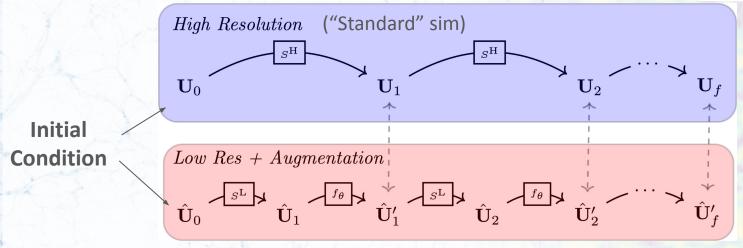
Even with GPU, some simulations are computationally expensive...



### The Future? Solver-in-Loop Models

Setup neural network to augment each timestep:  $f_{ heta}$ 



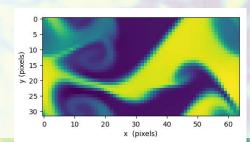


**Final State** 

Train model by minimizing loss over all timesteps:

$$\mathcal{L}_{ heta} = \sum_{i} (\hat{\mathbf{U}}_{i}'( heta) - \mathbf{U}_{i})^{2}$$

Could also include it at the level of flux and/or source calculations

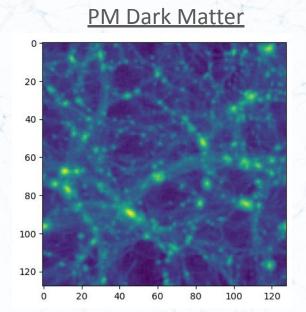


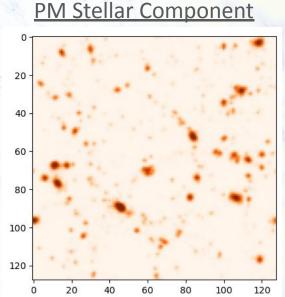
### **Solver-in-Loop Models: Star Formation**

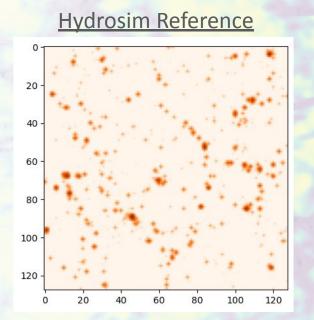
Train star formation field iteratively in loop to capture star formation history. Trained on "standard" hydrodynamical simulations, CAMELS simulations (Villaescusa-Navarro et al).



w/ Lillie Szemraj



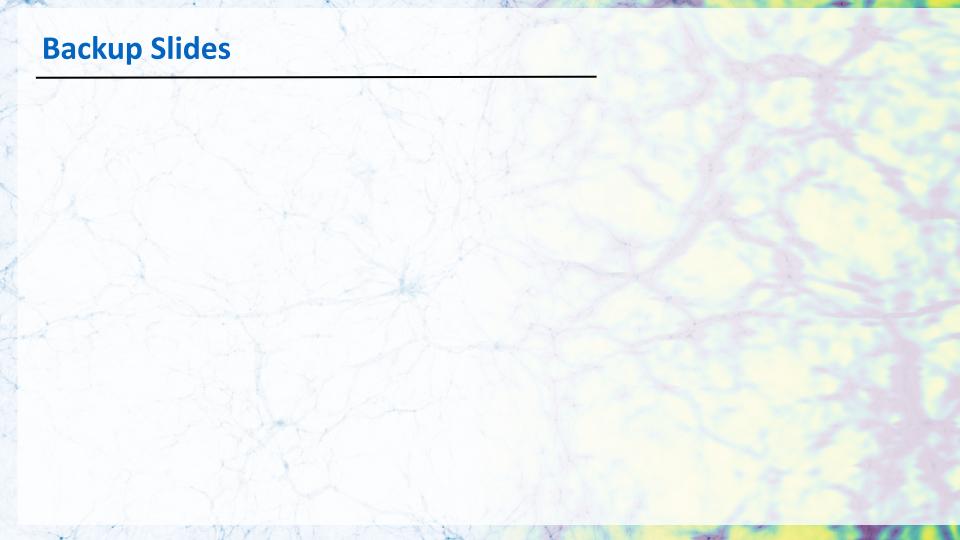




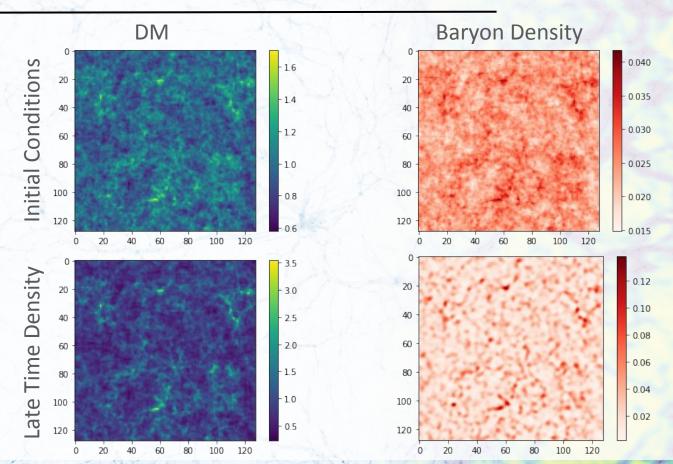
### **Summary**

The "machine learning revolution" is useful beyond making complex black-box models! Optimization methods, available GPUs, etc. have opened new doors for analysis.

- Machine learning can be used a surrogate model for realistic hydrodynamical physics in a forward model.
- Hydro-sims themselves can be able to be constructed in a differentiable fashion, even with complex stochastic feedback.
- In the future, ML-assisted hydrosims could maintain generalizability while vastly outperforming current classes of simulations.

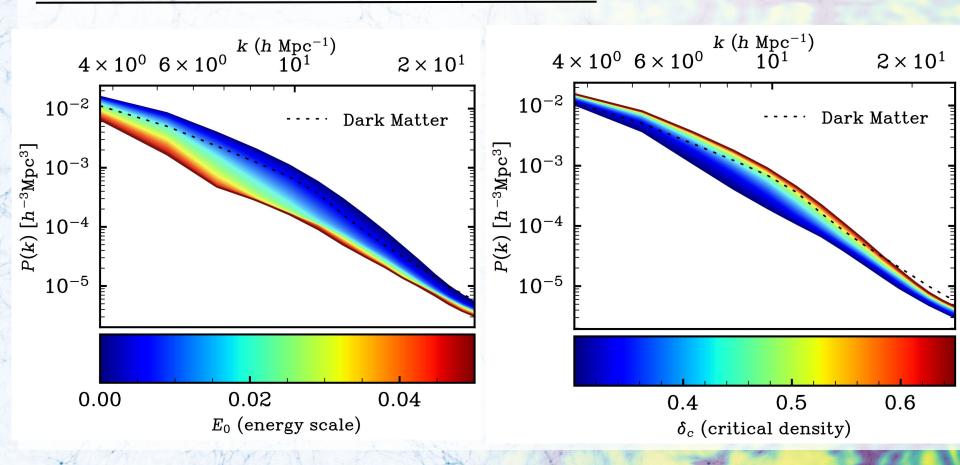


### Couple to dm-solver (PMWD)

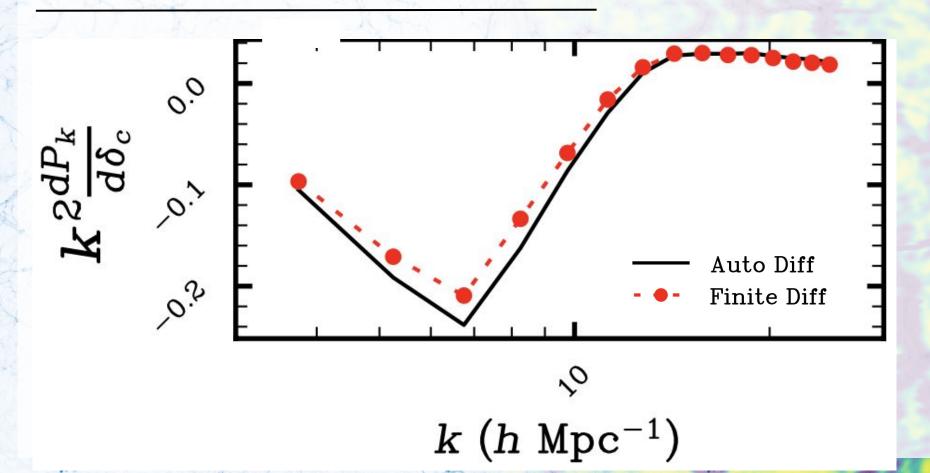


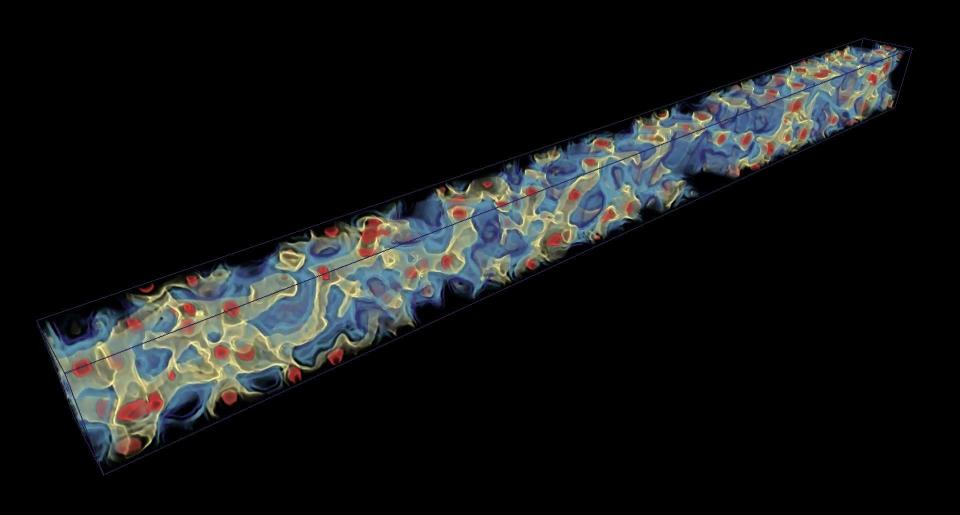
BH + Lukic (2025)

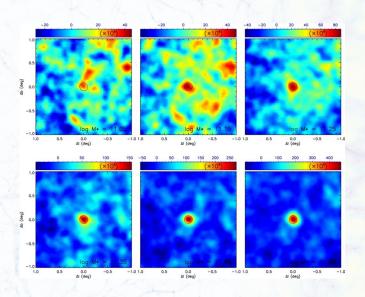
### **Power Spectra: Varying Critical Density**



### **Derivatives of Summary Statistics**







### **Hydrodynamics**

### **State vector:**

**Combined Conservation Equation:** 

$$\mathbf{U} = (\rho_b, a\rho_b U, a^2 \rho_b E)$$

$$\frac{\partial \mathbf{U}}{\partial t} = -\nabla \cdot \mathbf{F} + S_e + S_g$$

Flux Term:

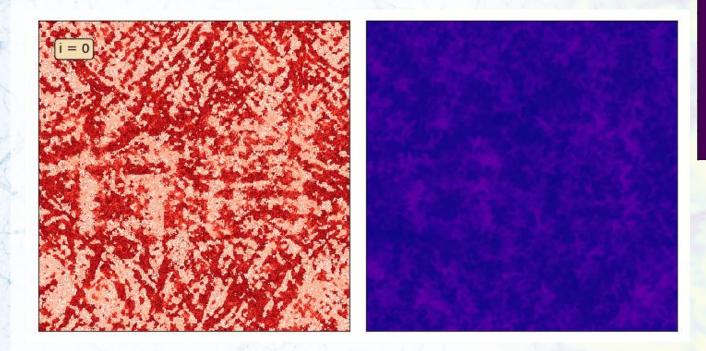
$$\mathbf{F} = ((1/a)\rho_b U, \rho_b U U, a(\rho_b U E + p U))$$

**Source Terms:** 

$$S_e = (0, 0, -ap\nabla \cdot U)$$
$$S_g = (0, \rho_b \mathbf{g}, a\rho_b U \cdot \mathbf{g})$$

Can solve numerically time-step by timestep on a grid.

### **Optimization in Progress**





(used fewer timesteps, so easier than 3 blast example...)

### **Dealing with Stochasticity and Discreteness**

Taking derivatives through random variables

$$z = f(\theta, \epsilon)$$
 with  $\epsilon \sim \mathbb{P}_{\epsilon}$ 

Reparametrization Trick... Common with VAEs

$$\frac{\partial}{\partial \theta} \mathbb{E}_{z \sim p_{\theta}} [h(z)] = \mathbb{E}_{\epsilon \sim p_{\epsilon}} \left[ \frac{\partial}{\partial \theta} h(f(\theta, \epsilon)) \right]$$

 $\begin{array}{c|c} f \\ \hline \\ \hline \\ \phi \\ \hline \\ \theta \\ \hline \end{array} \sim q_{\phi}(z|\theta) \\ \hline \\ \phi \\ \hline \\ \theta \\ \hline \\ \varepsilon \\ \sim P(\varepsilon) \\ \hline \end{array}$ 

From F. Errica

Classic Multivariable Gaussian example

$$z \sim \mathcal{N}(\mu, \sigma^2)$$
  $z = \mu + \sigma \epsilon$   $\epsilon \sim \mathcal{N}(0, I)$ 

Same technique for Differentiable Halo Occupancy Distribution in BH+ (2022)

### **Taking Derivative Through Discrete Stochastic Process**

Sampling a discrete random variable differentiably with a Gumbel random g

$$z = \text{onehot} \left( \operatorname{argmax}_{i} [g_{i} + \log (\pi_{i})] \right)$$

Introduce tau, temperature relaxation parameter: (Maddison+2016, Jang+2016)

$$\hat{z}_i = \frac{\exp((\log(\pi_i) + g_i)/\tau)}{\sum_j \exp((\log(\pi_j) + g_j)/\tau)}$$

Simplifies a bit for one class:

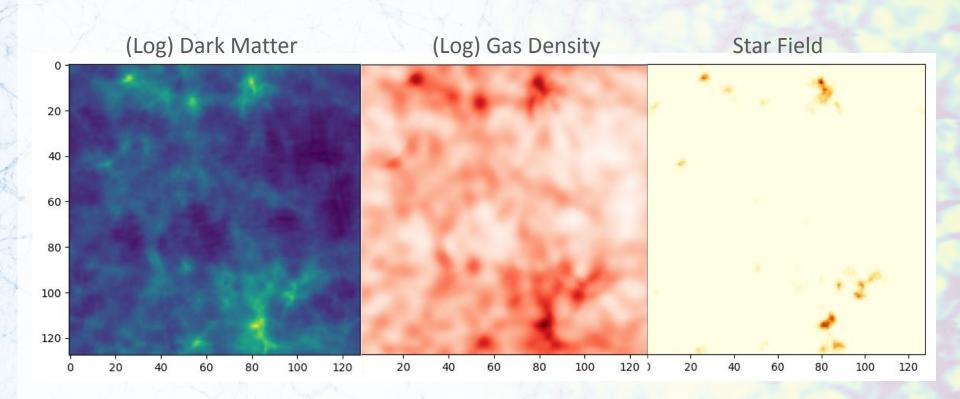
$$z = \frac{1}{1 + \exp(-(\log \pi + \epsilon)/\tau)} \text{ with } \epsilon \sim \text{Logistic}(0, 1)$$

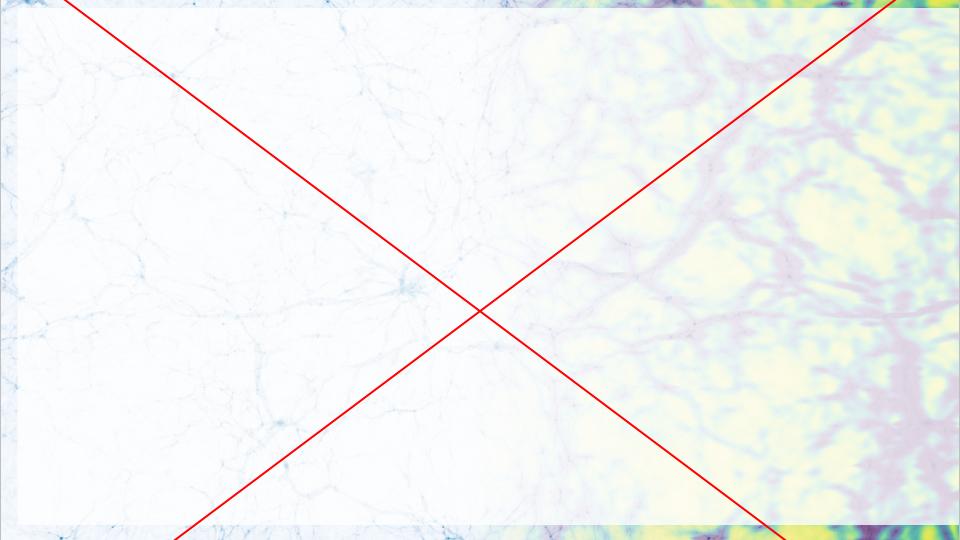
Same technique for Differentiable Halo Occupancy Distribution in BH+ (2022)

### **More Realistic Simulation**

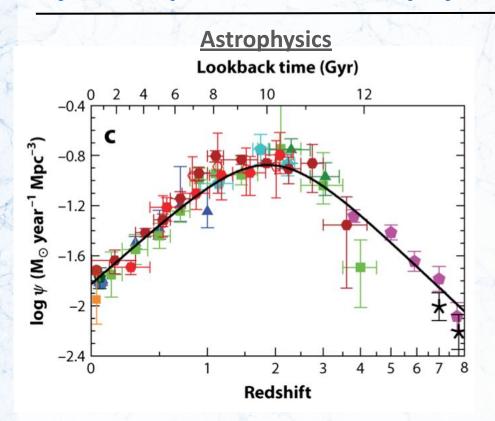


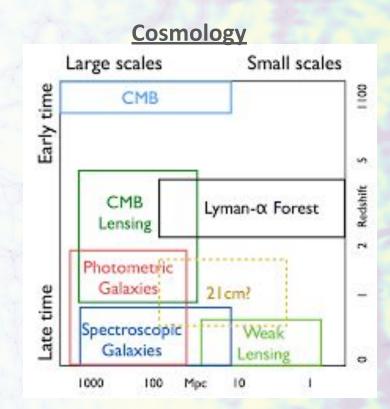
### Slice Through (more realistic) Simulation





### Lyman Alpha Forest: Astrophysics and Cosmology





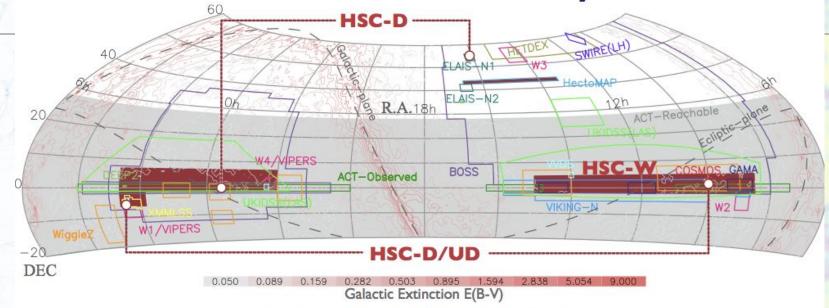
### **PFS** - Fast facts

- Subaru Prime Focus Spectrograph:
   The spectroscopy part of the "SuMIRe" project.
  - Wide field: ~1.4 deg diameter
  - High multiplicity: 2394 fibers
    - Fiber diameter: ~1.05 arcsec
    - Fiber positioner pitch: ~85 arcsec
    - Minimum fiber separation: ~30 arcsec
  - Quick fiber reconfiguration: ~60-120 sec (TBC)
  - VIS-NIR coverage: 380-1260nm simultaneously
    - Low resolution mode: ~2.5 A resolution
    - Medium resolution mode (around 800nm): ~1.6 A resolution





# Subaru HSC/PFS Survey fields



HSC-SSP: 8 years, 300 nights, completed

Wide: ~1200 sq deg to 26, Deep: 30 sq deg to 27, Ultra-Deep 3 sq deg to 28

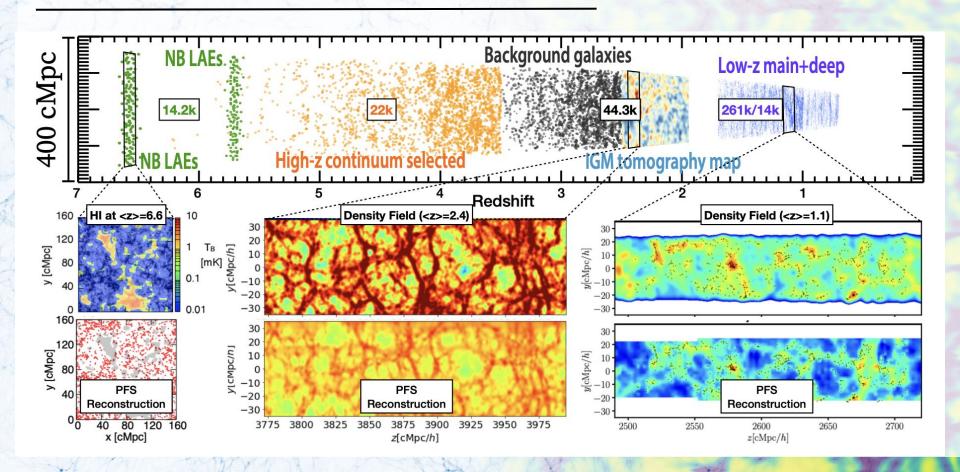
PFS-SSP: 5 years, 360 nights, starting S2025

### **Key Pillars of the PFS-SSP**

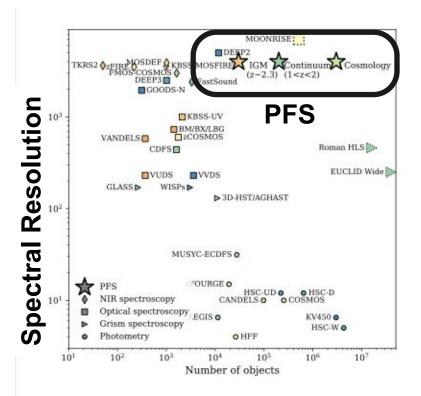
- CO Cosmology
- GA Galactic Archaeology
  - GE Galaxy Evolution

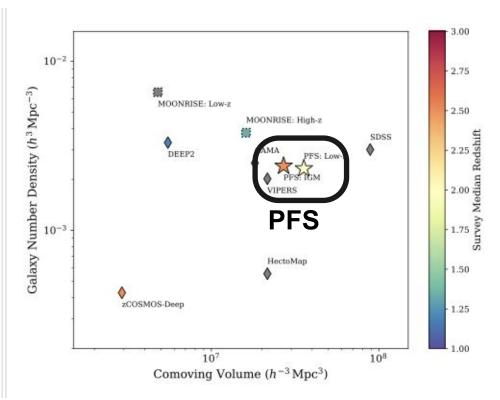
	Testing ACDM	Assembly history of galaxies	Importance of IGM
• Exp • PFS • Cur • Prin • Nat • Stru	ure & role of neutrinos pansion rate via BAO up to $z$ =2.4 S+HSC tests of GR vature of space: $\Omega_{\rm K}$ mordial power spectrum ure of DM (dSphs) acture of MW dark halo all-scale tests of structure growth	<ul> <li>PFS+HSC synergy</li> <li>Absorption probes with PFS/SDSS QSOs around PFS/HSC host galaxies</li> <li>Stellar kinematics and chemical abundances – MW &amp; M31 assembly history</li> <li>Halo-galaxy connection: M*/Mhalo</li> <li>Outflows &amp; inflows of gas</li> <li>Environment-dependent evolution</li> </ul>	<ul> <li>Search for emission from stacked spectra</li> <li>dSph as relic probe of reionization feedback</li> <li>Past massive star IMF from elemen abundances</li> <li>Physics of cosmic reionization via LAEs &amp; 21cm studies</li> <li>Tomography of gas &amp; DM</li> </ul>

### Prime Focus Spectraph: Redshift Evolution of the Galaxy - Environment Relation



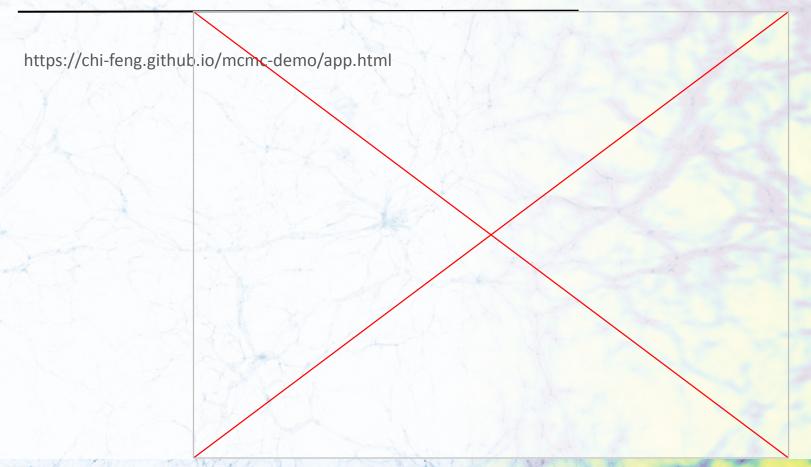
# Unprecedented combination: spectral resolution, wavelength coverage, multiplex





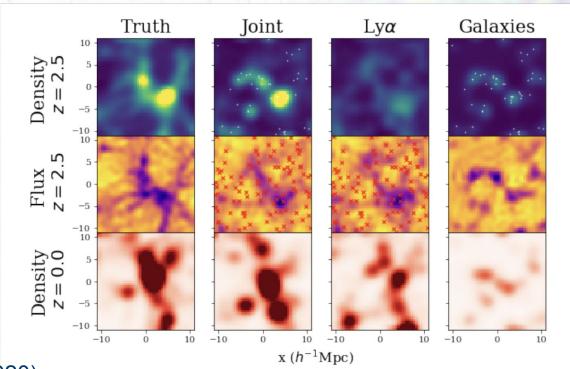
# **Differentiable Simulations**

### **How Derivatives Help: Sampling**



### **Protocluster Science**

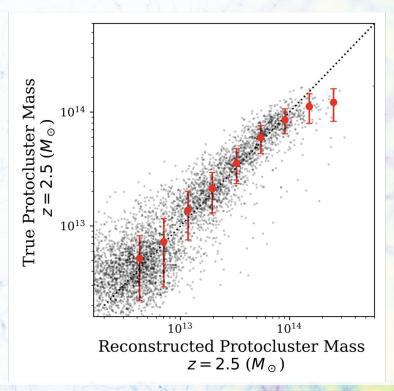
Continue to evolve reconstructed field to z=0, identify clusters using standard methods, then look at corresponding Lagrangian volume at observed redshift!



BH et al. (2019, 2020)

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