



COSMOLOGY FROM HIGH-¹ PRECISION CMB LENSING MEASUREMENTS WITH THE ATACAMA COSMOLOGY TELESCOPE



Frank J. Qu DAMTP/KICC

University of Cambridge

in collaboration with



Blake Sherwin
(University of Cambridge)



Mathew Madhavacheril
(University of Pennsylvania)



Niall MacCrann
(University of Cambridge)



Dongwon Han
(University of Cambridge)

+ ACT
collaboration

Frank J. Qu Thursday 18th of May 2023

RPM talk

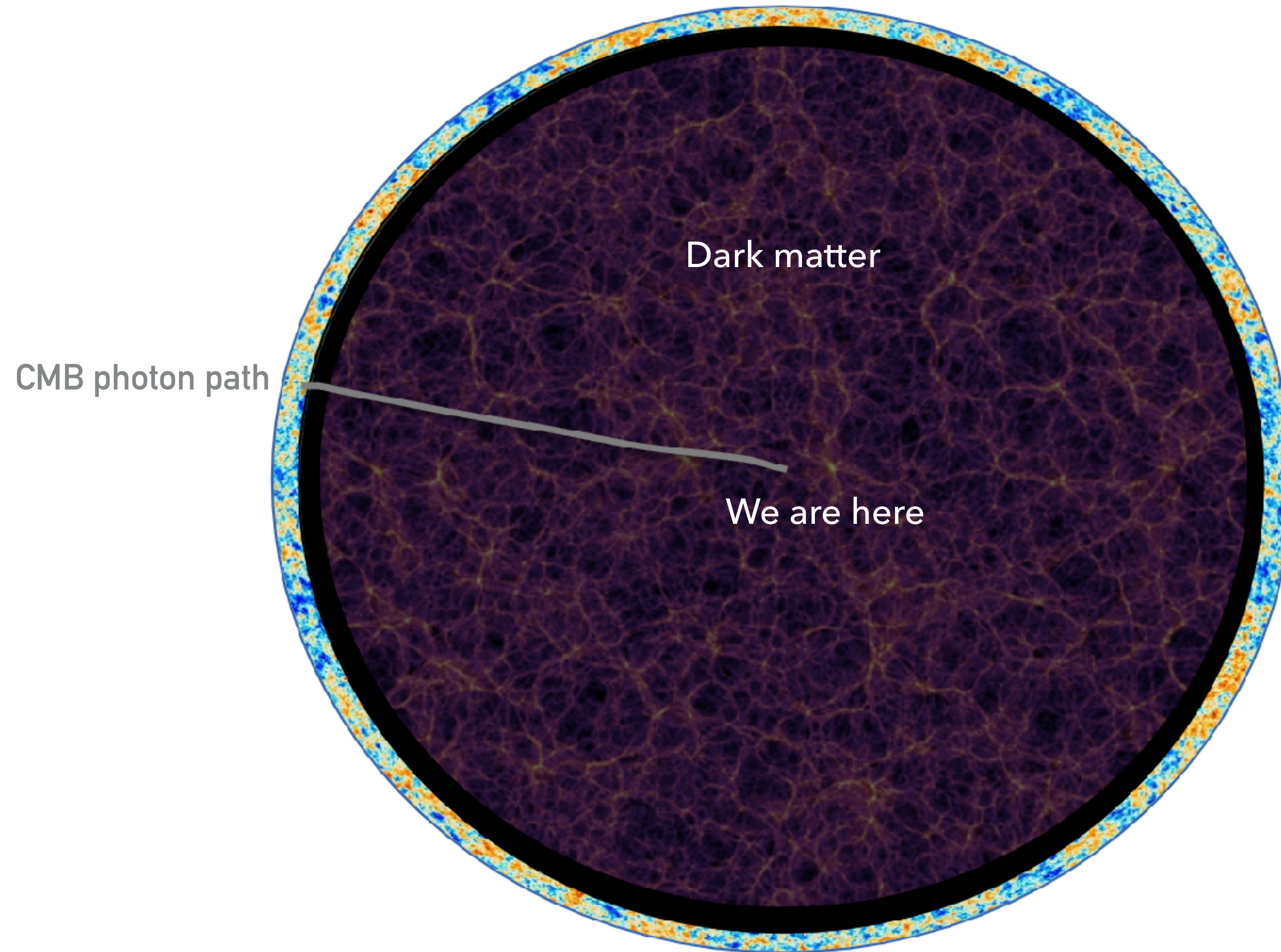


THE ACT COLLABORATION

160 Collaborators at 45 institutions

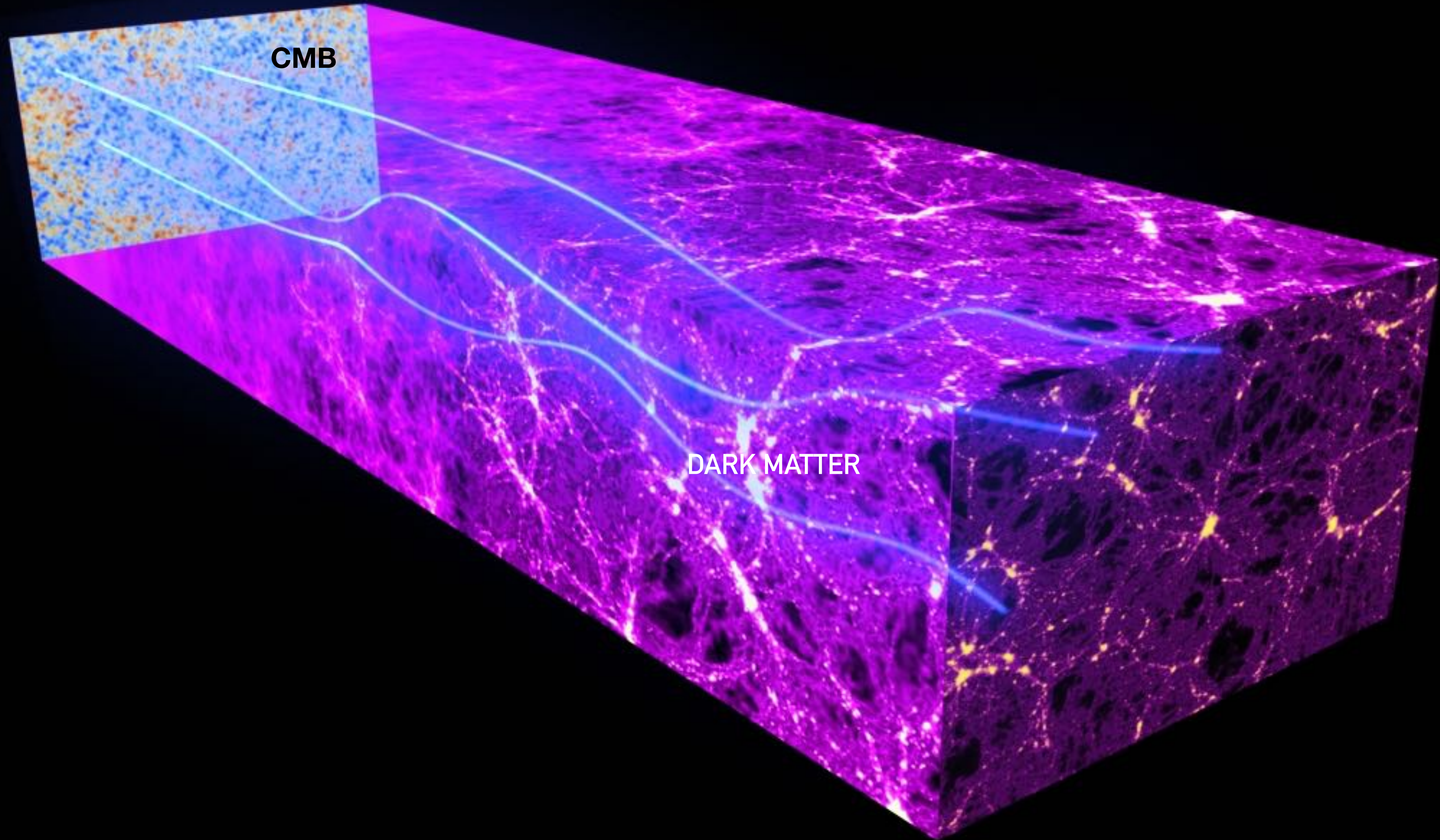


THE CMB AS A SOURCE OF GRAVITATIONAL LENSING

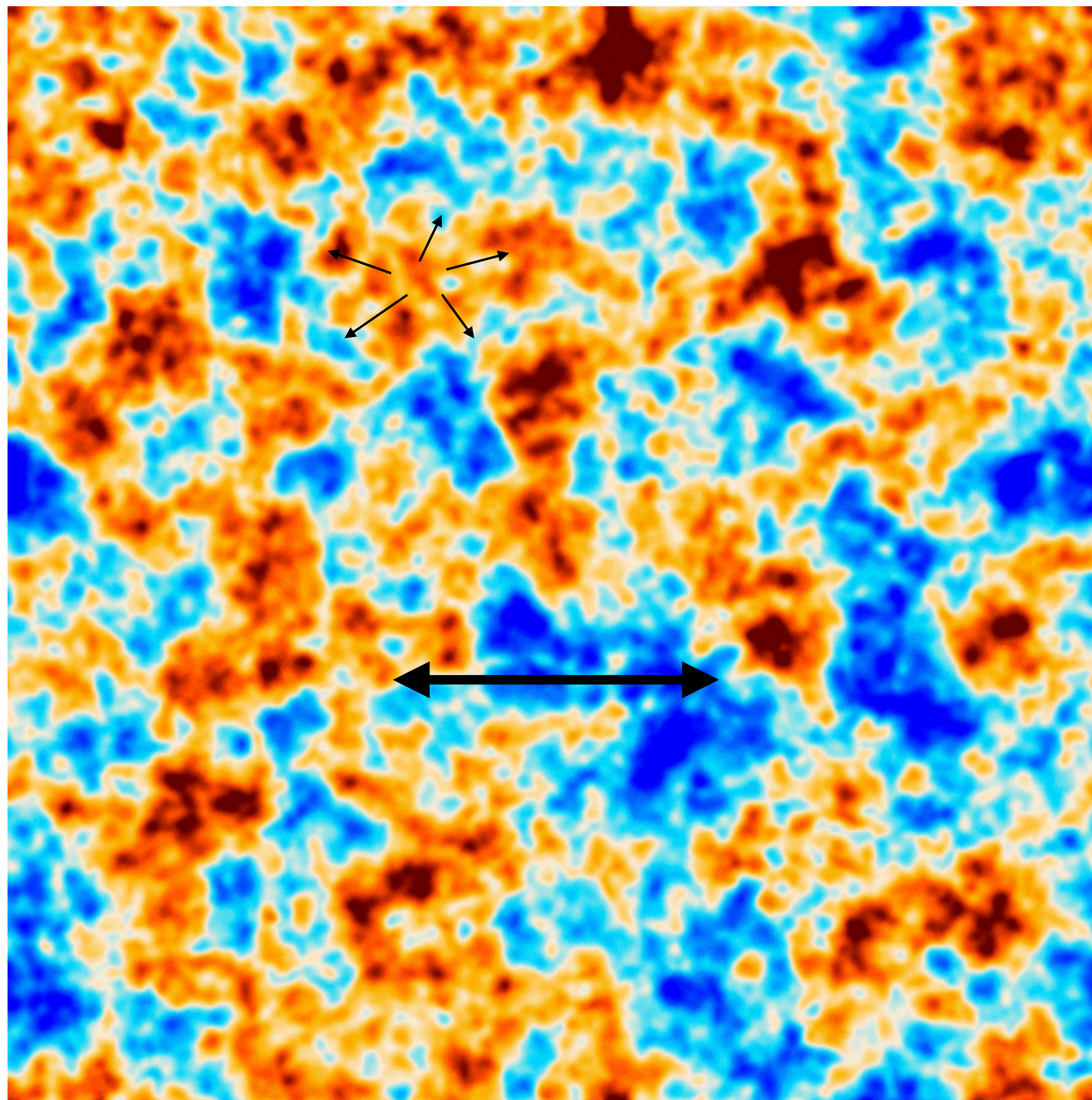


- Ideal Source for lensing**
- Known redshift origin
 - Known unlensed statistics
 - Probing all the mass (dark matter) distribution

BACKLIGHTING THE UNIVERSE WITH THE CMB



EFFECT OF CMB LENSING



$$T^{\text{lensed}} = T^0(\hat{n} + \nabla\phi)$$

Small-scale arc minute deflections described by deflection field $\nabla\phi$

Coherent over large degree-scales

Lensing convergence $\kappa = -\frac{1}{2}\nabla^2\phi$

LENSING RECONSTRUCTION VIA THE QUADRATIC ESTIMATOR (QE)

REAL SPACE

- ▶ **Unlensed CMB** translationally invariant.
- ▶ **Lensing** breaks the isotropy of the unlensed CMB statistics

FOURIER/ HARMONIC SPACE

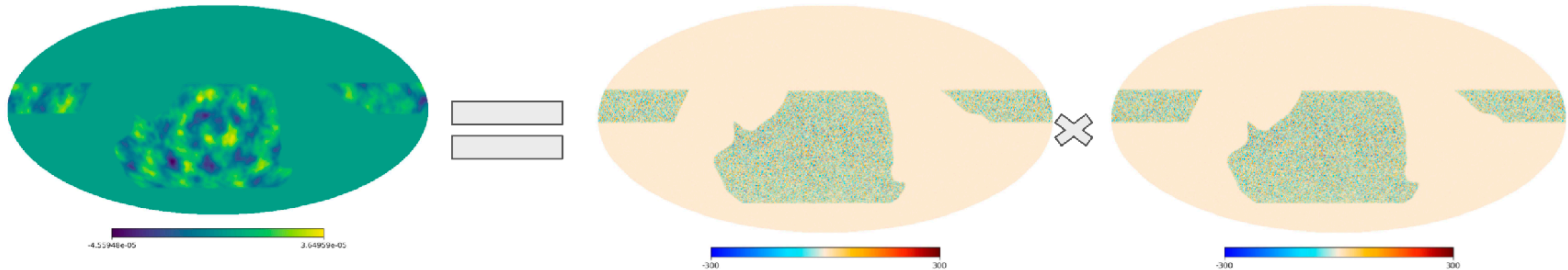
$$\langle T^0(\boldsymbol{\ell})T^{0*}(\boldsymbol{\ell} - \mathbf{L}) \rangle_{\text{CMB}} = 0$$

Mode coupling

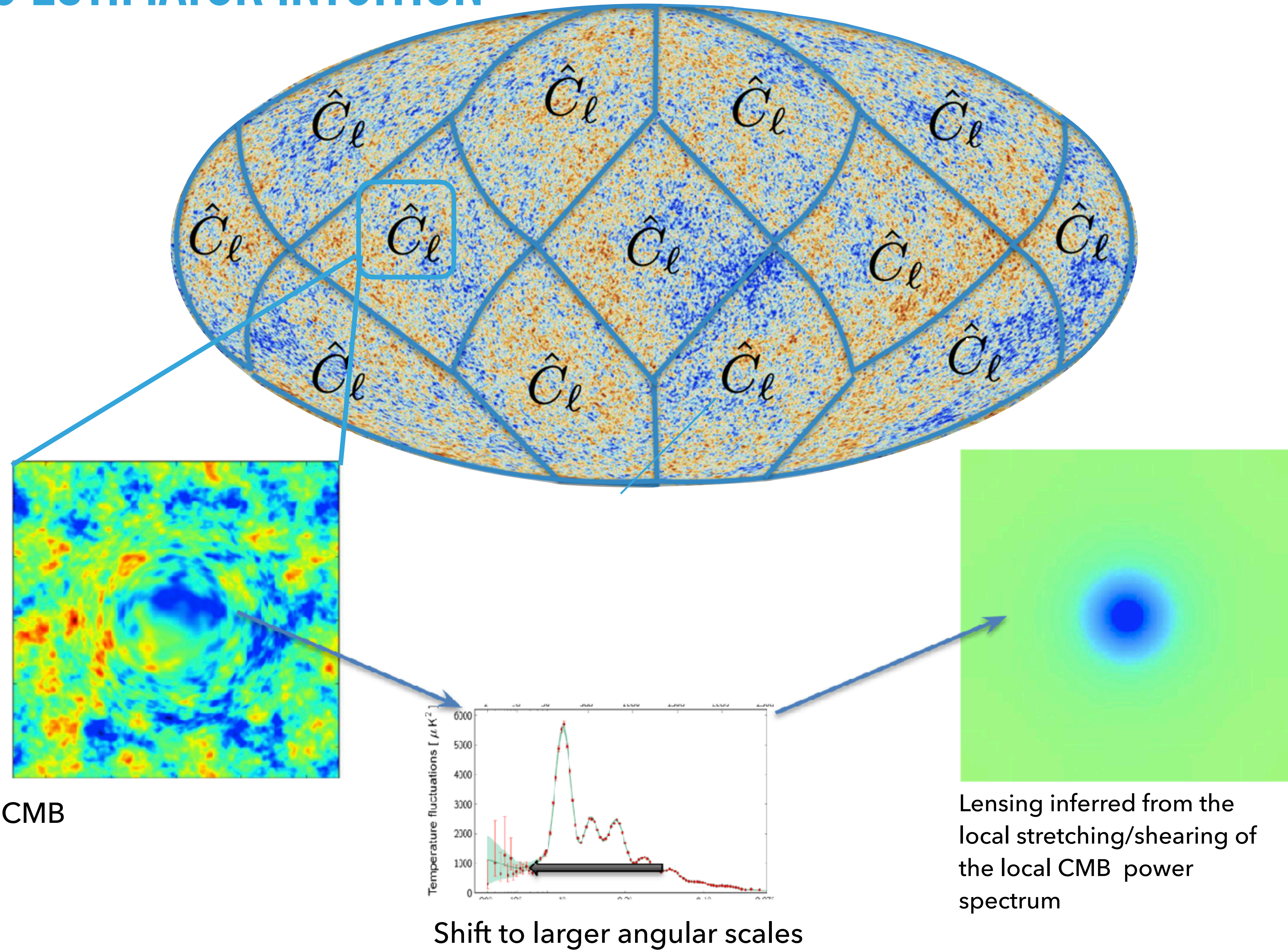
$$\langle T(\boldsymbol{\ell})T^*(\boldsymbol{\ell} - \mathbf{L}) \rangle_{\text{CMB}} \sim \phi(\mathbf{L})$$

Mode by mode reconstruction of lensing from quadratic CMB combinations

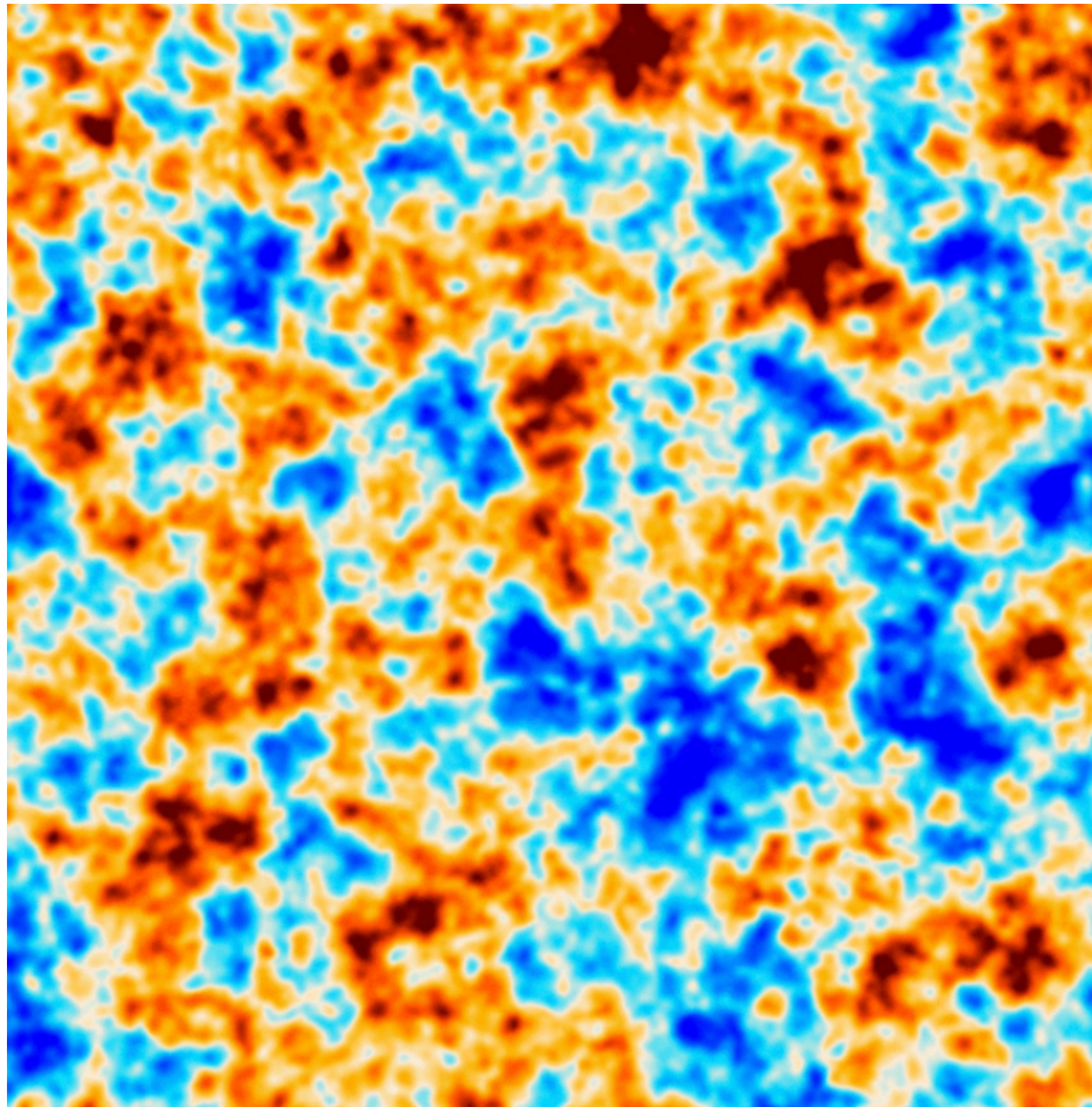
$$\hat{\phi}(\mathbf{L}) \sim \int d^2\boldsymbol{\ell} T(\boldsymbol{\ell})T^*(\boldsymbol{\ell} - \mathbf{L}) \sim \text{QE}(T_{\text{CMB}}, T_{\text{CMB}})$$



QUADRATIC ESTIMATOR INTUITION



LENSING RECONSTRUCTION VIA THE QUADRATIC ESTIMATOR

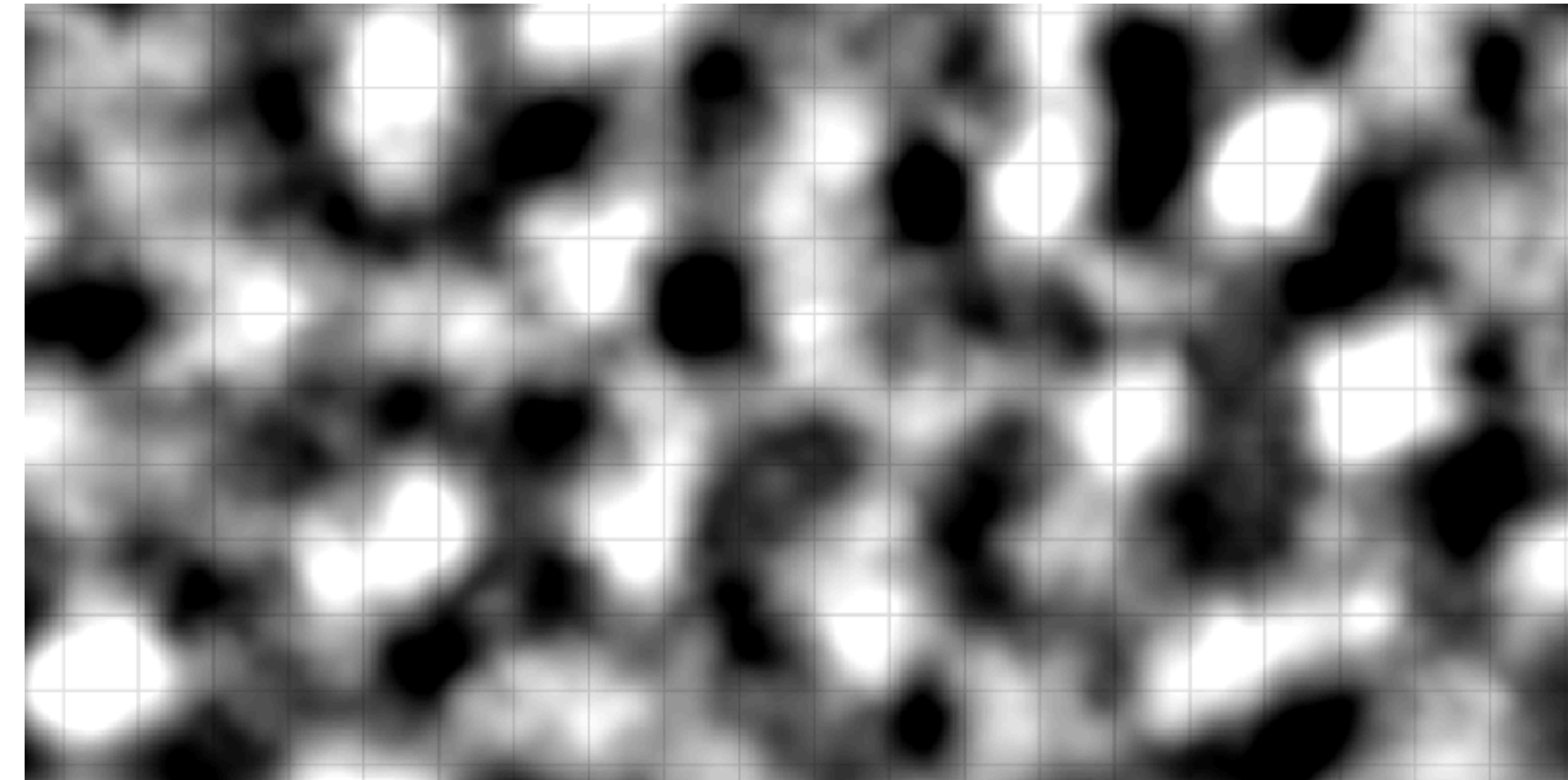


Typically use $600 < \ell < 3000$

$$\hat{\phi}(\mathbf{L}) \sim \int d^2\ell T(\ell) T^*(\ell - \mathbf{L})$$

→

Use **small scale**
CMB modes to
reconstruct **large**
scale lenses

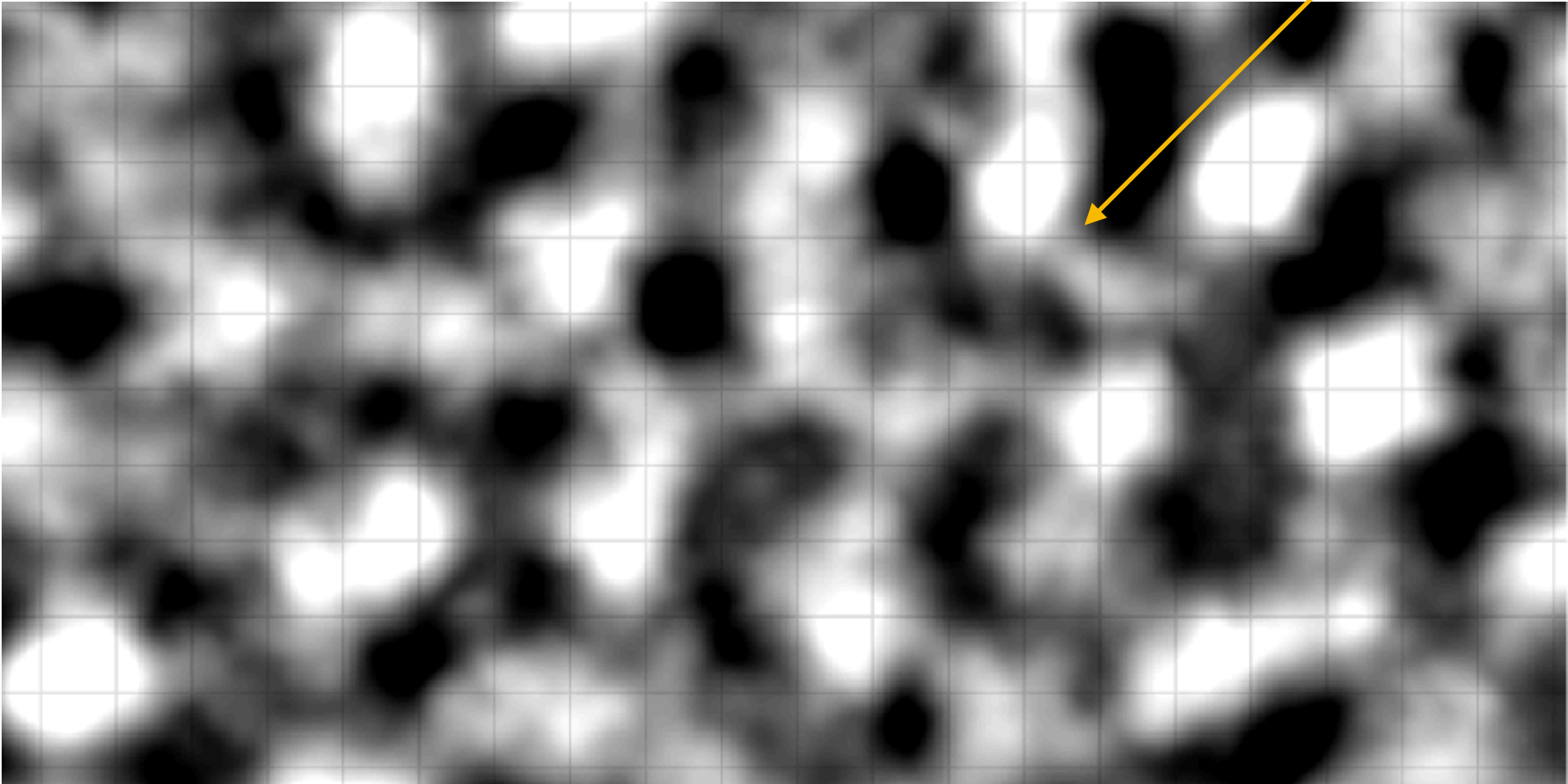


Reconstructed CMB Lensing Matter
Distribution

Benefit from **high resolution** CMB measurements

KEY STATISTICS: LENSING POWER SPECTRUM

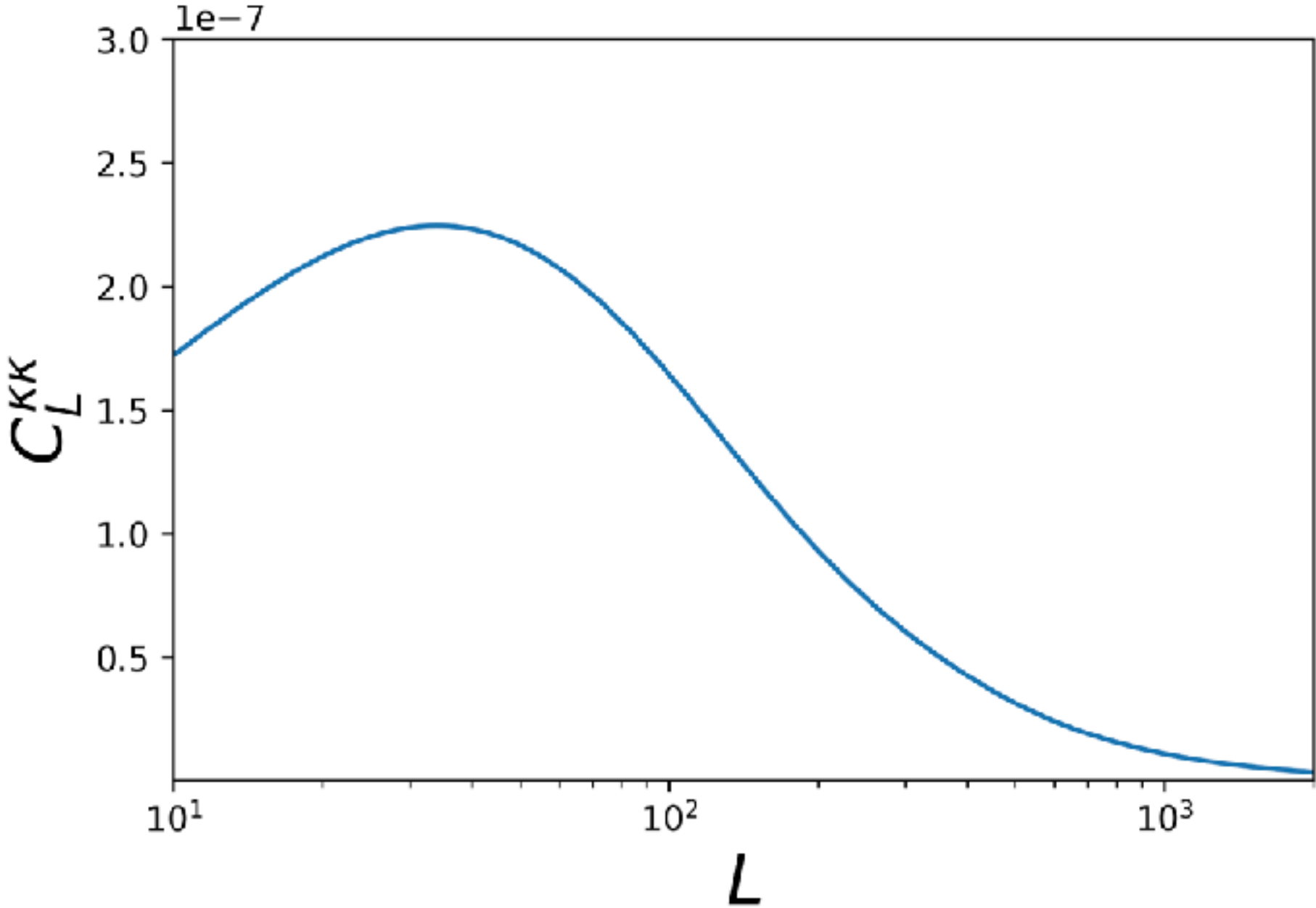
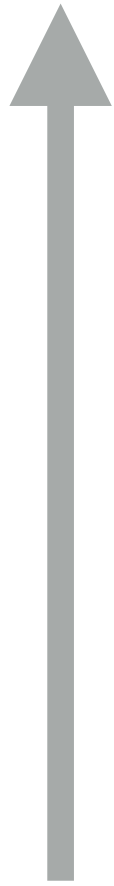
Bright regions = High Density



Reconstructed mass map

$$\hat{C}_L^{\phi\phi} \sim \langle \hat{\phi}_{LM} \hat{\phi}_{LM}^* \rangle$$

y-axis: How much lensing there is



x-axis: For a lens of angular size $\sim \frac{1}{L}$



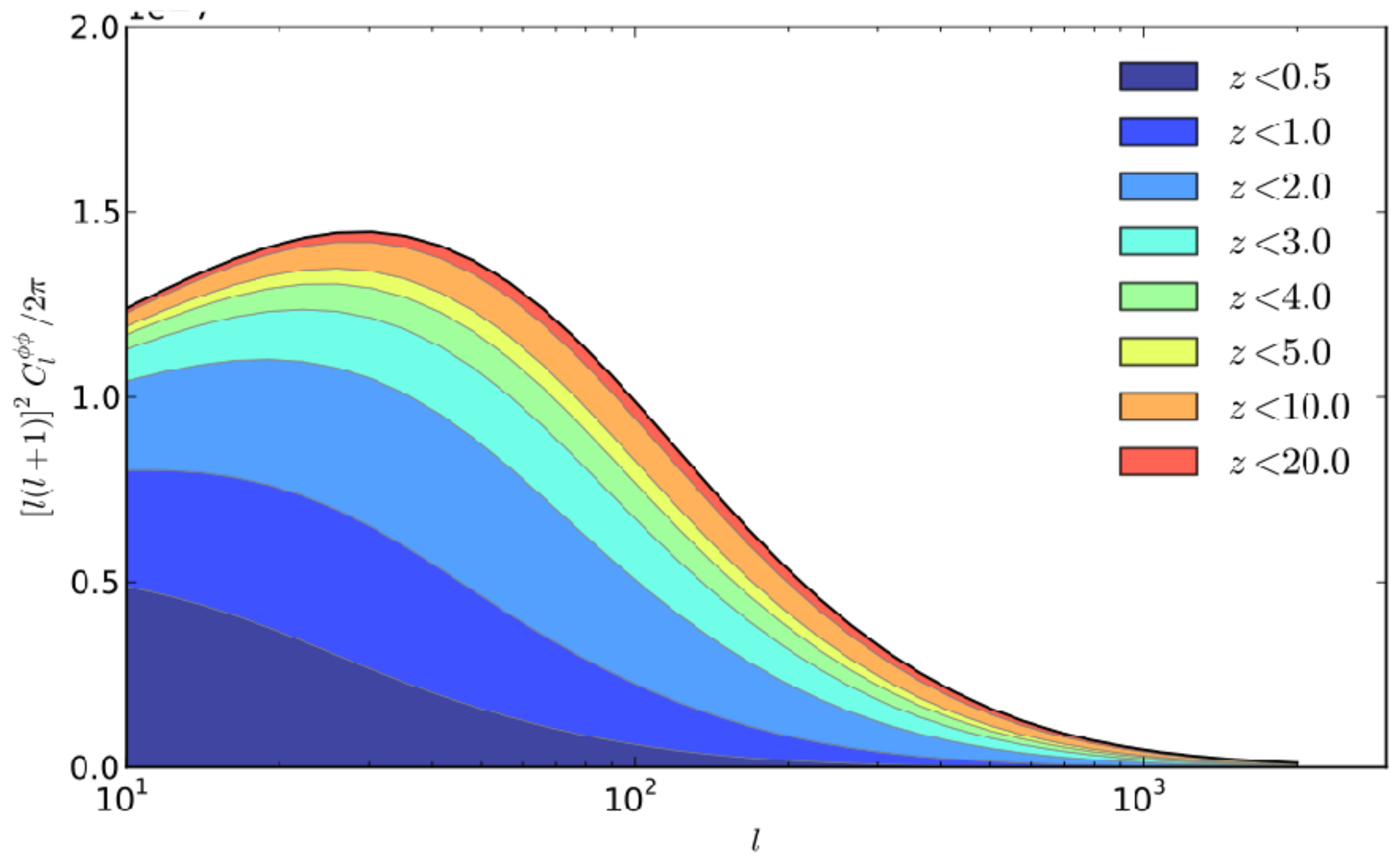
MOTIVATION: WHY IS CMB LENSING INTERESTING?

- ▶ Lensing probes the projected mass distribution to high redshifts.
- ▶ Hence the lensing power spectrum is the projected matter power spectrum

$$\kappa(\hat{\mathbf{n}}) \sim \int_0^{z_\star} dz \underbrace{W^\kappa(z)}_{\text{Projection kernel}} \underbrace{\delta(\hat{\mathbf{n}}, z)}_{\text{Fractional mass overdensity}}$$

$$L^4 C_L^{\phi\phi} / 4 = \int_0^{1100} dz (\tilde{W}^\kappa(z))^2 P(k = L/\chi, z)$$

lensing power spec. redshift kernel matter power spectrum

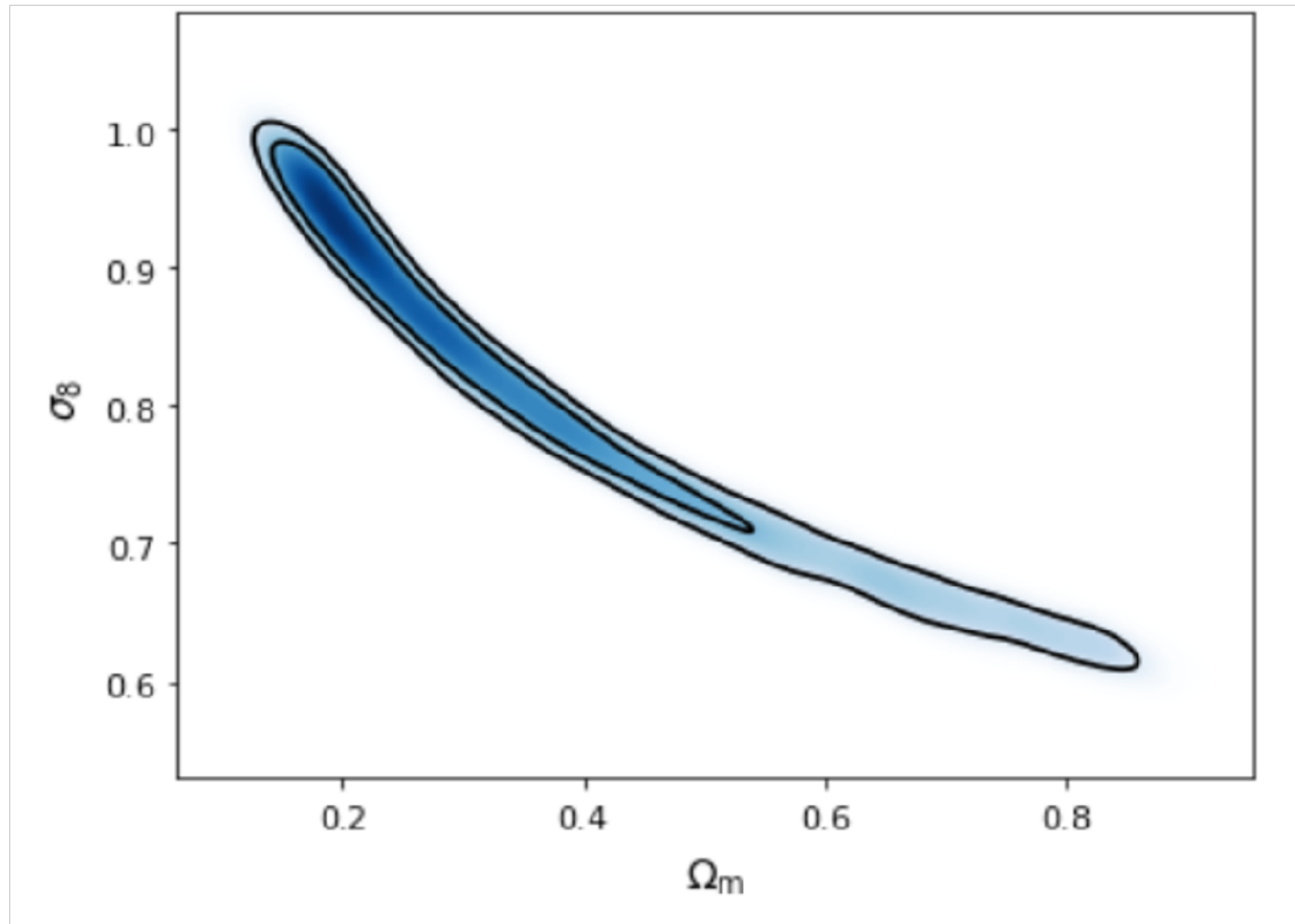


Redshift origin of the signal: mean at $z \sim 2$, peak at $z \sim 1$, broad support over extended redshifts $z = 0.5 \sim 6$

COSMOLOGICAL PARAMETER DEPENDENCE

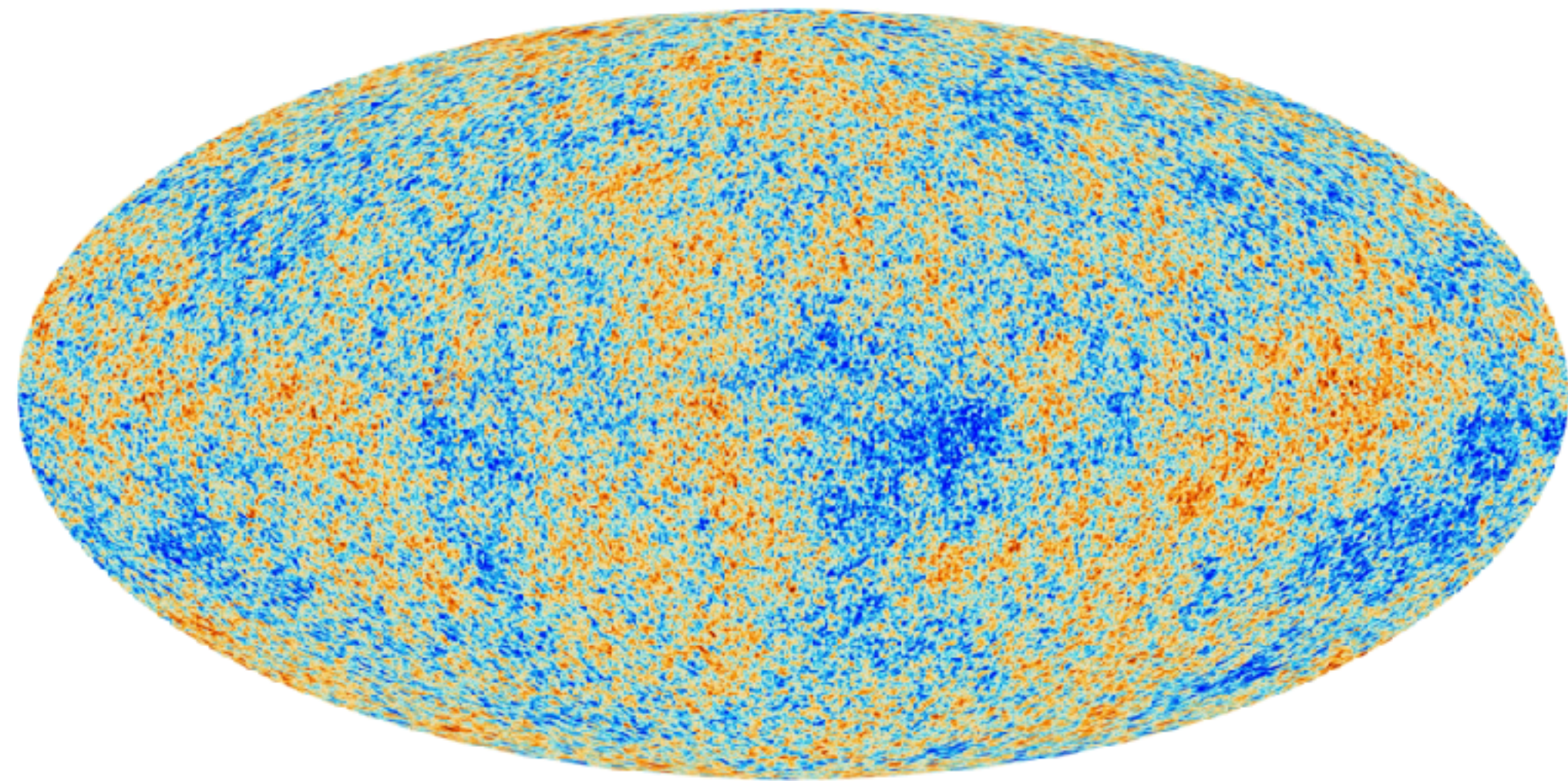
- ▶ Combination of **clumpiness** (amplitude of clustering on scales of 8Mpc/h) and the **total amount of matter**

$$\sigma_8 \Omega_m^{0.25}$$



MOTIVATION: LENSING MASS MAPS AS TESTS OF STRUCTURE GROWTH

- ▶ CMB lensing provide a powerful test of the Standard Cosmological model.
- ▶ Do observations match predictions of standard structure growth (dark matter, dark energy and GR)?

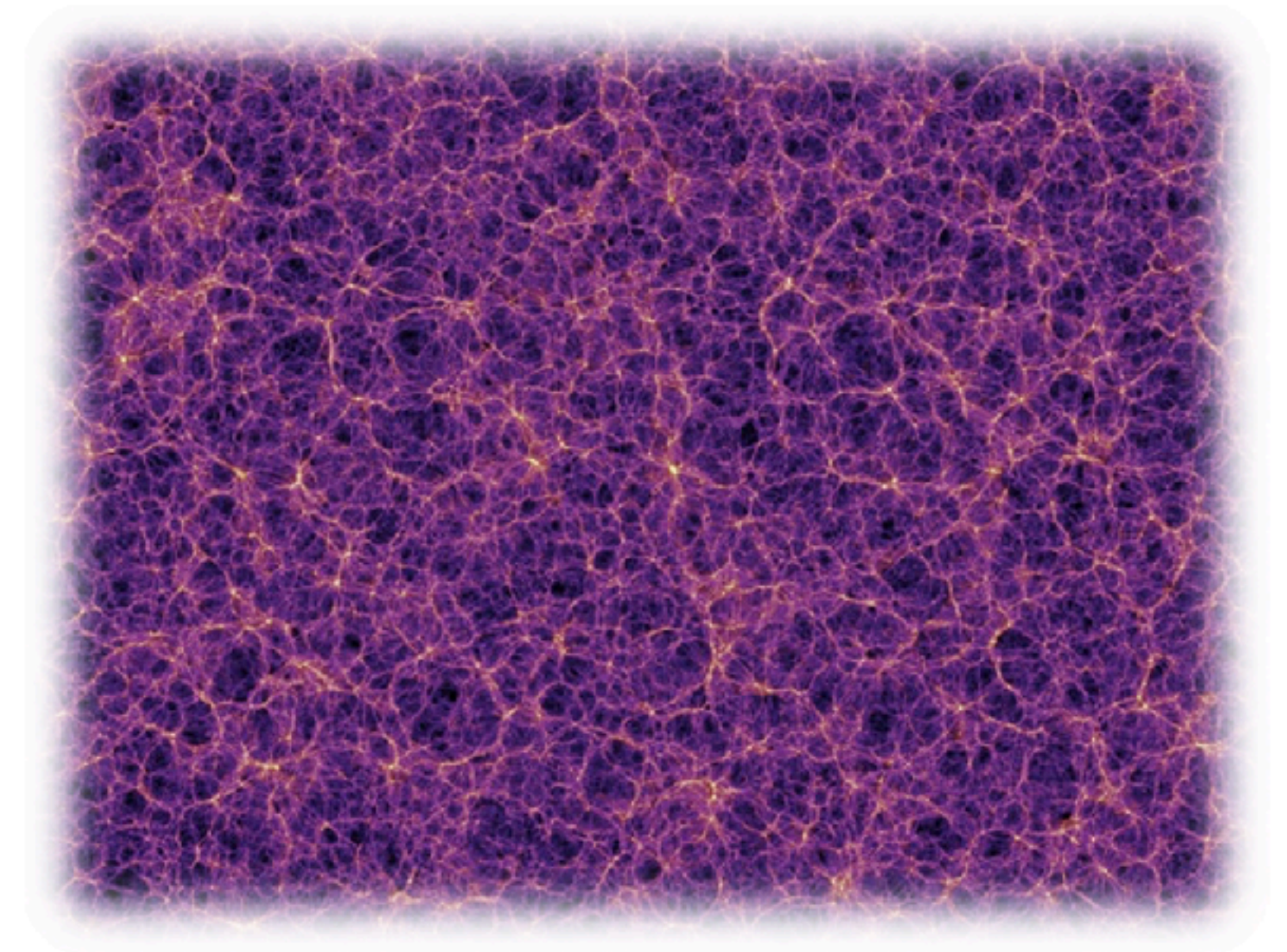


Fit standard cosmological model to the CMB at early times.

$t = 0.0004\text{Gyr}$

Predict size of structure formation at late times

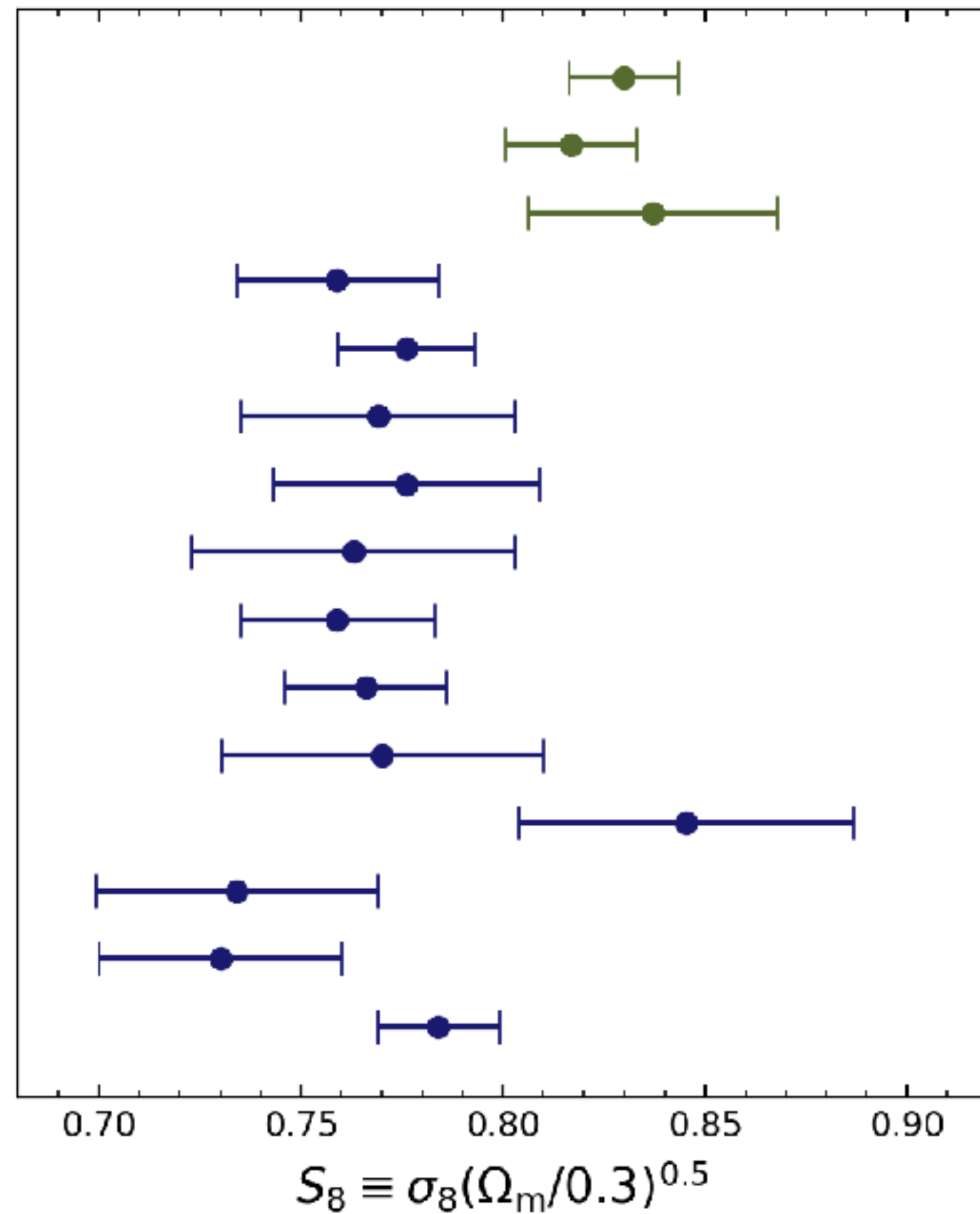
- ▶ Parametrize structure size today with σ_8 , RMS of matter density fluctuations smoothed on scales of $8\text{Mpc}/h$



Compare with observations

$t > 1\text{Gyr}$

MOTIVATION : LENSING MASS MAPS AS TESTS OF STRUCTURE GROWTH 'S₈ TENSION'



- CMB: Planck CMB aniso.
- CMB: Planck CMB aniso. (+A_{lens} marg.)
- CMB: WMAP+ACT CMB aniso.
- WL: DES-Y3 galaxy lensing
- WL: DES-Y3 3x2
- WL: HSC-Y3 galaxy lensing (Real)
- WL: HSC-Y3 galaxy lensing (Fourier)
- WL: HSC-Y3 3x2
- WL: KiDS-1000 galaxy lensing
- WL: KiDS-1000 3x2
- GC: BOSS EFT 2-pt + 3-pt
- GC: eBOSS BAO+RSD
- CX: SPT/Planck CMB lensing x DES
- CX: Planck CMB lensing x DESI LRG
- CX: Planck CMB lensing x unWISE

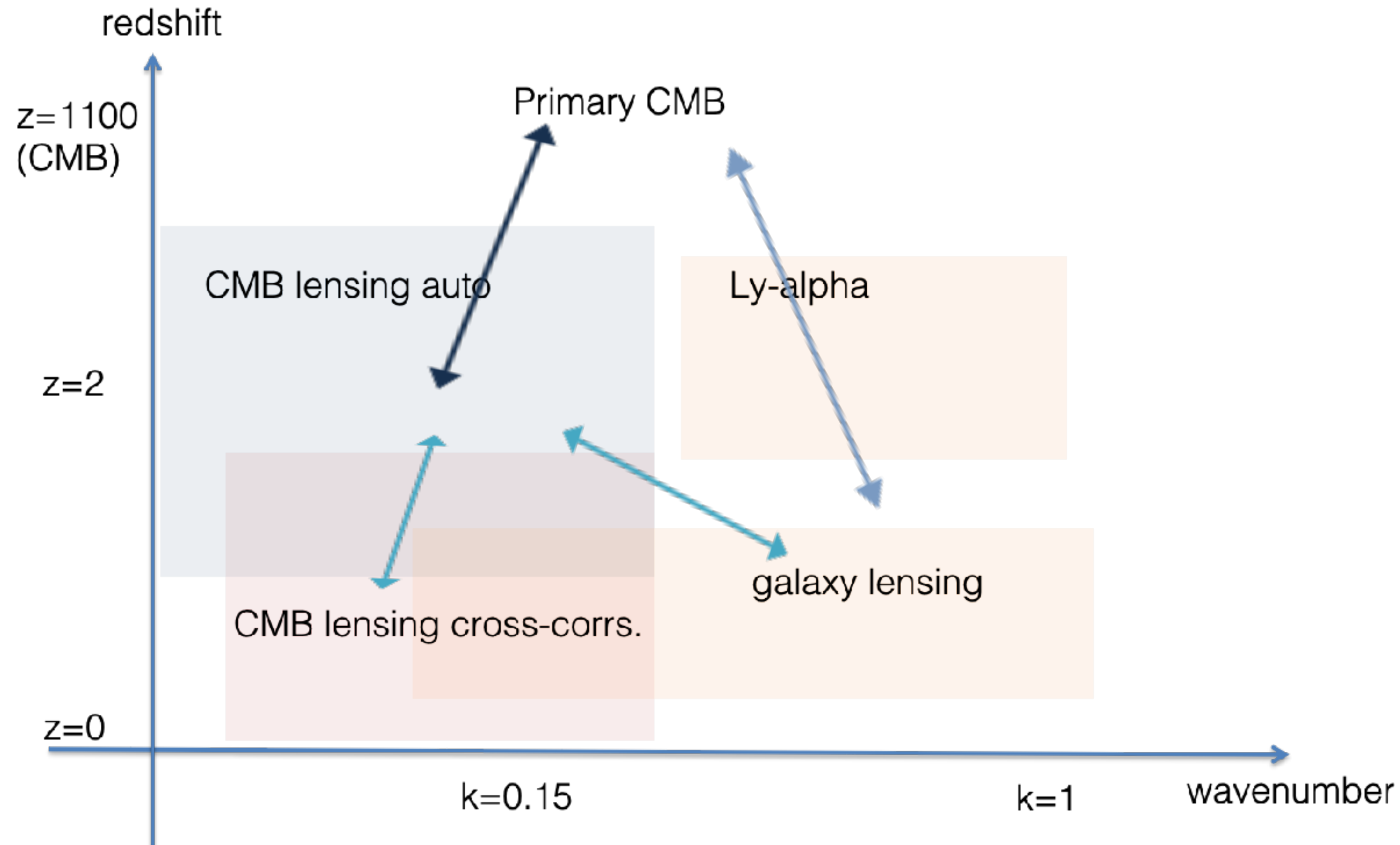


Direct low z measurements from galaxy surveys: 2-3 sigma low in several channels

We will present ~2% measurements of $\sigma_8\Omega_m^{0.25}$, S_8 and σ_8

HOW CAN CMB LENSING CLARIFY THE S_8 TENSION?

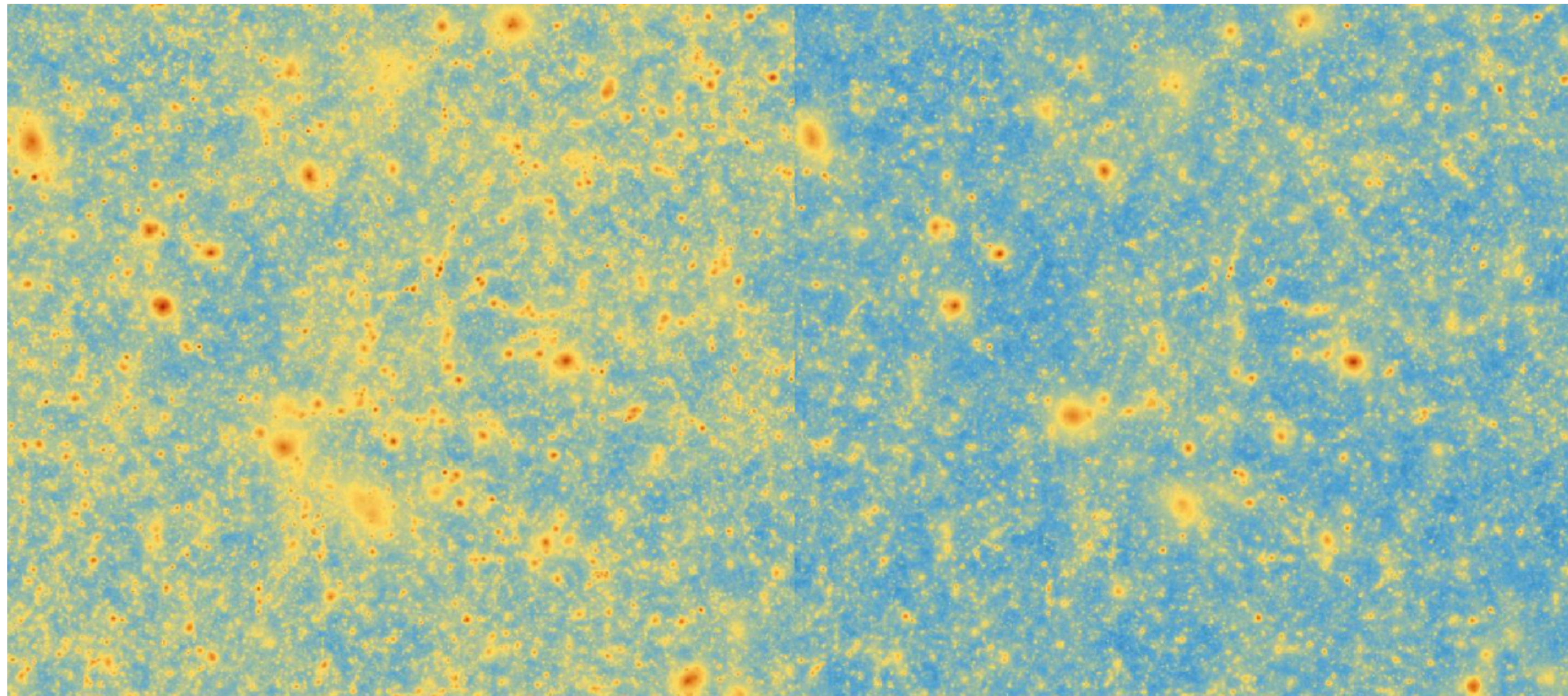
- ▶ Can give insight into systematics and test z/k dependence of any new physics



MOTIVATION 2 : MEASURING NEUTRINO MASS SUM

- ▶ Neutrinos affect structure growth: the more massive the neutrinos, the more the small scale growth are suppressed.

Large-scale mass
distribution



Massless neutrino

Massive neutrino

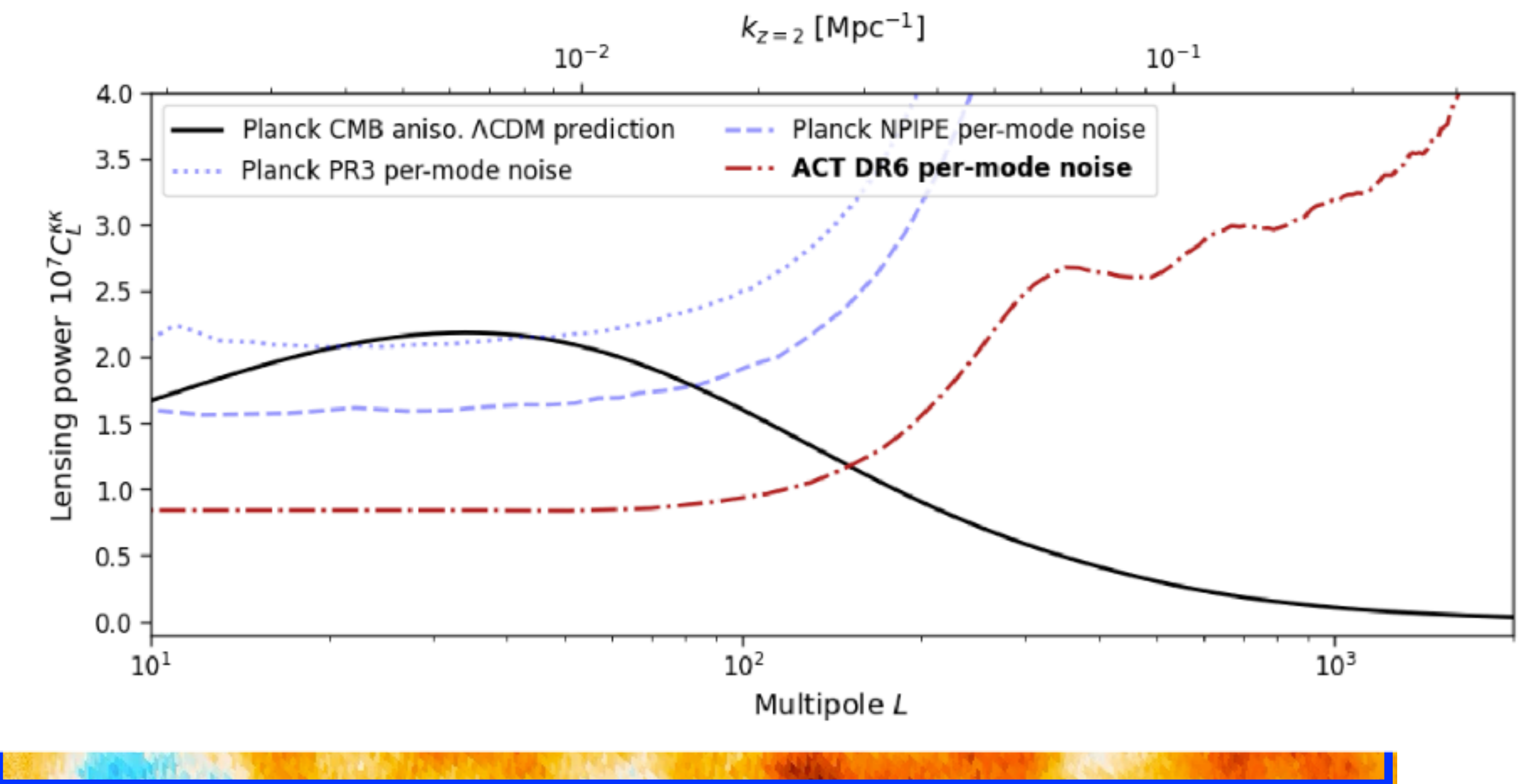
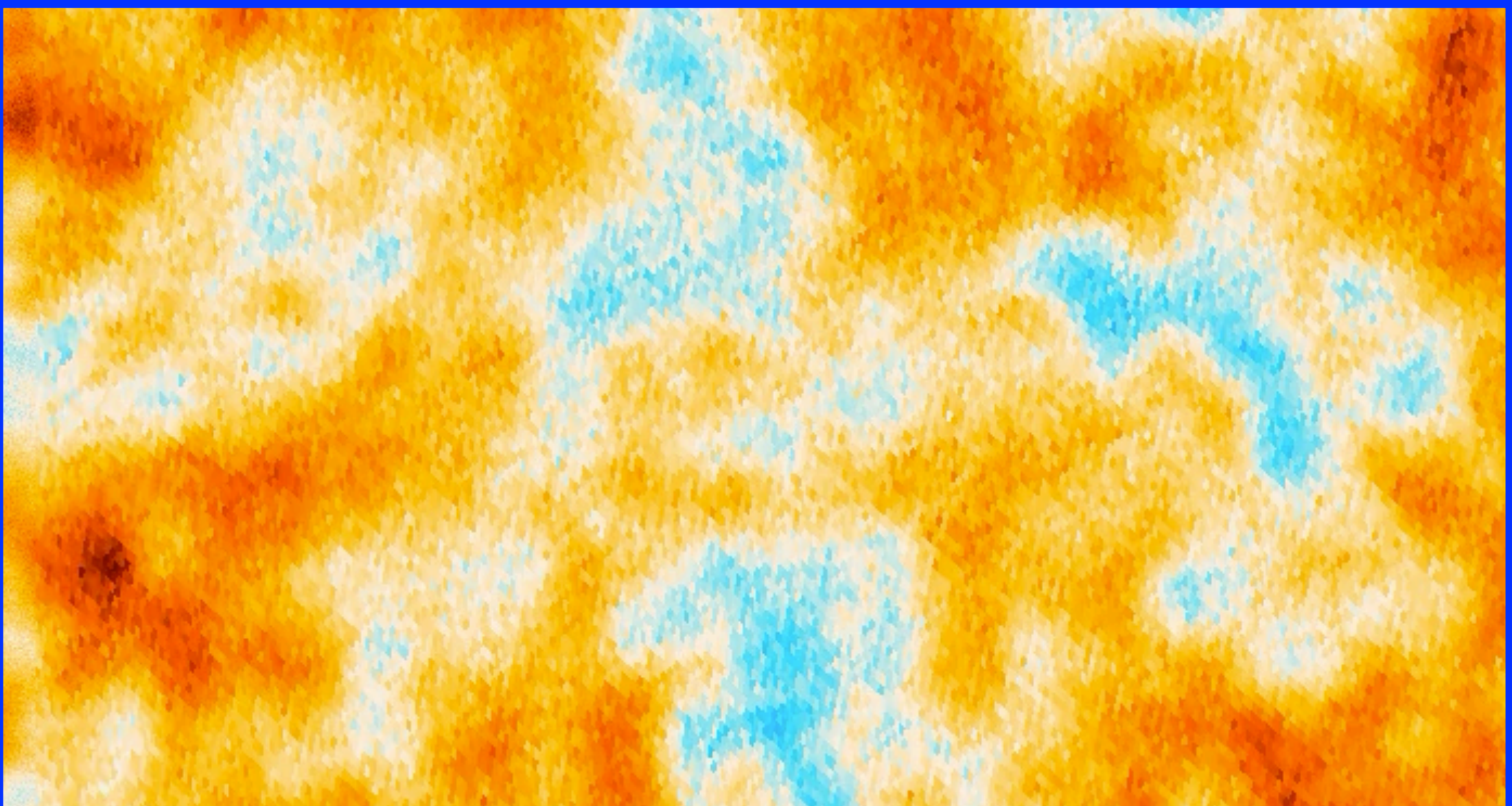
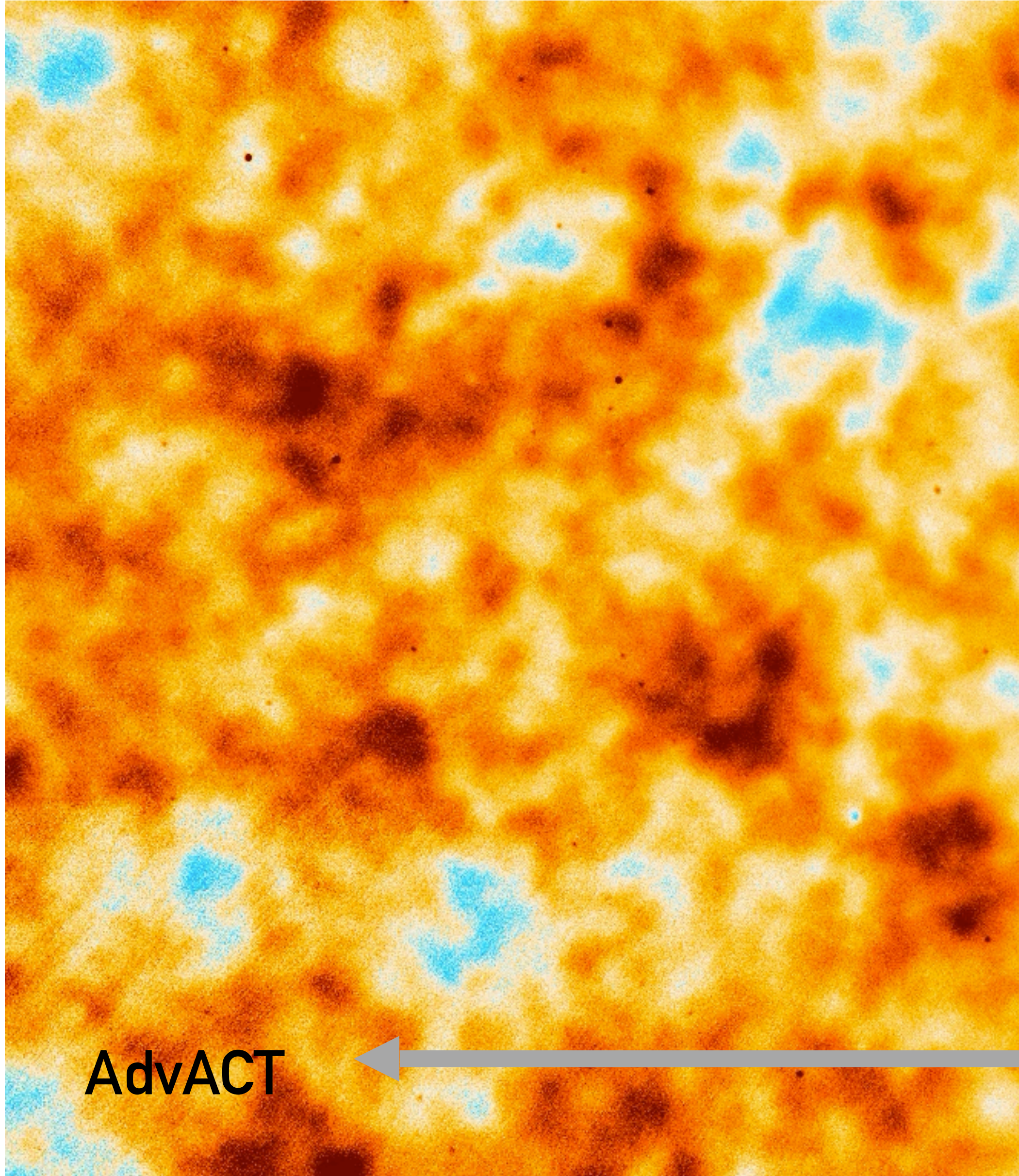
Probes approaching the 60meV lower limit using AdvACT, SPTPOL, SO, S4

ATACAMA COSMOLOGY TELESCOPE

Arcminute resolution CMB telescope, located in the Chilean Atacama desert



HIGH RESOLUTION CMB LENSING MEASUREMENTS FROM ADVACT

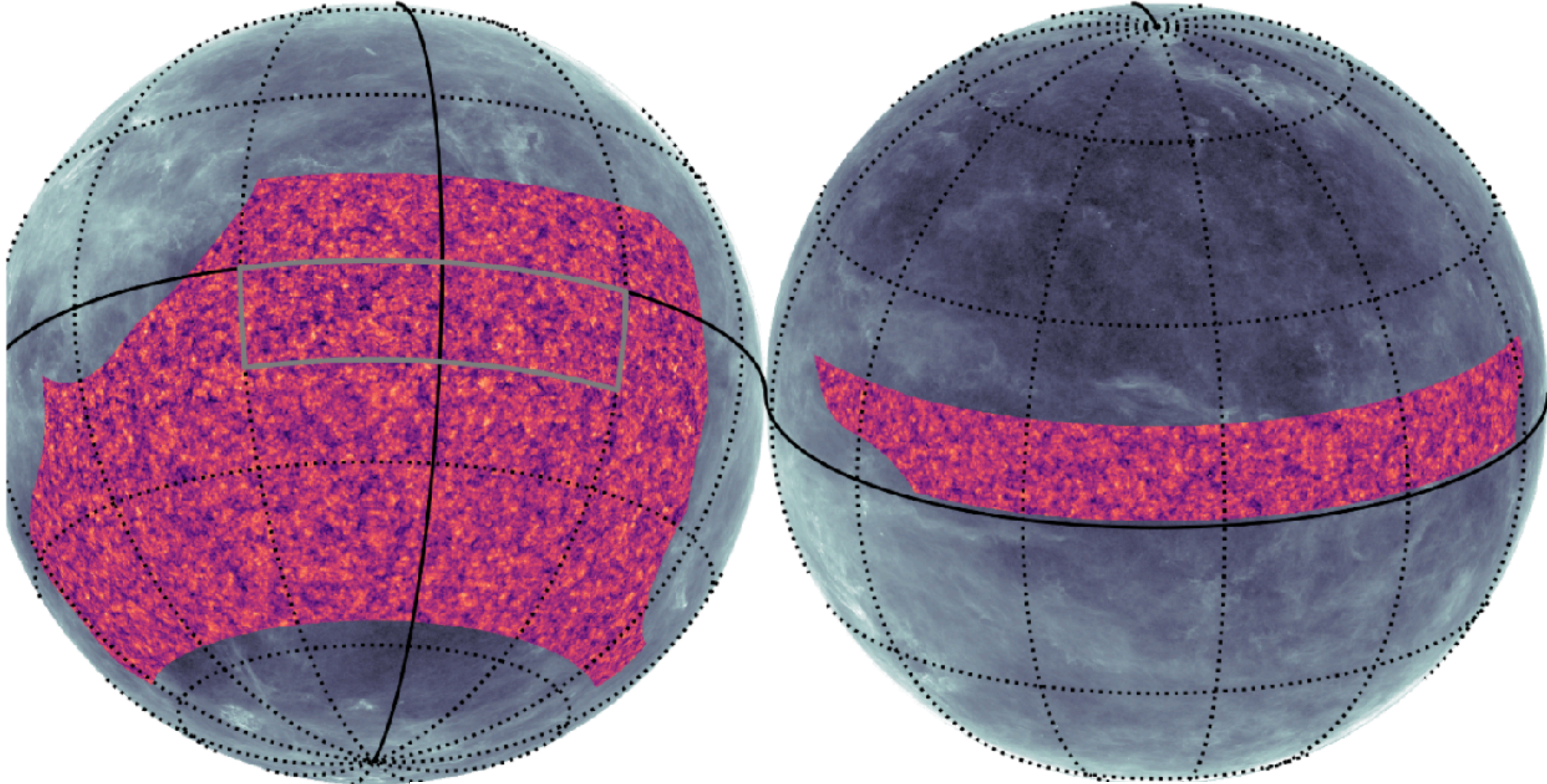


New DR6 AdvACT maps: 15uk 18000 sq degrees

Credits: Sigurd Naess

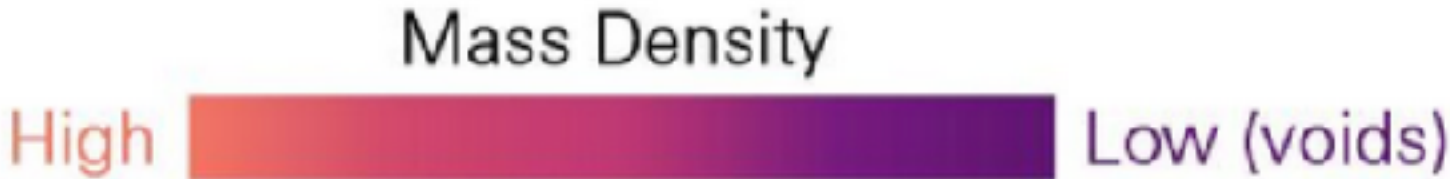
HIGH RESOLUTION CMB LENSING MEASUREMENTS FROM ADVACT

ACT DR6 CMB lensing mass map

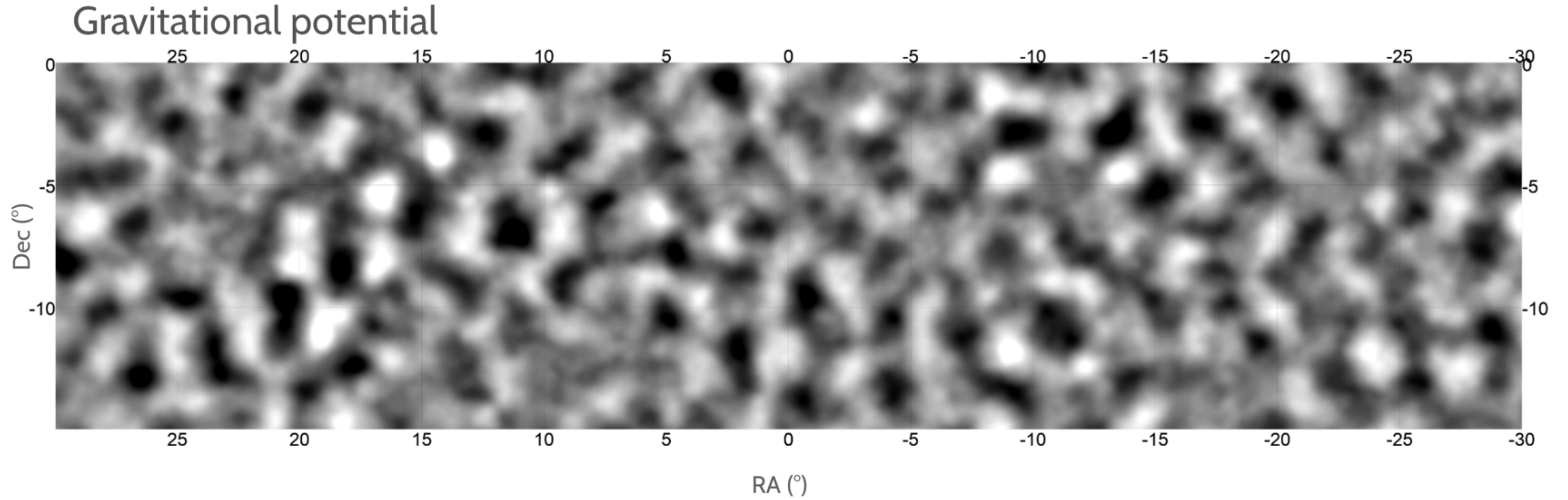


Gravitational Lensing Convergence

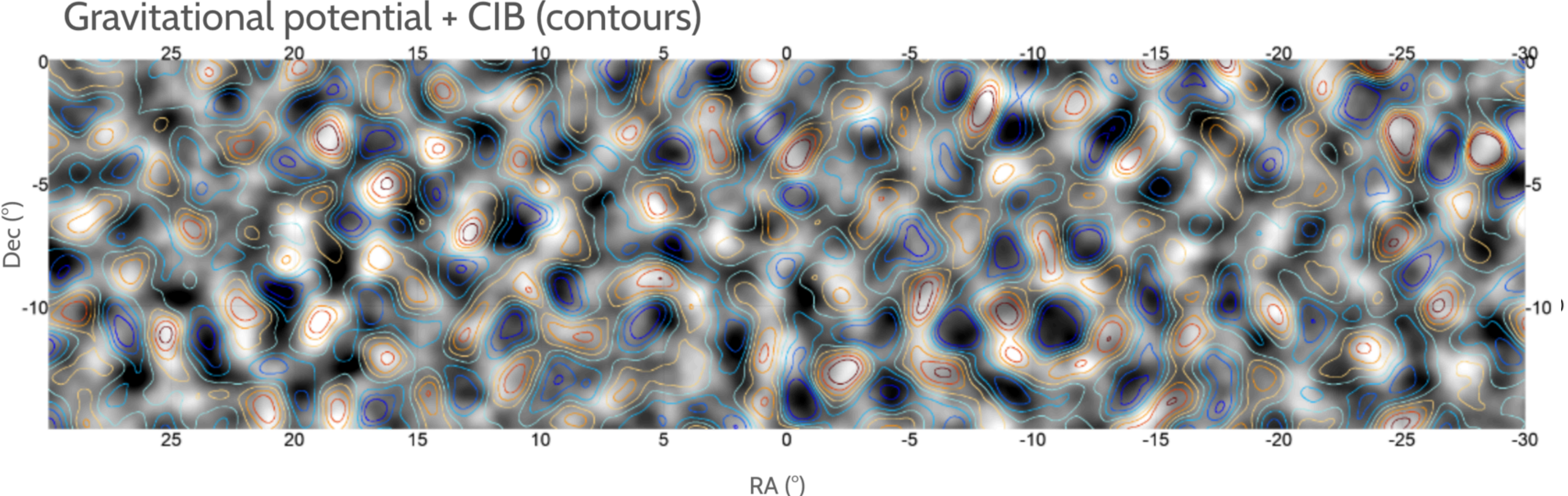
- ▶ Signal dominated lensing maps covering a quarter of the sky.
- ▶ These are high fidelity-> enabling seeing the dark matter by eye!



ZOOM IN OF 900 SQ. DEG OF THE 9400 SQ. DEG. MASS MAP

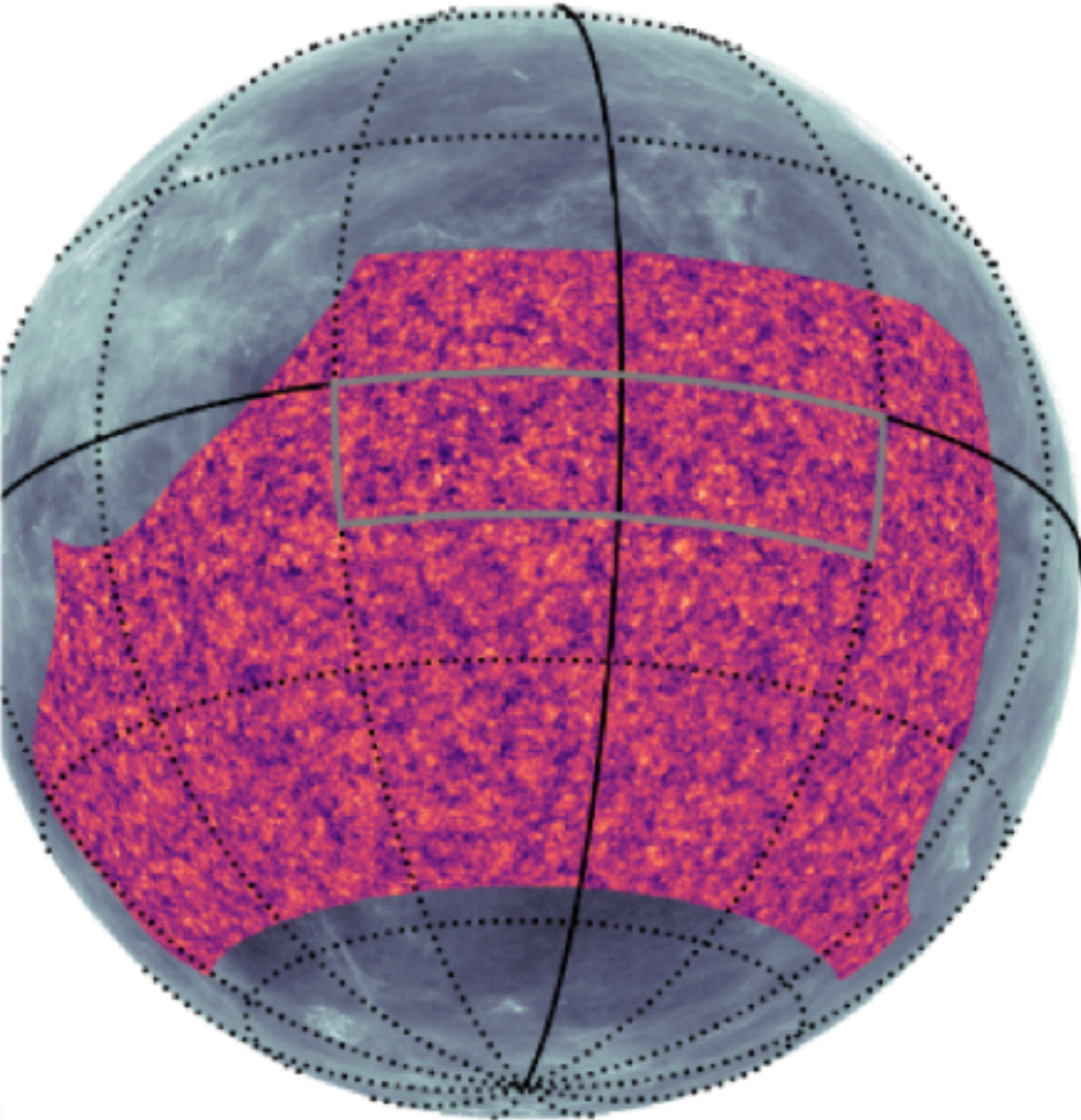


ZOOM IN OF 900 SQ. DEG OF THE 9400 SQ. DEG. MASS MAP

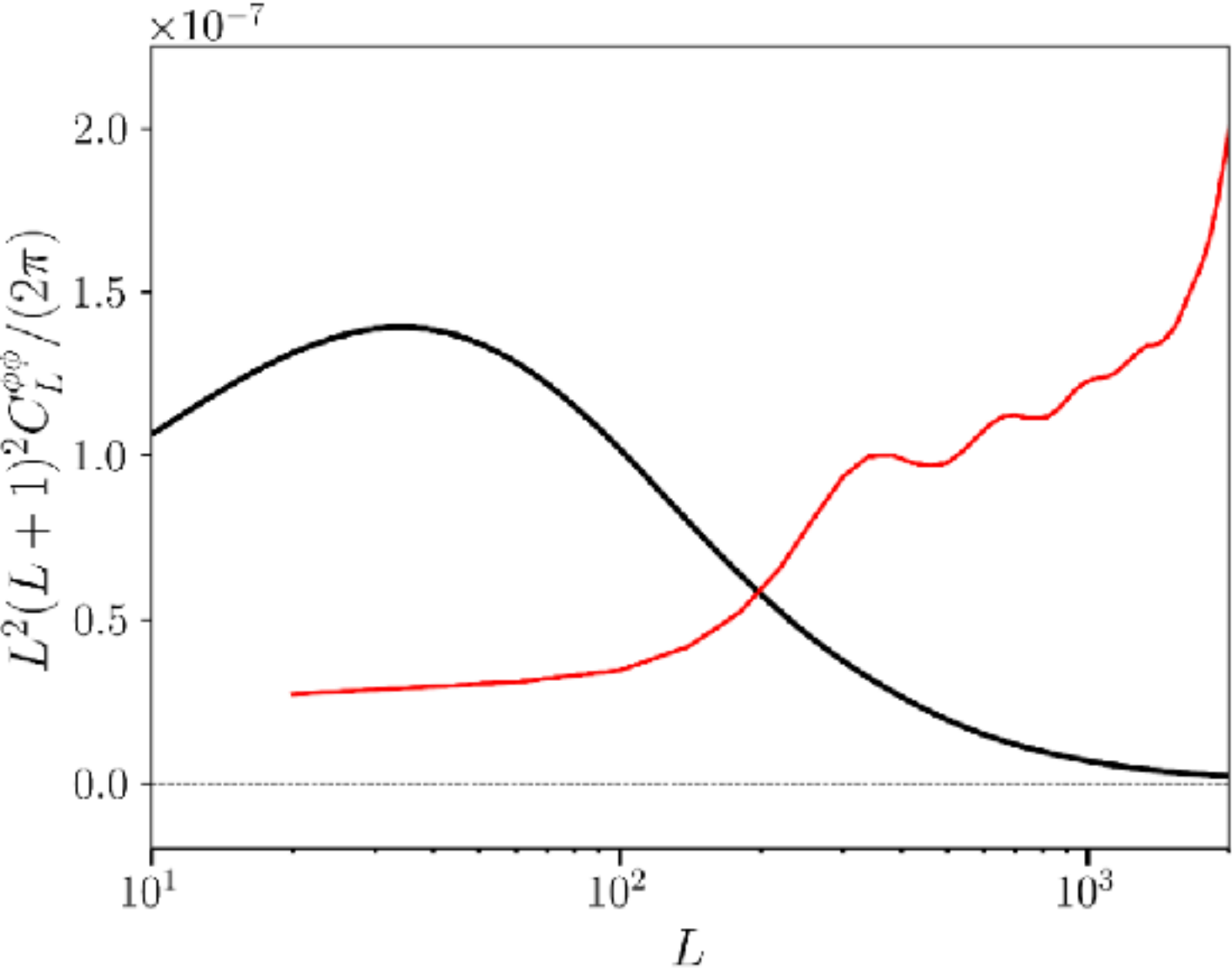


Correlation with dusty galaxies seen by eye

MEASURING THE CMB LENSING POWER SPECTRUM (NEW LENSING PIPELINE)



$$\hat{C}_L^{\phi\phi} \sim \langle \hat{\phi}_{LM} \hat{\phi}_{LM}^* \rangle$$



$$C_L^{\phi\phi} \sim \langle \phi(\mathbf{L}) \phi^*(\mathbf{L}) \rangle - \text{Gaussian bias}$$

Schematically

$$\langle TTTT \rangle - \langle TT \rangle \langle TT \rangle$$

Gaussian contractions give large bias

Our lensing spectrum pipeline subtracts **noise biases** from naive power spectrum

BLINDED ANALYSIS FRAMEWORK WITH EXTENSIVE NULL TEST SUITE

- ▶ DR6 lensing analysis follows blinded analysis procedure. (No comparison with theory/ other data, parameter runs)
- ▶ DR6 dataset allows rigorous check for consistency and presence of systematics.

200 null tests broadly divided into the following categories:

Foreground tests

- Polarization vs temperature consistency
- Frequency consistency in map and spectrum.
- Shear estimator
- Galactic foreground/ sky area tests

Signal Isotropy tests

Cross linking tests
Patch based tests
North vs South

Curl deflection tests

Scale tests

- k-space filtering
- min-max multipole variation
 - 300 < ℓ < 3000
 - 500 < ℓ < 3000
 - 600 < ℓ < 3000
 - 600 < ℓ < 2500
 - 1500 < ℓ < 3000

Instrument related tests

Noise only tests
Array difference tests
PWV tests
Season difference tests

SYSTEMATIC CHALLENGES FOR OUR MEASUREMENT

Generally, CMB lensing quite robust: known redshift and source, near-linear matter with baryonic effects currently negligible.

Key challenges:

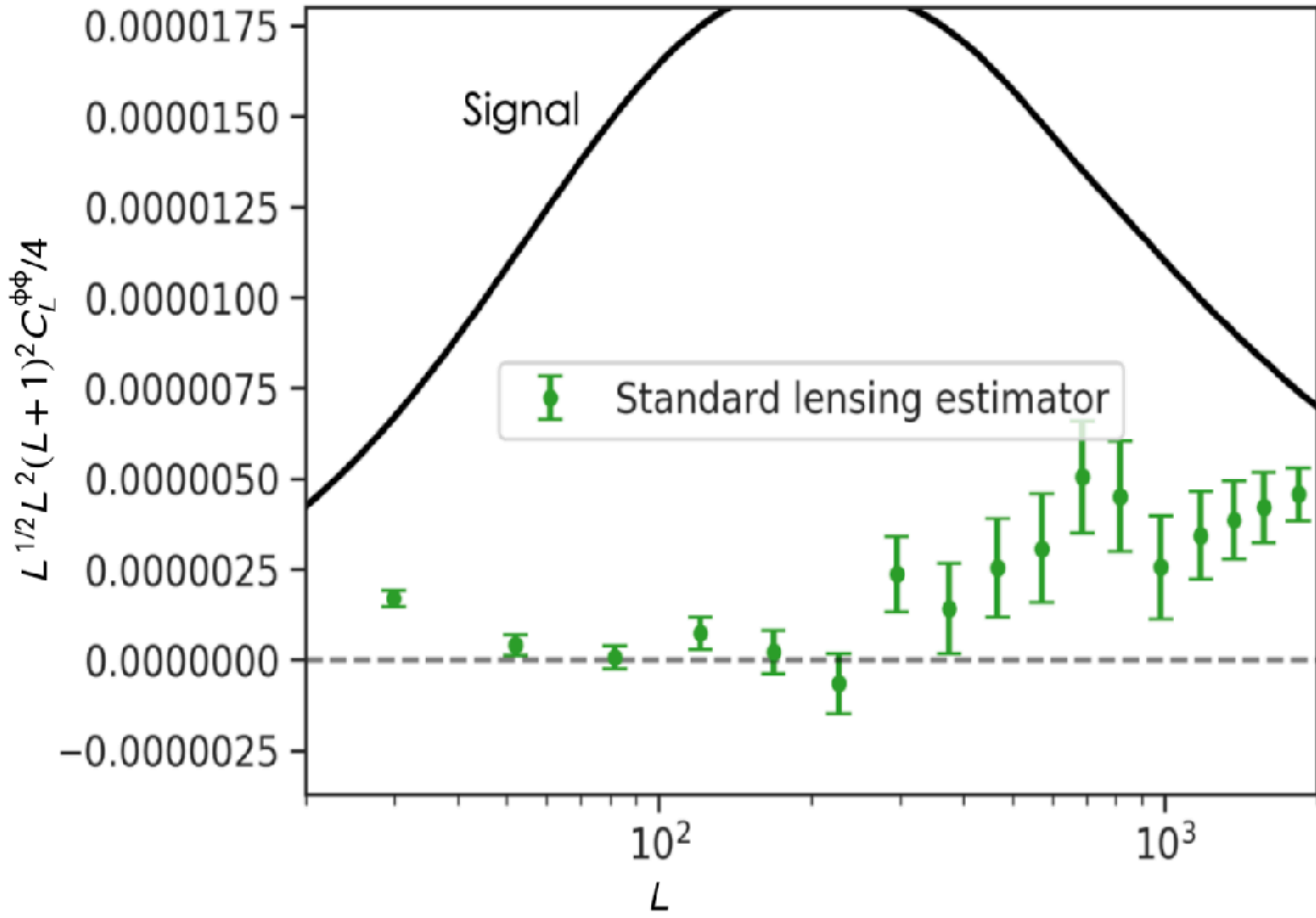
- **Accuracy of ground-based noise bias subtraction**
- **Foregrounds! Mainly extragalactic**

Today's focus

Also investigated instrument-related systematics with simulations and data - crucial work led by DW. Negligible effects found (earlier simulations also show subdominant levels at our SNR).



CHALLENGE I: NOISE BIAS SUBTRACTION

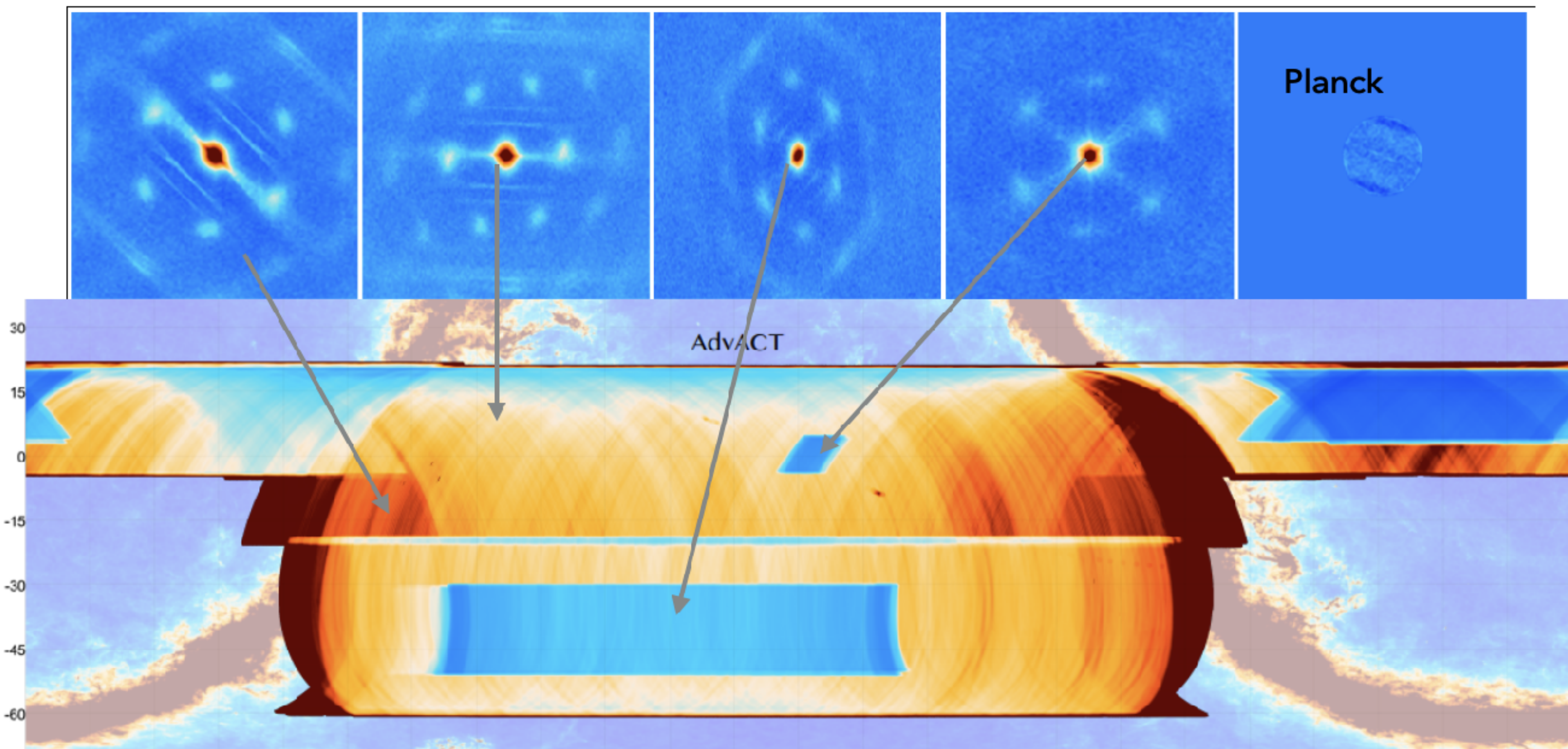


- ▶ Run data **noise only** maps through lensing power spectrum pipeline.

Expectation
Result should be consistent with zero.

Reality
U shape failure

CHALLENGE I: NOISE BIAS SUBTRACTION



Noise complexities for ground based surveys difficult to model.

- ▶ atmospheric noise
- ▶ spatial inhomogeneities from scan strategy

Lot of noise simulation improvements

See Atkins et al 2023



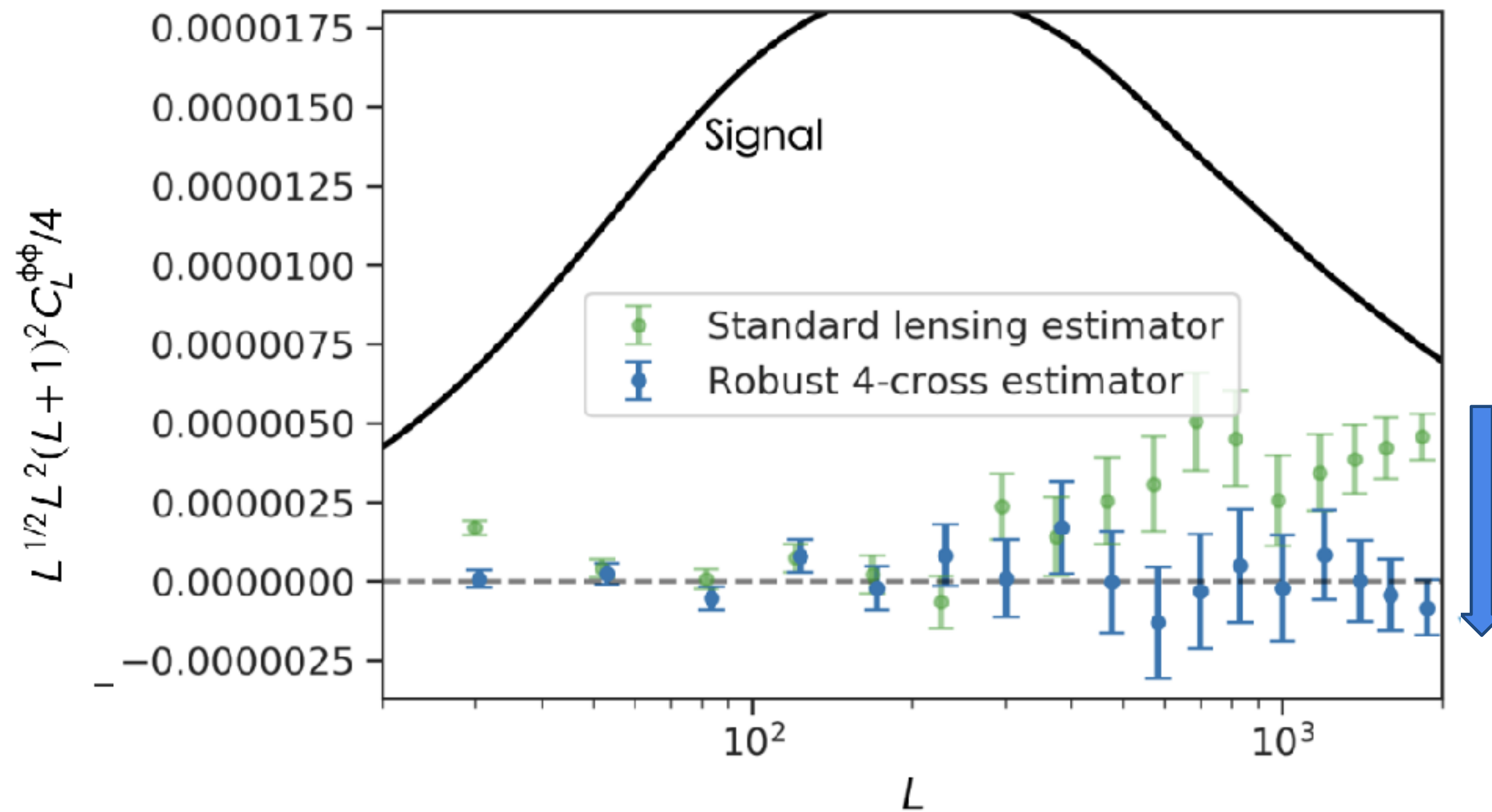
SOLUTION: CROSS CORRELATION BASED ESTIMATOR

- Use 4 CMB maps with independent noise.
Immune to noise modelling

Madhavacheril, Smith, Sherwin, Naess et al 2020, JCAP

$$C_L^{\phi\phi, \text{cross}} \sim \langle T_1 T_2 T_3 T_4 \rangle$$

maps with independent noise



- Run data noise only maps through lensing power spectrum pipeline

now pass the null test with robust cross estimator

CHALLENGE II: CONTAMINATION FROM EXTRA-GALACTIC FOREGROUNDS

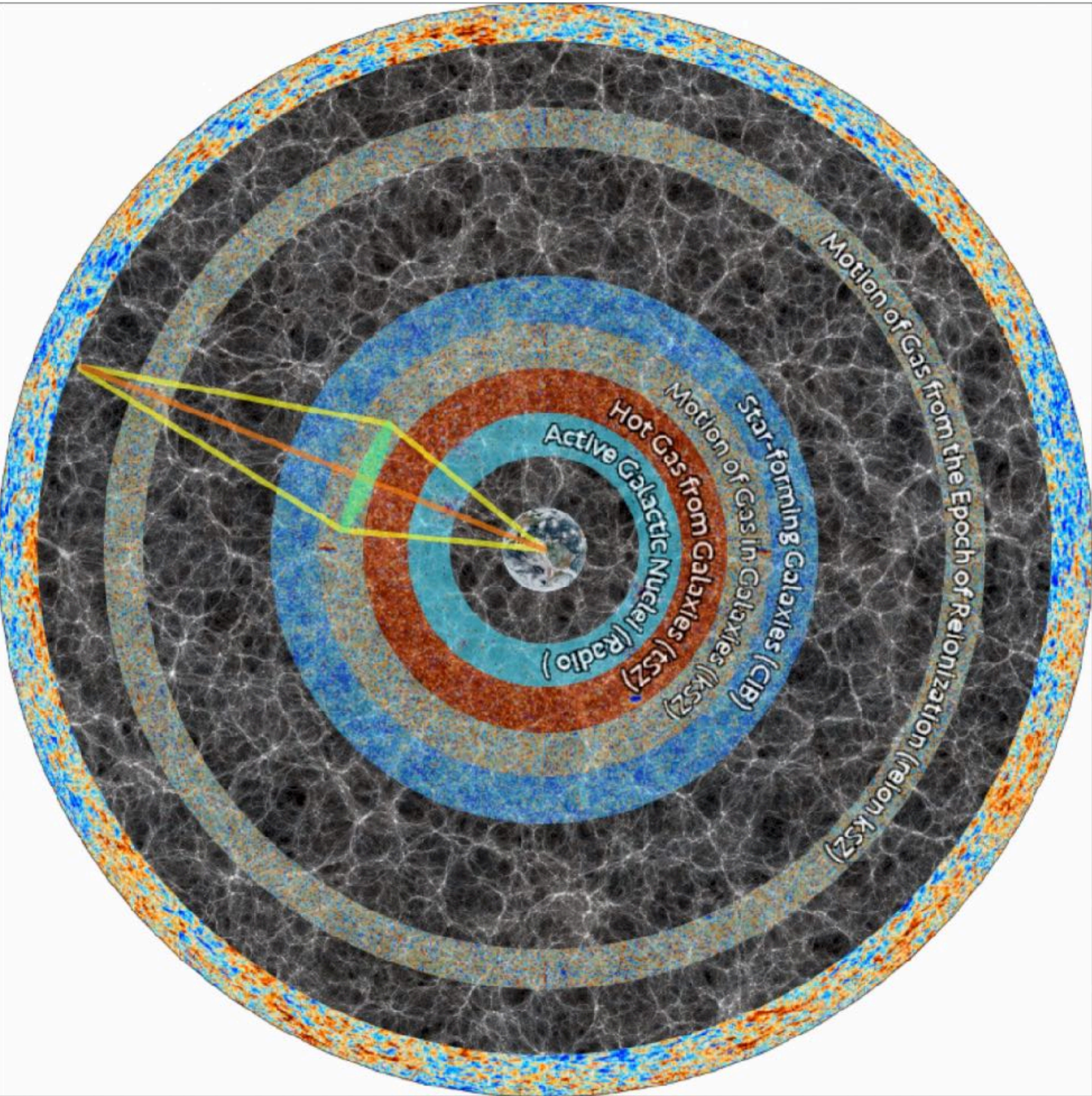
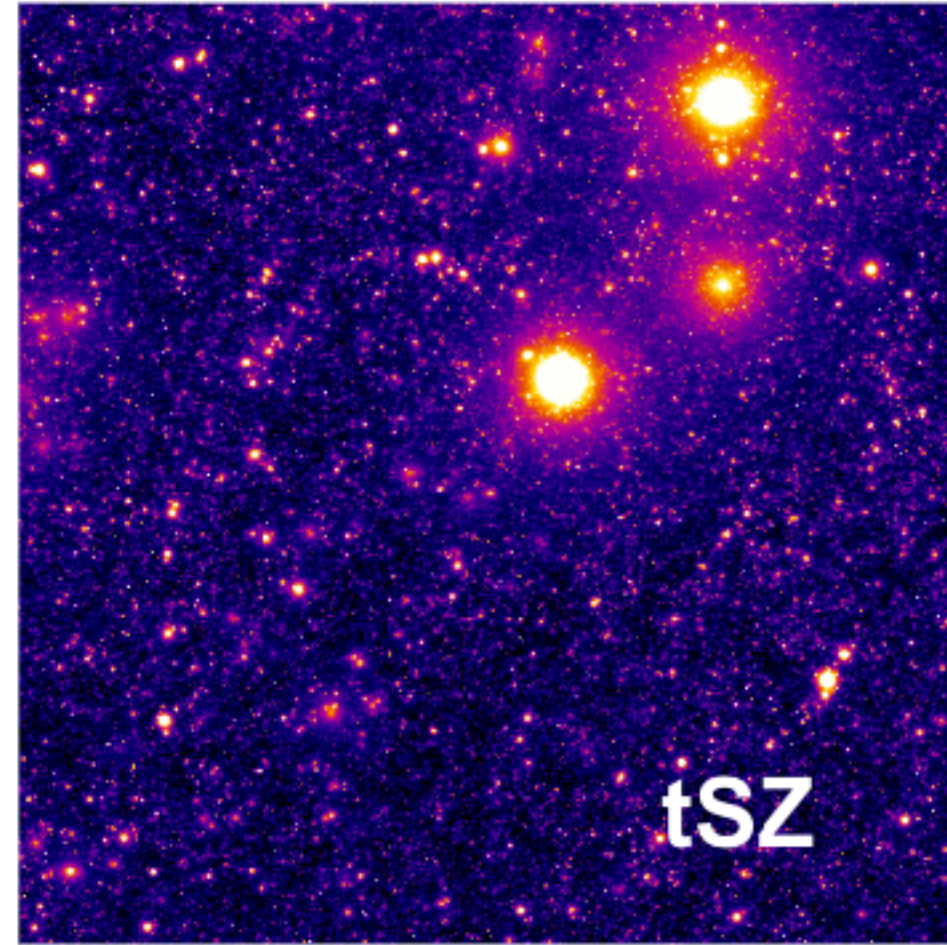
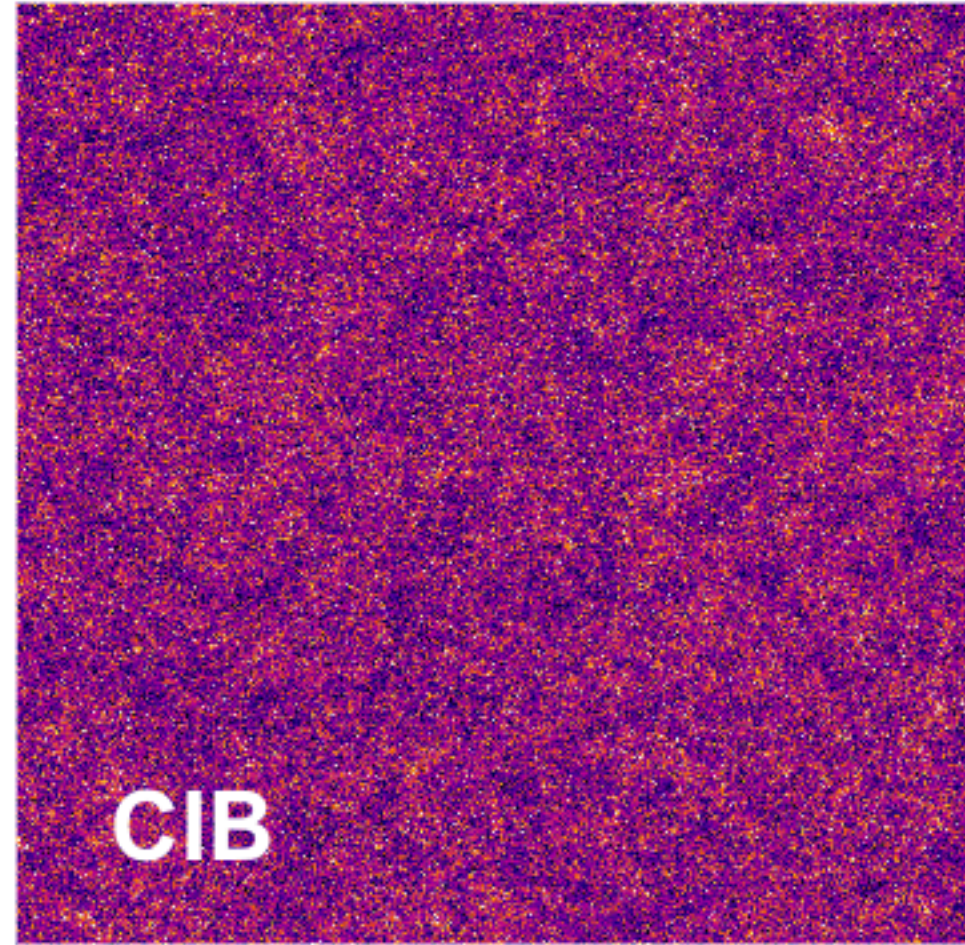


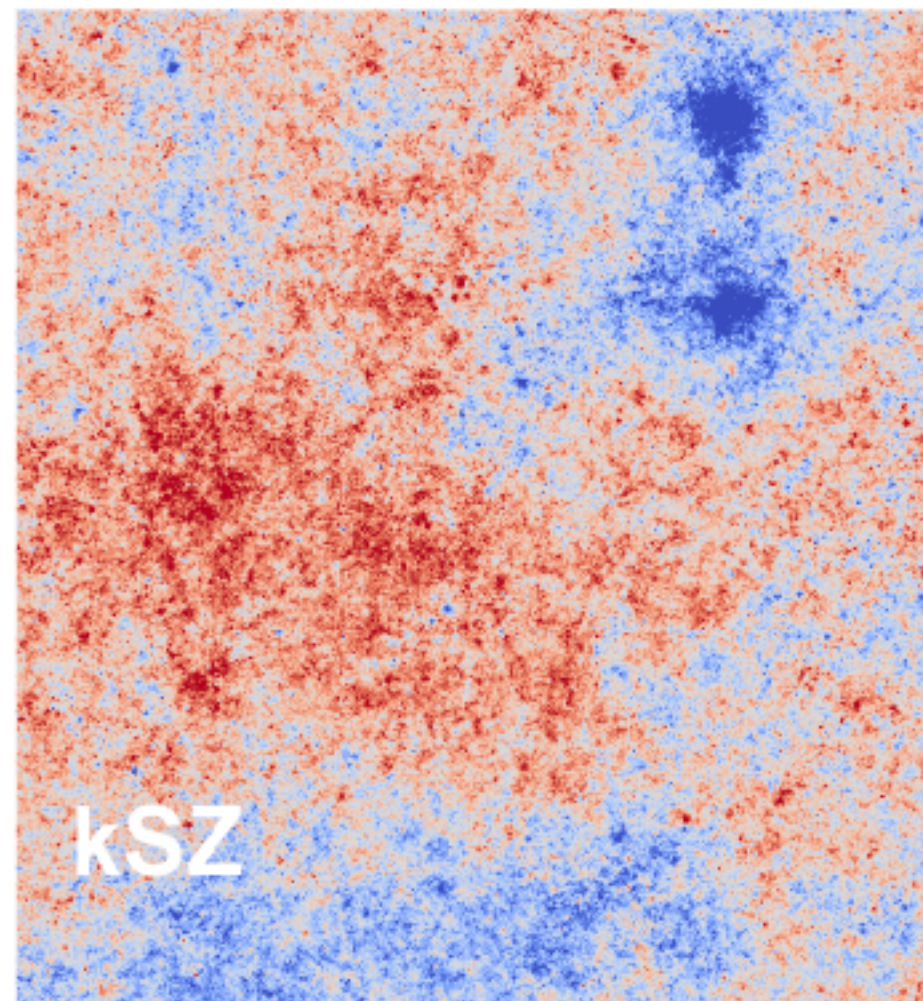
image credit: Dongwon Han

Challenge II: Biases From Extragalactic foregrounds



- ▶ CMB maps contains from radio point sources, cosmic infrared background (CIB), thermal and kinetic SZ effects.

$$T = T_{\text{CMB}} + f$$

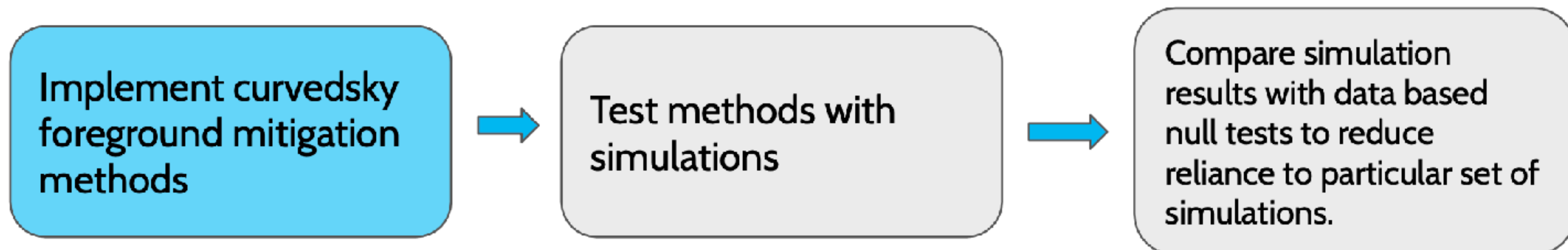


$$C_L^{\phi\phi} \sim \langle \text{QE}[T_{\text{CMB}}, T_{\text{CMB}}] \text{QE}[T_{\text{CMB}}, T_{\text{CMB}}] \rangle \text{ Lensing signal}$$

$$+ 2 \langle \text{QE}[T_{\text{CMB}}, T_{\text{CMB}}] \text{QE}[f, f] \rangle + 4 \langle \text{QE}[T_{\text{CMB}}, f] \text{QE}[T_{\text{CMB}}, f] \rangle$$

$$+ \langle \text{QE}[f, f] \text{QE}[f, f] \rangle \text{ Foreground induced biases}$$

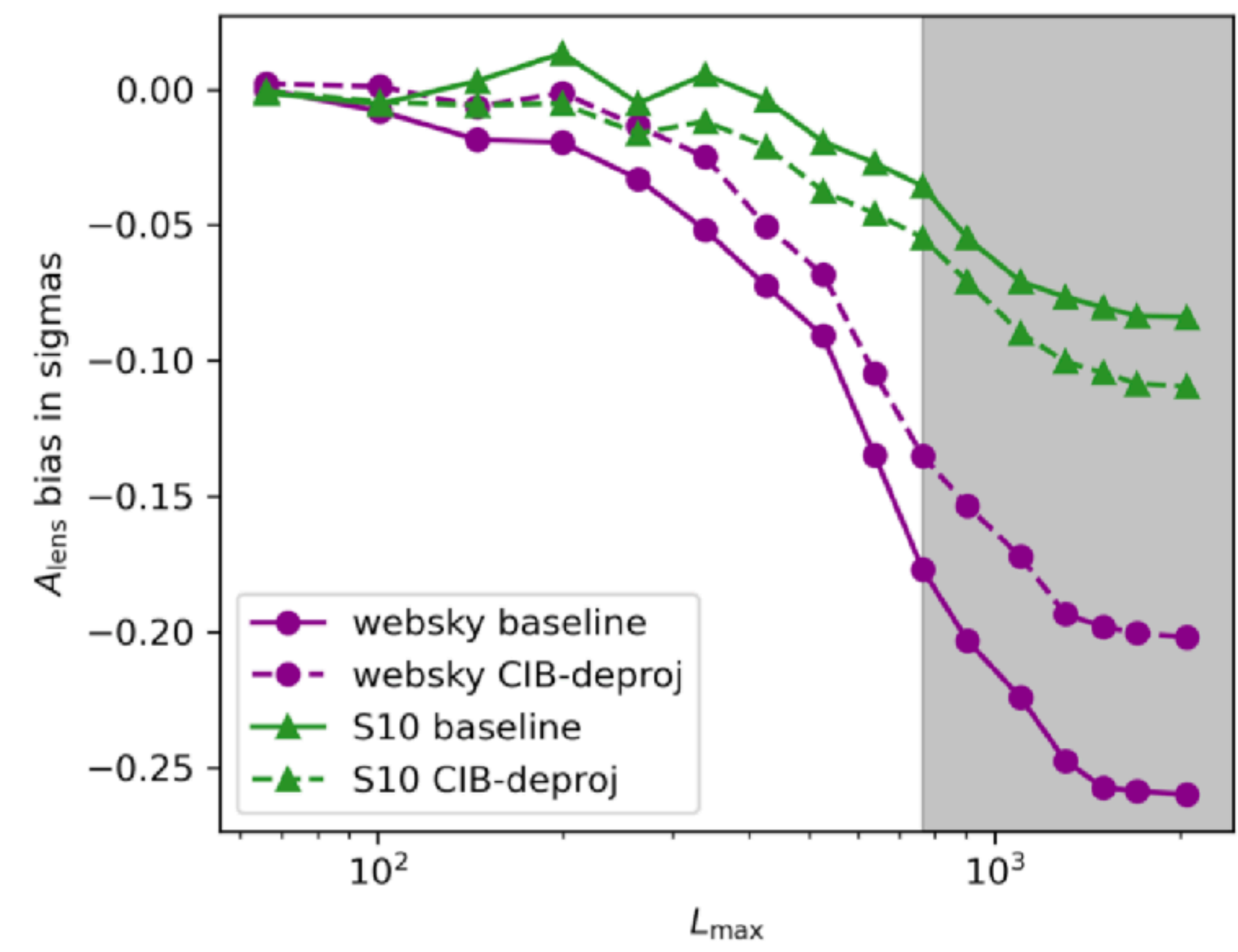
Foreground mitigation pipeline (Simulate bias estimates)



AdvACT Lensing: Repertoire of mitigation methods

- ▶ **Geometric methods**
 - ▶ Profile hardening [Sailer+2022](#)
 - ▶ Shear [Schaan+Ferraro 2019, Qu+2022](#)
- ▶ **Multifrequency**
 - ▶ CIB deprojection + Profile hardening
- ▶ **Simulated biases negligible in both methods (2 different sims)**

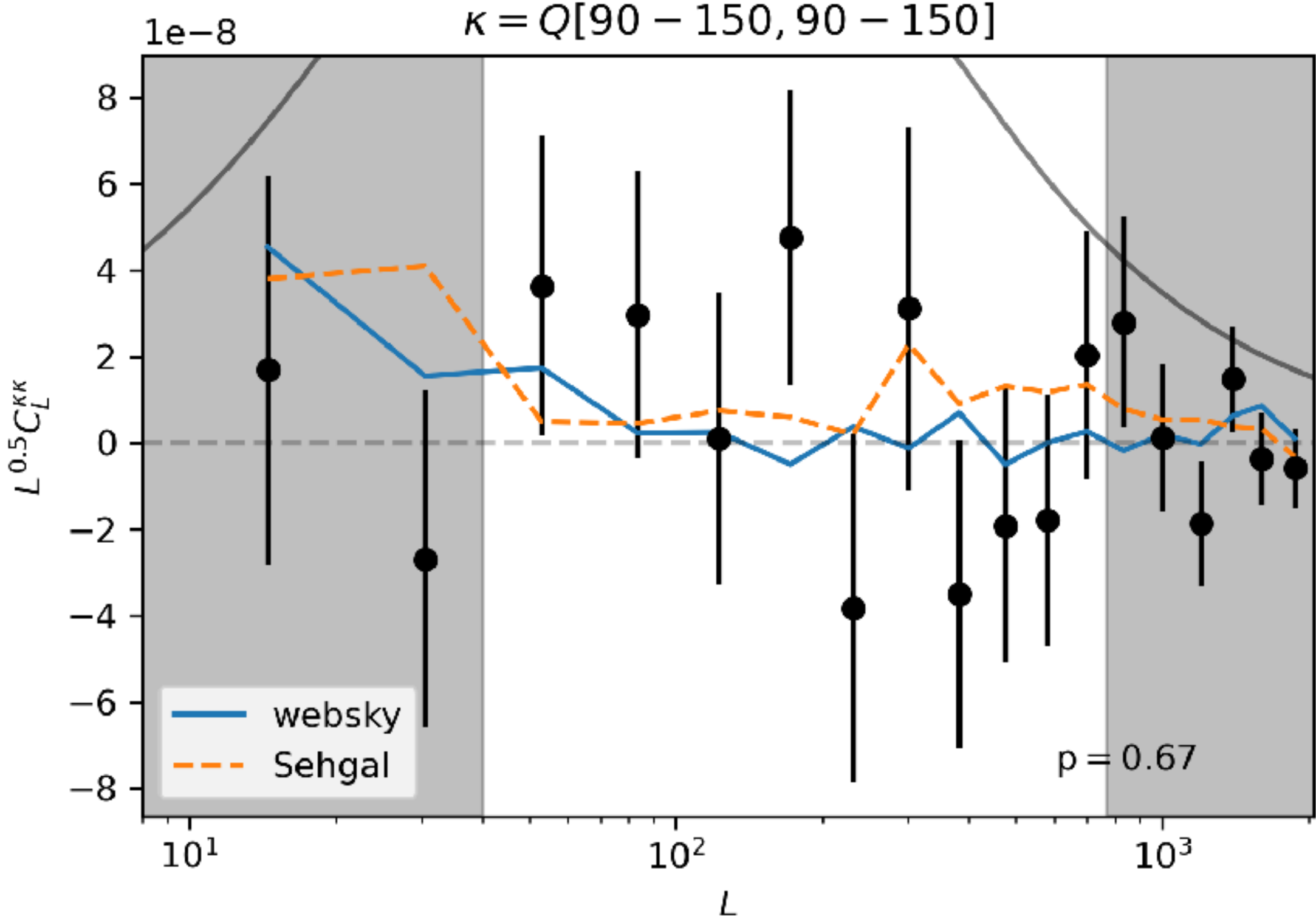
Gives foreground bias $< 0.2 \times$ statistical uncertainty



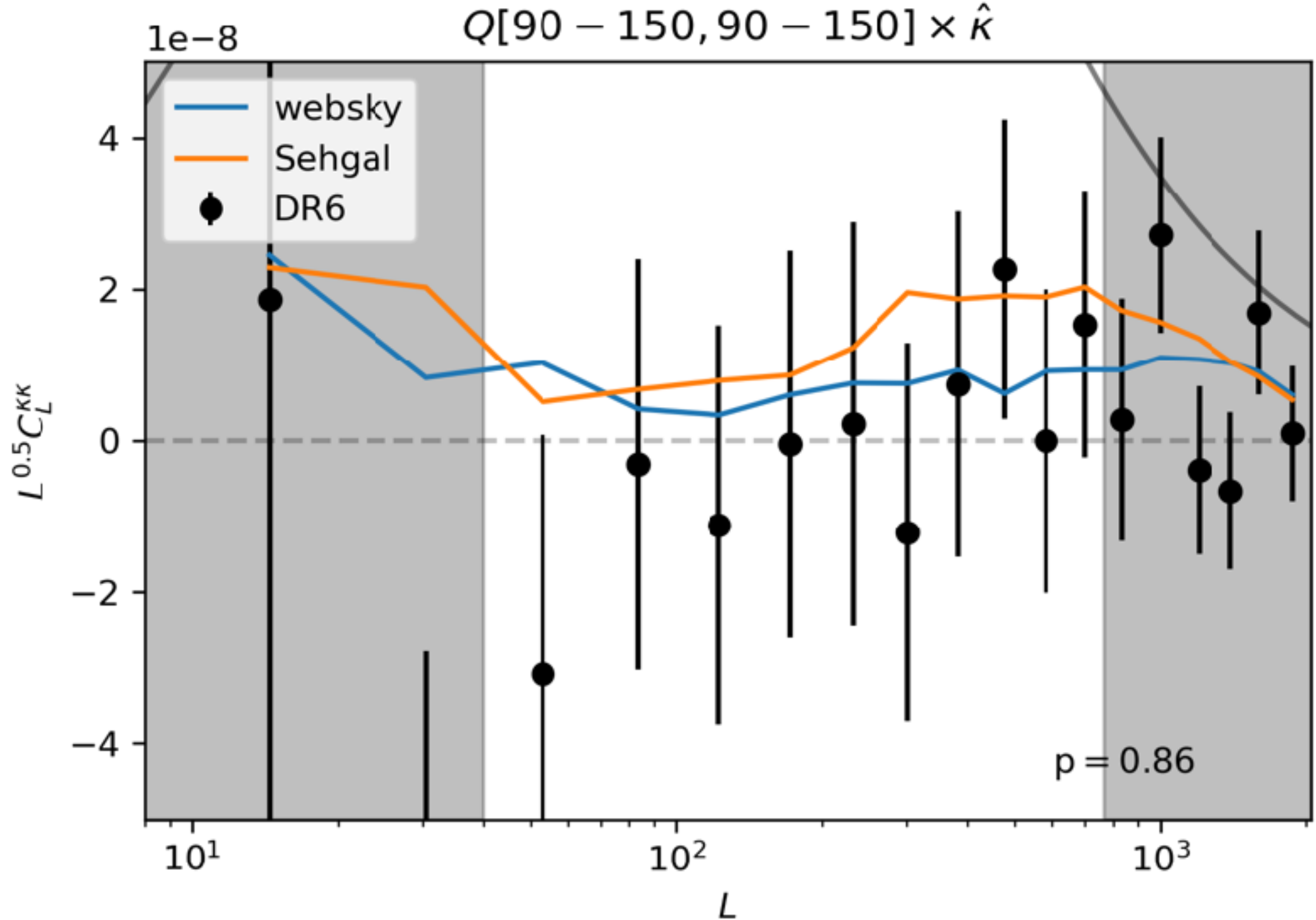
BASELINE MITIGATION TECHNIQUE: PROFILE HARDENING

Construct estimators that are insensitive to mode couplings generated by a particular field (tSZ clusters/CIB/point sources)

Null tests leveraging the 90 and 150 GHz frequencies to isolate the different foreground biases

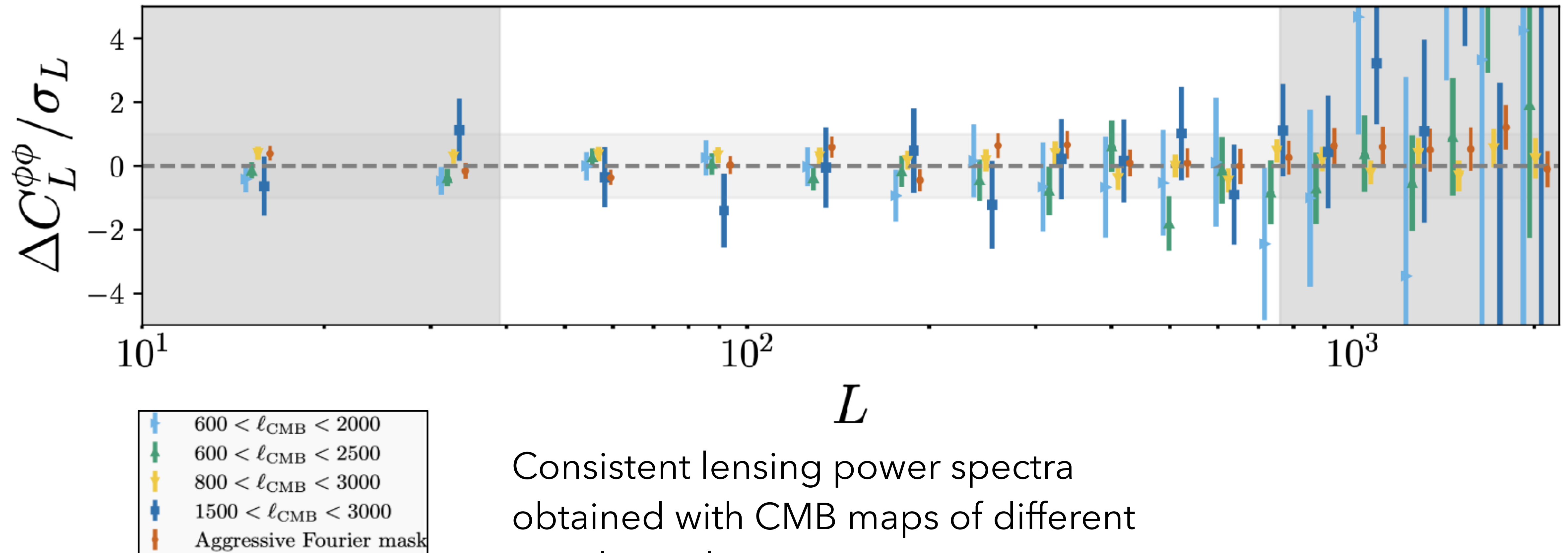


Testing the foreground trispectrum



Testing the primary bispectrum

NULL TESTS NOW PASSES! ONE EXAMPLE:

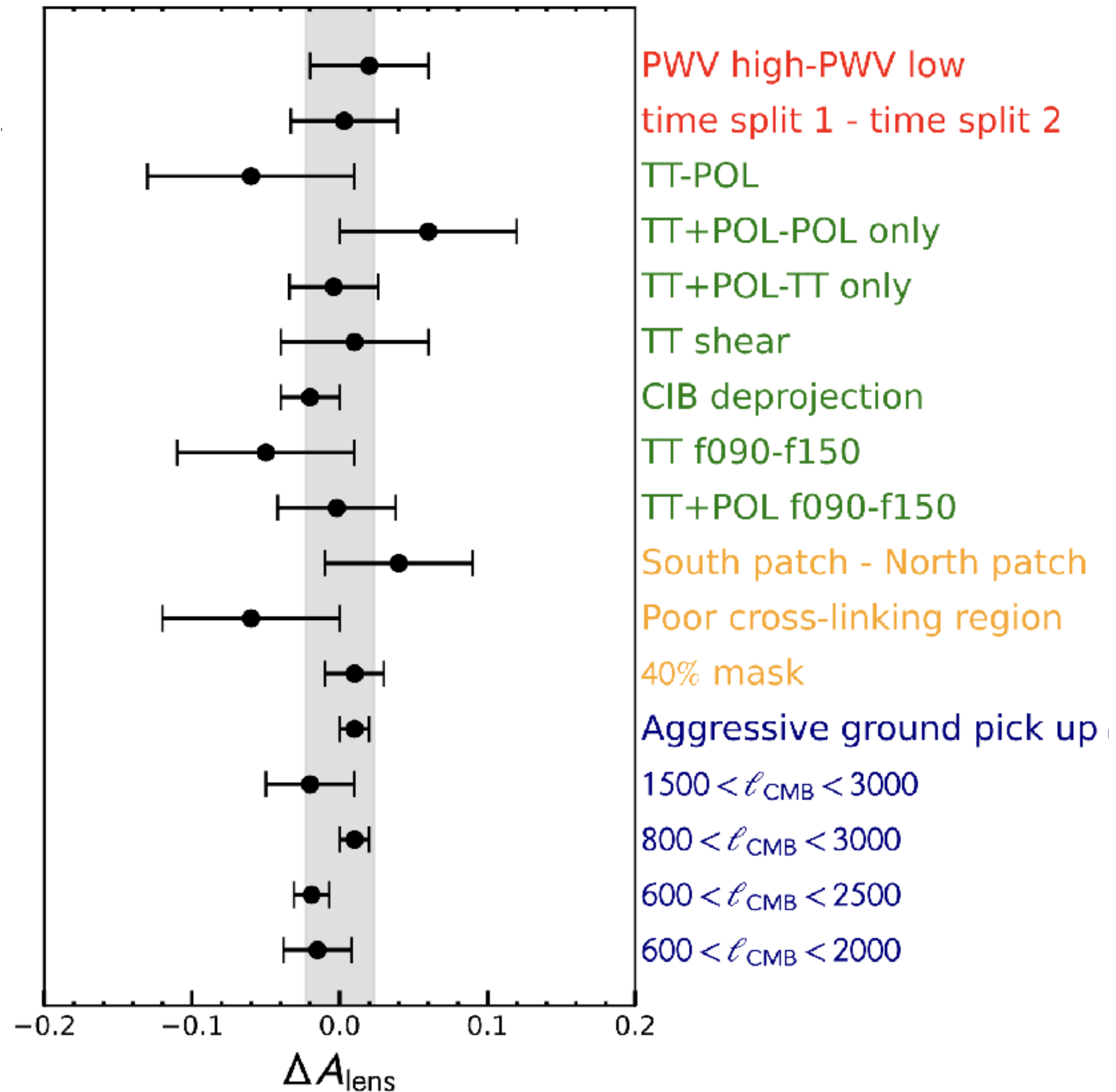


Consistent lensing power spectra obtained with CMB maps of different angular scales.

- **Consistent** lensing spectra obtained across scales, regions, frequencies, polarization combinations, instrument arrays, time,...

NULL TESTS NOW PASSES! STABILITY OF THE LENSING SPECTRUM

Consistent amplitude of lensing spectrum A_{lens}



at different times

in polarization

w. different foreground cleaning

at different frequencies

in different parts of sky

on different scales

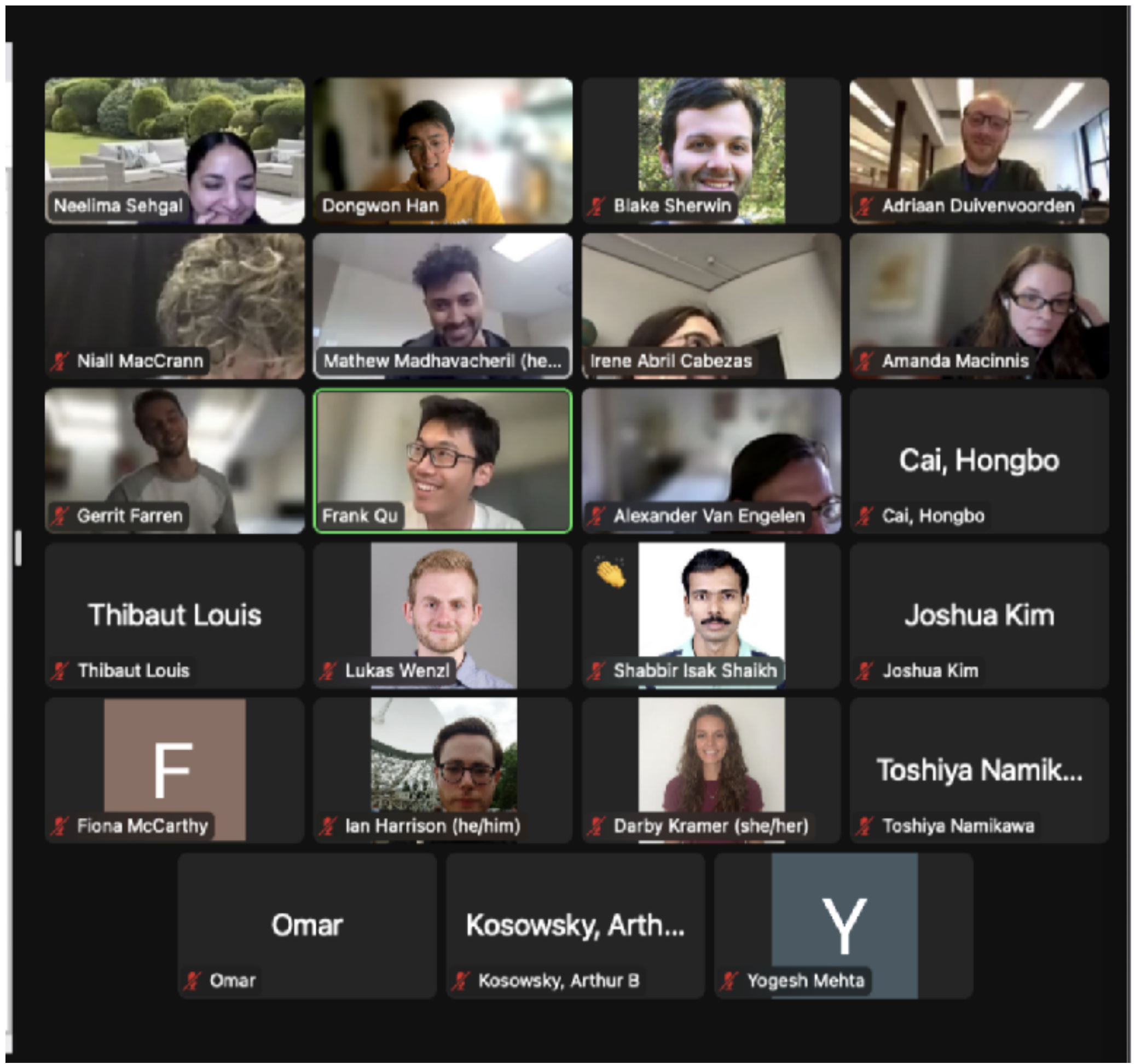
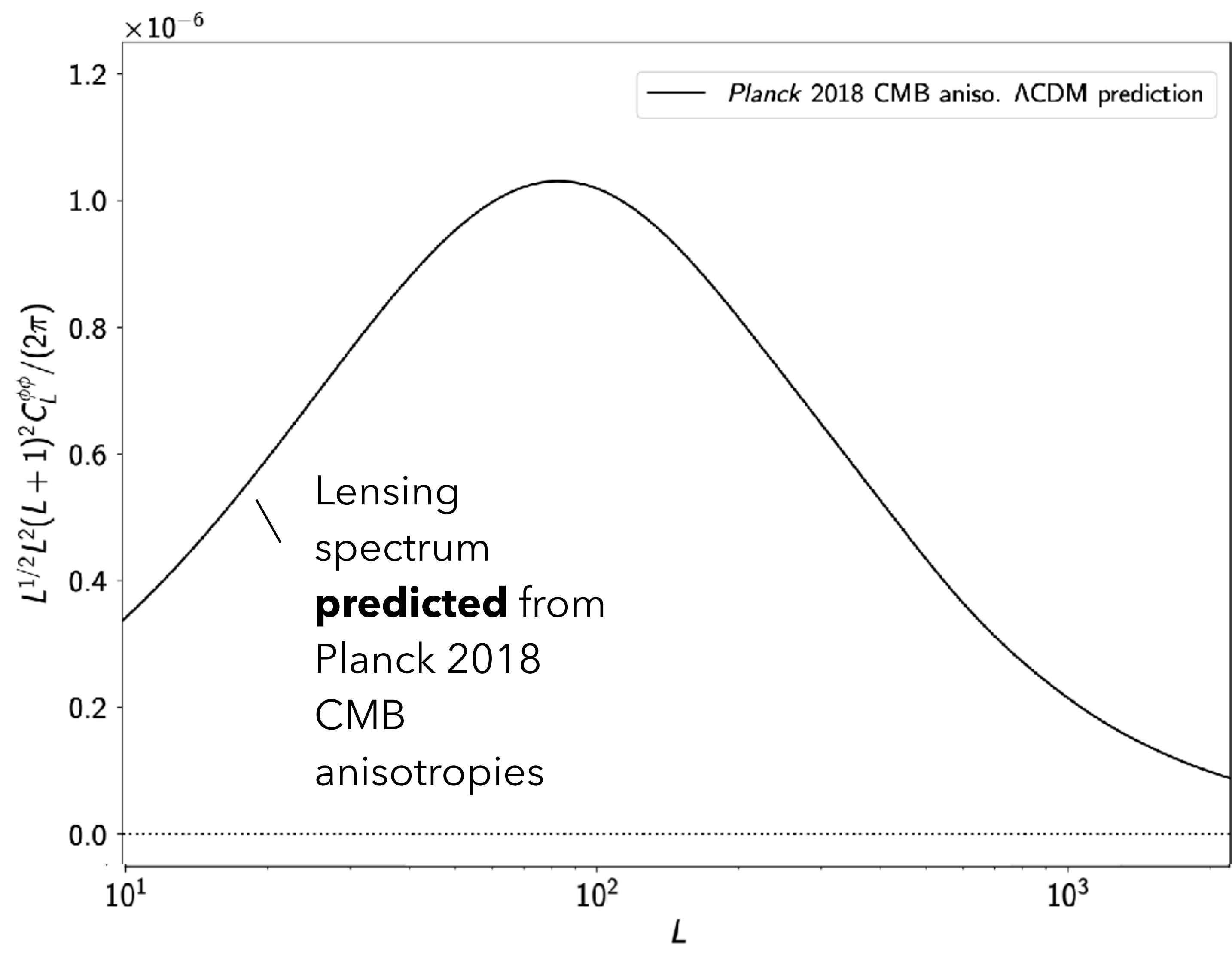
+... many more tests!

Difference in Amplitude of lensing

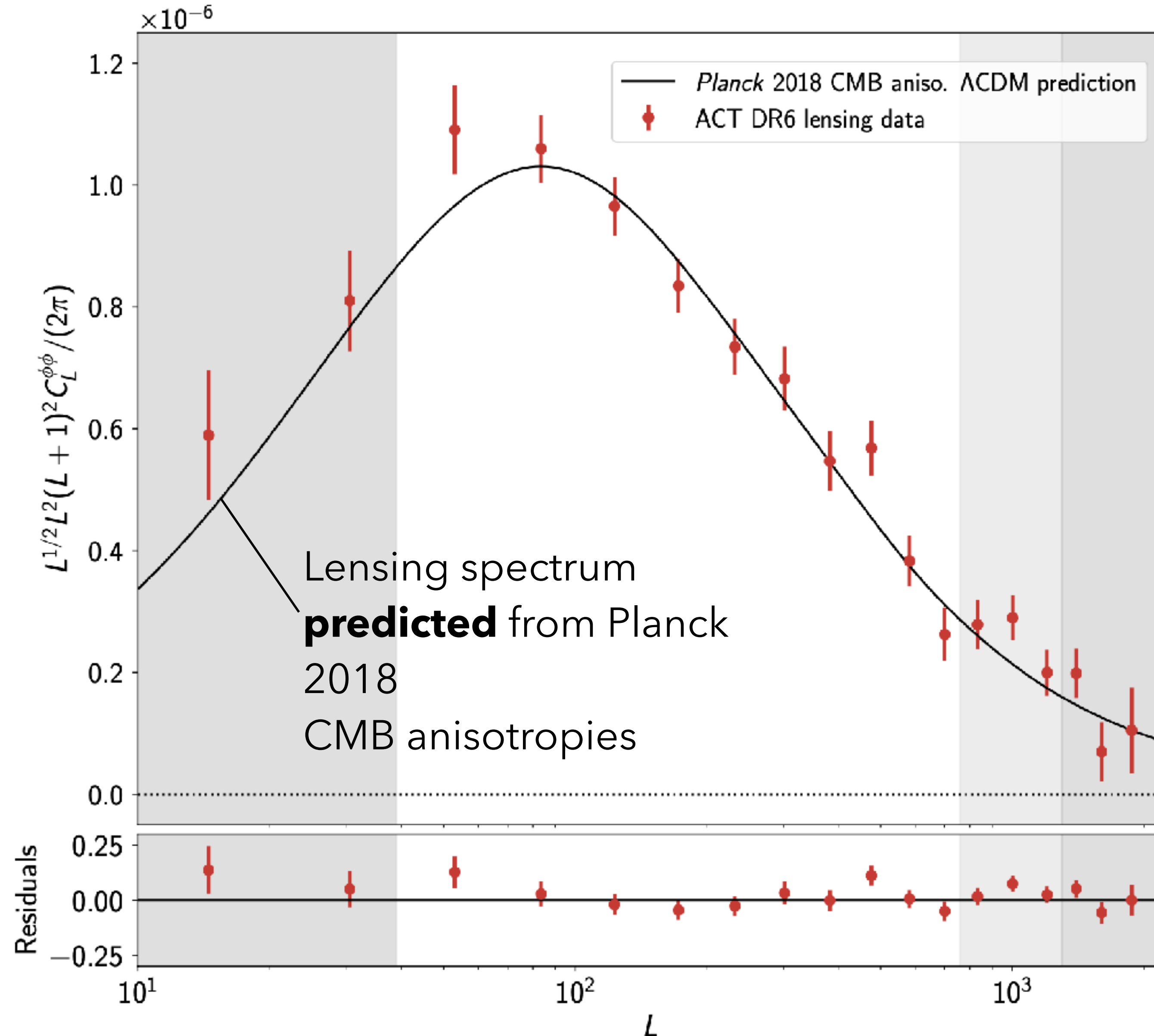


CMB LENSING POWER SPECTRUM: RESULTS AND IMPLICATIONS

PLANCK CMB ANISOTROPY PREDICTION



UNBLINDED RESULTS: ACT DR6 LENSING POWER SPECTRUM



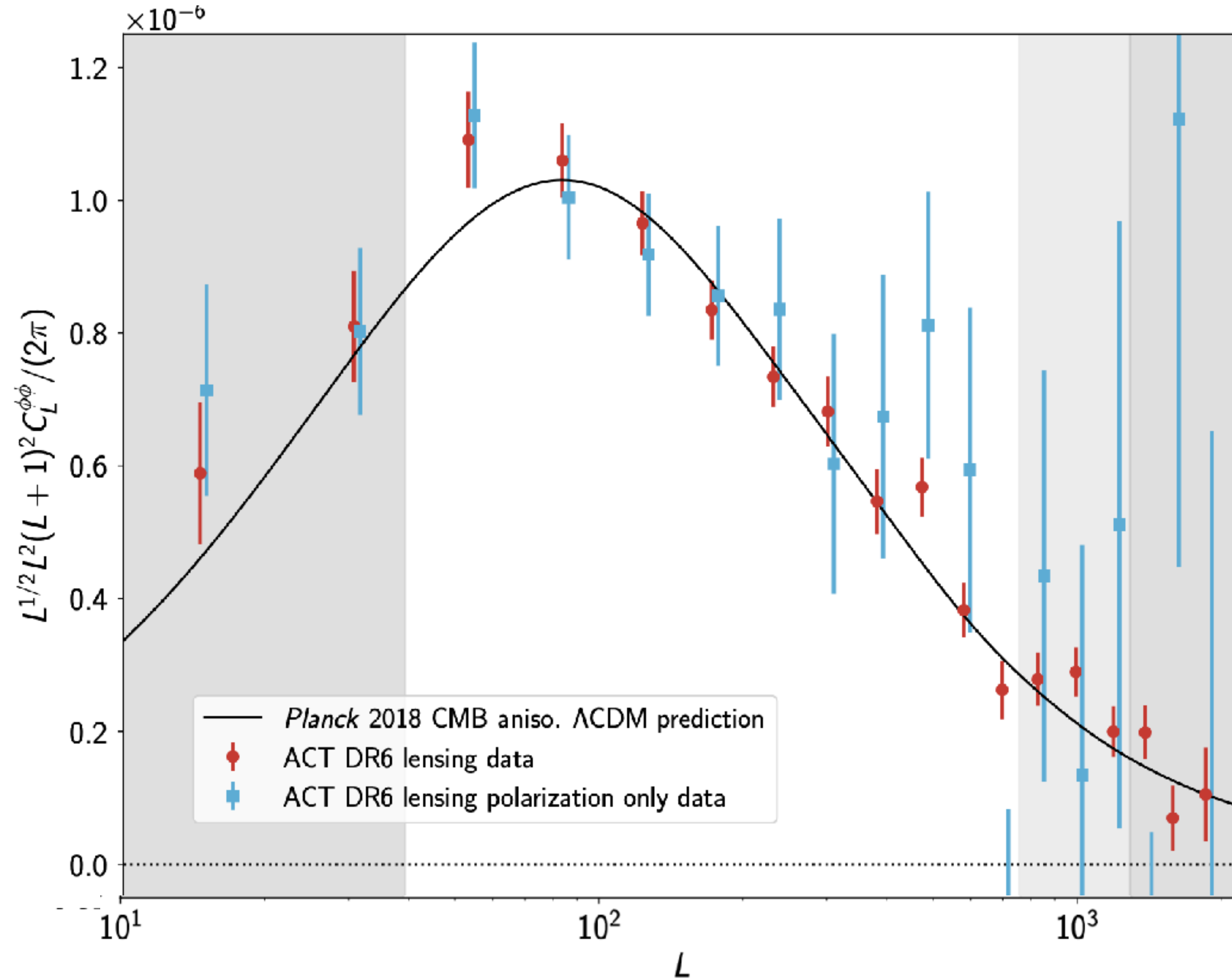
- Excellent agreement of our measurement (with no free parameters) with the Λ CDM theory predictions based on *Planck* 2018 CMB power spectra. A PTE of 0.17

- Amplitude of lensing (relative to theory amplitude) determined to 2.3%

$$A_{\text{lens}} = 1.013 \pm 0.023$$

- SNR of 43

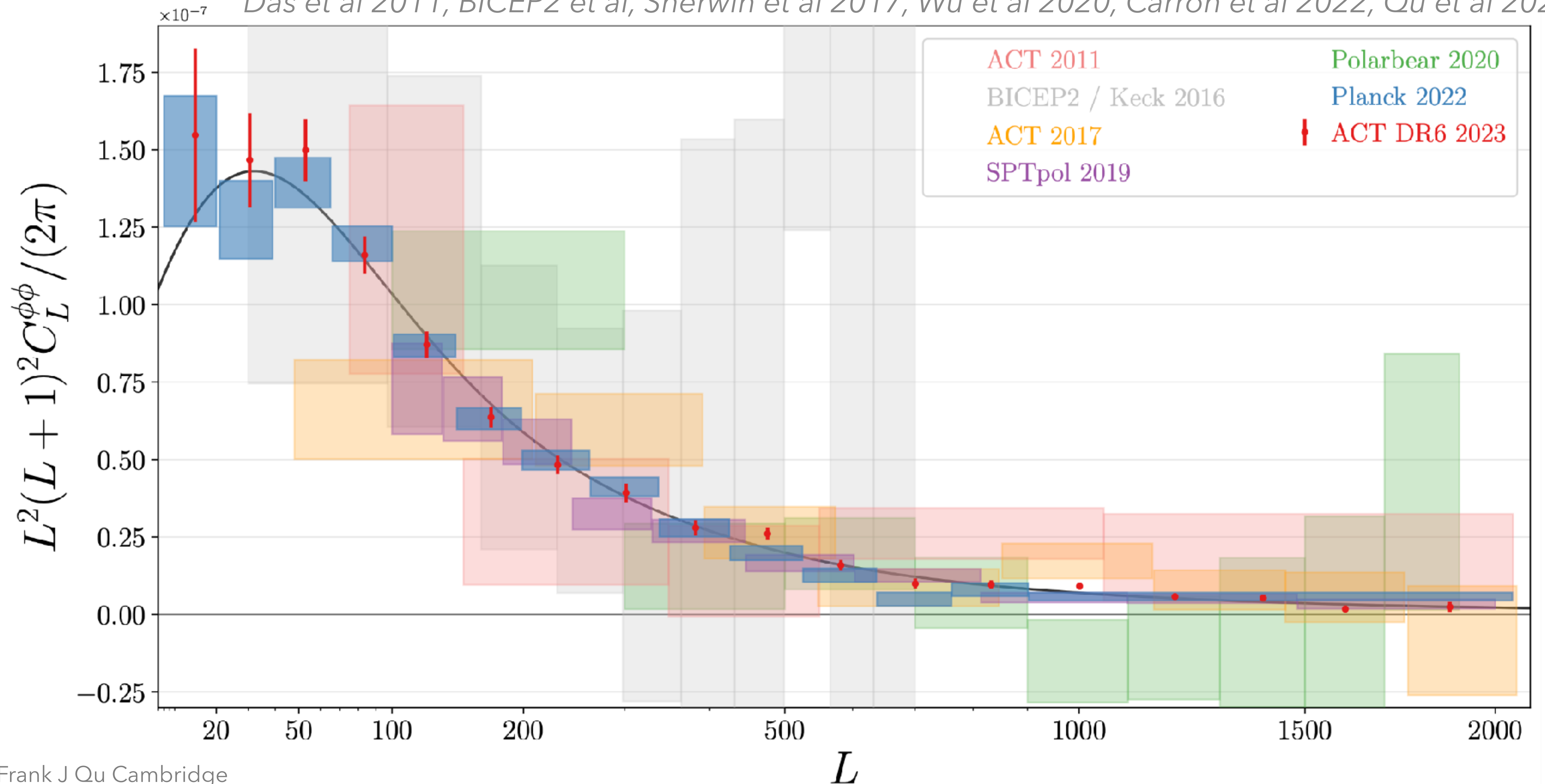
UNBLINDED RESULTS: ACT DR6 LENSING POWER SPECTRUM



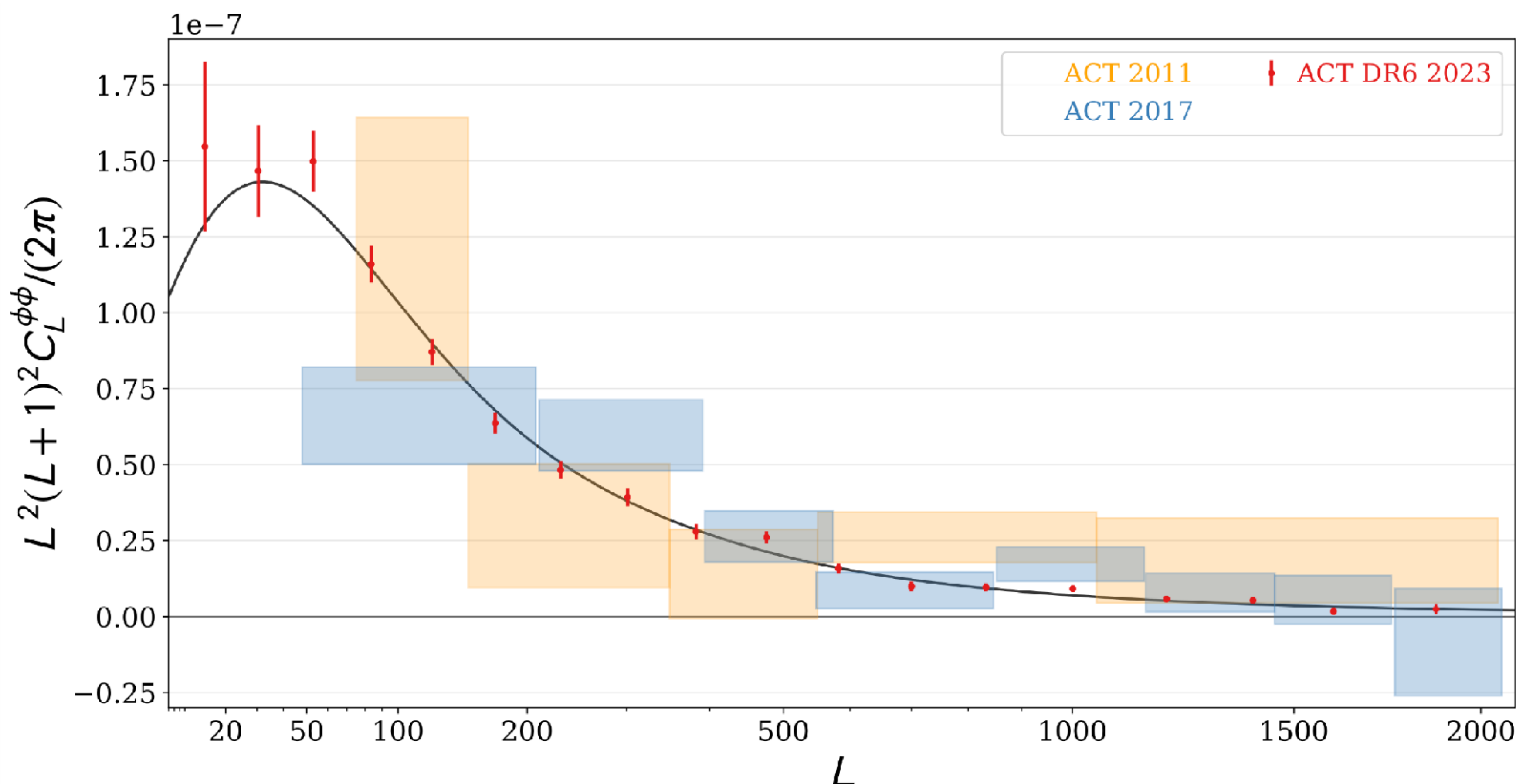
- Signal-to-noise ratio in baseline range ~ 43 competitive with all other weak lensing probes and Planck
- SNR - 20 using polarization data only (consistent)

PUTTING OUR MEASUREMENT IN CONTEXT

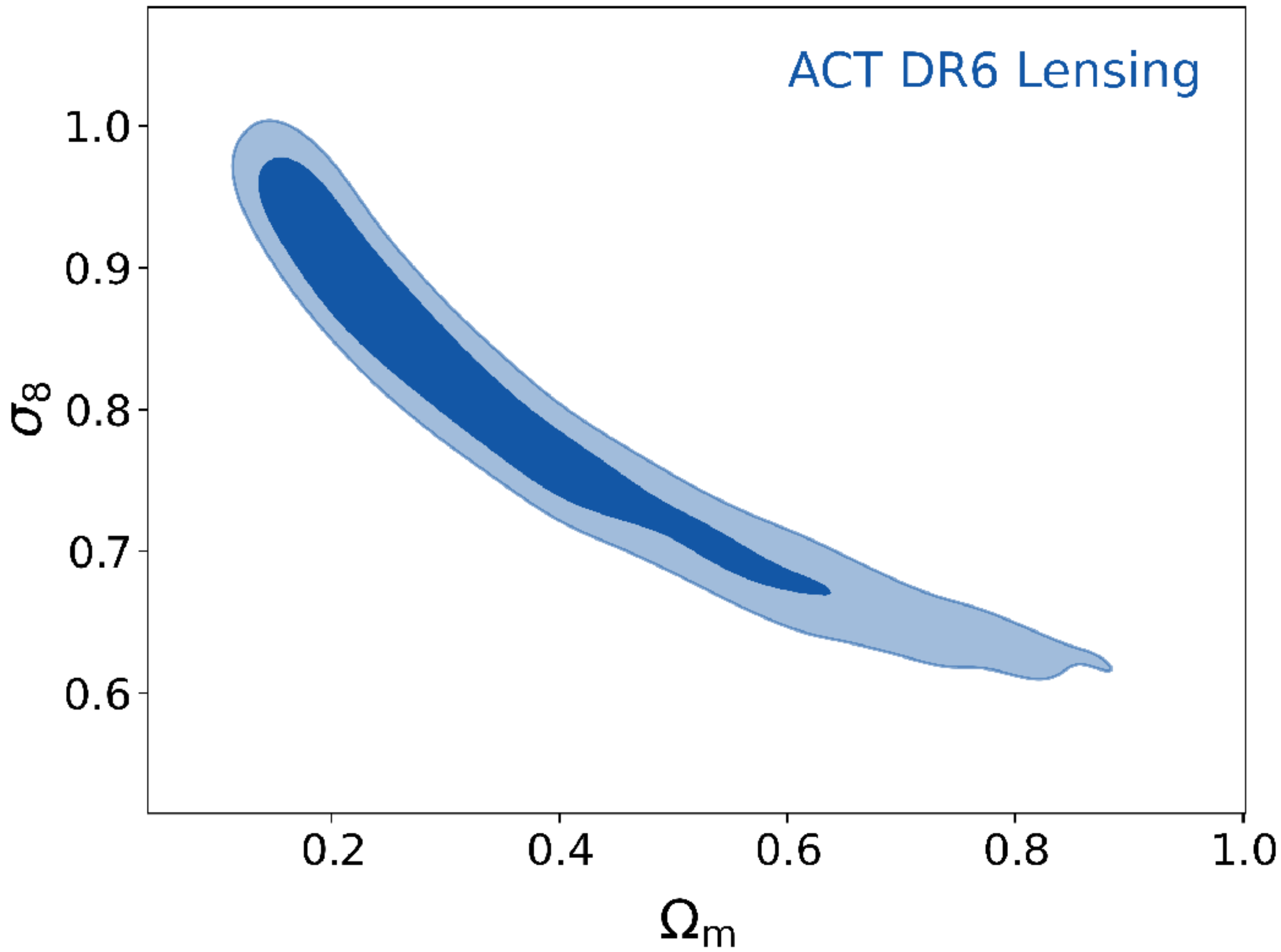
Das et al 2011, BICEP2 et al, Sherwin et al 2017, Wu et al 2020, Carron et al 2022, Qu et al 2023



RAPID PROGRESS OVER THE LAST DECADE WITH ACT AND OTHER EXPERIMENTS



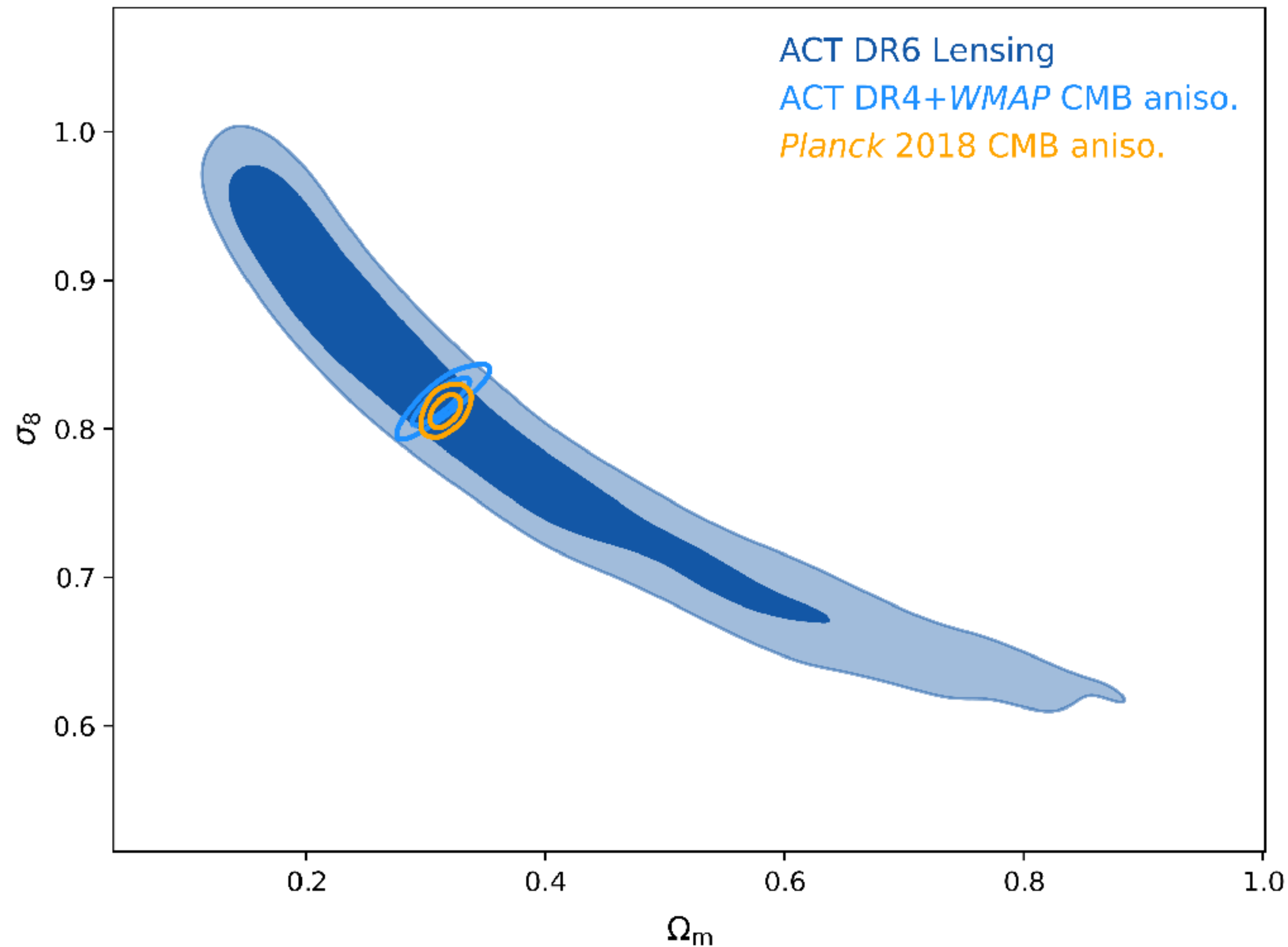
COSMOLOGY FROM DR6 CMB LENSING



$$S_8^{\text{CMBL}} \equiv \sigma_8 \left(\frac{\Omega_m}{0.3} \right)^{0.25}$$

$S_8^{\text{CMBL}} = 0.818 \pm 0.022$
2.7 % measurement

EXCELLENT AGREEMENT WITH PREDICTION FROM CMB POWER SPECTRA—OUR LENSING IS NOT LOW



$$S_8^{\text{CMBL}} \equiv \sigma_8 \left(\frac{\Omega_m}{0.3} \right)^{0.25}$$

$$S_8^{\text{CMBL}} = 0.818 \pm 0.022$$

Early time CMB predictions

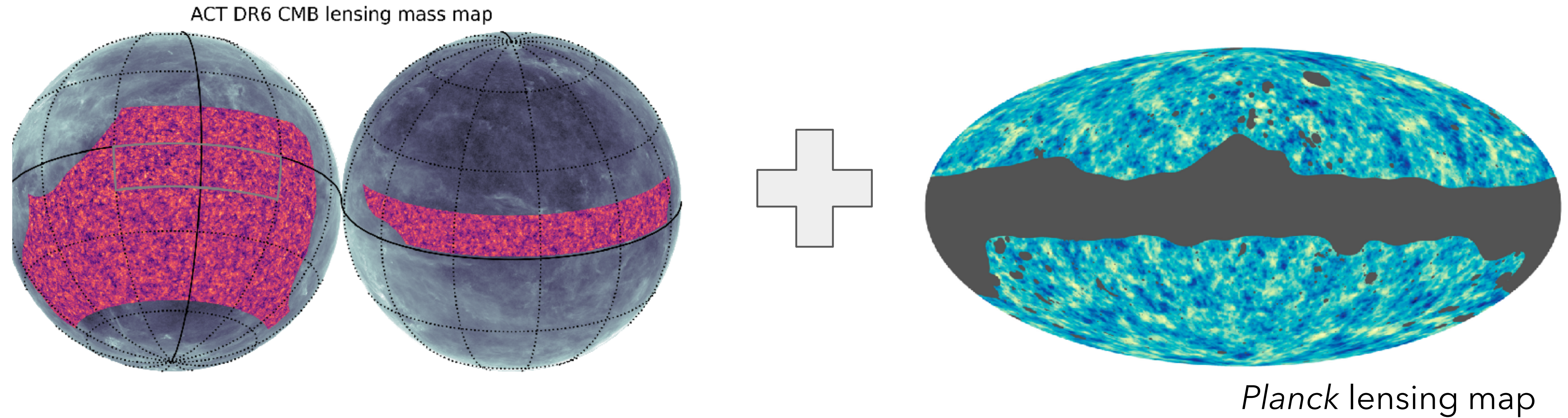
ACT DR4 + WMAP CMB aniso.

$$S_8^{\text{CMBL}} = 0.828 \pm 0.020$$

Planck 2018 CMB aniso.

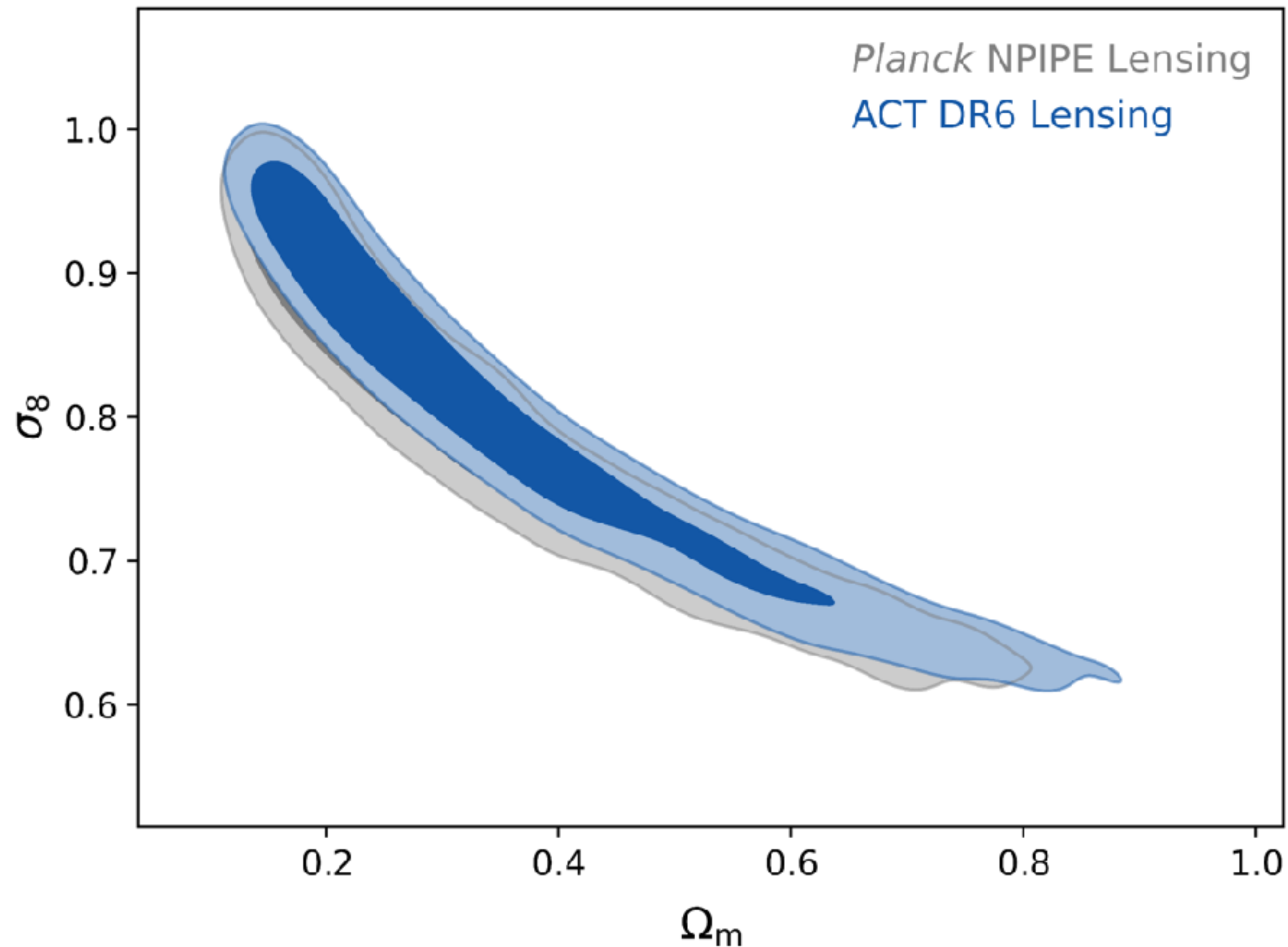
$$S_8^{\text{CMBL}} = 0.823 \pm 0.011$$

ACT+PLANCK COMBINATION: TOWARDS THE MOST PRECISE CMB LENSING MEASUREMENT TO DATE



- ACT lensing and *Planck* lensing maps have significantly independent information.
 - different noise and instrument related systematics.
 - different sky overlap.
 - different angular scales.

COMPARING ACT AND PLANCK NPIPE LENSING CONSTRAINTS



ACT DR6

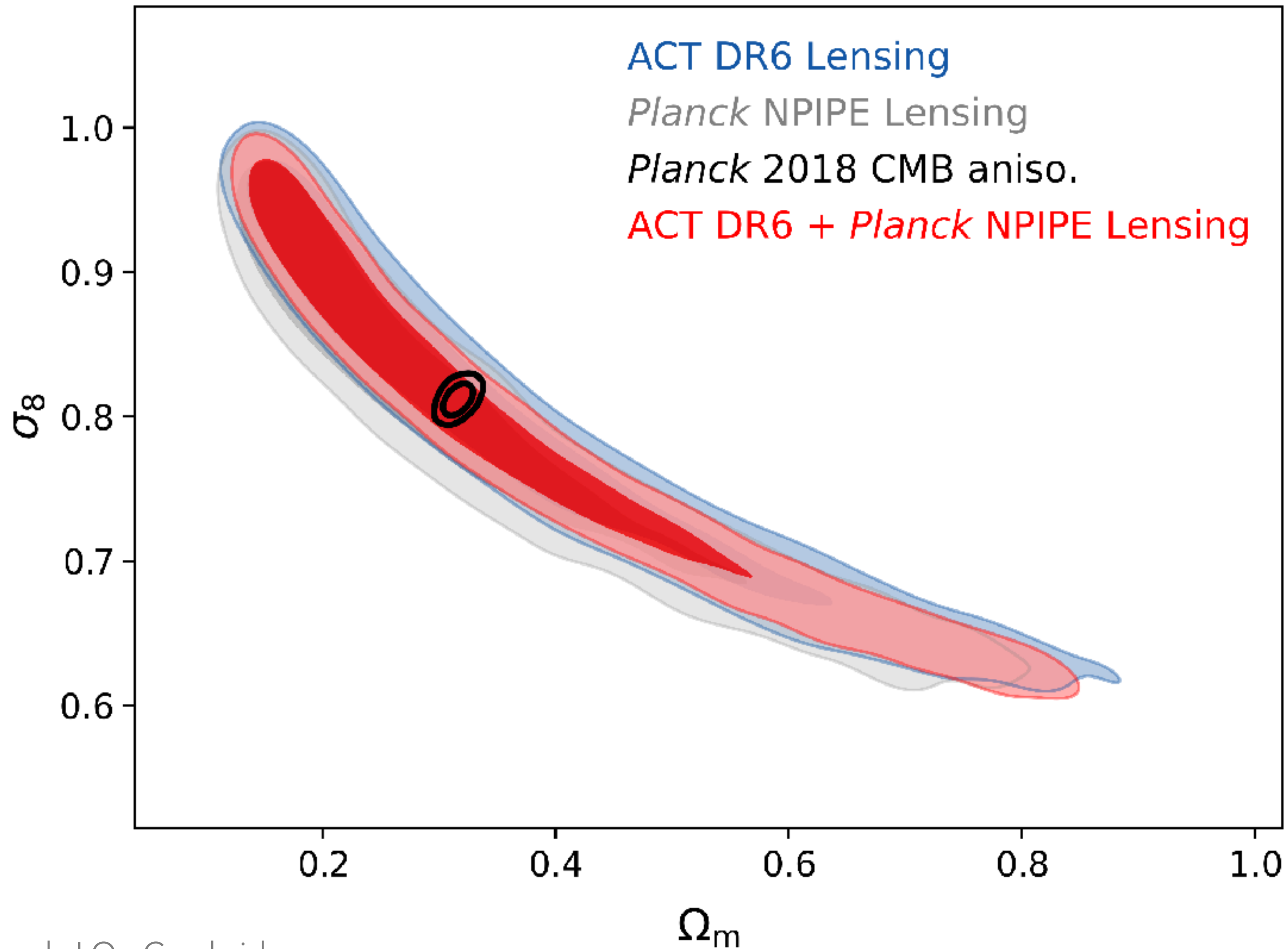
$$S_8^{\text{CMBL}} = 0.818 \pm 0.022$$

Planck reanalysis

$$S_8^{\text{CMBL}} = 0.802 \pm 0.024$$

- As expected, they are very consistent. Can combine!
- Since partial overlap in scales in area, must compute covariance.
- Use simulated ACT and Planck analyses of same sky to get covariance and joint likelihood

CONSTRAINT FROM ACT LENSING AND PLANCK NPIPE LENSING JOINT LIKELIHOOD

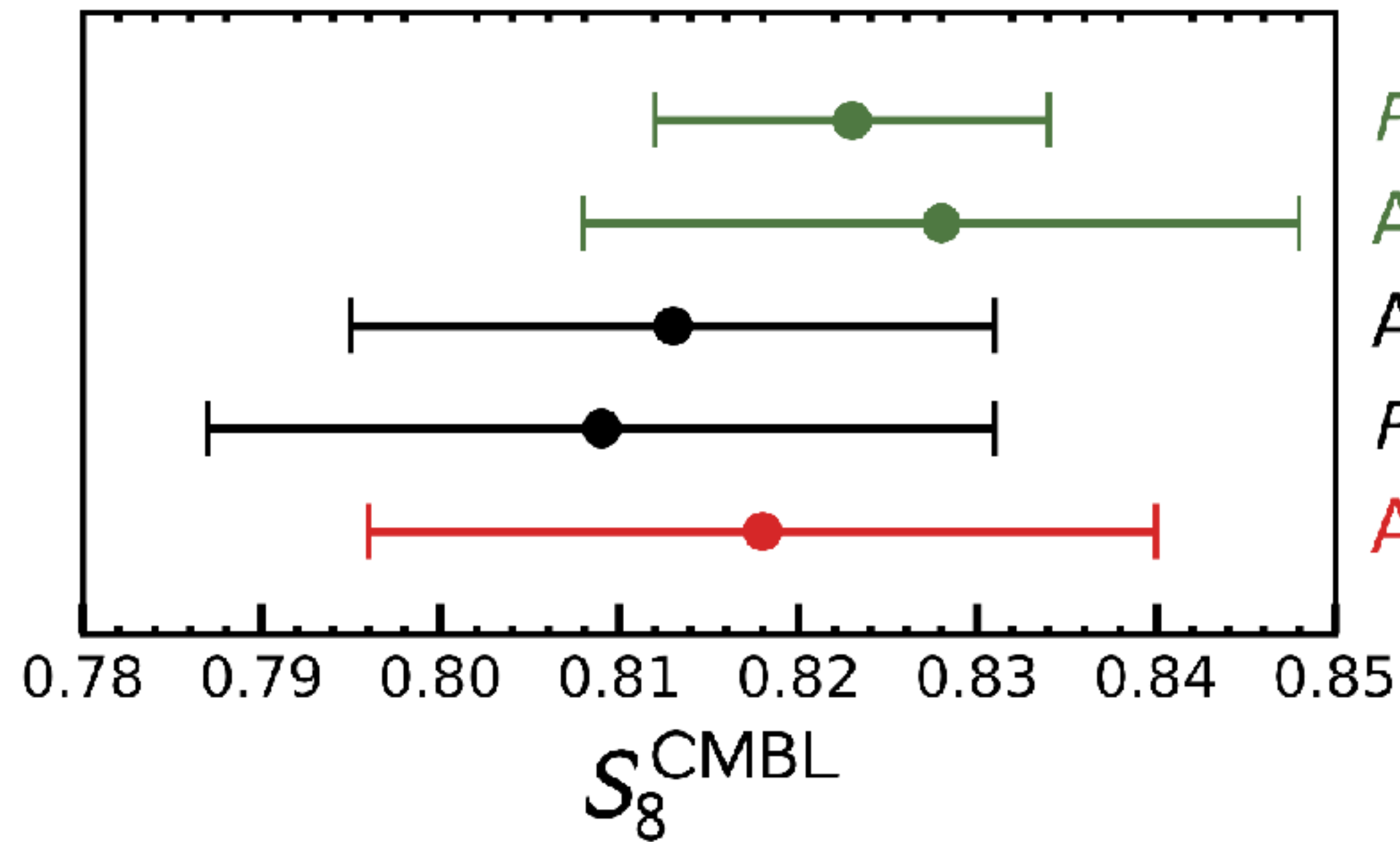


ACT+NPIPE constraint:

$$S_8^{\text{CMBL}} = 0.813 \pm 0.018$$

2.2% constraint from single weak lensing observable alone

DR6 CMB LENSING SPECTRUM + PLANCK COMBINATION: IMPLICATIONS



Planck 2018 CMB aniso.

ACT DR4+WMAP CMB aniso.

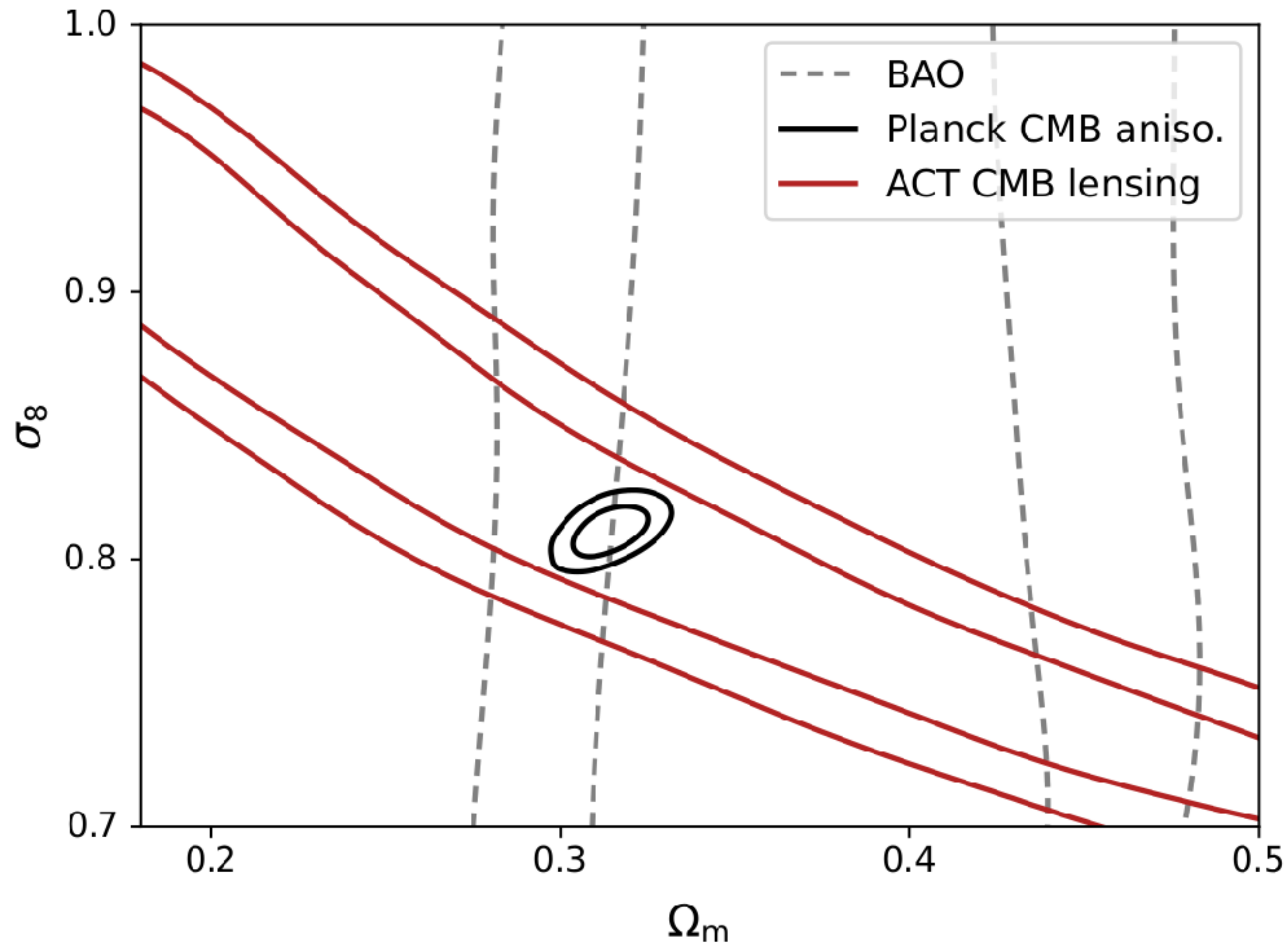
ACT DR6+Planck NPIPE Lensing

Planck NPIPE Lensing

ACT DR6 Lensing (baseline)

- ▶ A success for LCDM: fit Planck CMB at $z \sim 1100$, predict structure to low- z , predict lensing signal arising over a wide range of z and trispectrum in ACT - agrees to 2%. Signal is not low!
- ▶ Agreement with Planck lensing + CMB - no evidence for Planck systematics
- ▶ Disfavours new physics explanations that change structure growth at high z ($z > 1$) and low k .

DR6 CMB LENSING + BAO



CMB lensing alone

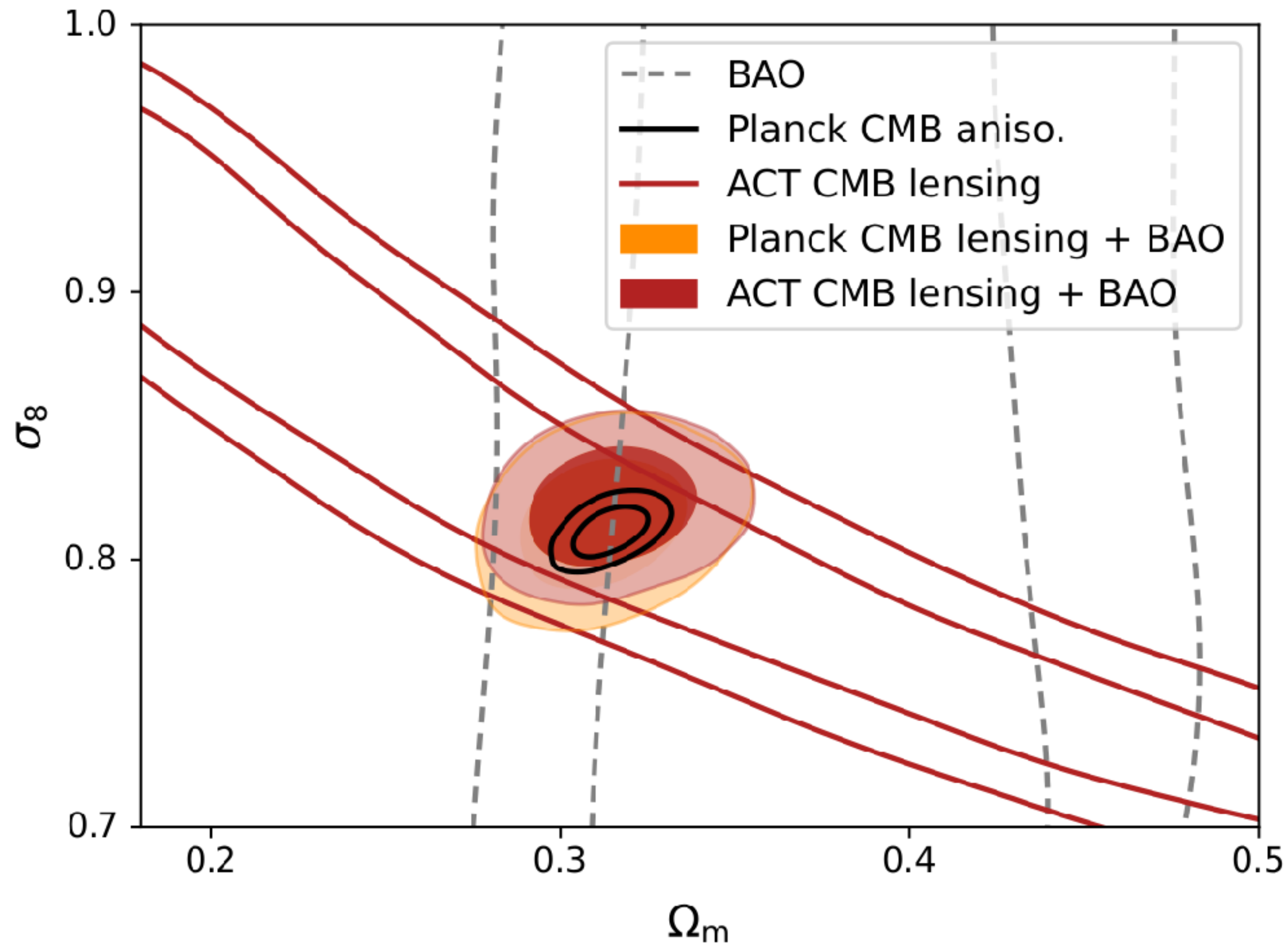
measures $\sigma_8 \Omega_m^{0.25}$

Combination with BAO*

isolates σ_8

*BAO data set includes 6df, SDSS MGS, BOSS and eBOSS LRGs

DR6 CMB LENSING + BAO



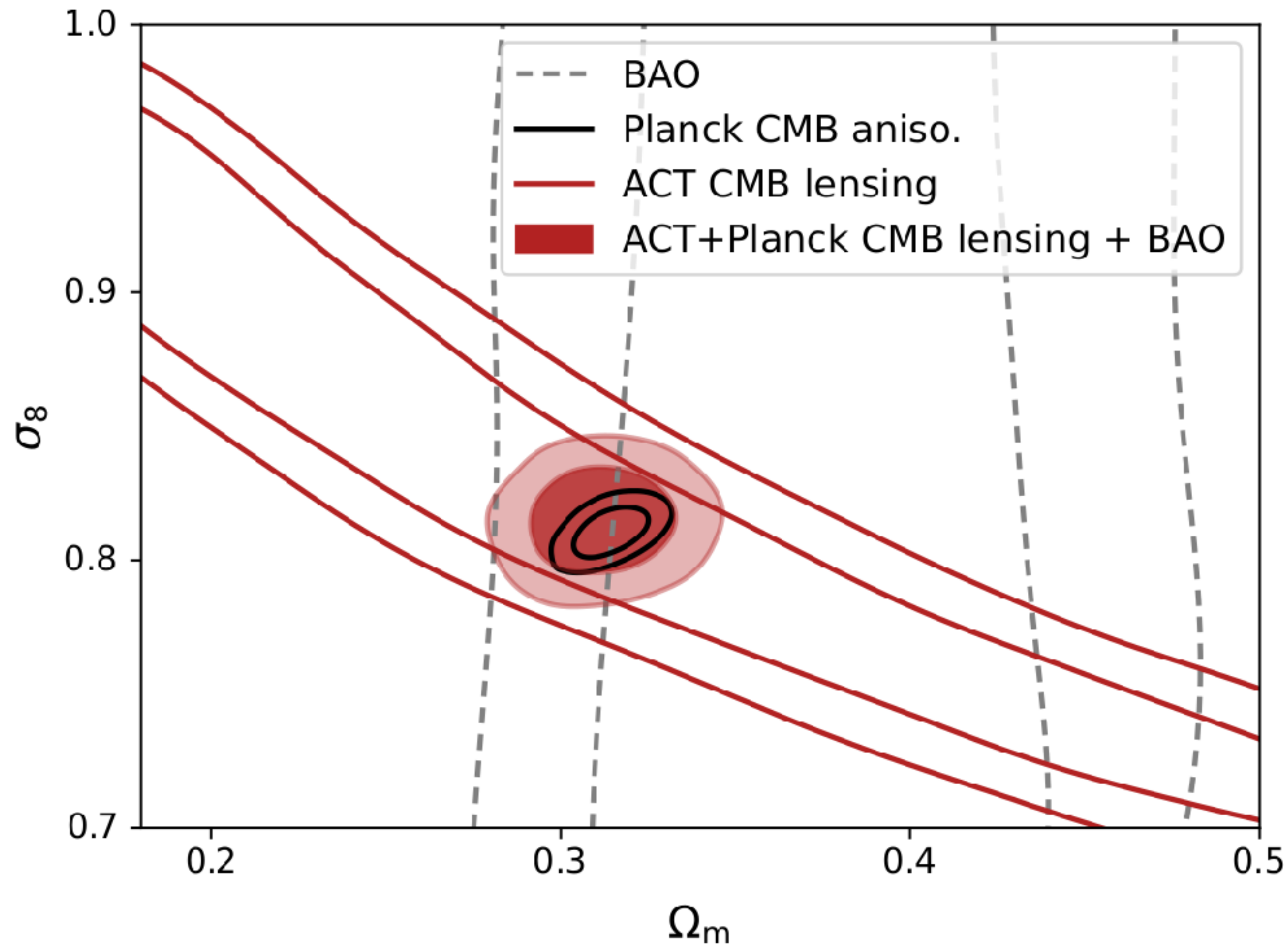
CMB lensing alone
measures $\sigma_8 \Omega_m^{0.25}$

Combination with BAO
isolates σ_8

$$\sigma_8 = 0.819 \pm 0.015$$

1.8% measurement

DR6 + PLANCK CMB LENSING + BAO



CMB lensing alone
measures $\sigma_8 \Omega_m^{0.25}$

Combination with BAO
isolates σ_8

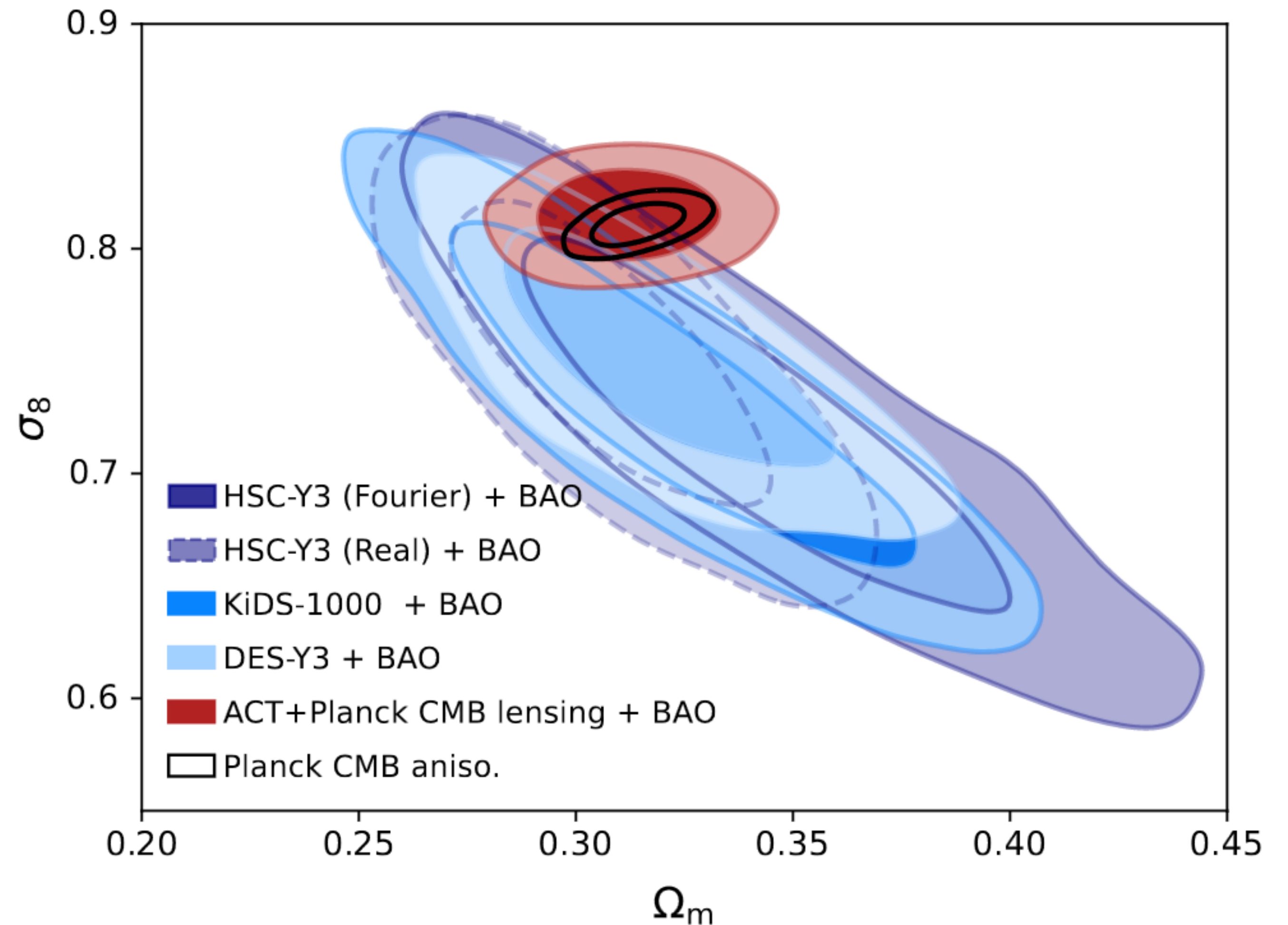
$$\sigma_8 = 0.812 \pm 0.013$$

1.6% measurement for
ACT+Planck lensing
combination

COMPARISON WITH OTHER WEAK LENSING PROBES

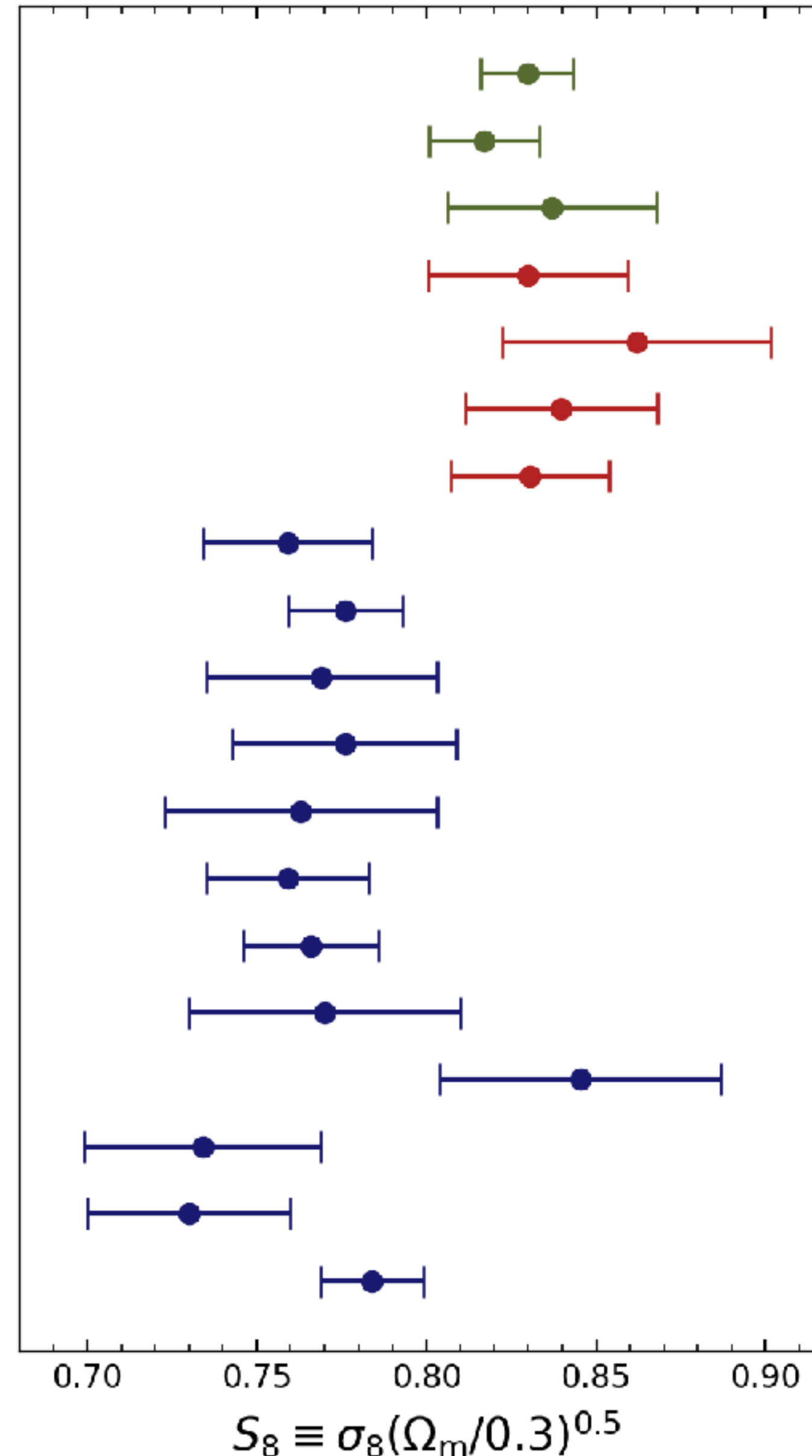
Shown against various **cosmic shear** measurements with consistent priors and BAO

Wider range of scales probed by **CMB lensing** allows tight constraint compared to cosmic shear



OUTLOOK FOR S_8

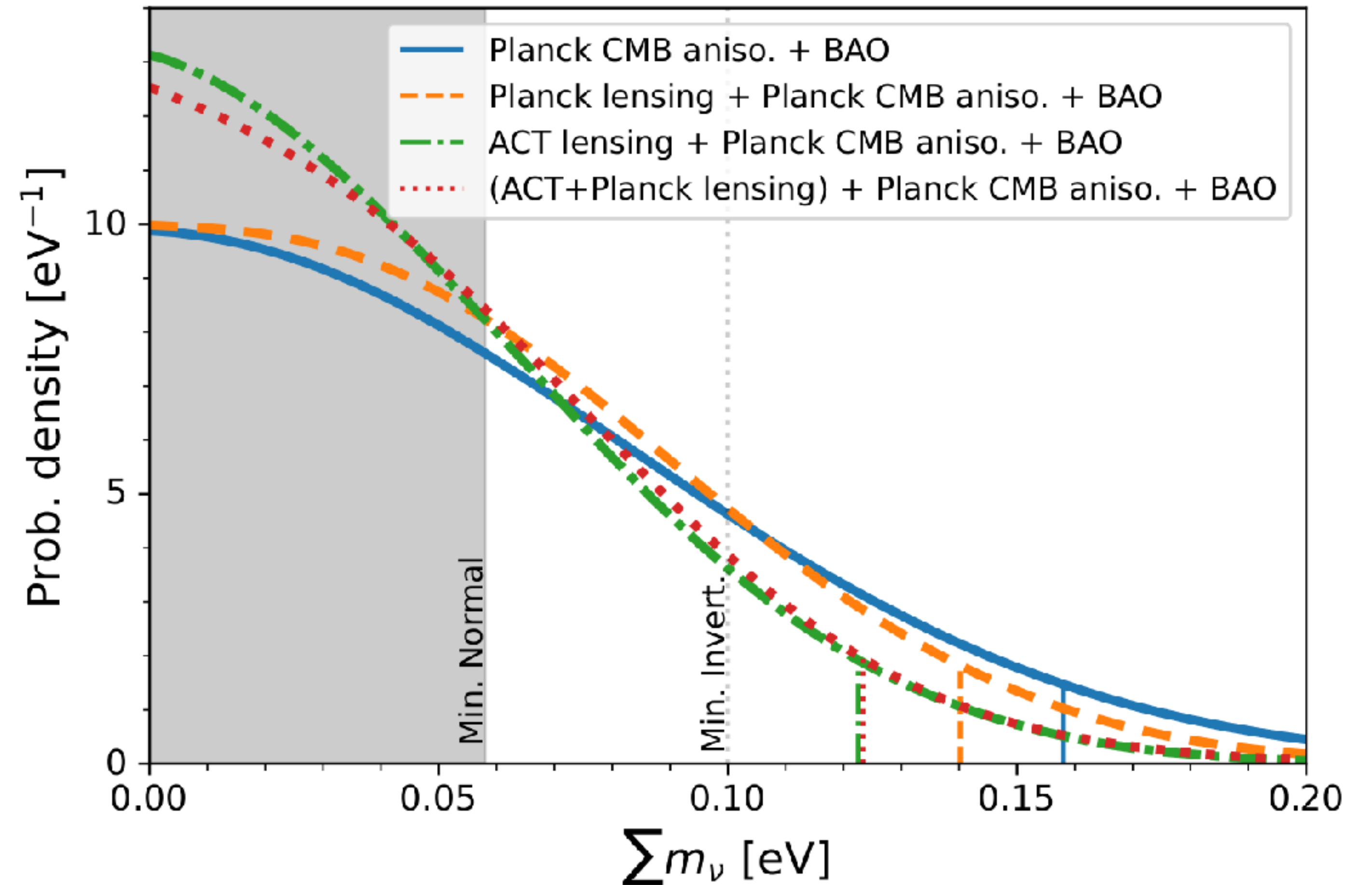
- CMBLens from $z=0.5-5$ and **linear scales** is consistent with early universe prediction
- Probes of $z < \sim 0.5$ and **smaller scales** generally fall lower
- **New outlook:** Motivates not just CMB vs. LSS comparisons, but **intermediate-z/linear-scales** vs. **low-z/non-linear scale**



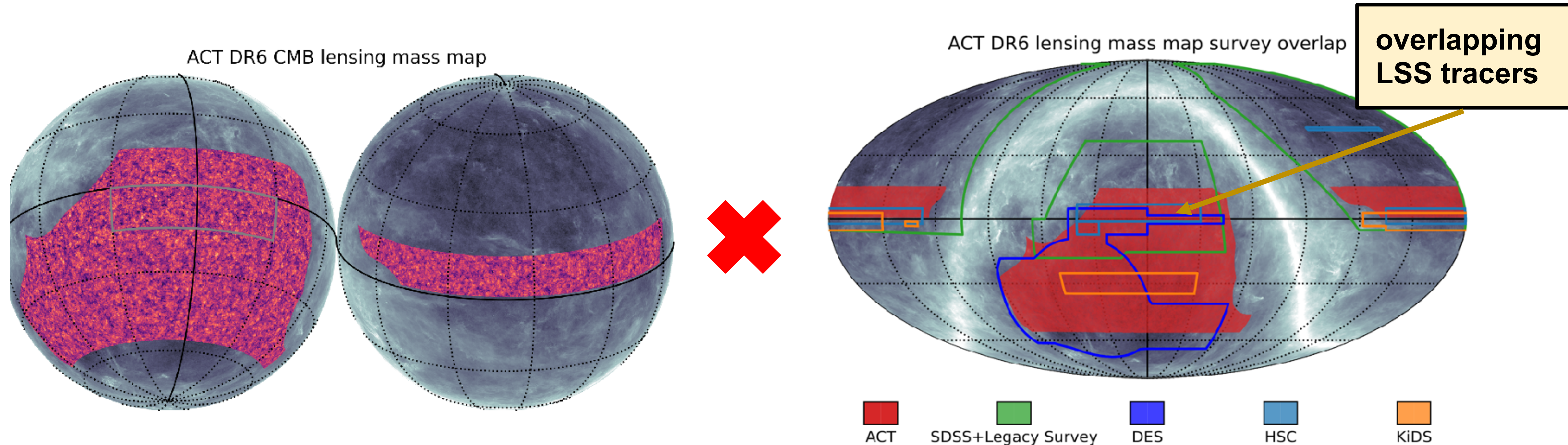
- CMB: Planck CMB aniso.
- CMB: Planck CMB aniso. (+ A_{lens} marg.)
- CMB: WMAP+ACT CMB aniso.
- CMBL: Planck CMB lensing + BAO
- CMBL: SPT CMB lensing + BAO
- CMBL: ACT CMB lensing + BAO**
- CMBL: ACT+Planck CMB lensing + BAO**
- WL: DES-Y3 galaxy lensing
- WL: DES-Y3 3x2
- WL: HSC-Y3 galaxy lensing (Real)
- WL: HSC-Y3 galaxy lensing (Fourier)
- WL: HSC-Y3 3x2
- WL: KiDS-1000 galaxy lensing
- WL: KiDS-1000 3x2
- GC: BOSS EFT 2-pt + 3-pt
- GC: eBOSS BAO+RSD
- CX: SPT/Planck CMB lensing x DES
- CX: Planck CMB lensing x DESI LRG
- CX: Planck CMB lensing x unWISE

CONSTRAINING NEUTRINO MASSES

- We combine with CMB anisotropies which predict low-redshift clustering amplitude
- Translate observed low-redshift clustering amplitude to suppression caused by massive neutrinos
- **$m < 0.12$ eV 95% c.l.**
Compare to:
($m < 0.14$ eV; Planck lensing)
($m < 0.16$ eV; no lensing, only CMB+BAO)



FUTURE DIRECTIONS: DR6 ACT LENSING X LSS

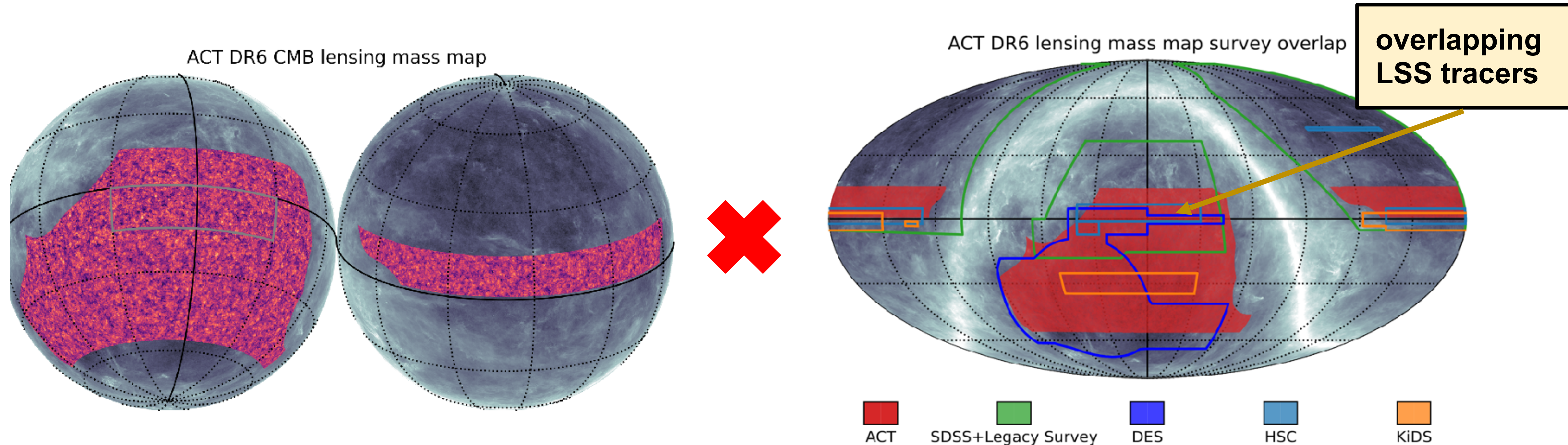


3D tomographic information of the matter distribution!



1. Probe of structure growth vs. redshift: **ACT x unWISE**, Farren et al. (in prep), **ACT x DES**, Marques et al. (in prep), Shaikh et al (in prep), Darwish et al. (in prep), Kim et al. (in prep)... + > 10 ongoing projects with DESI
2. Tests of gravity: **ACT x SDSS**, Wenzl et al. (in prep)...
3. Astrophysics at high-z: **ACT x Planck CIB**, Mehta et al (in prep)...
-

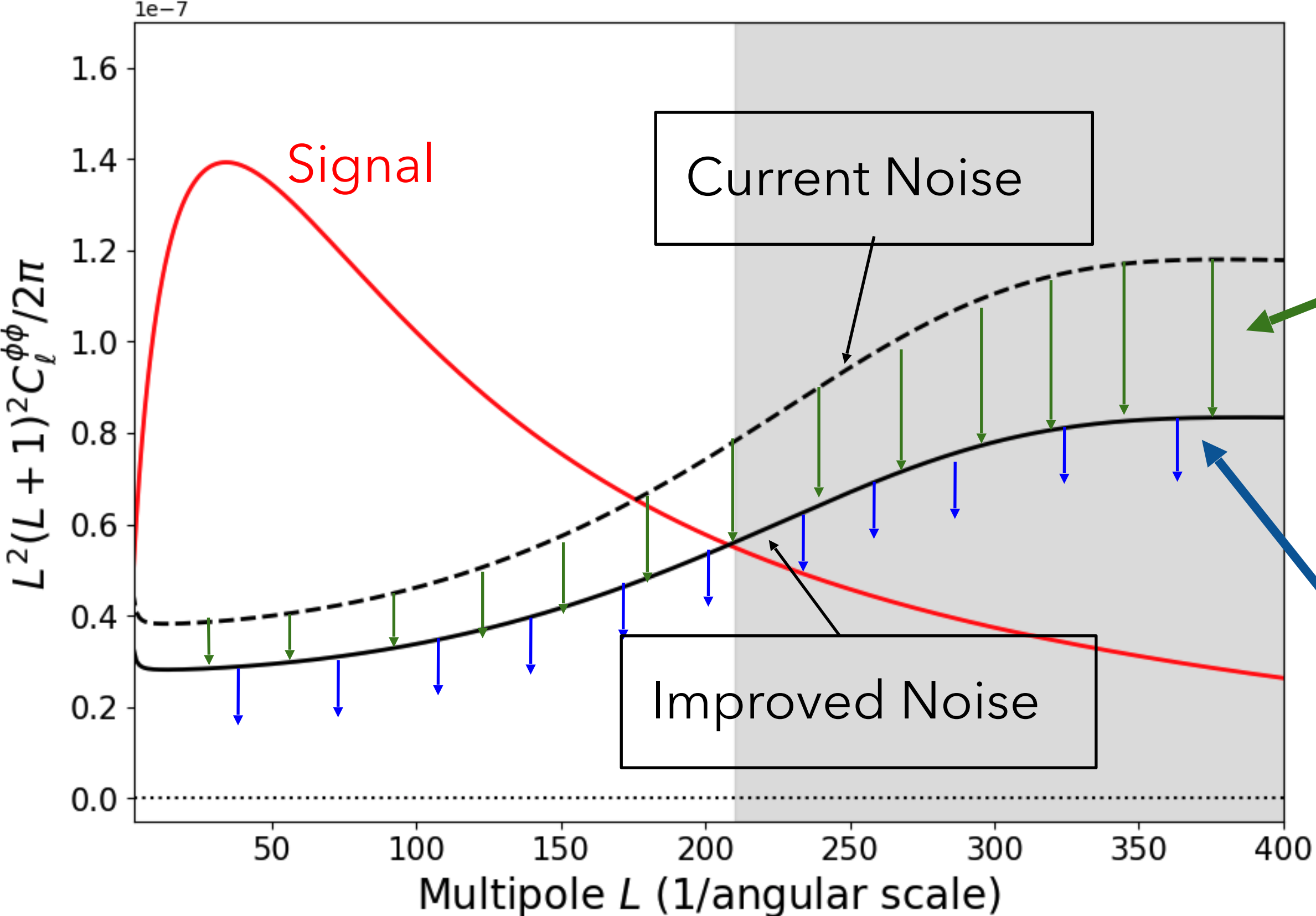
FUTURE DIRECTIONS: DR6 ACT LENSING X LSS



ACT DR6 lensing map will be released upon publication of the 3 papers, likelihood available here:

(NASA LAMBDA: https://lambda.gsfc.nasa.gov/product/act/actadv_prod_table.html)

FUTURE DIRECTIONS: FURTHER IMPROVEMENTS ON MASS MAPPING



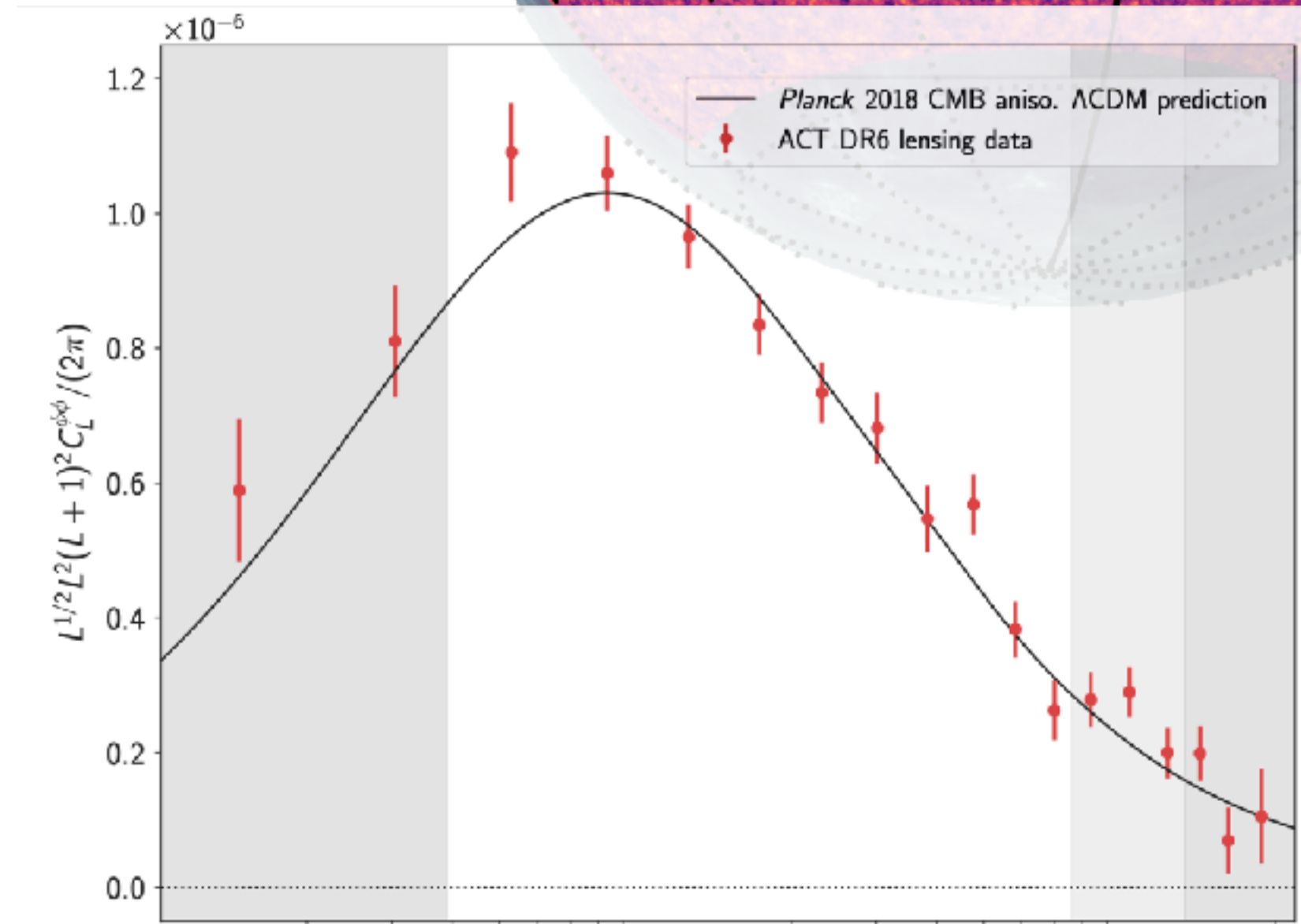
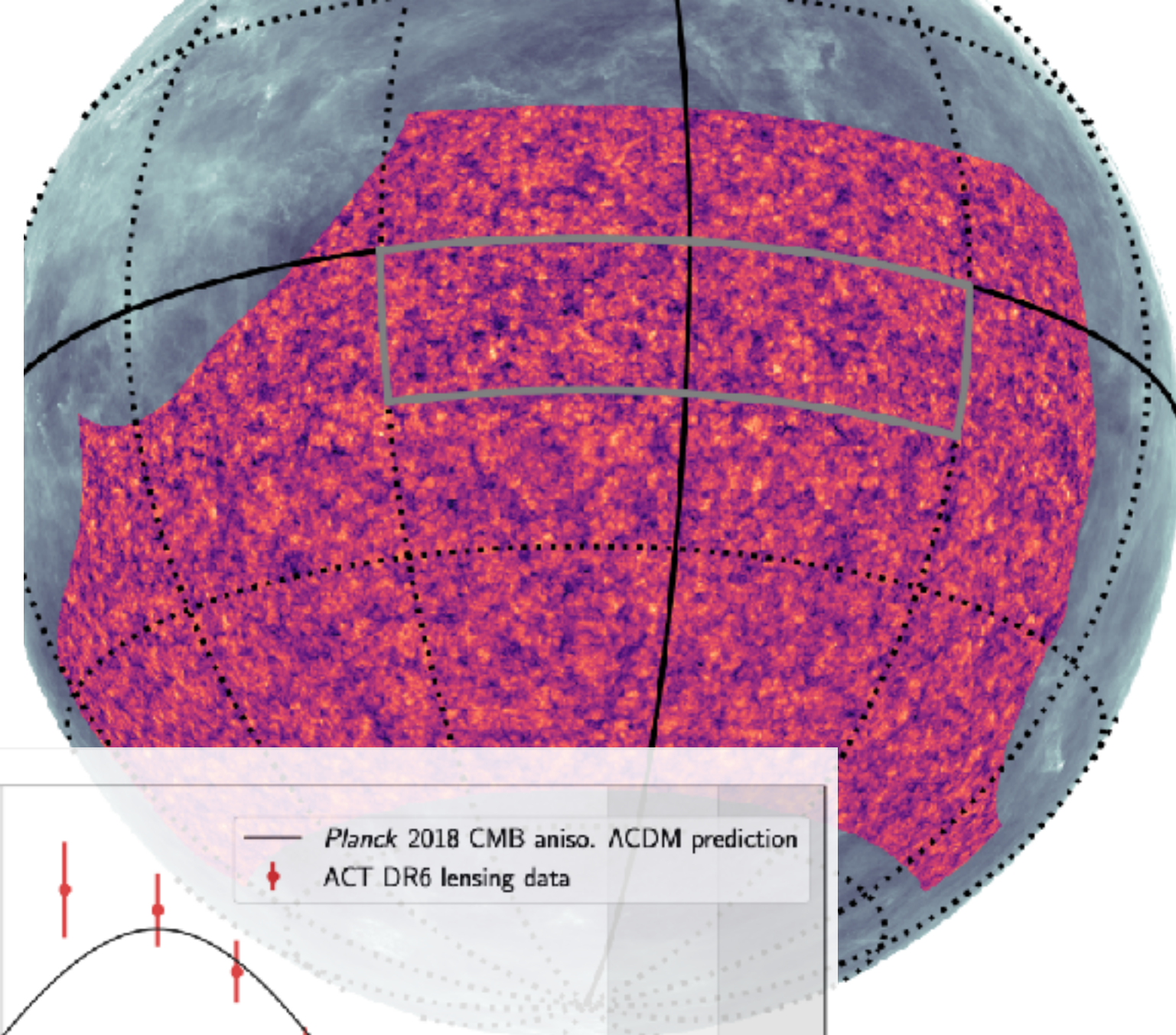
Expected Improvements for the next set of analyses

- Inclusion of the daytime data: ~ 1.7x amount of the data
- Additional Seasons (Season 2021-2022)
- Optimal Filtering (10-15% improvement)
- Increase the number of splits used for the cross-estimator (~10% improvement)
- Improve sky-cuts (~10% improvement)
- Map-level combination with Planck

More great lensing science from the ACT collaboration in the near future!

SUMMARY

- CMB lensing power spectrum with high precision, SNR~43; tested extensively
- High-fidelity lensing map over ¼ sky
- Excellent agreement with Planck or ACT CMB power spectrum predictions. No evidence for low value



THANK YOU FOR YOUR ATTENTION

jq247@cam.ac.uk

Papers
available on
arxiv

Qu, Sherwin, Madhavacheril, Han, Crowley et al 2304.05202

A Measurement of the DR6 CMB Lensing Power Spectrum and its Implications for Structure Growth

Madhavacheril, Qu, Sherwin, MacCrann, Li et al 2304.05203

DR6 Gravitational Lensing Map and Cosmological Parameters

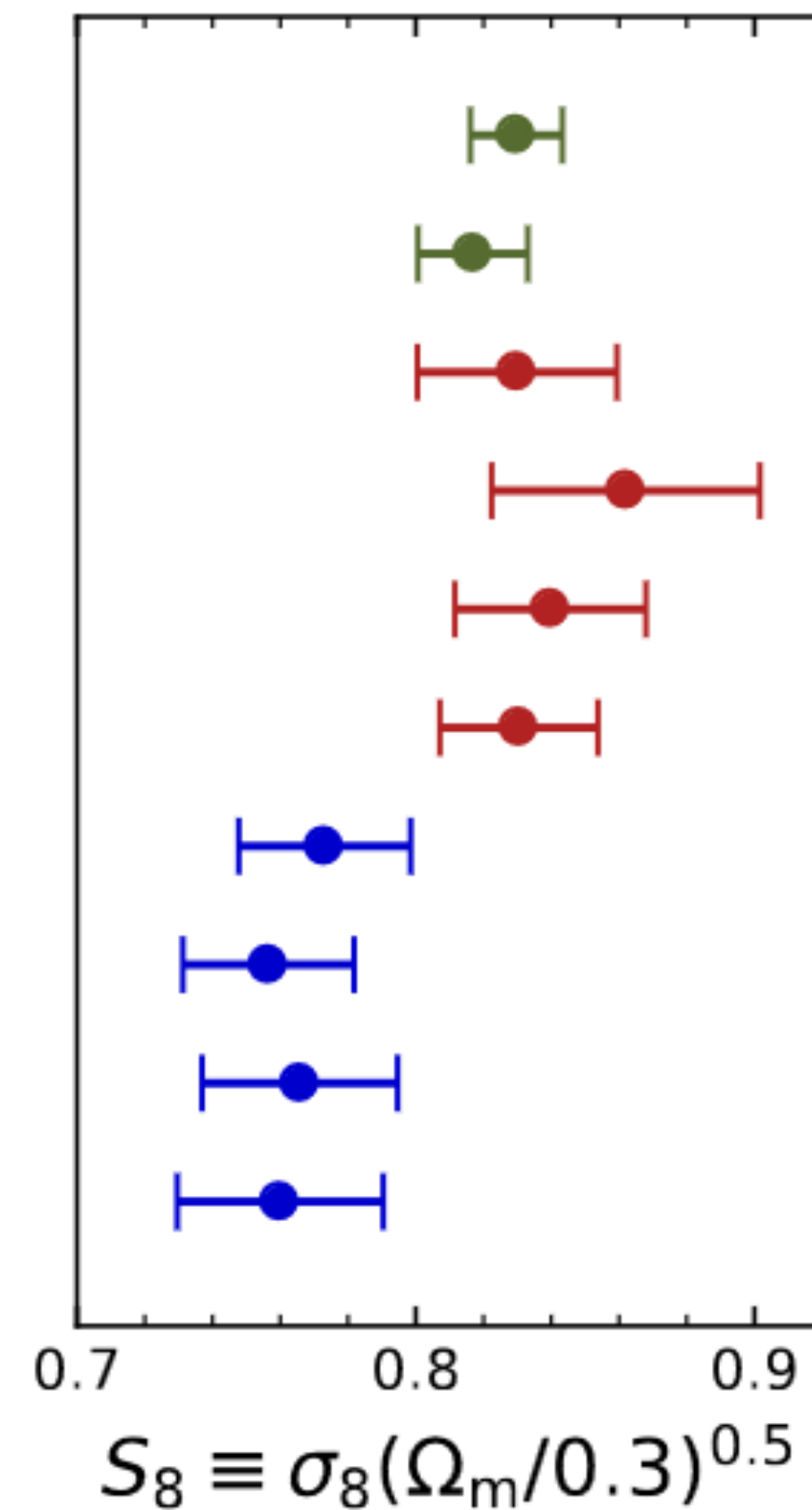
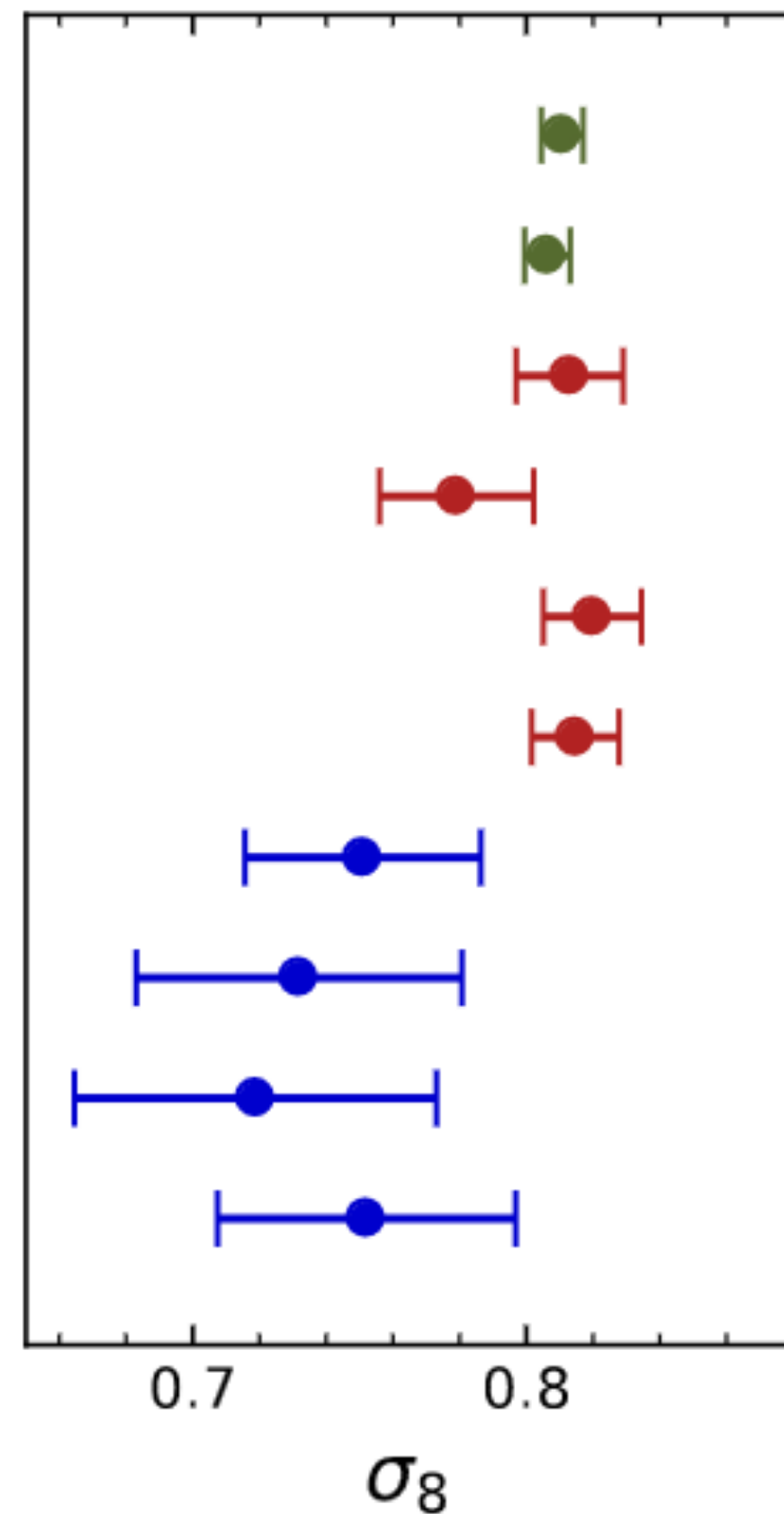
MacCrann, Sherwin, Qu, Namikawa, Madhavacheril et al 2304.05196

Mitigating the impact of extragalactic foregrounds for the DR6 CMB lensing analysis

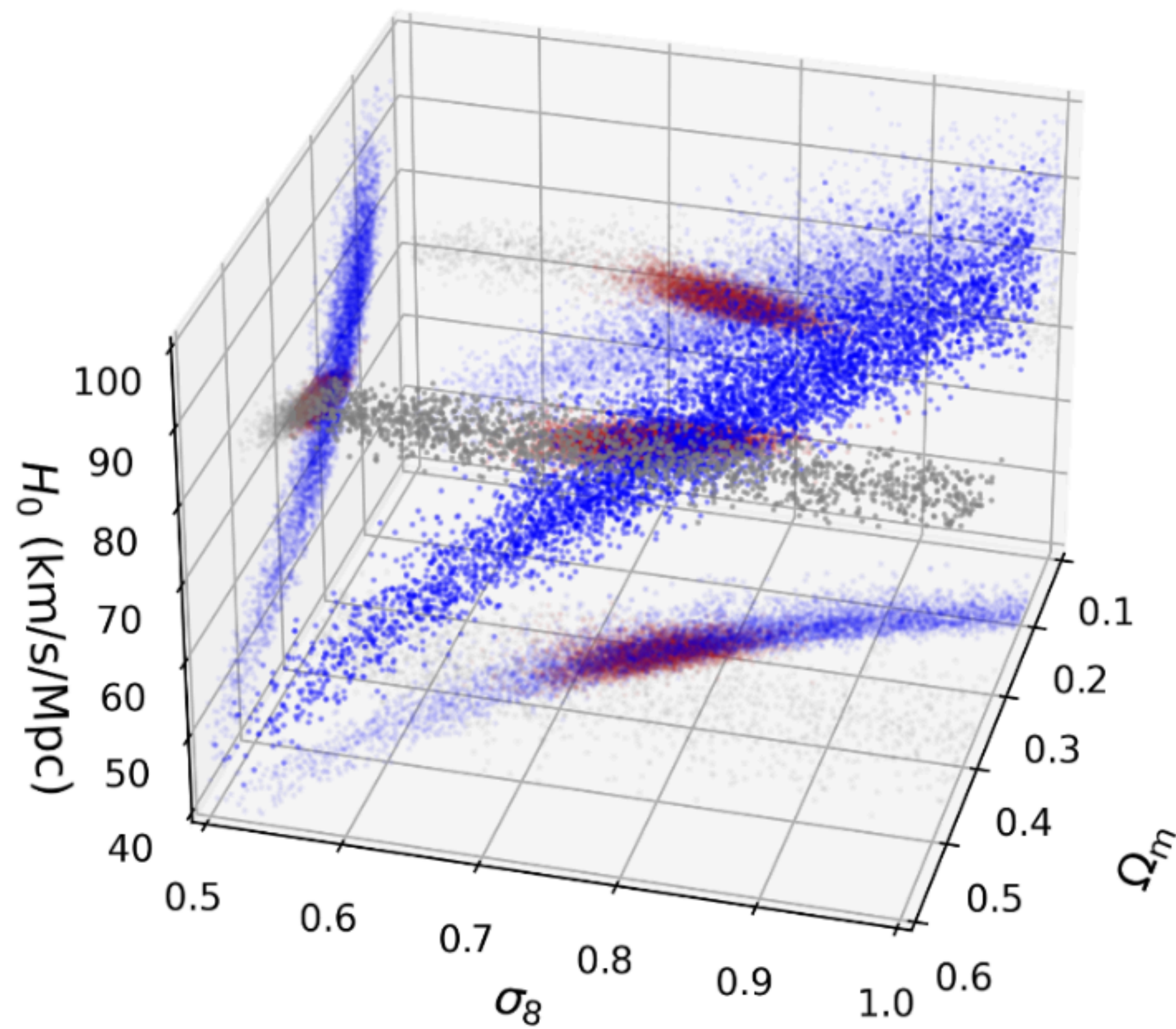
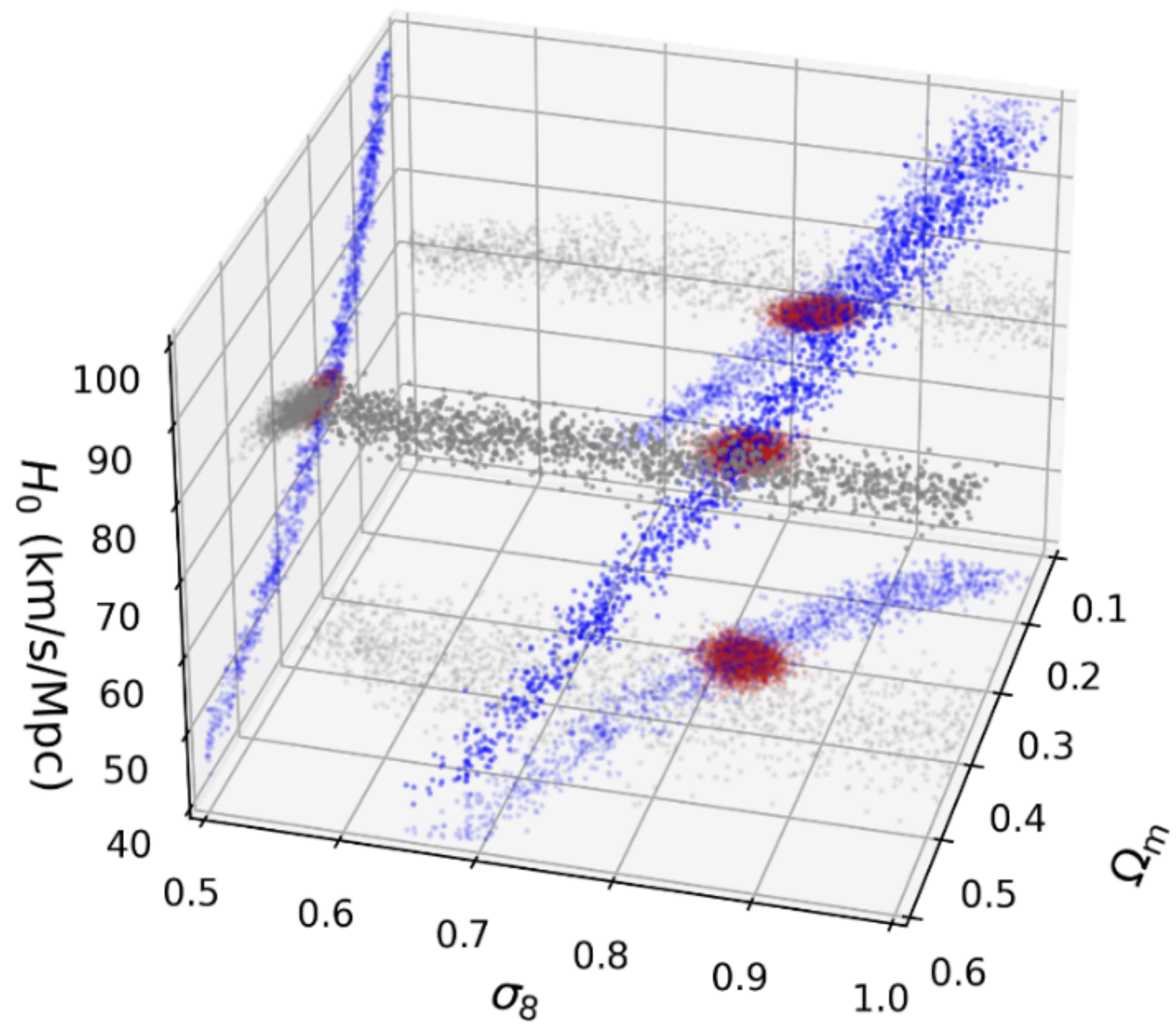
EXTRA SLIDES

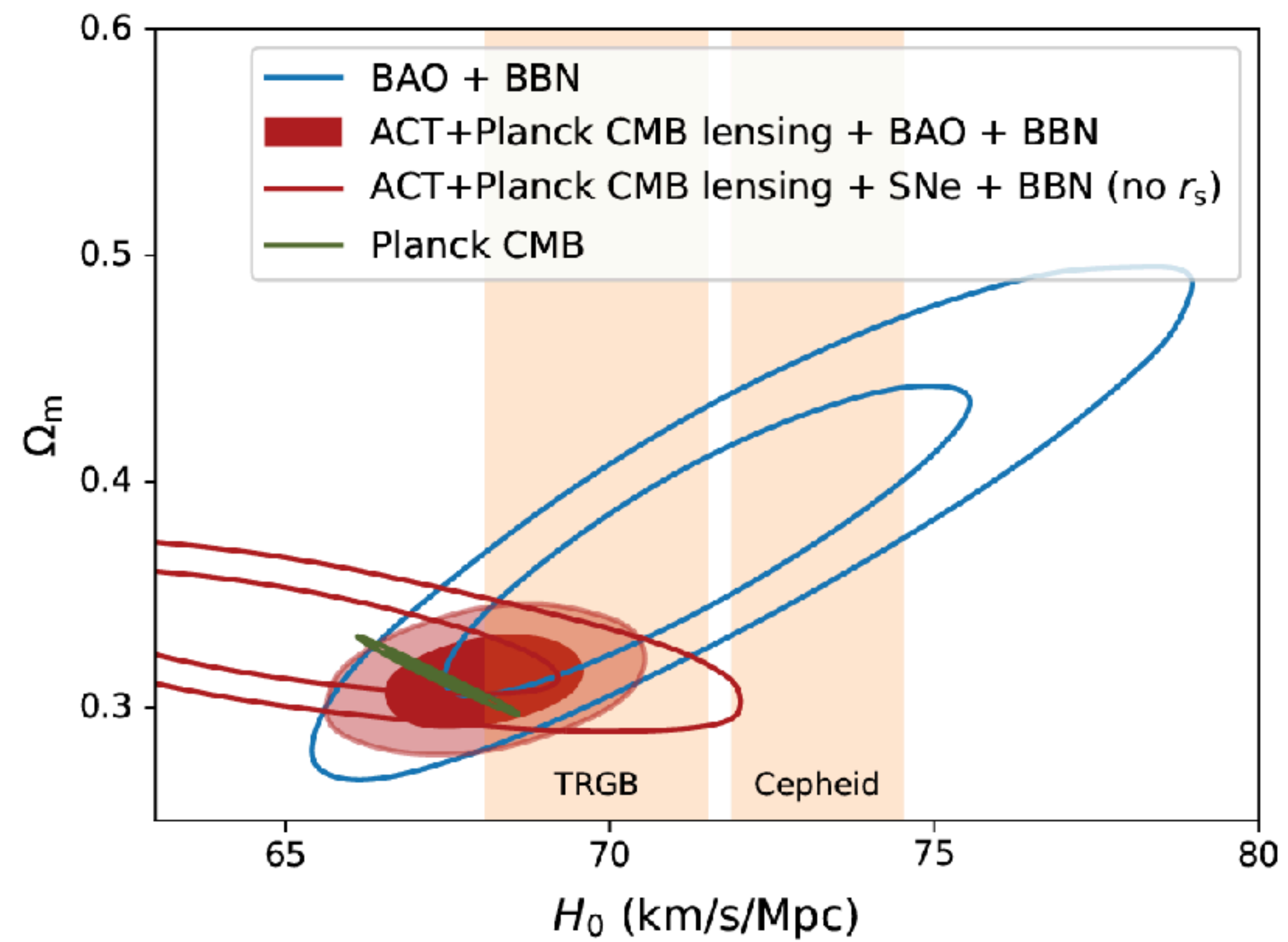
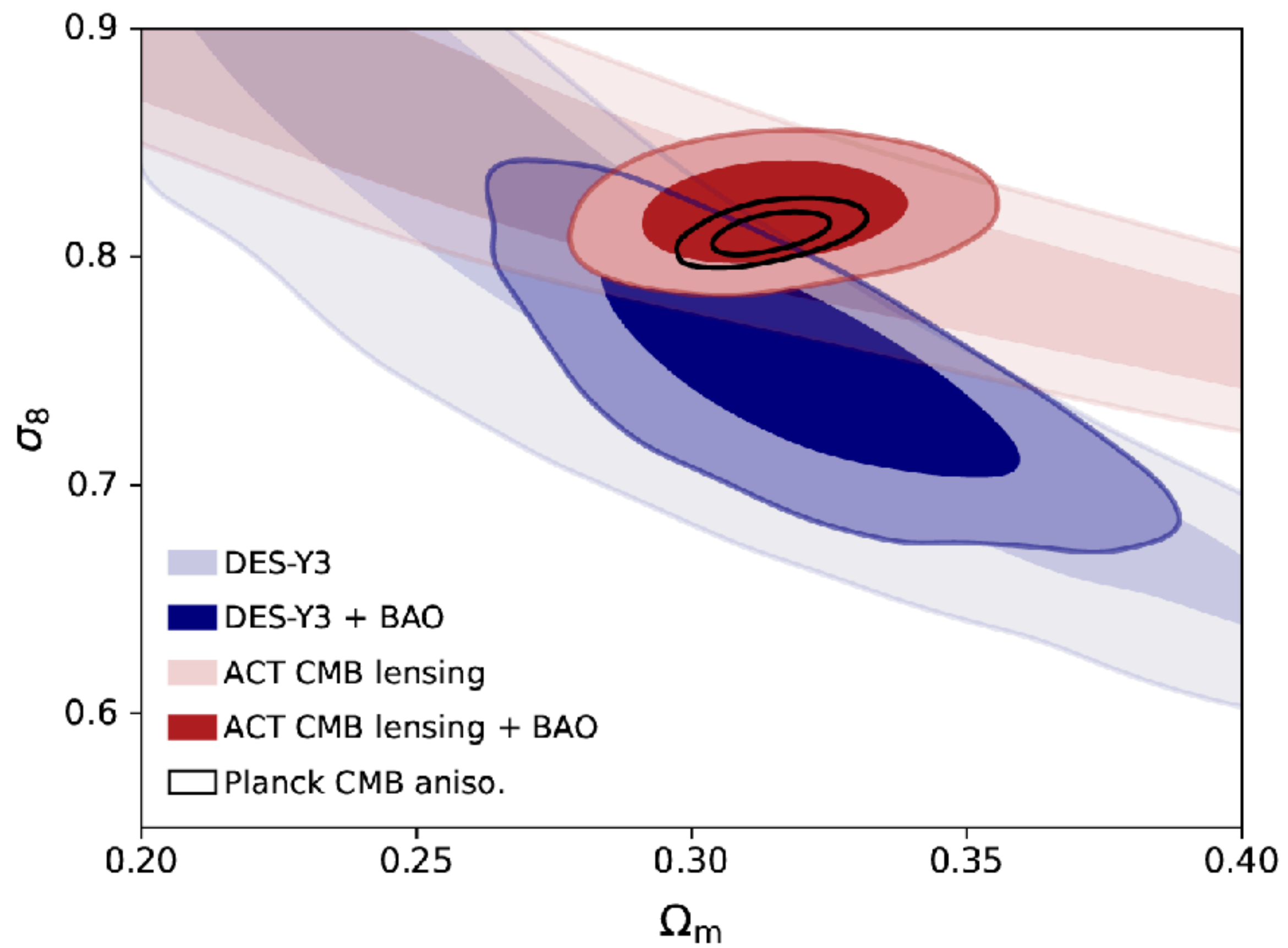
COSMIC SHEAR 1.7 TO 2.1 SIGMA LOWER THAN CMB LENSING

- Quantify tension in S_8 space, where both CMB lensing and cosmic shear have good constraining power
- But σ_8 constrained significantly better by CMB lensing

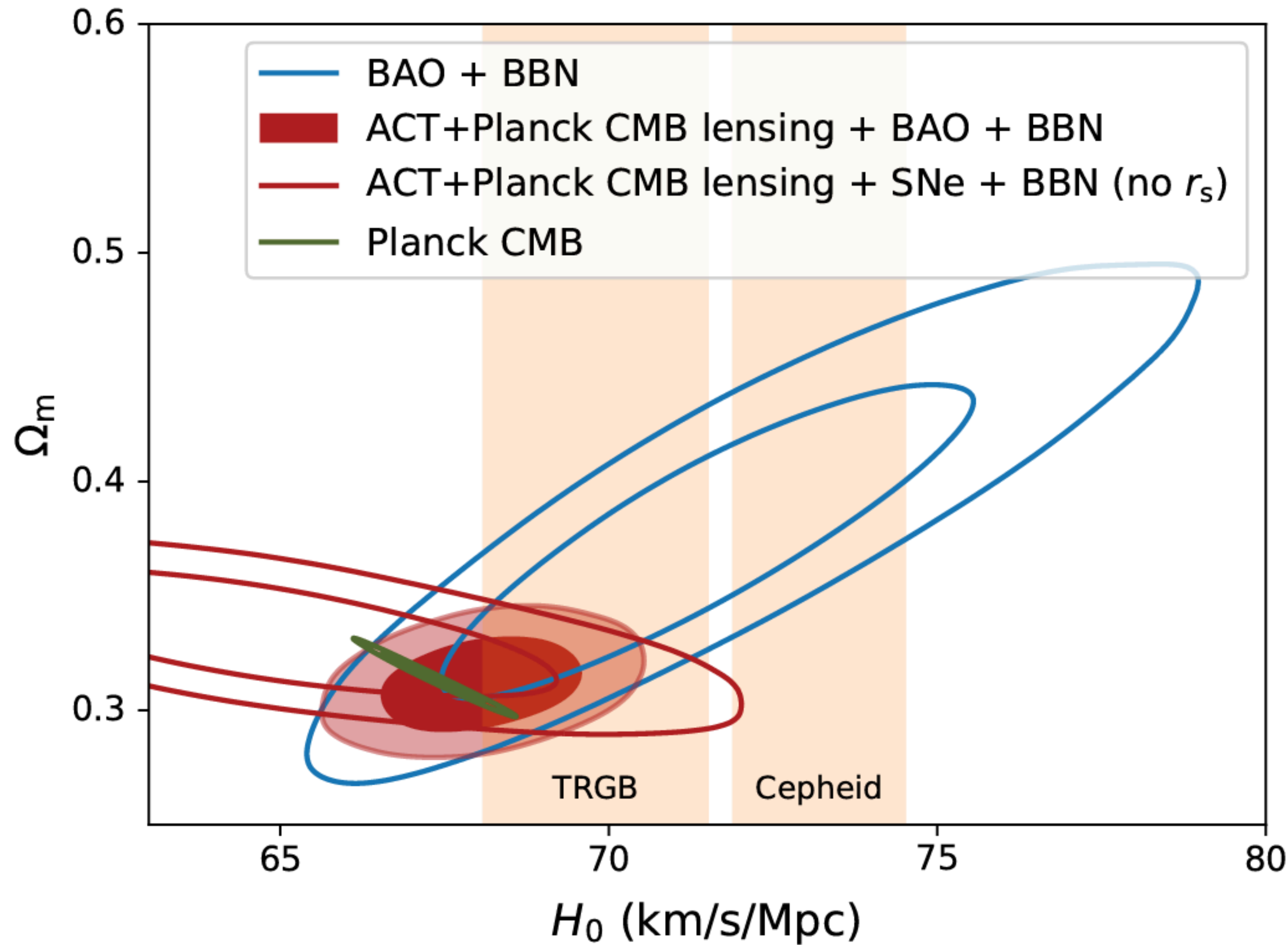


- Planck CMB aniso.
- Planck CMB aniso. (+ A_{lens} marg.)
- Planck CMB lensing + BAO
- SPT CMB lensing + BAO
- ACT CMB lensing + BAO**
- ACT+Planck CMB lensing + BAO**
- DES-Y3 galaxy lensing + BAO
- KiDS-1000 galaxy lensing + BAO
- HSC-Y3 galaxy lensing (Fourier) + BAO
- HSC-Y3 galaxy lensing (Real) + BAO





HUBBLE CONSTANT FROM LENSING



DR6 lensing+ BAO

$$H_0 = 68.3 \pm 1.1 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

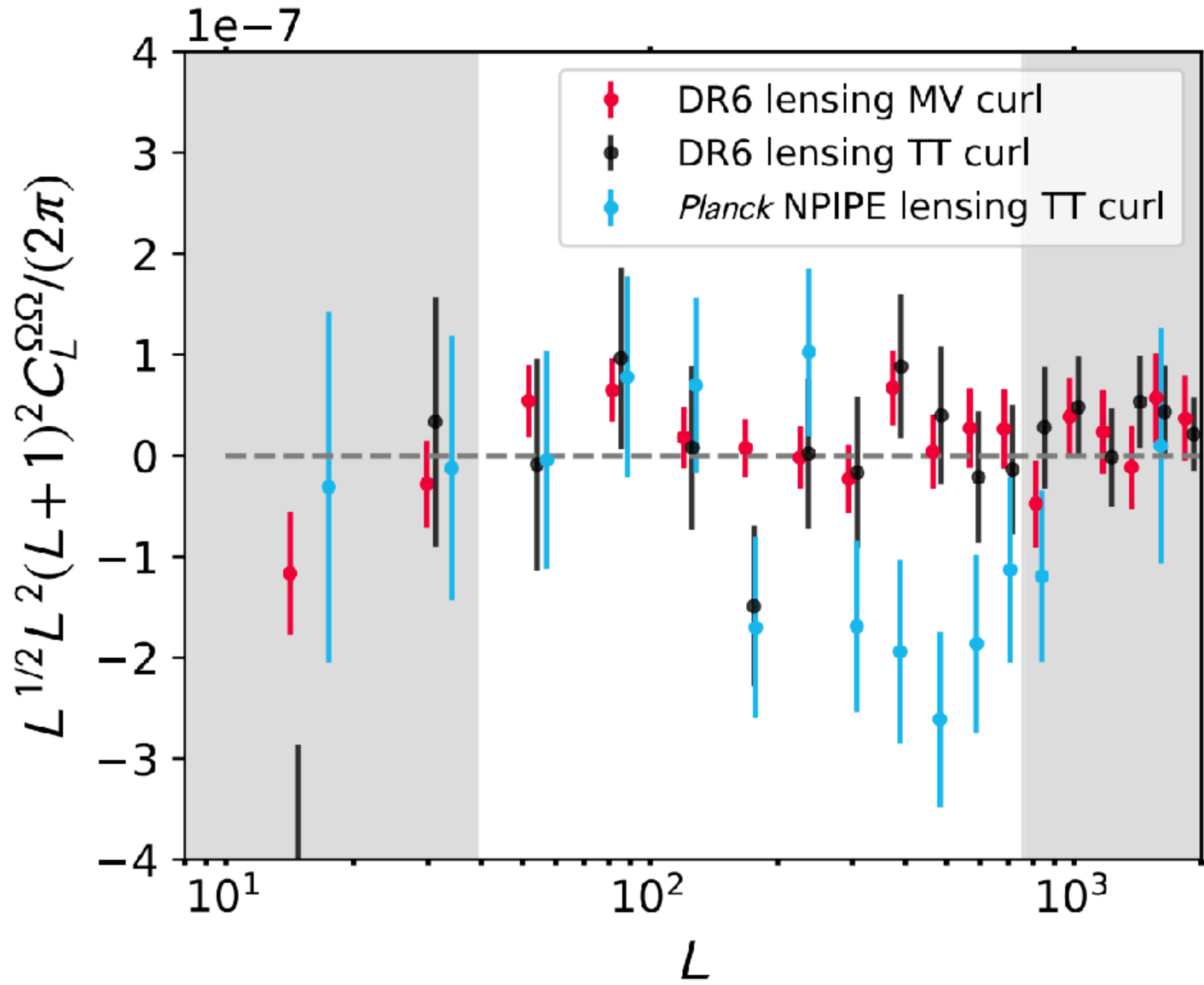
DR6+Planck CMB lensing+BAO

$$H_0 = 68.1 \pm 1.0 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

Sound horizon independent constraint

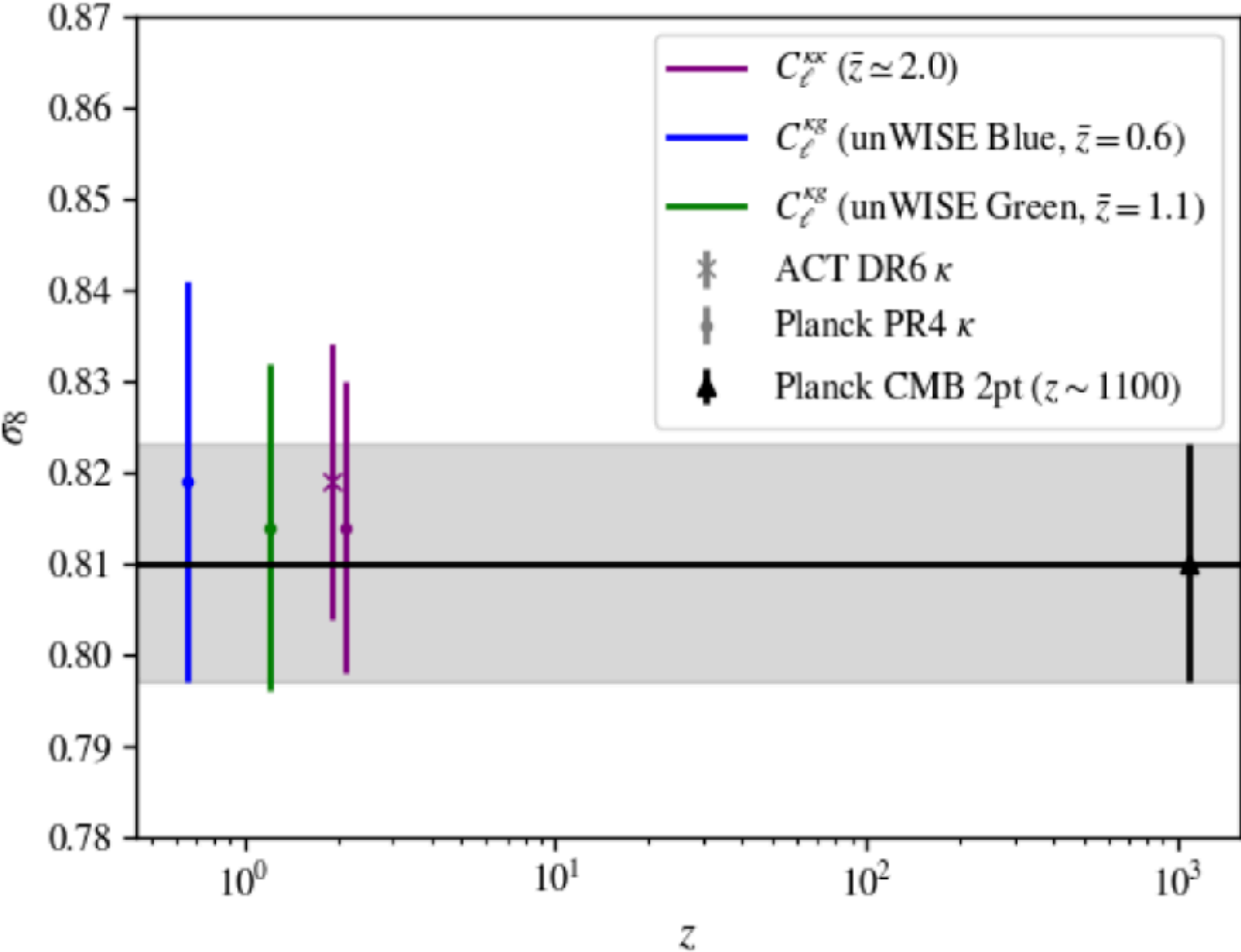
$$H_0 = 64.9 \pm 2.8 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

CURL MODES



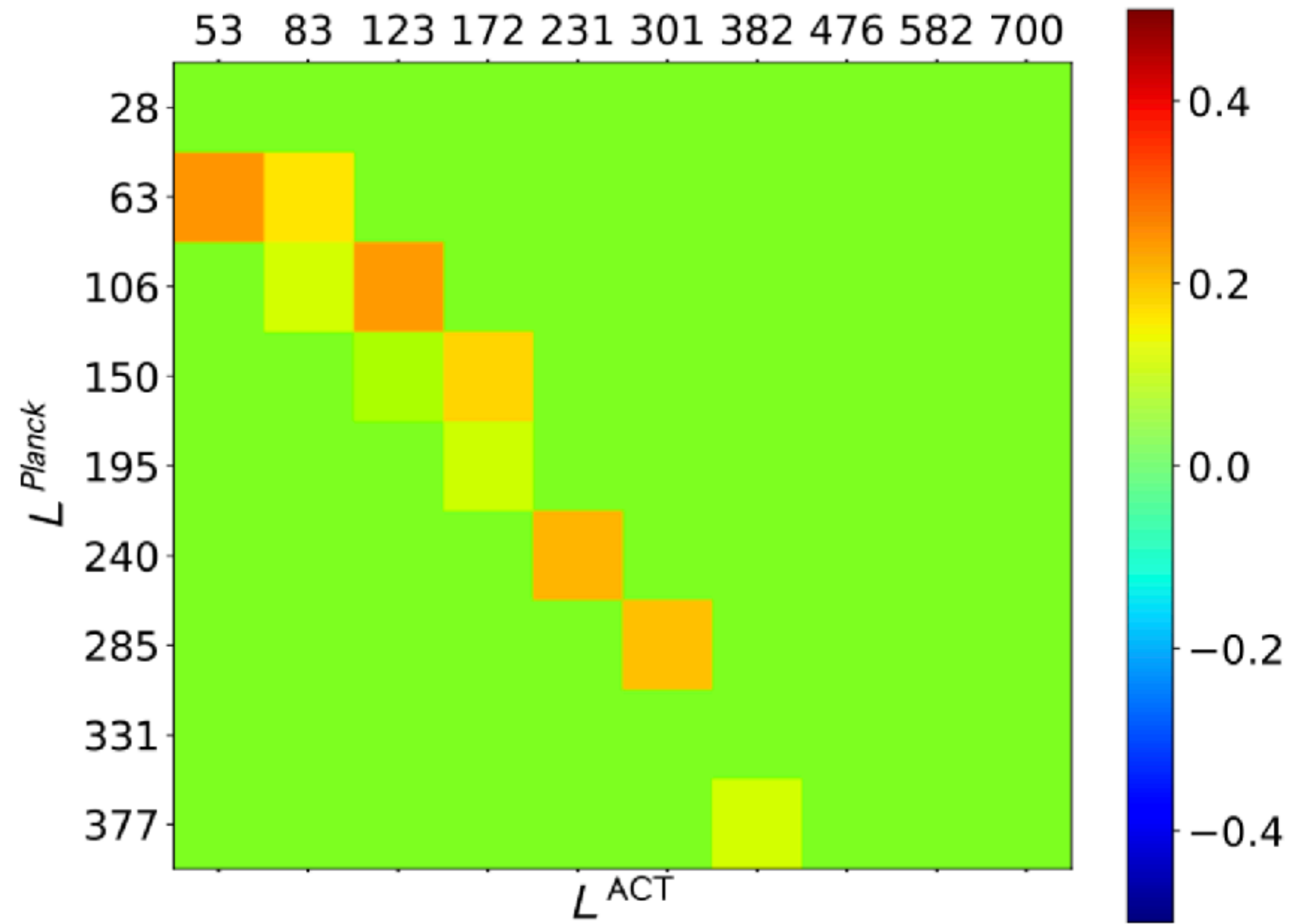
CROSS CORRELATIONS

$\sigma_8(z)$

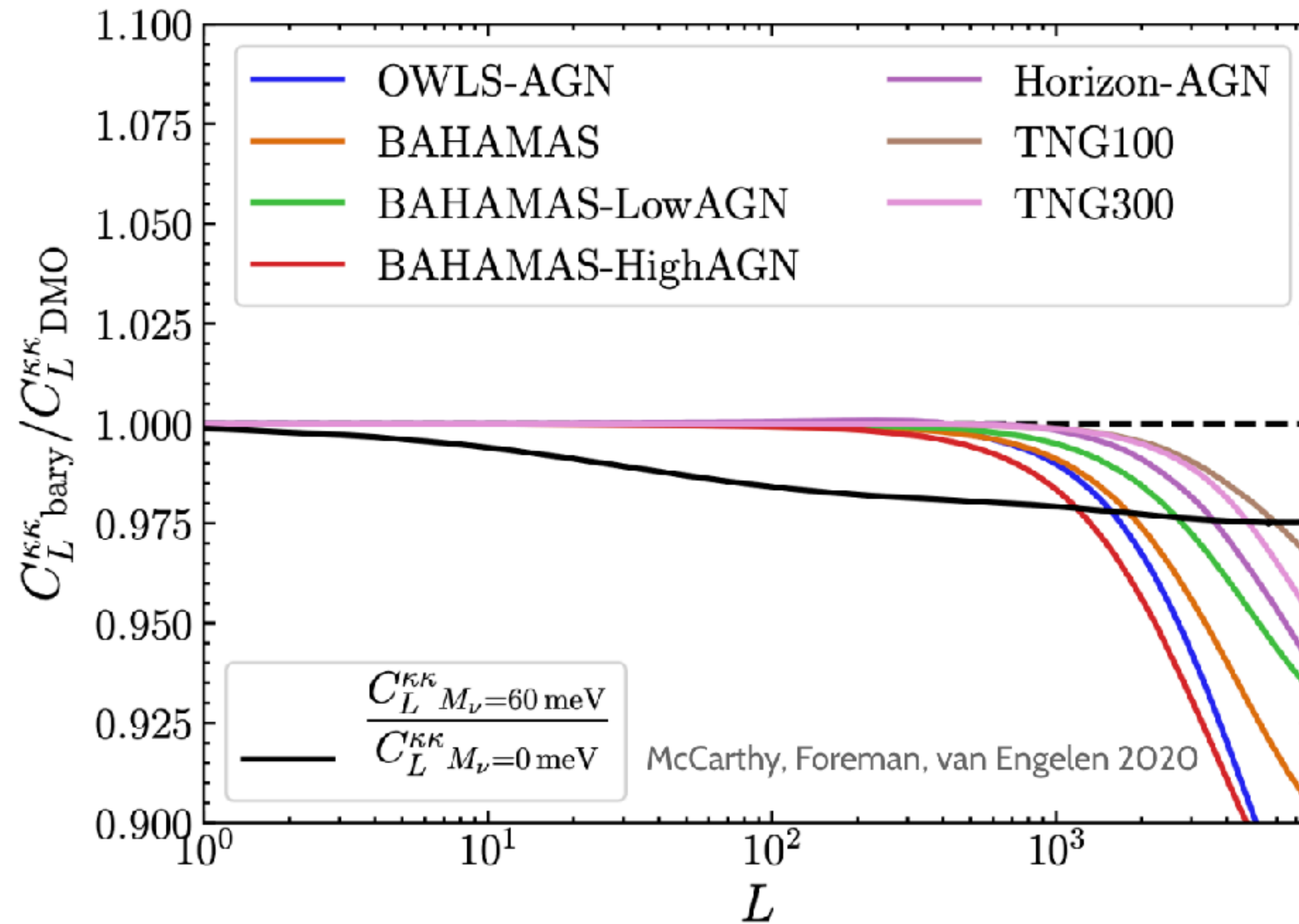


cc Farren

Offdiagonal covmat ACT+Planck



Baryonic effects - suppression negligible where our SNR arises (L<500)



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