The probability distribution of the flux in the Ly$\alpha$ forest

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Outline

- The Ly\(\alpha\) forest in quasar spectra
- Probing structure formation with the forest
- The probability distribution of the Ly\(\alpha\) flux
The Ly$\alpha$ forest in quasar spectra

(resonant) absorption phenomenon in the foreground of quasars, $\lambda_\alpha = 1216 \, \text{Å}$
Basic observables

Beside the discrete absorption lines, the basic observable of the Ly\(\alpha\) forest is the transmitted flux,

\[ F(\omega) = \frac{I_{\text{obs}}(\omega)}{I_{\text{cont}}(\omega)} = \exp \left[ -\tau(\omega) \right] \]
The Lyα forest in CDM cosmologies

The Lyα forest smoothly traces a cosmic web of dark matter sheets and filaments.
The Physical state of the absorbing gas

Gunn & Peterson (1965), Bahcall & Salpeter (1965)

The optical depth for Lya scattering in the resonance at redshift $z$

$$\tau(z) \simeq 4.15 \times 10^8 \left( \frac{n_{HI}}{n_H} \right) (\Omega h^2)^{-1/2} (1 + z)^{-3/2} \left( \frac{n_H(z)}{1 \text{ cm}^{-3}} \right)$$

In the spectra of quasars: $\tau \sim 1 \rightarrow n_{HI}/n_H \ll 1$

The gas responsible for the Lya forest is highly ionized

$$z_{\text{reion}} = ?$$
Modelling the Lyα forest

Fluctuating Gunn-Peterson Approximation:

$$\tau(\omega) = \frac{c \sigma_0}{H(z)} \int_{-\infty}^{+\infty} \frac{dx}{\sqrt{\pi}b(x)} n_{HI}(x) \exp \left[ -\frac{(\omega - x - v_\parallel(x))^2}{b(x)^2} \right]$$

Mimic observed spectra by taking into account the noise and the instrumental resolution.
What makes the Lyα forest interesting?

Tegmark & Zaldarriaga (2002)
Measuring matter clustering with the Ly$\alpha$ forest

+ other statistics
  (bispectrum etc.)
Constraints from the Ly\(\alpha\) flux power spectrum


\[ \sigma_8 = \text{present-day, rms fluctuation amplitude of the density in spheres of 8 Mpc/h} \]

\[ \sigma_8 \approx 0.85 - 0.95 \pm 0.03 \pm 0.15 \]
Constraints from the Lyα flux PS and PDF

Desjacques & Nusser (2005)

Including the PDF in the analysis has a large impact on the inferred value of the clustering amplitude.
Lyα forest and WMAP 3-year data

<table>
<thead>
<tr>
<th>WMAP Cosmological Parameters</th>
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<tbody>
<tr>
<td>Model: $\Lambda$cdm</td>
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<tr>
<td>Data: wmap</td>
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$10^2\Omega_b h^2 = 2.23^{+0.07}_{-0.09}$

$A = 0.68^{+0.06}_{-0.04}$

$A_{0.002} = 0.80^{+0.04}_{-0.05}$

$\Delta^2_{k_R}(k = 0.002/\text{Mpc}) = (2 \times 10^{-10} \pm 1 \times 10^{-10}) \times 10^{-10}$

$h = 0.73^{+0.03}_{-0.04}$

$H_0 = 73^{+3}_{-4} \text{ km/s/Mpc}$

$\xi_A = 3026^{+9}_{-9}$

$n_s = 0.951^{+0.019}_{-0.015}$

$n_s(0.002) = 0.951^{+0.015}_{-0.025}$

$\Omega_b = 0.042^{+0.003}_{-0.006}$

$\Omega_b h^2 = 0.0223^{+0.0007}_{-0.0009}$

$\Omega_c = 0.20^{+0.02}_{-0.04}$

$\Omega_{\Lambda} = 0.76^{+0.04}_{-0.03}$

$\Omega_m = 0.24^{+0.04}_{-0.01}$

$\Omega_m h^2 = 0.127^{+0.007}_{-0.009}$

$\sigma_8 = 0.74^{+0.06}_{-0.06}$

$\sigma_8 \Omega_{m,0} = 0.31^{+0.04}_{-0.05}$

$A_{S,0} = 0.99^{+0.09}_{-0.09}$

$\tau = 0.088^{+0.036}_{-0.034}$

$\theta_A = 0.595 \pm 0.002 \degree$

$z_{eq} = 3036^{+188}_{-250}$

$z_r = 10.9^{+2.7}_{-2.3}$

Spergel et al. (2006)
Systematics errors

Incorporate other statistics of the Ly$\alpha$ forest, e.g.

- Probability distribution (PDF)
- Bispectrum
- Line statistics

Understand

- Systematics in the measurements
  - continuum fitting
  - metal contamination
- Systematics in the theoretical models
  - reionisation history
  - feedback from galaxies/quasars
  - numerical modelling
The PDF of the Ly$\alpha$ flux from a sample of SDSS quasars

Use the probability distribution (PDF) of the Lya transmitted flux to understand better the systematics associated with (large) sample of low resolution quasar spectra such as SDSS
The data

A sample of 3492 quasars included in the SDSS DR3 data release

Ly$\alpha$ forest: $1080 - 1160\text{Å}$
Continuum fitting: hint from composite spectra

Composite spectra: quasar continuum $\approx$ powerlaw + emission lines

Bernardi et al. (2003)
The distribution of spectral indices

Perform a continuum fitting on a spectrum-by-spectrum basis

\[ I_{\text{cont}}(\nu) = I_0 \nu^{\alpha_\nu} + \text{em. lines} \]

\[ \langle \alpha_\nu \rangle = -0.59 \pm 0.36 \]
The probability distribution of the Ly\textalpha flux

The large noise creates pixels with $F \ll 0$ and $F \gg 1$
A lognormal model for the Ly$\alpha$ forest

Bi et al. (1993)

The gas density and velocity are obtained from a local mapping of the linear density and velocity fields

$$\delta_{\text{IGM}}(x, z) = \exp \left( \delta_L(x, z) - \sigma^2_L(z) \right) - 1$$

$$v_{\text{IGM}}(x, z) = v_L(x, z)$$

Assume photoionization equilibrium + equation of state $\rightarrow$ HI density

Model parameters:

- IGM filtering length $k$
- Adiabatic index $\gamma$
- Mean temperature $T$
- Mean flux $\langle F \rangle = \exp(-\tau_{\text{eff}})$
Constraining the model parameters

match the observed Lyα flux PS and PDF of Keck (high resolution) spectra

Lognormal model:

- Good fit at redshift z>3
- Best-fitting value of $\gamma=1$
at all redshift
SDSS mock spectra

Account for:

- Instrumental resolution $\sim 150$ km/s
- Noise (S/N $\sim 3$)
- Strong absorption systems
Comparison with the data

The lognormal model poorly fits the SDSS data at all redshift
Changing the continuum

Add some freedom to the continuum:

\[ I_{\text{cont}}(\nu) = y I_0 \nu^{\alpha_\nu} + \text{em. lines} \]

\[ P(y) = \exp \left[ -\frac{(y - \bar{y})^2}{2\Delta y^2} \right] \]

\[ \bar{y} \approx 0.86 \]

\[ \Delta y \approx 0.18 \]
A unseen break around 1200Å?

Zheng et al. (1997)
Telfer et al. (2002)

composite from low redshift surveys (z<2):
break around the Lyα emission line
Conclusion

- The lognormal model of the Ly$\alpha$ forest provides a good fit to the data at redshift $z \geq 3$
- Evidence for a break in the spectral slope of high-redshift quasars near the Ly$\alpha$ emission line
- Need large residual variations in the continuum normalisation (20 per cent) to account for the smooth shape of the observed PDF
Thank you for your attention