#### Cosmological simulations of galaxy formation

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# Cosmological hydro simulations

- Evolution from z>~100 to z ~< 10 of a representative part of the universe
- Expansion solved analytically and scaled out
- Initial conditions from the CMB & LSS
- Boundary conditions: periodic
- Components: cold dark matter, gas, stars, radiation (optically thin)
- Discretizaton: time, mass (SPH) or length (AMR)
- · Gravity and hydro solvers (and MHD, RT, ...)
- Sub-grid modules are a crucial part of the game

Subgrid models

Cosmological simulations

- $10^{-8}$  interparticle distance in stars
  - $10^{\circ}$  interparticle distance in ISM
  - $10^2$  interparticle distance in IGM
  - 10<sup>11</sup> stellar radii

Length Scales (cm)

- 10<sup>18</sup> interstar distance
- $10^{20}$  star clusters
- 10<sup>22</sup> galaxies
- $10^{24}$  clusters of galaxies
- 10<sup>28</sup> observable universe



#### Zooming into a massive galaxy at z=2: Gas density



Depth: 2 Mpc/h

Log M = 12.6 Log M\* = 11.5

Simulation: OWLS REF L025 N512

25 Mpc/h

### Where to put the gap?

Transition from warm (T ~  $10^4$  K) to cold, molecular (T <<  $10^4$  K) ISM expected at  $\Sigma_H \sim 10 M_{\odot} pc^{-2}$  ( $n_H \sim 10^{-2} - 10^{-1} cm^{-3}$  in warm phase).

- Determined by (dust) column needed to shield UV
- Associated with sharp reduction in Jeans scale  $\rightarrow$  star formation
- Threshold decreases with metallicity and increases with UV

(JS 04, Gnedin+ 09, Krumholz+ 09, 11, Gnedin & Kravtsov 11, Feldmann+ 11, Glover & Clark 12, Clark & Glover 13, ...)

#### Well-posed challenge:

Resolve the Jeans scales in the warm ISM

### **Basic resolution requirements**

- Convergence requires resolving the Jeans scales:  $M_{\rm J} \approx 1 \times 10^7 \, h^{-1} \, {\rm M}_{\odot} f_{\rm g}^{3/2} \left( \frac{n_{\rm H}}{10^{-1} \, {\rm cm}^{-3}} \right)^{-1/2} \left( \frac{T}{10^4 \, {\rm K}} \right)^{3/2}$  $L_{\rm J} \approx 1.5 \, h^{-1} \, {\rm kpc} \, f_{\rm g}^{1/2} \left( \frac{n_{\rm H}}{10^{-1} \, {\rm cm}^{-3}} \right)^{-1/2} \left( \frac{T}{10^4 \, {\rm K}} \right)^{1/2}$
- Resolving the warm phase requires:
  - Particle mass <<  $10^7 M_{\odot}$
  - Spatial resolution << 1 kpc
- Resolving gas with  $n_{H} \sim 10^{1} \text{ cm}^{-3}$  and T  $\sim 10^{2} \text{ K}$  requires :
  - particle mass <<  $10^3 M_{\odot}$
  - spatial resolution << 10 pc
  - Radiative transfer
  - Complex chemistry



#### But we are about to cross the gap in simulations of individual galaxies!



<u>Subgrid models for</u> <u>cosmological hydro simulations</u>

- Radiative cooling/heating
- Star formation
- Chemodynamics/stellar evolution
- Galactic winds driven by feedback from SF
- Black holes and AGN feedback
- Less conventional things. E.g.:
  - Turbulence (incl. mixing)
  - Cosmic rays
  - Dust

# Radiative cooling

- Standard assumptions:
  - H & He in photo-ionisation equilibrium (optically thin, UV background only)
  - Metals in collisional ionisation equilibrium (though many studies still assume primordial abundances!)
- Recent developments (e.g. Wiersma, JS & Smith '09; Shen+ '10; Vogelsberger+ '13, Aumer+ '13):
  - Metals also in photo-ionisation equilibrium
  - Relative abundance variations
- Cutting edge/future:
  - Non-equilibrium ionization
  - Radiative transfer
  - Local radiation sources
  - Molecules
  - Dust

#### Cooling: effect of non-equil. and photo-ionisation





 $n_{H}=10^{-4}$  cm<sup>-3</sup>, z=1, Z=Z<sub> $\odot$ </sub>

Oppenheimer & JS (2013a)

#### <u>Cooling: effect of non-equil. at T < 10<sup>4</sup> K</u>







 $n_{H}$ =10<sup>-4</sup> cm<sup>-3</sup>, T = 10<sup>4</sup> K, z=1, Z=Z<sub>☉</sub>

Oppenheimer & JS (2013b)



# AGN proximity zone fossils

Most intergalactic metals may reside in out-of-equilibrium AGN fossil zones!



# Galactic winds driven by SF

- Winds may be:
  - Energy-driven
  - Momentum-driven
  - Both
- Sources of energy/momentum:
  - Supernovae
  - Radiation pressure:
    - On dust
    - From photo-ionisation
    - From trapping of Lya
  - Stellar winds
  - Cosmic rays
  - Combination of the above

### Galactic winds driven by SF: WARNINGS

- Efficient feedback is required to match observations
- Feedback is often inefficient due to the numerical implementation...
- ... but inefficient feedback is sometimes interpreted as a need for different physical processes
- Nearly all implementations are extremely crude (e.g. radiation pressure w/o radiative transfer)
- At the current resolution, the different feedback processes are hardly distinguishable
- Many hydro simulations use tricks that make them more like SAMs than you may think. E.g.:
  - Wind velocity depends on halo mass or dark matter velocity dispersion (e.g. Okamoto+, Davé/Oppenheimer+, Viel+, Vogelsberger+)
  - Temporarily turn off hydro for winds (e.g. Springel/Hernquist, Davé/Oppenheimer, Viel, Vogelsberger)
  - Temporarily turn off radiative cooling (nearly everyone else)

### Implementing FB: recognized problems

<u>Simplest recipe</u>: star particles inject thermal energy into surroundings (e.g. Katz+ '96) <u>Recognized problems</u>:

- Much of the mass in the ISM is in the cold phase (T  $\prec$  10  $^{4}$  K )
- Simulations do not model cold phase
  - $\rightarrow$  intercloud density too high
    - $\rightarrow$  cooling rate too high
    - $\rightarrow$  feedback too inefficient
  - $\rightarrow$  SF insufficiently clustered
    - $\rightarrow$  feedback too inefficient

### Driving winds: brute force solution

- Allow for a cold phase
- Increase SF threshold (only sensible for cold phase)
- Still require subgrid recipe, but on smaller scale

Problem: need very high resolution

- → Can only model a small number of galaxies (zoomed simulations)
- $\rightarrow$  Need to pick initial conditions (e.g. merger history)

(e.g. Ceverino & Klypin '07, Hopkins+ '12, Ceverino+ '13)

### Driving winds: subgrid recipes

- Multiphase particles (e.g. Marri & White '93, Scannapieco, Murante, Aumer/White)
- Suppress cooling by hand (e.g. Gerritsen '97, Thacker, Stinson/Brook/Gibson/Governato/Maccio/Mayer/Wadsley/...)
- Inject momentum (i.e. kinetic feedback) (e.g. Navarro & White '93, Springel/Hernquist, Davé/Oppenheimer, Teyssier, OWLS/GIMIC, Vogelsberger, ...)
  - Most relevant advantage: can decrease initial mass loading
- Temporarily decouple winds from the hydrodynamics (e.g. Springel/Hernquist '03, Davé/Oppenheimer, Viel, Vogelsberger, ...)
- Multiple feedback processes (e.g. Hopkins+, Stinson+ '13, ...)

### Implementing FB: less recognized problems

- Reality: SNe (or BHs) inject lots of energy in very little mass
  - $\rightarrow$  High temperatures
  - $\rightarrow$  Long cooling times
  - $\rightarrow$  Efficient feedback
- Simulations: inject energy in large gas mass
  - $\rightarrow$  Low heating temperatures
  - $\rightarrow$  Short cooling times
  - $\rightarrow$  Inefficient feedback

e.g. Kay+ '03; Booth & JS '09; Creasey+ '11; Dalla Vecchia & JS '12

### Implementing FB: less recognized problems

- The SNII of an SSP of mass  $m_*$  can heat a mass  $m_{g,heat}$  by  $\Delta T = 4 \times 10^7 \text{ K} (m_*/m_{a,heat})$
- Reality:  $m_* \gg m_{g,heat}$  initially  $\rightarrow \Delta T \gg 10^8 \text{ K}$  $\rightarrow t_c \gg 10^8 \text{ yr} (n_H/1 \text{ cm}^{-3})^{-1}$
- In simulations:  $m_* \sim 0.01 0.1 m_{g,heat}$  $\rightarrow \Delta T \sim 10^6 K$ 
  - $\rightarrow$  t<sub>c</sub> ~ 10<sup>5</sup> yr (n<sub>H</sub>/1 cm<sup>-3</sup>)<sup>-1</sup>
  - $\rightarrow$  overcooling
- Note that in SPH simulations (m\*/ m<sub>g,heat</sub>) is independent of resolution!



Dalla Vecchia & JS (2012)

#### Implementing thermal FB: requirements

 FB only efficient if heated resolution elements expand faster than they cool radiatively:

 $t_c \gg t_s = h/c_s$ 

where h is the spatial resolution

- Adiabatic expansion does not change  $t_c / t_s$  (assuming Brehmsstrahlung)
- Required T depends on density and resolution

$$\frac{t_{\rm c}}{t_{\rm s}} = 2.8 \times 10^2 \left(\frac{n_{\rm H}}{1 \,\,{\rm cm}^{-3}}\right)^{-1} \left(\frac{T}{10^{7.5} \,\,{\rm K}}\right) \left(\frac{h}{100 \,\,{\rm pc}}\right)^{-1}$$
$$\frac{t_{\rm c}}{t_{\rm s}} \simeq 98 \left(\frac{n_{\rm H}}{1 \,\,{\rm cm}^{-3}}\right)^{-2/3} \left(\frac{T}{10^{7.5} \,\,{\rm K}}\right) \left(\frac{\langle m \rangle}{7 \times 10^4 \,\,{\rm M_{\odot}}}\right)^{-1/3}$$

Dalla Vecchia & JS (2012)



### Implementing efficient thermal FB:

- $\Delta T$  determined by resolution
- Stochastic FB
  - → given  $\Delta T$ , fraction of available energy that is injected,  $f_{th}$ , determines heating probability
- $f_{\text{th}}$  not predicted, unresolved thermal losses need to be calibrated



Dalla Vecchia & JS (2012)

#### Mass outflow rate: 10<sup>10</sup> Mo halo

- Particle mass  $7 \times 10^2 \text{ M}_{\odot} \rightarrow \frac{t_{\text{c}}}{t_{\text{s}}} \cong 5 \times 10^2 \left(\frac{n_{\text{H}}}{1 \text{ cm}^{-3}}\right)^{-2/3} \left(\frac{\Delta T}{10^{7.5} \text{ K}}\right)$
- Max  $n_H \sim 10^2 \text{ cm}^{-3} \rightarrow \text{insensitive to } \Delta \text{T for } \Delta \text{T} \geq 10^{6.5} \text{ K}$



### 10<sup>10</sup> Mo halo, edge-on, gas density

#### $\Delta T = 10^{6.5} \text{ K}$

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- 17.5 kpc/h-

 $\Delta T = 10^{7.5} \text{ K}$ 

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#### <u>Mass outflow rate: 10<sup>12</sup> Mo halo</u>

- Particle mass 7×10<sup>4</sup>  $M_{\odot} \rightarrow \frac{t_c}{t_s} \approx 1 \times 10^2 \left(\frac{n_H}{1 \, \mathrm{cm}^{-3}}\right)^{-2/3} \left(\frac{\Delta T}{10^{7.5} \, \mathrm{K}}\right)$
- Max  $n_H \sim 10^3 \text{ cm}^{-3} \rightarrow \text{insensitive to } \Delta T \text{ for } \Delta T \geq 10^{7.5} \text{ K}$



### 10<sup>12</sup> Mo halo, edge-on, gas density

 $\Delta T = 10^{6.5} \text{ K}$ 

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45 kpc/h

 $\Delta T = 10^{7.5} \text{ K}$ 



Dalla Vecchia & JS (2012)

# Self-regulated galaxy formation

- Feedback too weak compared to accretion
  - >Gas density increases
  - >Star formation /BH growth rate increases
  - >Feedback increases
- Feedback too strong compared to accretion
  - >Gas density decreases
  - Star formation/BH growth rate decreases
     Feedback decreases

# Consequences of self-regulated GF

Outflow rate is determined by inflow rate. Hence, it is independent of:

- SF law
  - > SFR independent of SF law
    - SF law determines the amount of gas that is involved in SF ("gas fraction")

### Varying the SF law: SFR(M)



Haas, JS, et al. (2013a)

### Varying the SF law: Gas fraction



Haas, JS, et al. (2013a)

# Consequences of self-regulated GF

Outflow rate is determined by inflow rate. Hence, it is independent of:

- SF law
  - > SFR independent of SF law
    - SF law determines the amount of gas that is involved in SF ("gas fraction")
- SF feedback efficiency
  - SFR, and hence M\*, inversely proportional to efficiency of SF feedback
- AGN feedback efficiency
  - BH accretion rate, and hence M<sub>BH</sub>, inversely proportional to efficiency of AGN feedback
  - > SFR independent of AGN feedback efficiency

### Varying the efficiency of AGN feedback





Self-regulation on scale of DM haloes! (Booth & JS 2010, 2011)

Booth & JS (2009)

#### The effect of baryons on the distribution of matter



McCarthy, JS+ (2011)

#### The effect of baryons on the distribution of matter



← 10 Mpc/h ----->

McCarthy, JS+ (2011)

# Group gas and stellar contents



McCarthy, JS+ (2010)



# **Optical vs X-ray luminosity**



Stott+ (2012)



#### Baryons and the matter power spectrum





#### Baryons and the matter power spectrum





#### <u>Biases due to galaxy formation</u> for a Euclid-like weak lensing survey



Galaxy formation provides a challenge (target?) for weak lensing

Semboloni+ (2011)



#### Two and three point statistics



Semboloni, Hoekstra, JS '13

Euclid w<sub>o</sub> marginalised



#### Two and three point statistics



Semboloni, Hoekstra, JS '13





### Cosmic shear

- Baryonic effects can be dramatic (bias for Euclid ~10s of per cent if untreated)
- Power spectrum affected up to very large scales (k > 0.3 h/Mpc)
- Impact on bispectrum even higher
- Effects dominated by gas ejection

   → Underestimated by models suffering from overcooling
   → Calibration should use gas rather than star fractions
- Modified halo models can capture most of the effects, but currently use input from simulations

### What next for galaxy simulations?

- Resolve cold ISM down to 10<sup>2</sup> K in individual (dwarf) galaxy
- Non-equilibrium chemistry including molecules
- Radiation-hydrodynamics

### What next for cosmological simulations?

# Evolution and Assembly of Galaxies and their Environments



- 100 Mpc volume
- 2x1504<sup>3</sup> particles
- To z = 0
- Resolves warm ISM
- Subgrid recipes dependent only on local hydro quantities
- Feedback efficiency calibrated to match mass function







