

**Final results from the Sloan Digital Sky Survey:
geometry of the universe and constraints on
cosmological neutrinos**

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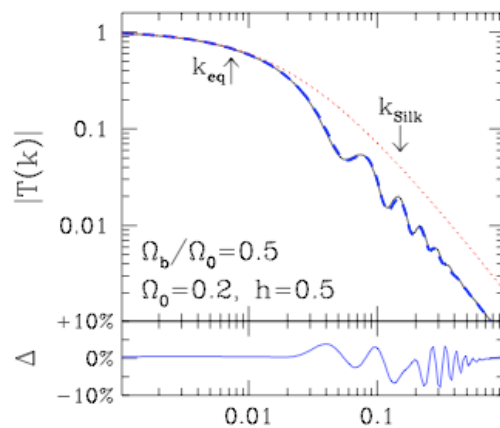
Outline

- Physics of Large Scale Structure (LSS): linear theory
- The “theory” of observing LSS
- SDSS DR7 BAO results: geometric constraints
- Modeling the DR7 Power Spectrum Shape
- Constraints on Cosmological Neutrinos

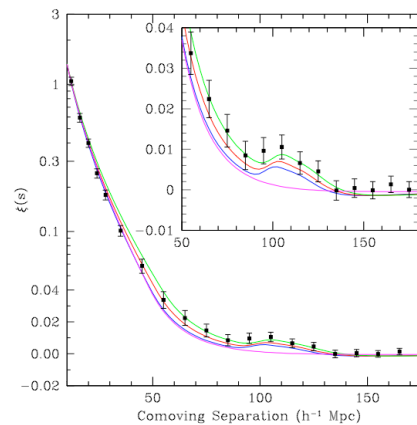
The Physics of LSS: CDM, baryons, photons, neutrinos I

$$P_{\text{matter}}(k, z) = T^2(k) P_{\text{prim}}(k) D^2(z)$$

- Primordial Perturbations: Gaussian and adiabatic $P_{\text{prim}}(k) = A_0 (k/k_0)^{n_s}$
- Transfer function $T(k)$ describing physics at matter-radiation equality
 - depends only on $\Omega_m h^2$, $\Omega_b h^2$, $\Omega_r h^2 = \Omega_\gamma h^2 (1 + 0.2271 N_{\text{eff}})$
 - horizon at matter-radiation equality [$k_{\text{eq}} = \Omega_m h^2 (\Omega_r h^2 / 2)^{-1/2} \sim 0.01 \text{ Mpc}^{-1}$]
 - sound horizon at the baryon drag epoch r_s
- All modes grow at the same rate during matter-domination: $D(z)$
- CMB peak height ratios give us $\Omega_b h^2$, $\Omega_m h^2 / \Omega_r h^2 = 1 + z_{\text{eq}}$



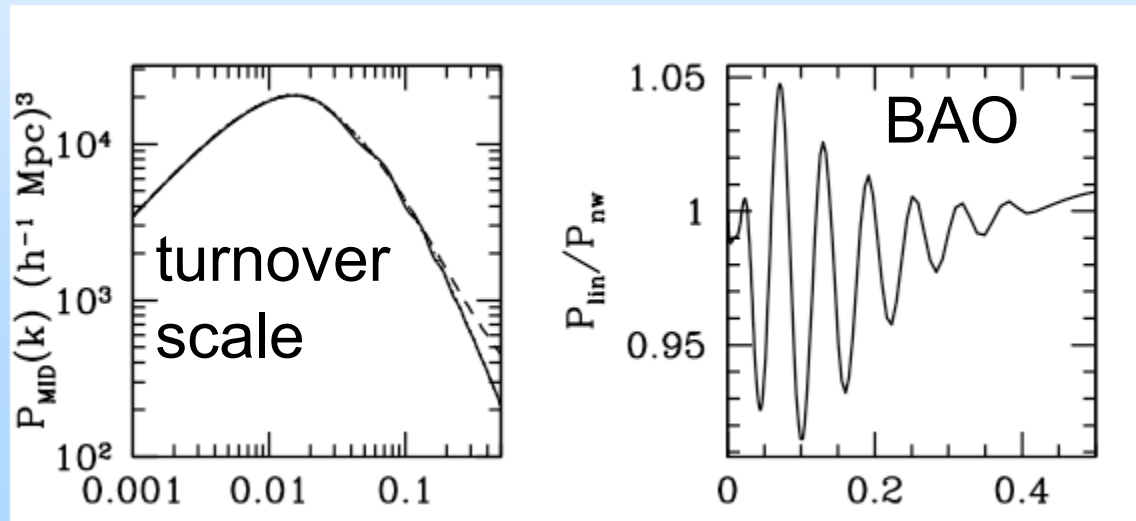
Eisenstein & Hu, 1998, ApJ, 496, 605



Eisenstein et al. 2005, ApJ, 633, 560

Physics of LSS: $P(k)$ as a standard ruler

- WMAP5 almost fixes* the expected $P_{\text{lin}}(k)$ in Mpc^{-1} through $\Omega_c h^2$ (6%) and $\Omega_b h^2$ (3%), independent of θ_{CMB} (and thus curvature and DE).

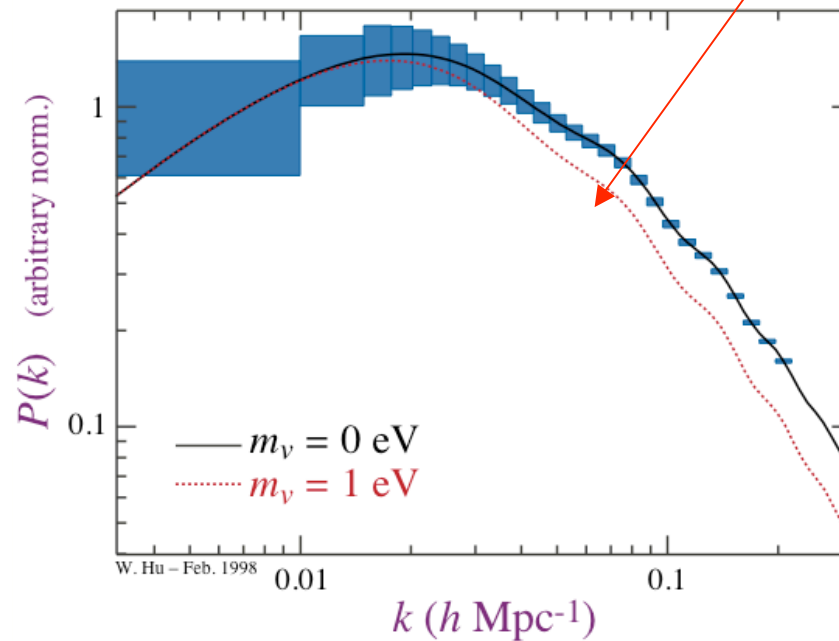


- In the minimal model ($N_{\text{eff}} = 3.04$, $\Sigma m_\nu = 0$), entire $P(k)$ shape acts as a “std ruler” and provides an impressive consistency check -- same physics that generates the CMB at $z=1100$ also determines clustering at low z .

Physics of LSS: massive neutrinos

- Massive neutrinos $\Sigma m_\nu < \sim 1$ eV become non-relativistic AFTER recombination and suppress power on small scales

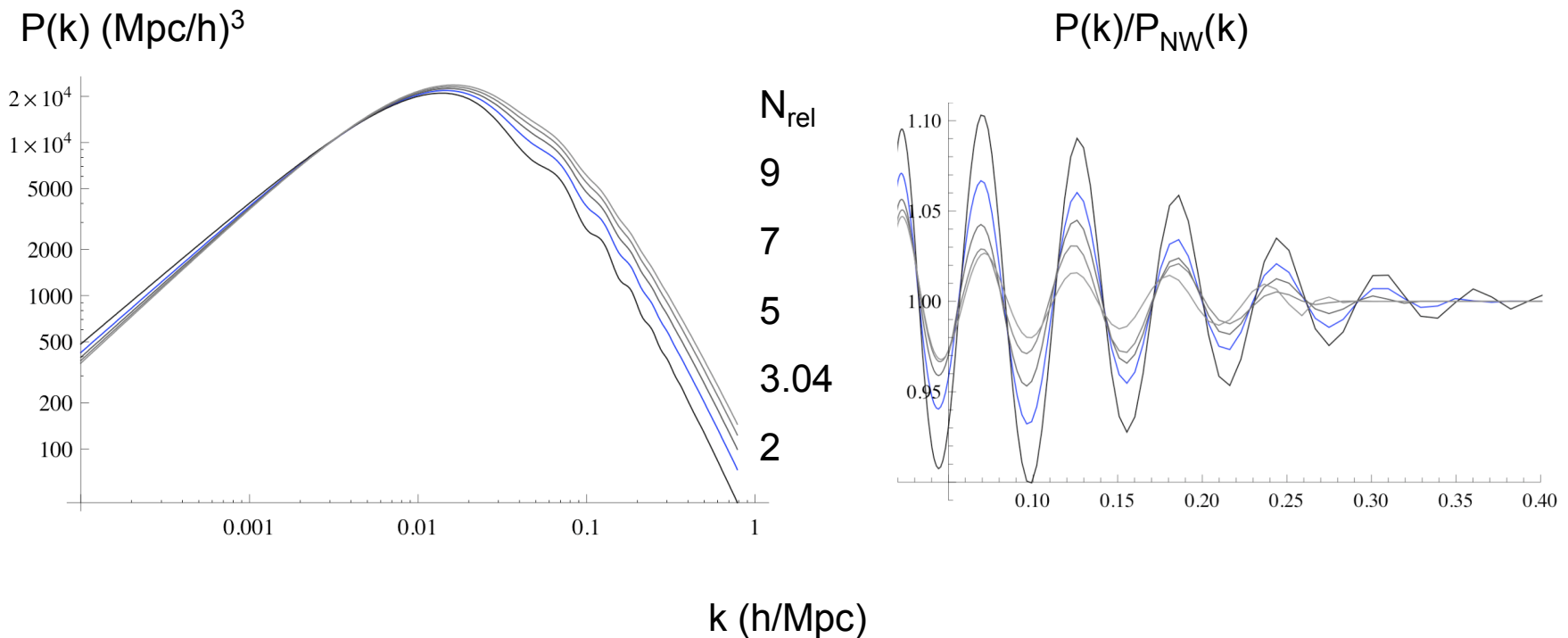
$$P_{\text{matter}}(k, z) = T^2(k) P_{\text{prim}}(k) D^2(z, k, \Sigma m_\nu)$$



Courtesy of W. Hu

Physics of LSS: relativistic species

- N_{rel} affects matter-radiation equality; degenerate with $\Omega_c h^2$ in WMAP
(Not true for Planck!)
- Along WMAP degeneracy, both $P(k)$ shape and the Ω_b/Ω_c change:



“Theory” of Observing LSS: Geometry

- We measure θ, φ, z ; need a model to convert to co-moving coordinates.

- Transverse: $\chi(z) = \int_0^z \frac{c \, dz}{H(z)}$ Along LOS: $\Delta\chi(z) = \frac{c \, \Delta z}{H(z)}$

- Spherically averaged, isotropic pairs constrain

$$D_V(z) = \left[(1+z)^2 D_A^2(z) \frac{cz}{H(z)} \right]^{1/3}$$

SDSS DR7 Results

- BAOs only: [arXiv:0907.1660](#)
- LRG $P(k)$: [arXiv:0907.1659](#)

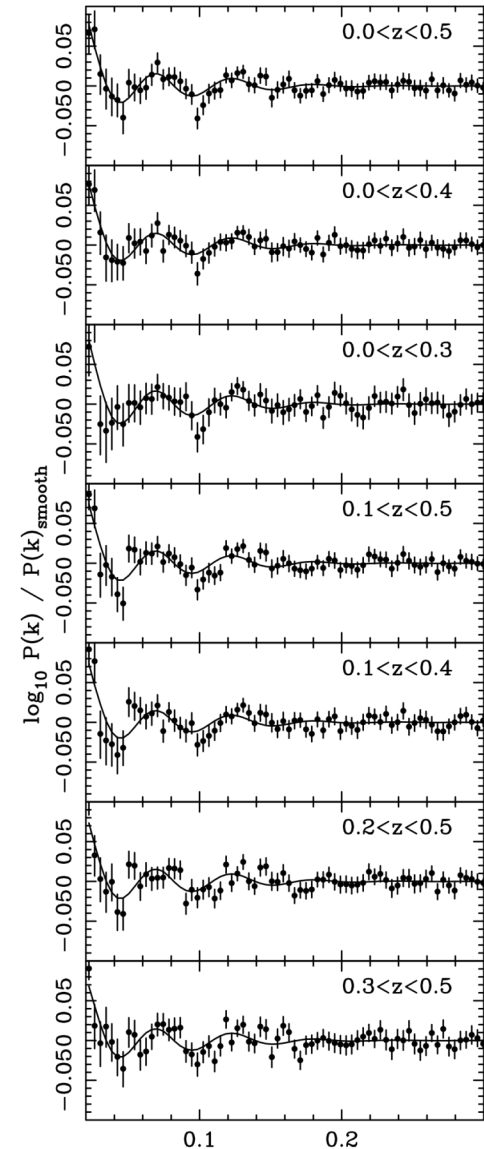
BAO in SDSS DR7 + 2dFGRS power spectra

- Combine 2dFGRS, SDSS DR7 LRG and Main Galaxies
- Assume a fiducial distance-redshift relation and measure spherically-averaged $P(k)$ in redshift slices
- Fit spectra with model comprising smooth fit $\times$ damped BAO

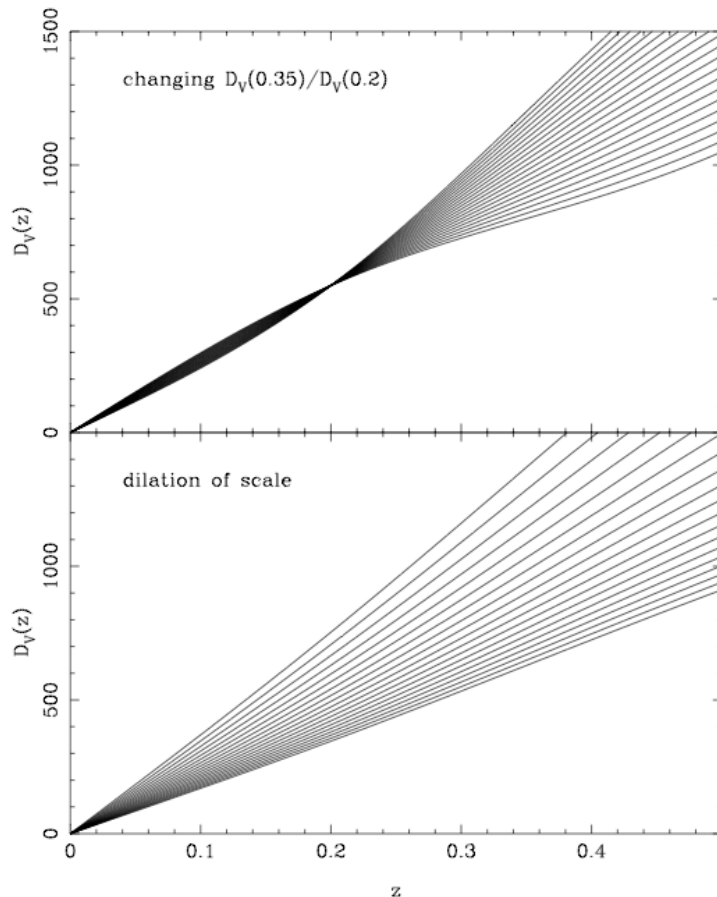
- To first order, isotropically distributed pairs depend on

$$D_V(z) = \left[(1+z)^2 D_A^2(z) \frac{cz}{H(z)} \right]^{1/3}$$

- Absorb cosmological dependence of the distance-redshift relation into the window function applied to the model $P(k)$
- Report model-independent constraint on $r_s/D_V(z_i)$



SDSS DR7 BAO results: modeling the distance-redshift relation

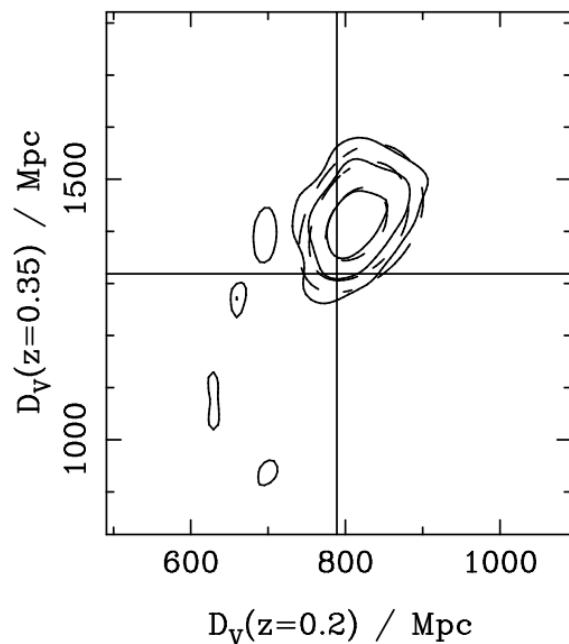


Parameterize distance-redshift relation by smooth fit: can then be used to constrain multiple sets of models with smooth distance-redshift relation

For SDSS+2dFGRS analysis, choose nodes at $z=0.2$ and $z=0.35$, for fit to D_V

$$D_V(z) = \left[(1+z)^2 D_A^2(z) \frac{cz}{H(z)} \right]^{1/3}$$

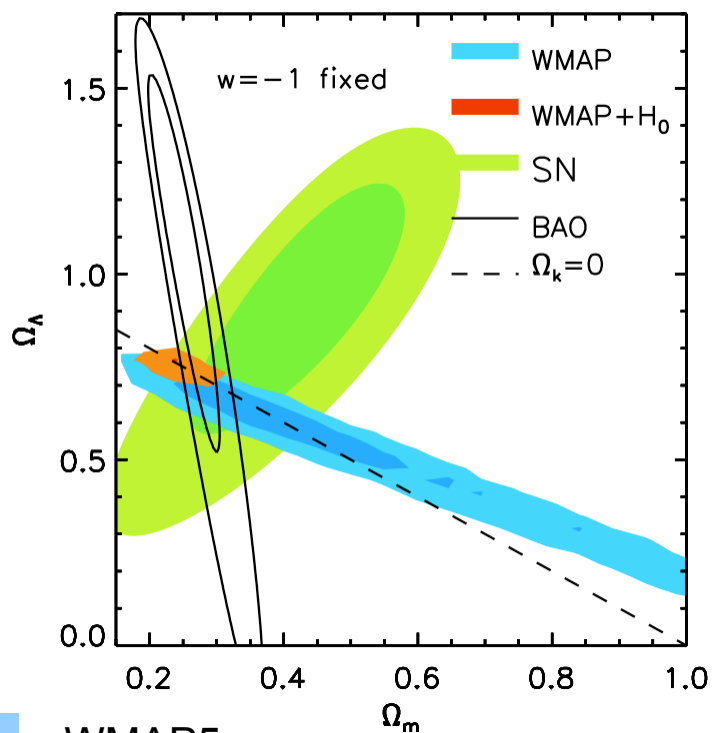
BAO in SDSS DR7 + 2dFGRS power spectra



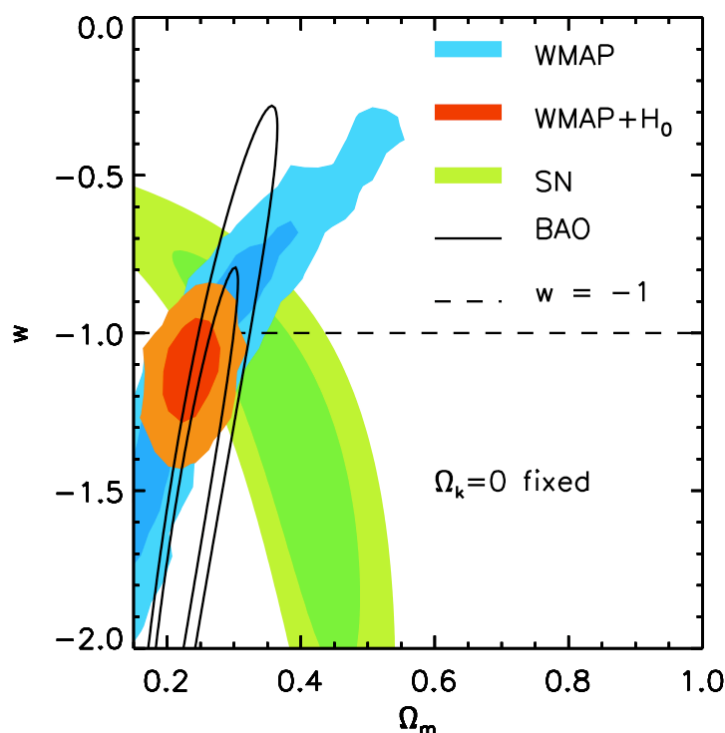
- results can be written as independent constraints on a distance measure to $z=0.275$ and a tilt around this
$$r_s(z_d)/D_V(0.275) = 0.1390 \pm 0.0037 \text{ (2.7\%)} \\ D_V(0.37)/D_V(0.2) = 1.736 \pm 0.065$$
- consistent with Λ CDM models at 1.1σ when combined with WMAP5

Cosmological Constraints

Λ CDM models with curvature



flat wCDM models



WMAP5

WMAP5+ H_0 [Riess et al. 2009]

Union supernovae

$r_s(z_d)/D_V(0.2)$ & $r_s(z_d)/D_V(0.35)$

WMAP5+BAO Λ CDM:

$\Omega_m = 0.278 \pm 0.018$, $H_0 = 70.1 \pm 1.5$

WMAP5+BAO+SN wCDM + curvature:

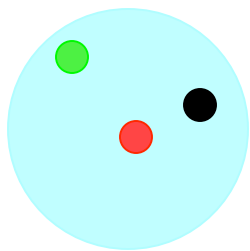
$\Omega_{\text{tot}} = 1.006 \pm 0.008$, $w = -0.97 \pm 0.10$

Percival, **BR**, et al. (2009, arXiv:0907.1660)

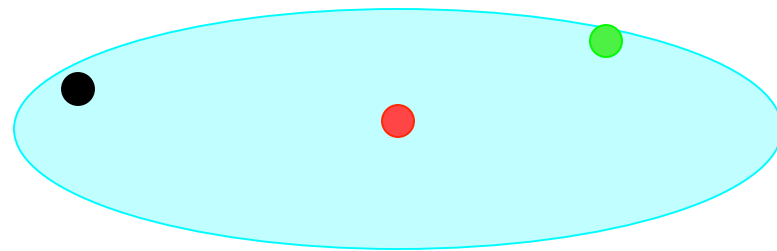
Modeling $P_{\text{gal}}(\mathbf{k})$: Challenges

- density field goes nonlinear
- uncertainty in the mapping between galaxy and matter density fields
- galaxy positions observed in redshift space

“Finger-of-God” (FOG)

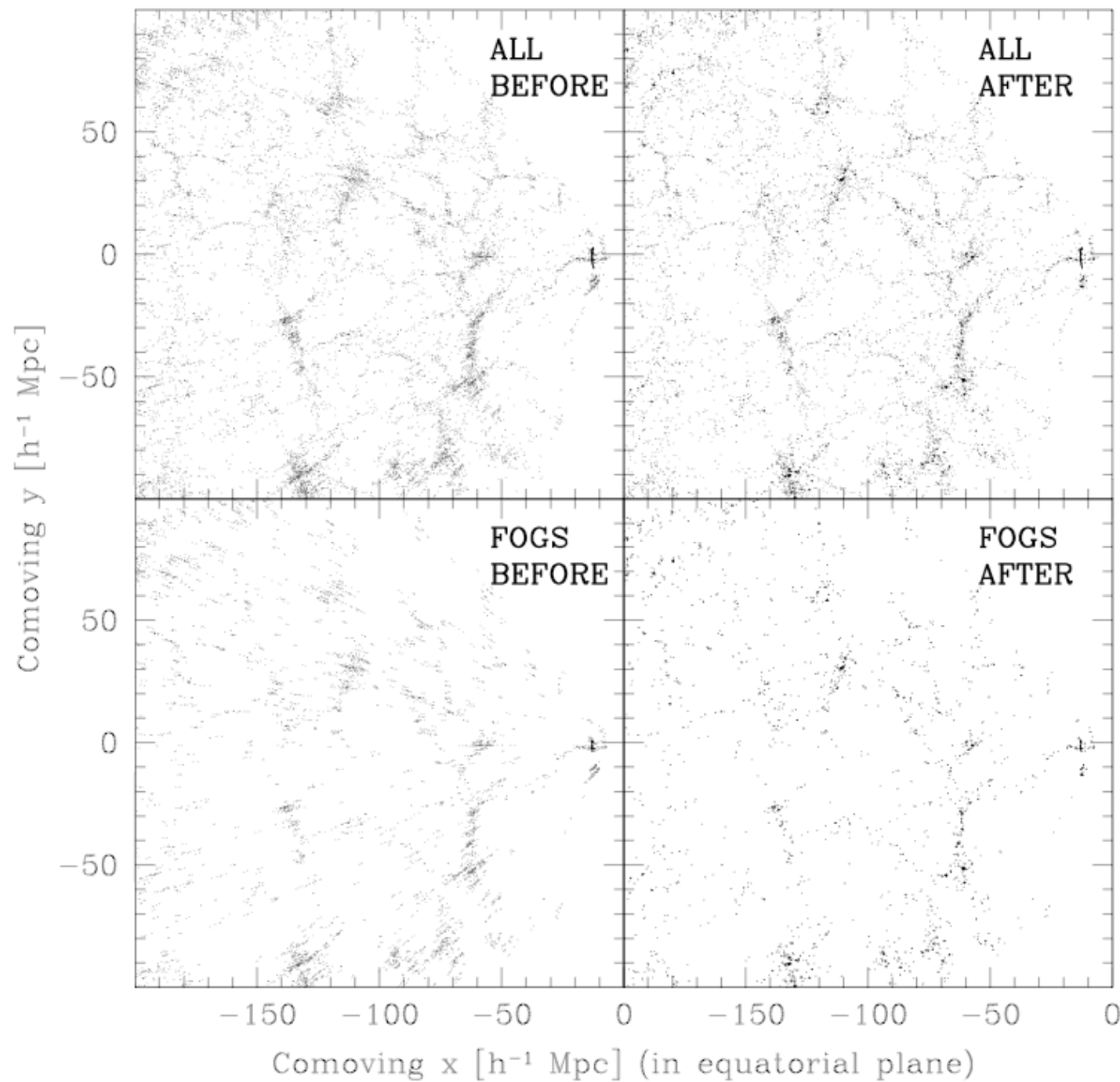


Real space



Redshift space

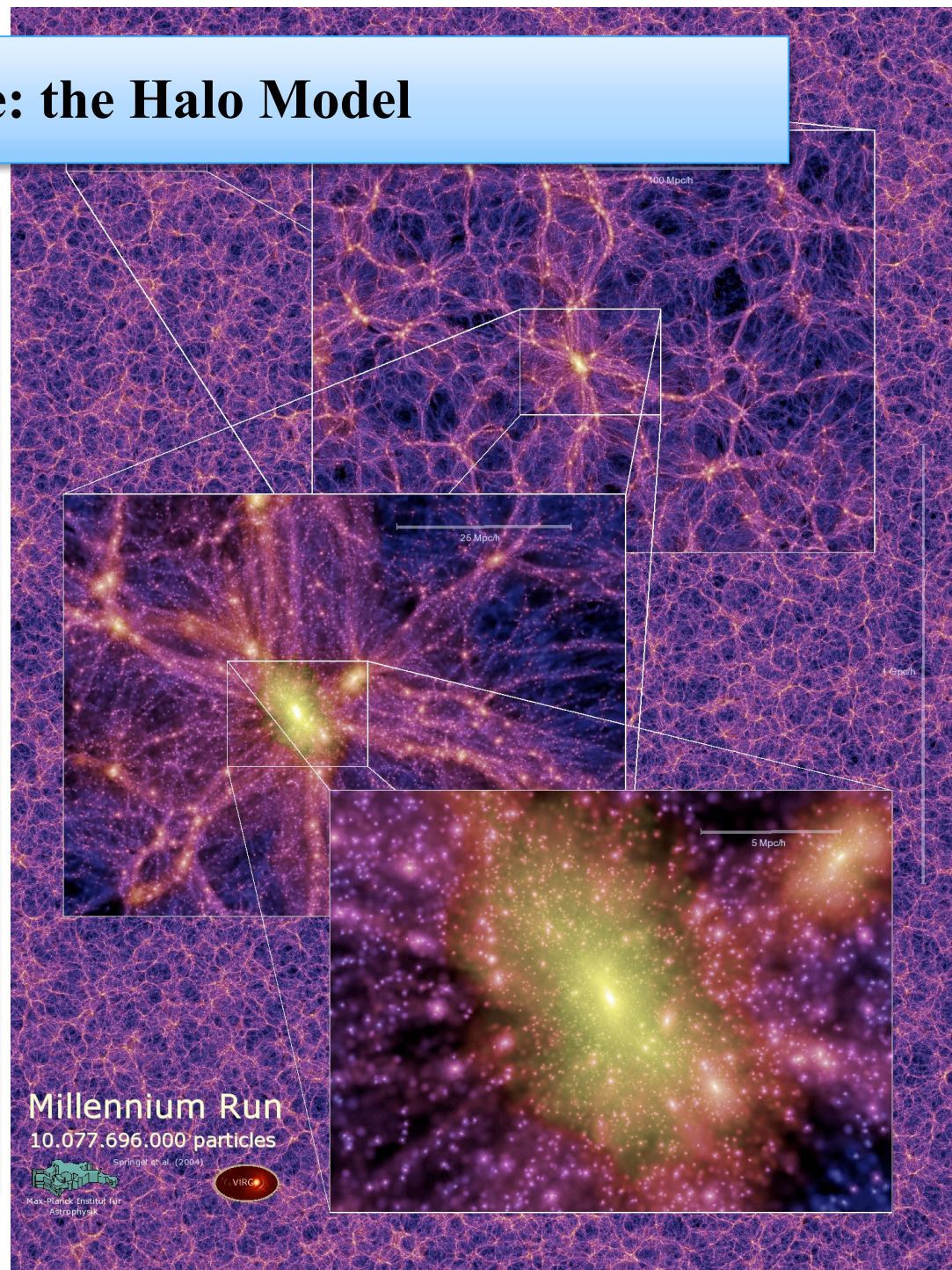
z



From:
Tegmark et al 04

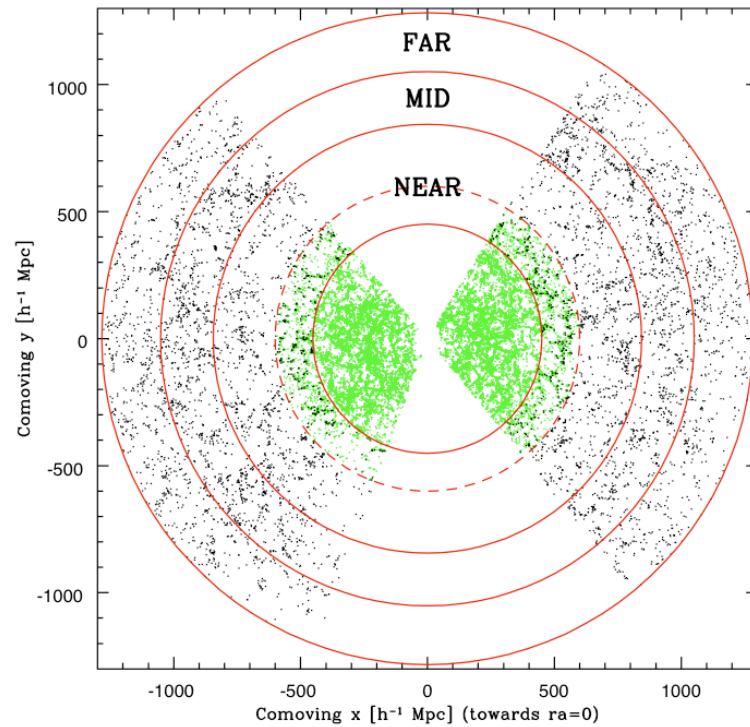
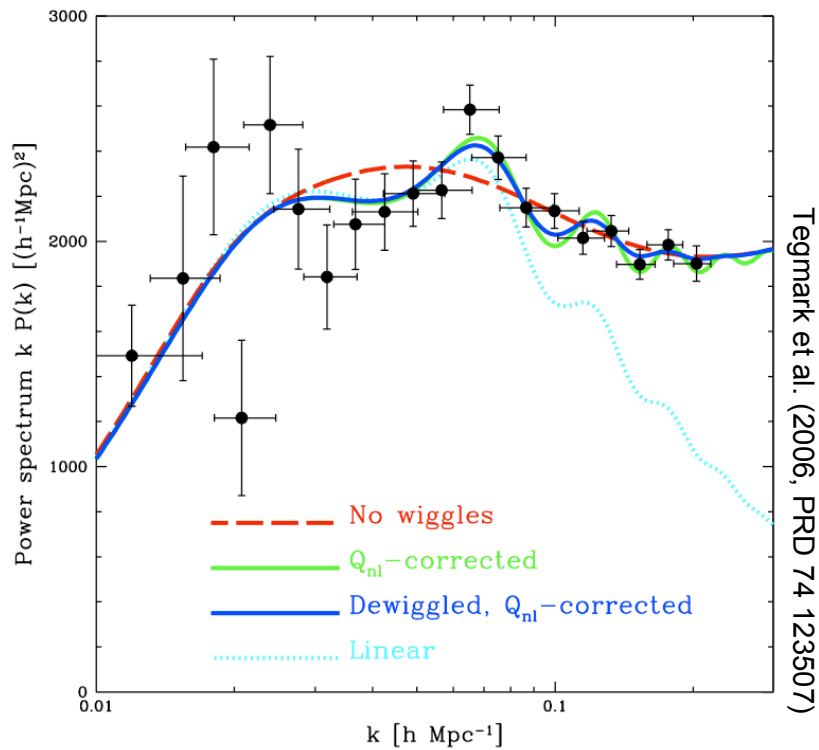
Interlude: the Halo Model

- Galaxy formation from first principles is HARD!
- Linear bias model insufficient!
$$-\delta_{\text{gal}} = b_{\text{gal}} \delta_{\text{m}} \longrightarrow$$
$$P_{\text{gal}}(k) = b_{\text{gal}}^2 P_{\text{m}}(k)$$
- Halo Model Key Assumptions:
 - Galaxies only form/reside in halos
 - N-body simulations can determine the statistical properties of halos
 - Halo mass entirely determines key galaxy properties
- Provides a non-linear, cosmology-dependent model and framework in which to quantify systematic errors



Luminous Red Galaxies

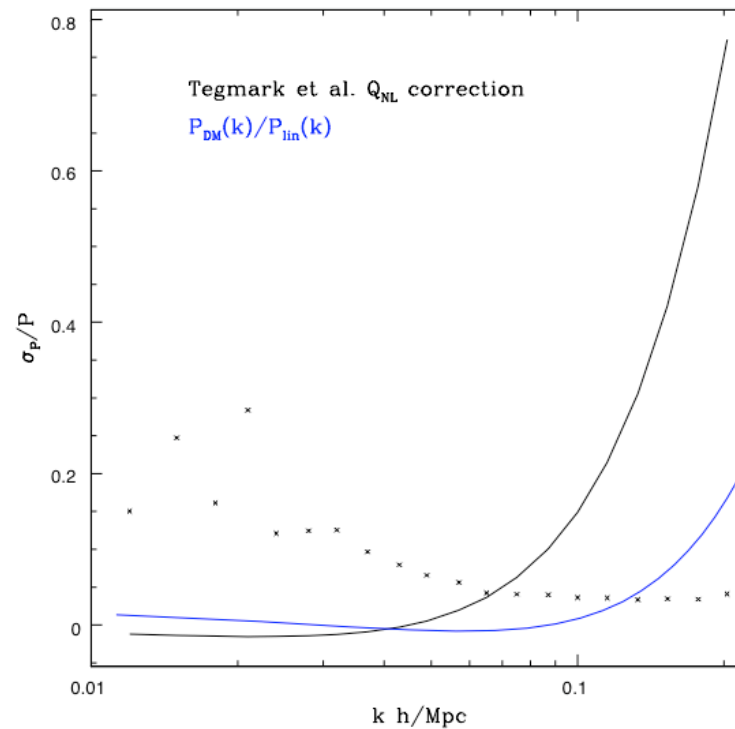
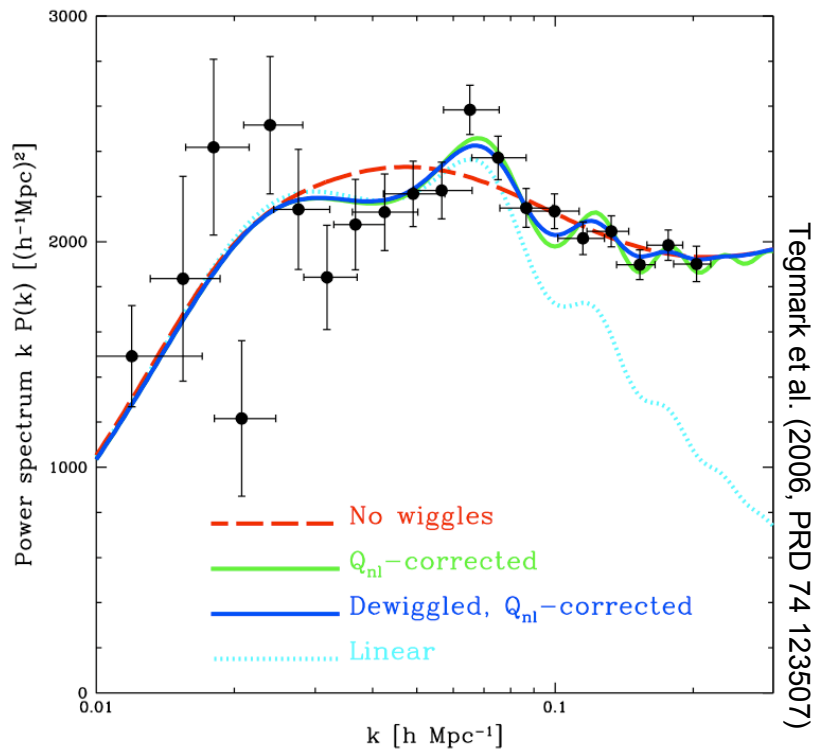
- DR5 analysis: huge deviations from $P_{\text{lin}}(k)$ -- WHY?



Luminous Red Galaxies

- DR5 analysis: huge deviations from $P_{\text{lin}}(k)$ -- WHY?

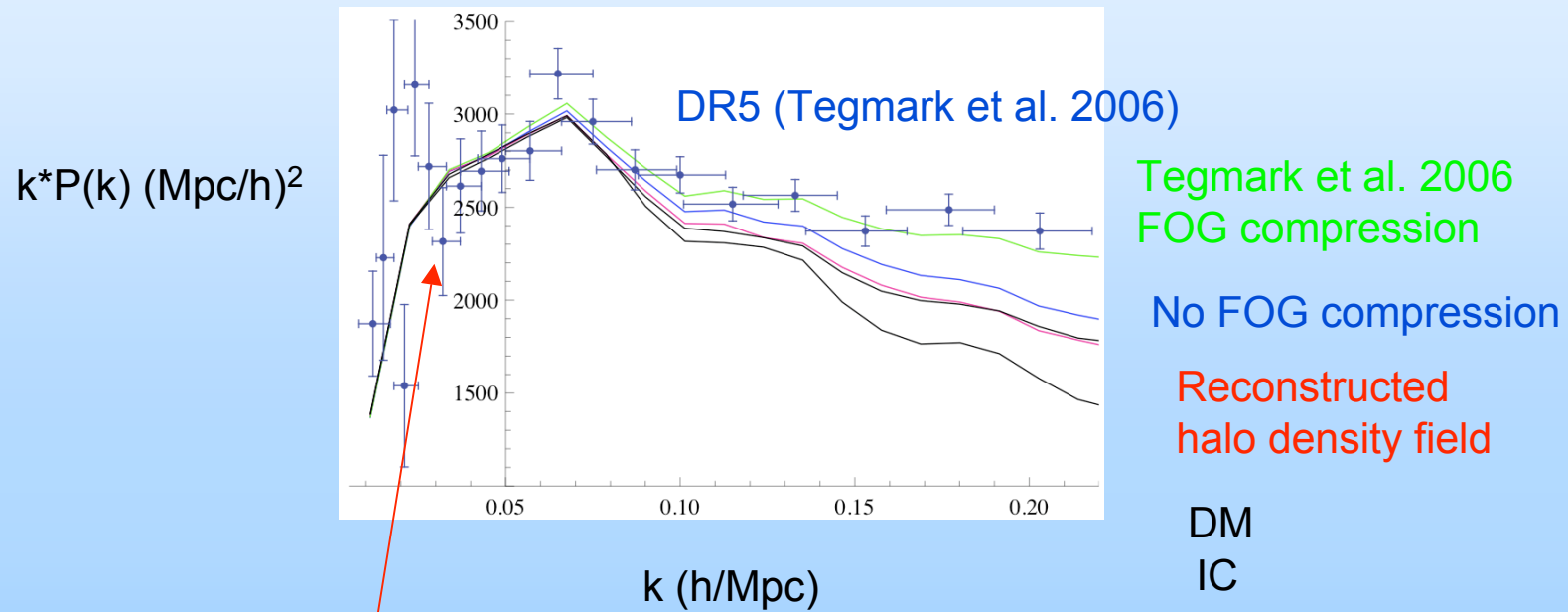
$$P_g(k) = P_{\text{dewiggled}}(k) b^2 \frac{1 + Q_{\text{nl}} k^2}{1 + 1.4k}$$



LRG Non-linearity: Answer in a nutshell

- $n_P \sim 1$ to probe largest effective volume
 - shot noise correction important; on large scales, one-halo pairs contribute an excess shot noise
 - LRGs occupy massive halos $\rightarrow$ large FOG features
- Large non-linear correction can be well-understood as the “one-halo” term after FOG compression, *even though only $\sim 5\%$ of LRGs are satellite galaxies!*
- Impact: Q_{NL} approach biases cosmological parameters and reduces statistical power of the sample

FOG treatment changes $P(k)$ shape!



(Normalized to match
on large scales)

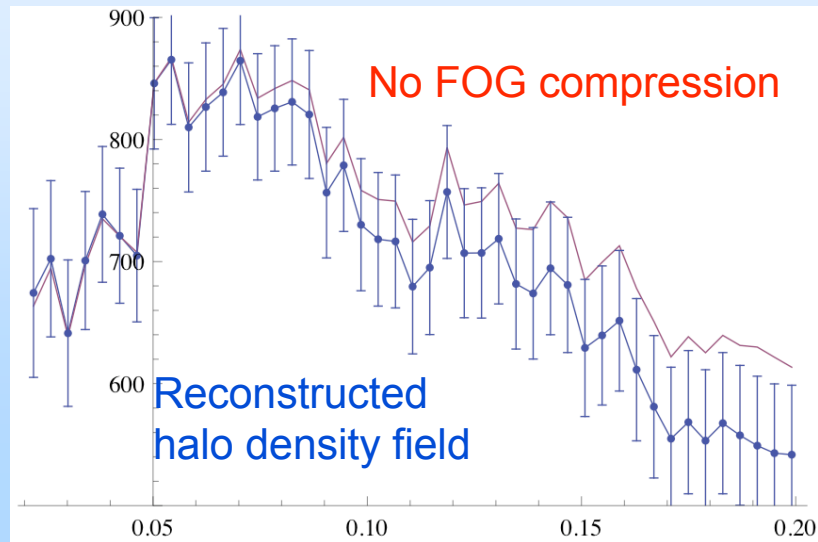
Small deviations from linear theory should be
predictable from small scale power!

Calibrating halo density field reconstruction

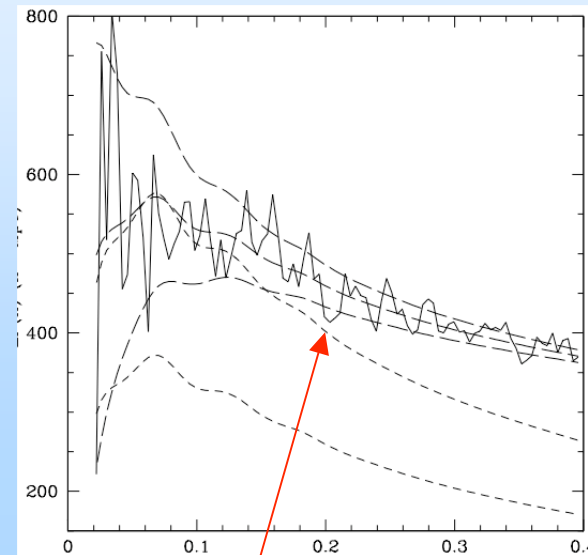
- Basic ideas:
 - constrain galaxy bias on quasi-linear scales from measurements on small scales, where “one-halo” terms dominate
 - n_{LRG} small $\rightarrow$ identify one-halo pairs with fidelity
- CiC group multiplicity function [measures the “one-halo” shot noise]
- Intra-group velocity distribution
- Calibrate errors on high-fidelity mock LRG catalogs
- Removes redshift evolution of $P(k)$ shape

FOG treatment in DR7

$k P(k) \text{ (Mpc/h)}^2$



$\Delta P(k) \text{ (Mpc/h)}^3$



$k \text{ (h/Mpc)}$

Matches mocks + expected excess shot noise from fiber collisions with interlopers

Final model & Systematic Errors

$$P_{halo}(k, \mathbf{p}) = P_{damp}(k, \mathbf{p}) r_{DM,damp}(k, \mathbf{p}) r_{halo,DM}(k, \mathbf{p}_{fid}) F_{nuis}(k)$$

$$F_{nuis}(k) = b_0^2 \left(1 + a_1 \left(\frac{k}{k_\star} \right) + a_2 \left(\frac{k}{k_\star} \right)^2 \right)$$

- This form of $F_{nuis}(k)$ describes
 - excess shot noise
 - slowly varying scale-dependent halo/galaxy bias
 - suppression from intra-halo velocities (**potentially largest systematic**)

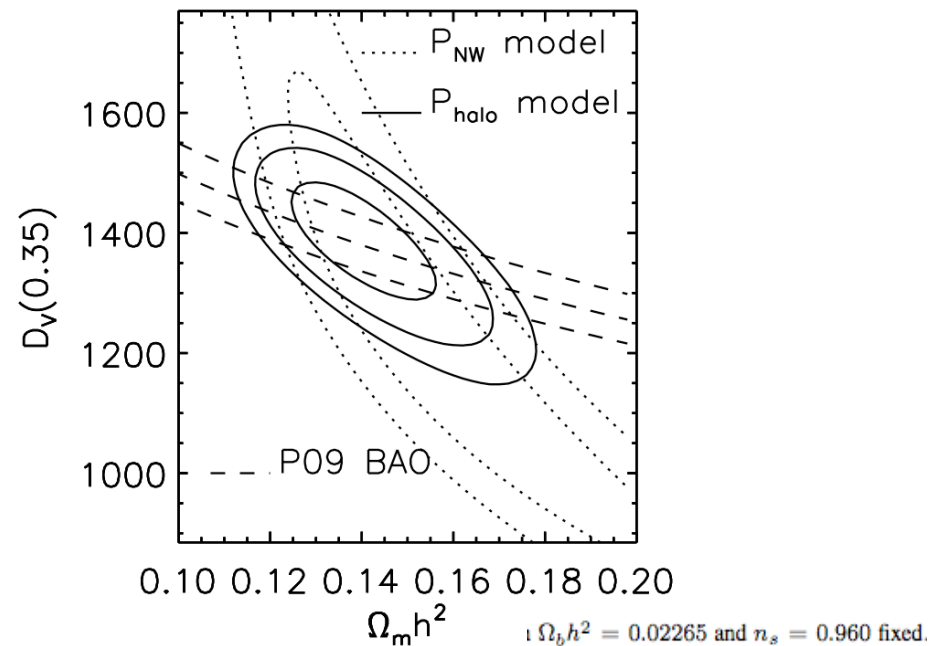
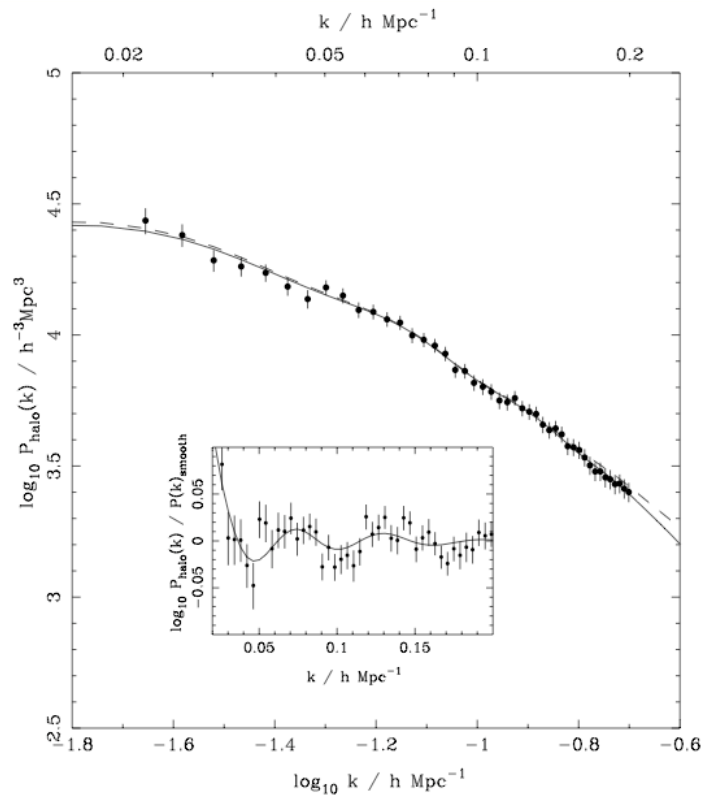
DR7 P(k): What's new?

- Replace uncalibrated FOG compression algorithm with calibrated method to **reconstruct halo density field**
 - Better tracer of underlying matter $P(k)$
- Replace heuristic nonlinear model (Tegmark et al. 2006 DR5) with cosmology-dependent, nonlinear model calibrated on accurate mock catalogs and with better understood, smaller modeling systematics
- What we gain:
 - Increase k_{max} from 0.1 to 0.2 h/Mpc; 8x more modes!
 - Simultaneously constrain k_{eq} and BAO scale
 - Additional leverage on massive neutrino suppression of $P(k)$

$P_{\text{halo}}(k)$ Results

- Constrains turnover ($\Omega_m h^2 D_V$) and BAO scale (r_s/D_V)

$$D_V(z) = \left[(1+z)^2 D_A(z)^2 \frac{cz}{H(z)} \right]^{1/3}$$

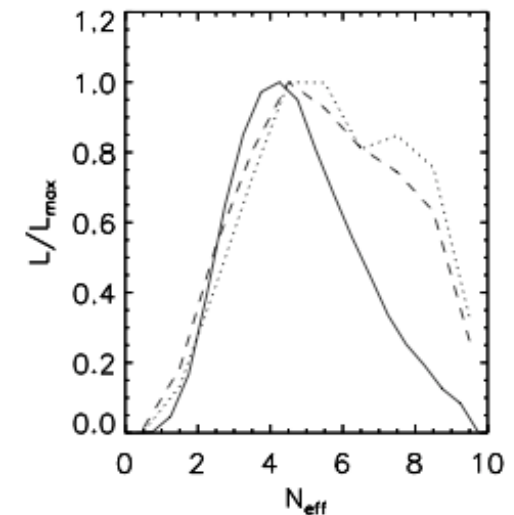
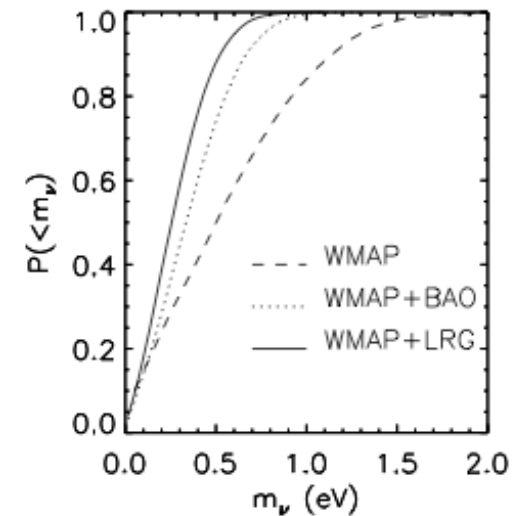


$$\Omega_m h^2 (n_s/0.96)^{1.2} = 0.141 \pm 0.011$$

$$D_V(z=0.35) = 1380 \pm 67 \text{ Mpc}$$

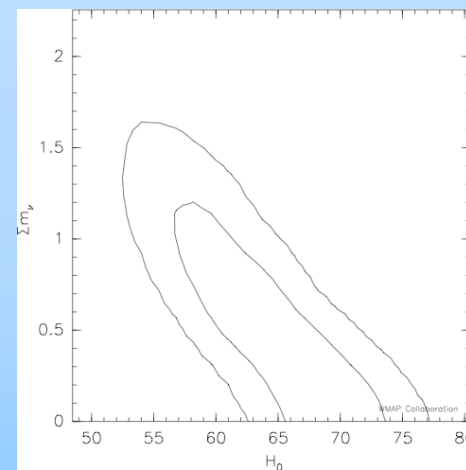
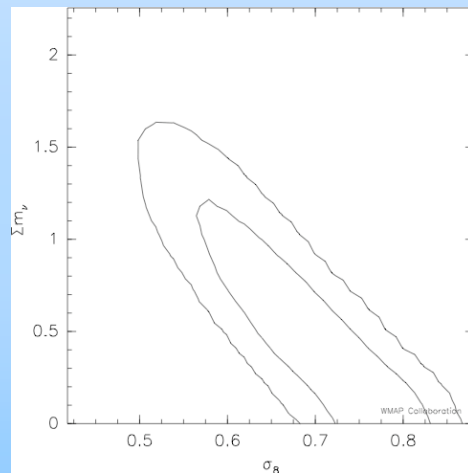
WMAP+ $P_{\text{halo}}(k)$ Constraints: Neutrinos in Λ CDM

- $P_{\text{halo}}(k)$ constraints tighter than P09 BAO-only
- Massive neutrinos suppress $P(k)$
 - WMAP5: $\Sigma m_\nu < 1.3$ eV (95% confidence)
 - WMAP5+LRG: $\Sigma m_\nu < 0.62$ eV
 - WMAP5+BAO: $\Sigma m_\nu < 0.78$ eV
- Effective number of relativistic species N_{rel} alters turnover and BAO scales differently
 - WMAP5: $N_{\text{rel}} = 3.046$ preferred to $N_{\text{rel}} = 0$ with $> 99.5\%$ confidence
 - WMAP5+LRG: $N_{\text{rel}} = 4.8 \pm 1.8$



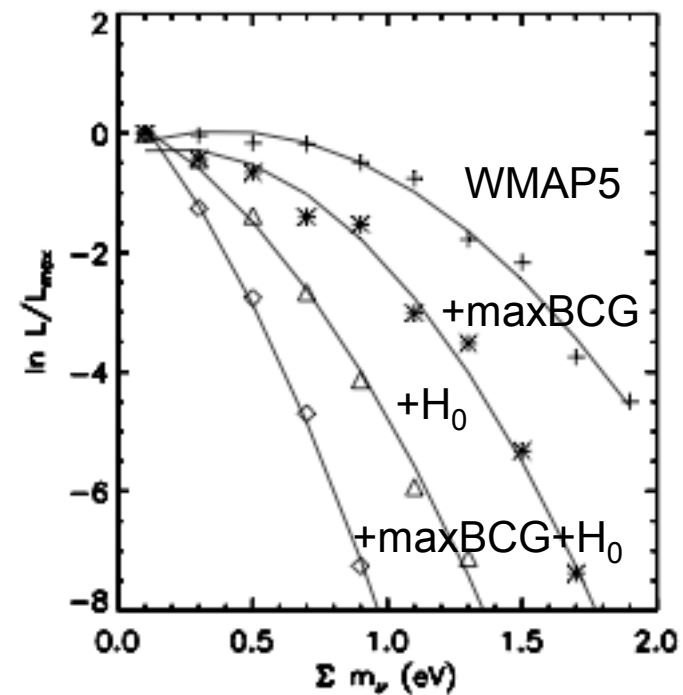
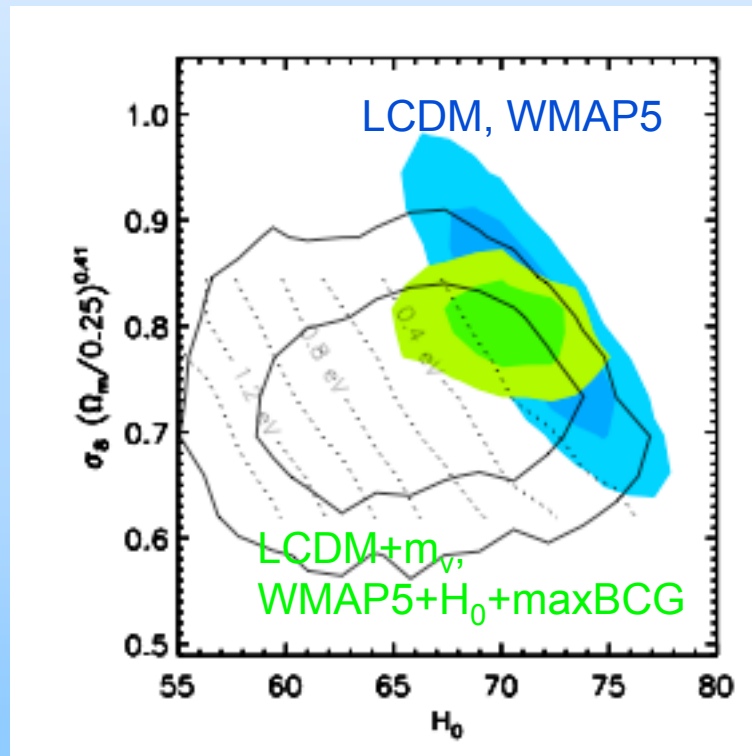
Robust Neutrino Constraints by Combining Low Redshift Observations with the CMB

- WMAP5 presents many constraints as +BAO+SN. Can other low redshift measurements improve neutrino constraints? Yes.
- SDSS maxBCG clusters constrain σ_8 $(\Omega_m/0.25)^{0.41} = 0.832 \pm 0.033$ [Rozo et al. 2009, arXiv:0902.3702]
- New H_0 constraint: 74.2 ± 3.6 km/s/Mpc [Riess et al. 2009, ApJ 699, 539]



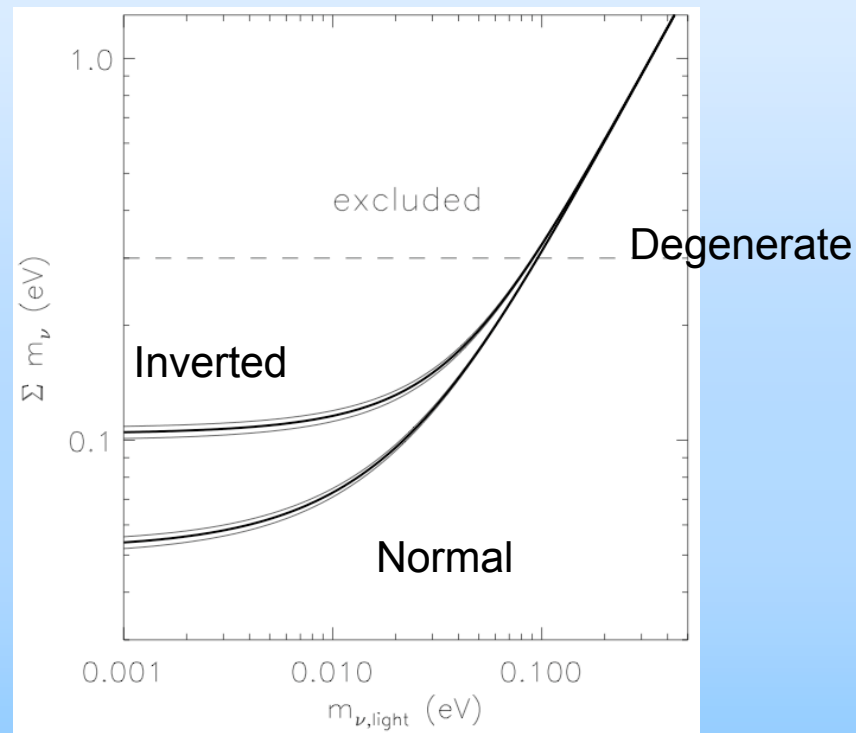
Neutrino Mass

- WMAP5+ H_0 +maxBCG: $\Sigma m_\nu < 0.4$ eV at 95% confidence, even with tensors or running of the spectral index
- Profile likelihood is “independent” of priors; gives comparable results



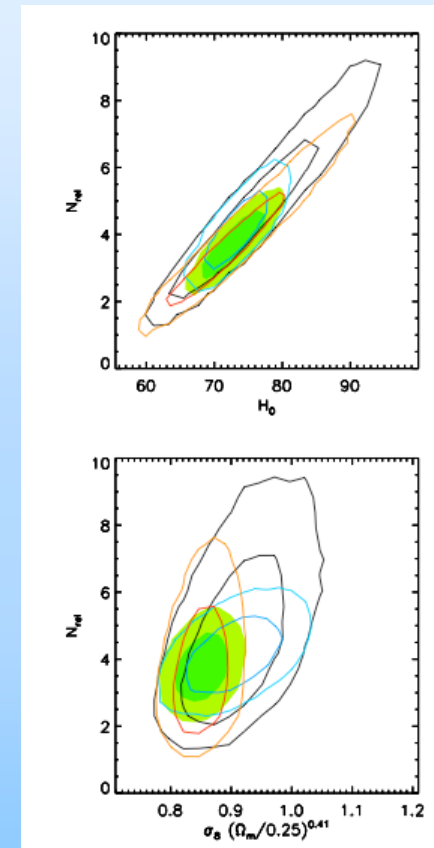
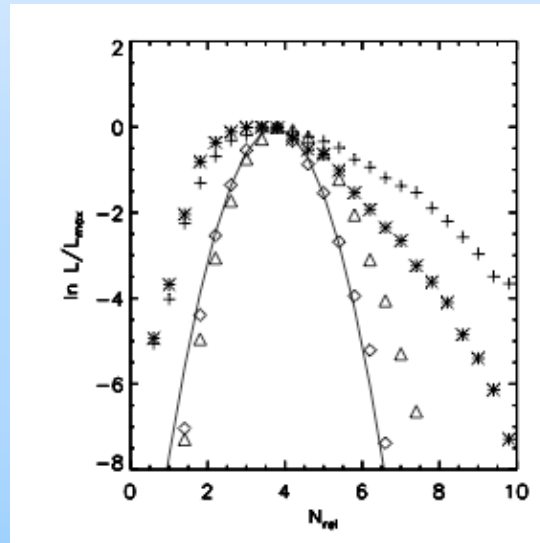
Neutrino Mass -- where do we stand?

- Most optimistically, we are close to ruling out “degenerate” scenario



N_{rel} Results

- $N_{\text{rel}} = 3.7 \pm 0.7$ and profile likelihood becomes Gaussian with WMAP5+ H_0 +maxBCG combination

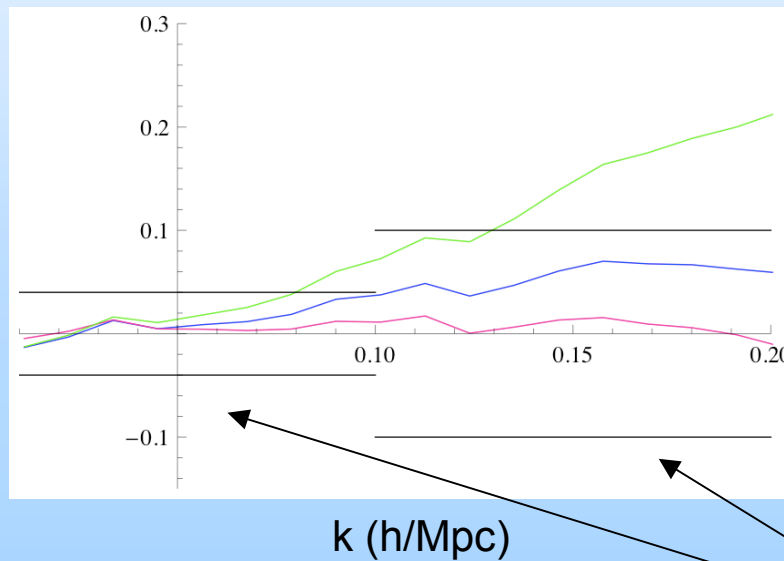


Conclusions

- BAOs provide tightest geometrical constraints
 - consistent with Λ CDM models at 1.1σ when combined with WMAP5
 - improved error analysis, $n(z)$ modeling, etc.
- DR7 $P(k)$ improvement: We use **reconstructed halo density field** in cosmological analysis
 - Halo model provides a framework for quantifying systematic uncertainties
- Result: 8x more modes, improved neutrino constraints compared with BAO-only analysis
- Likelihood code available in new CosmoMC or here:
 - <http://lambda.gsfc.nasa.gov/toolbox/lrgdr/>
- Shape information comes “for free” in a BAO survey!
- Neutrino Constraints substantially improved for data combination WMAP5+ H_0 +maxBCG

FOG treatment changes $P(k)$ shape!

$P(k)/P_{\text{DM}}(k) - 1$



Tegmark et al. 2006
FOG compression

No FOG compression

Reconstructed
halo density field

Systematic error
bounds