

Combining Probes of Large-Scale Structure

Analysis Strategies for the
Precision Cosmology Era

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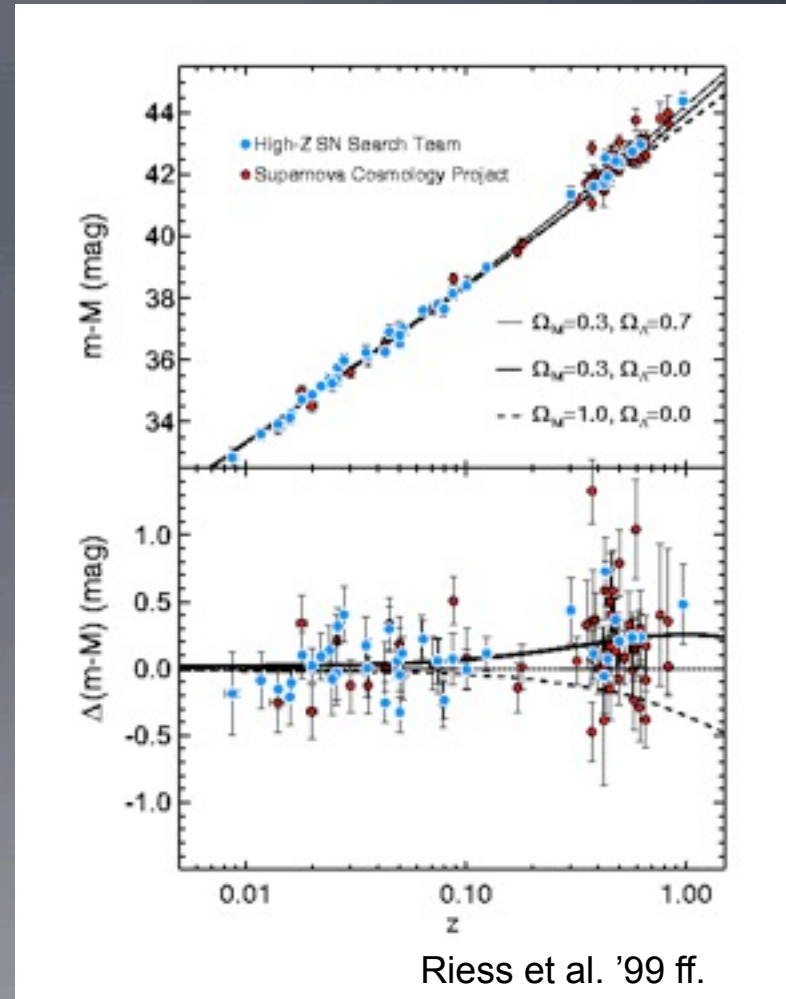
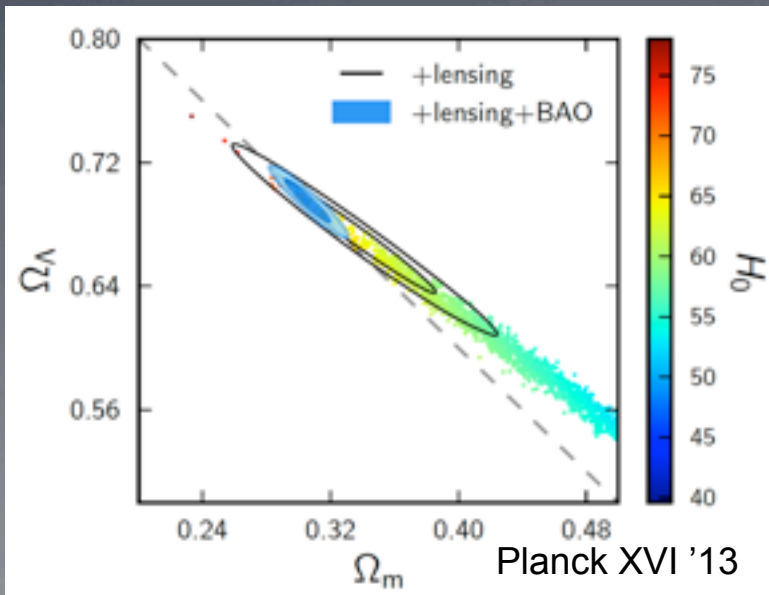
Overview

- **Cosmological constraints from combining probes of large-scale structure (LSS)**
 - focus on challenges of joint analysis
(modeling of individual probes material for many individual talks)
 - CosmoLike software package
 - systematics limited analysis
 - blind analysis strategies

with Tim Eifler, Carlos Cunha, Scott Dodelson, DES collaboration

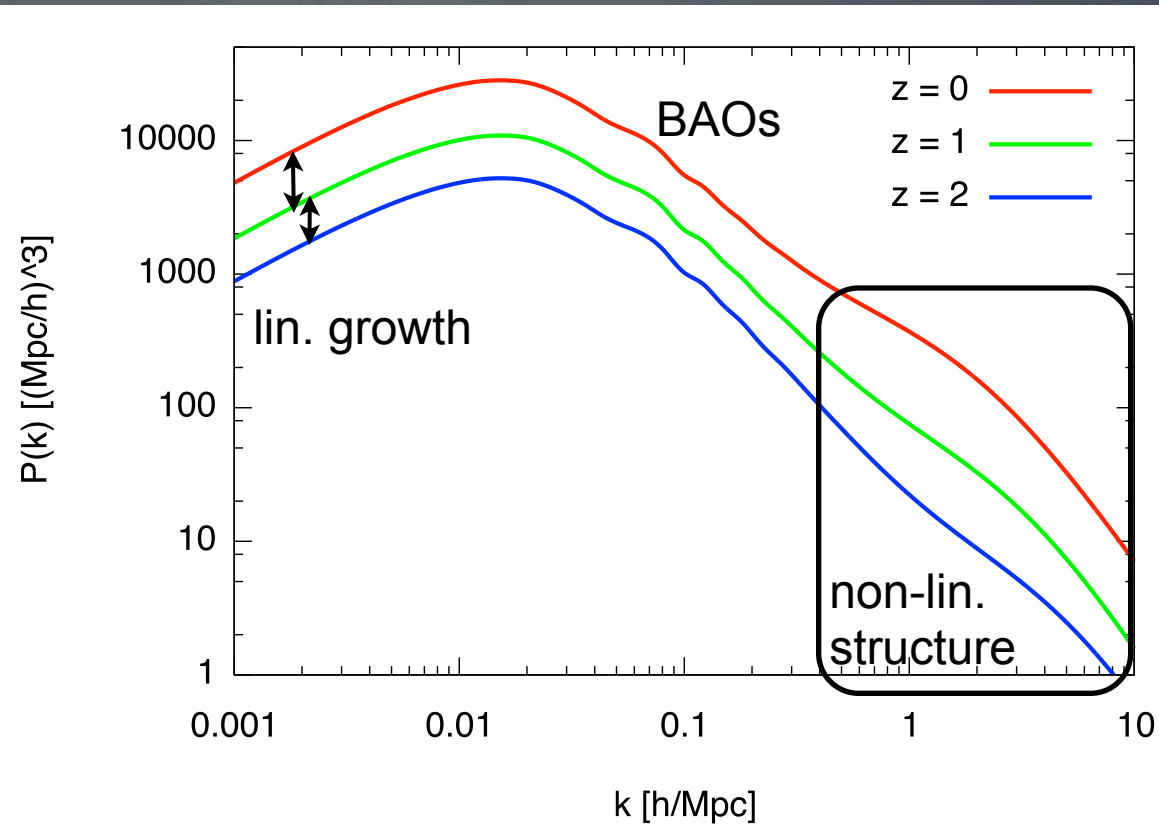
Dark Energy

- first detected with SN surveys
- current constraints (Planck ++): $\Omega_\Lambda \sim 0.7$, equation of state poorly constrained



Dark Energy with LSS

- Dark Energy (modified gravity?) changes expansion rate
- dominates energy density at low redshift, affects
 - distances (standard rulers, - candles),
 - volume elements
 - growth of structure
- LSS ideal probe for late-time evolution



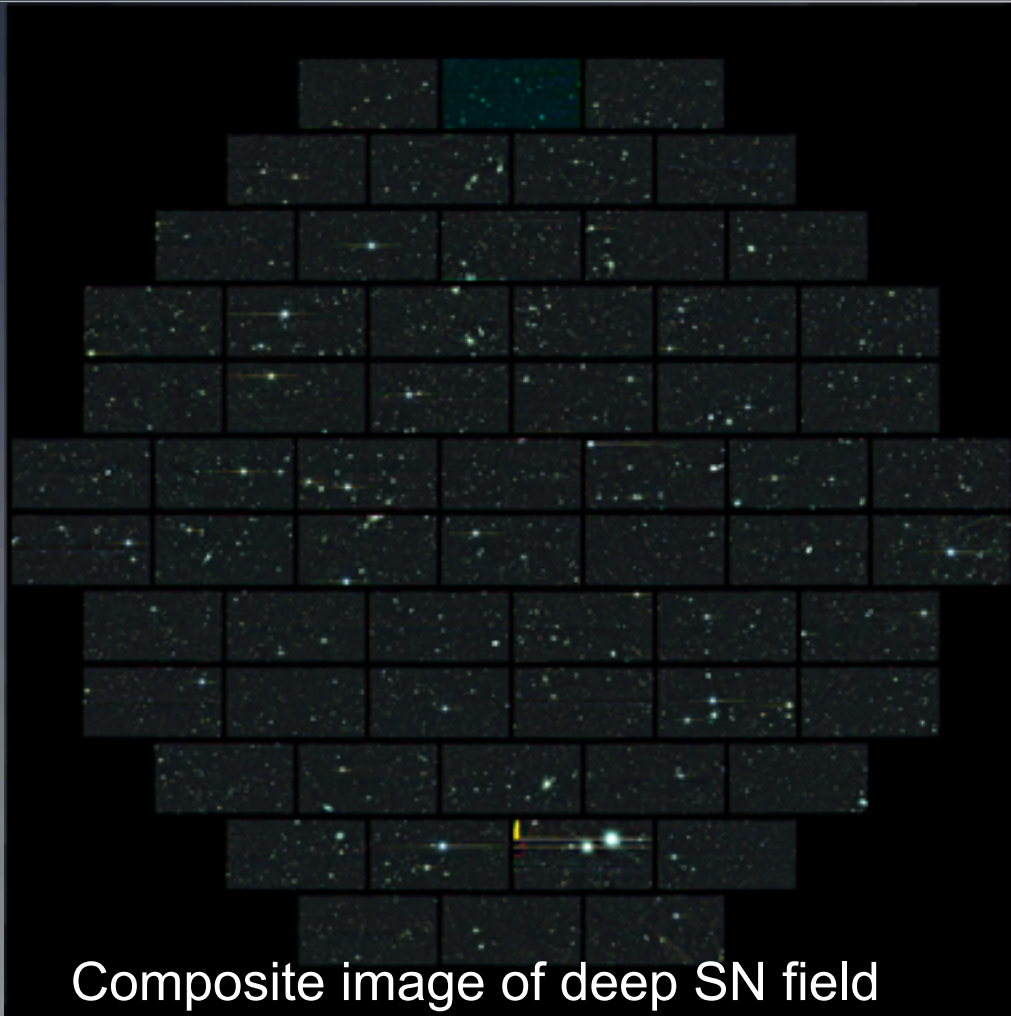
Dark Energy Survey

- **Two multiband imaging surveys:**
 - 300 million galaxies over 1/8 sky
 - 4000 supernovae (time-domain)
- **New 570 Megapixel Dark Energy Camera on the Blanco 4-meter**
Science Verification complete
Survey 2013-2018 (525 nights)
Survey mode started Sept 1!



DECam on the Blanco 4m at NOAO Cerro Tololo InterAmerican Observatory

DECam

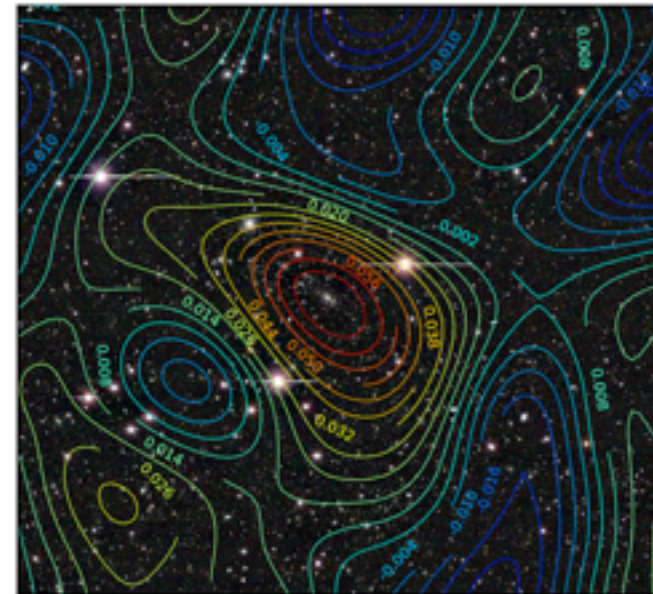
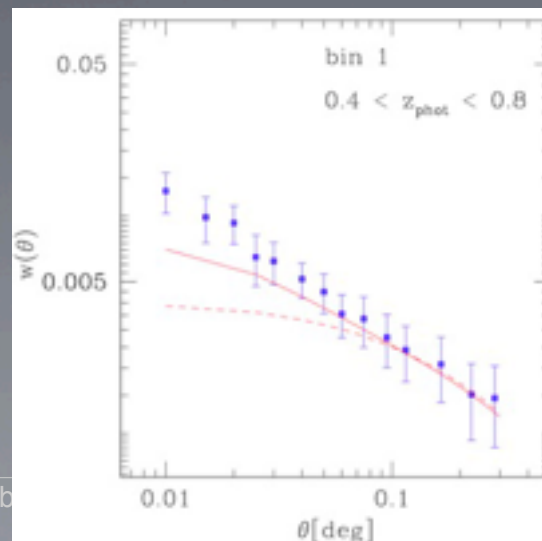
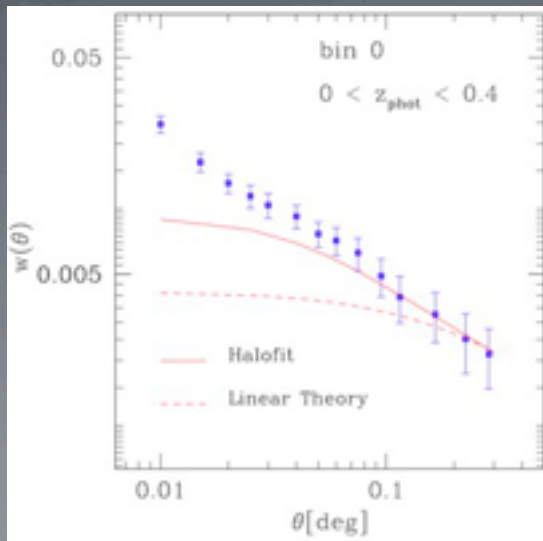


Composite image of deep SN field



Science Verification Data

- 100 sq deg to full depth from science verification
 - detected and confirmed super novae (SN working group)
 - discovered many high- z clusters already (Rozo, Rykoff, et al.)
 - detected galaxy-galaxy lensing (Clampitt, EK + WL group)
 - early clustering measurements (Bauer + LSS group)
- working hard to understand instrument
 - cosmology can wait to year 1 data...



RXJ2238, Melchior et al.

Dark Energy Survey

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 - 300 million galaxies over 1/8 sky
 - 4000 supernovae (time-domain)
- **New 570 Megapixel Dark Energy Camera on the Blanco 4-meter**
Science Verification complete
Survey 2013-2018 (525 nights)
- **Stage III Survey using 4 complementary techniques:**
 - I. Galaxy Clusters
 - II. Weak Gravitational Lensing
 - III. Galaxy Clustering
 - IV. Supernovae

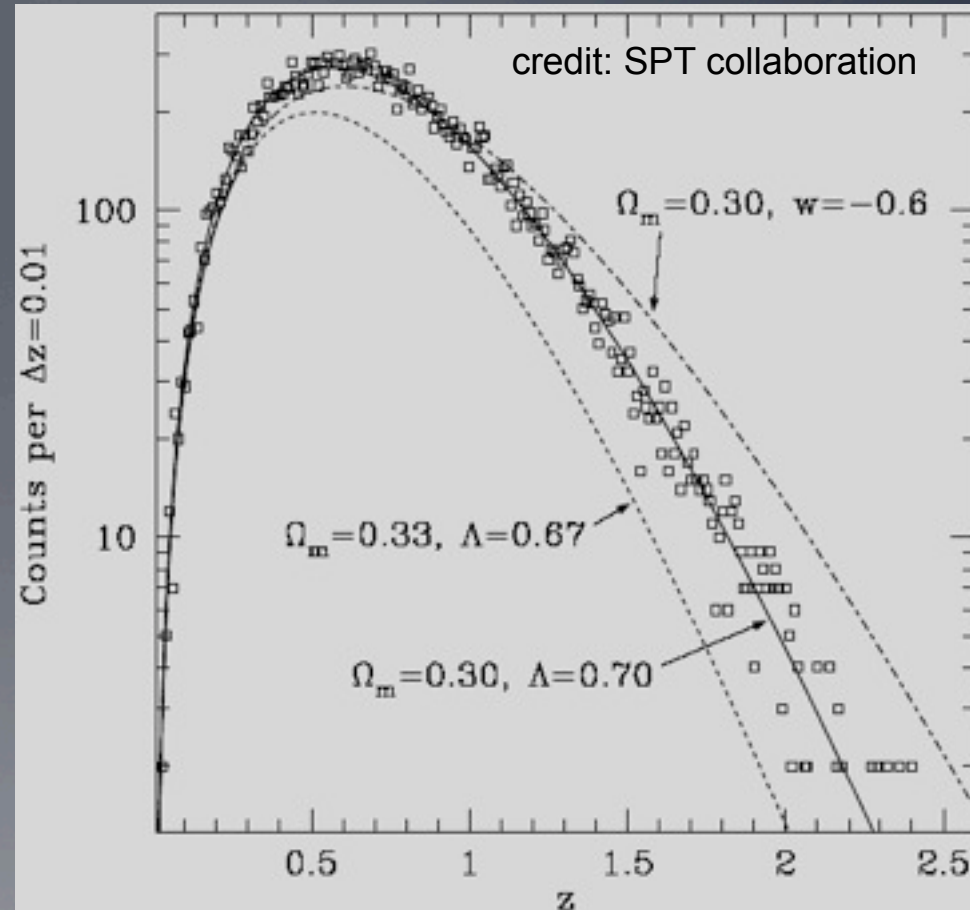


DECam on the Blanco 4m at NOAO Cerro Tololo InterAmerican Observatory

LSS Probes of Dark Energy I

Galaxy Clusters

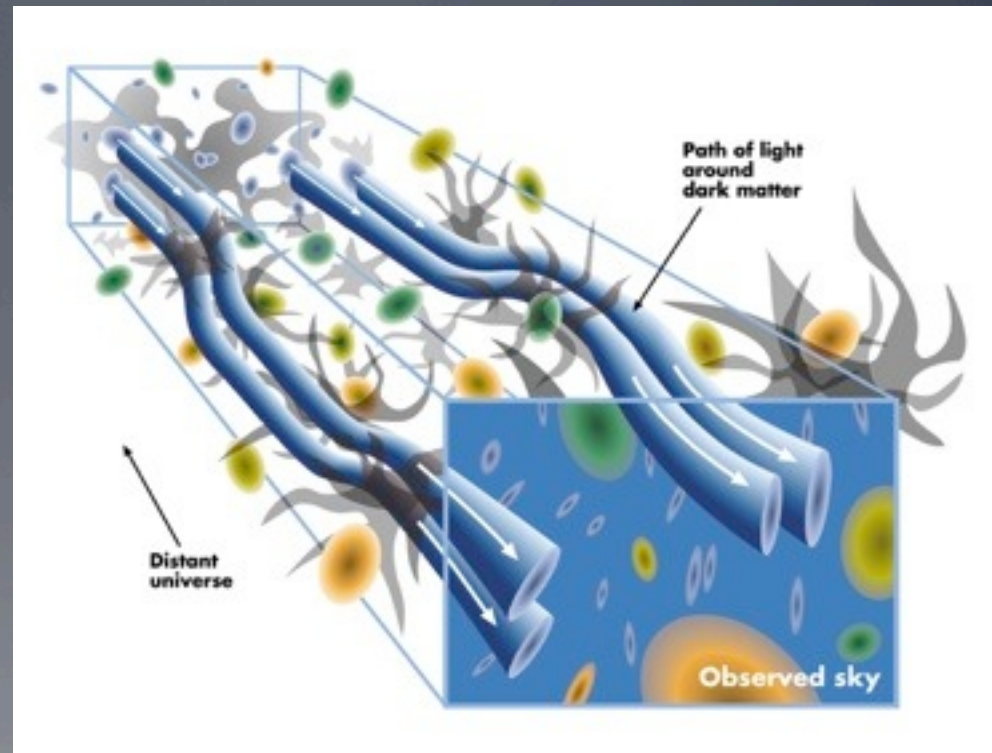
- measure number counts (+ clustering)
 - growth of structure, expansion history
- DES: 100,000 clusters to $z \sim 1$
- overlap with SPT



LSS Probes of Dark Energy II

Weak Gravitational Lensing

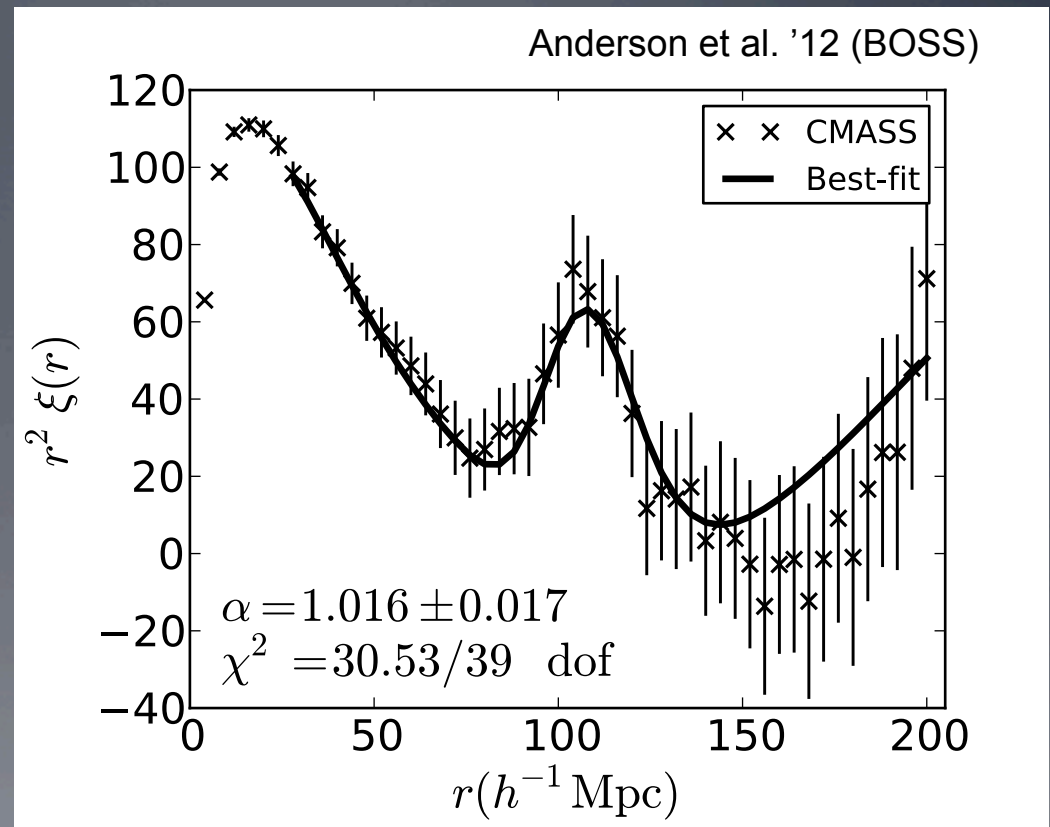
- Light deflected by tidal field of LSS
- Coherent distortion of galaxy shapes (“shear”)
- Shear statistically related to (projected) matter distribution
→ growth of structure, expansion history
- **DES: shapes of 200 million galaxies**



LSS Probes of Dark Energy III

Galaxy Clustering

- measure BAOs + shape of correlation function
→ growth of structure, expansion history
- DES: 300 million galaxies to $z \sim 1.5$

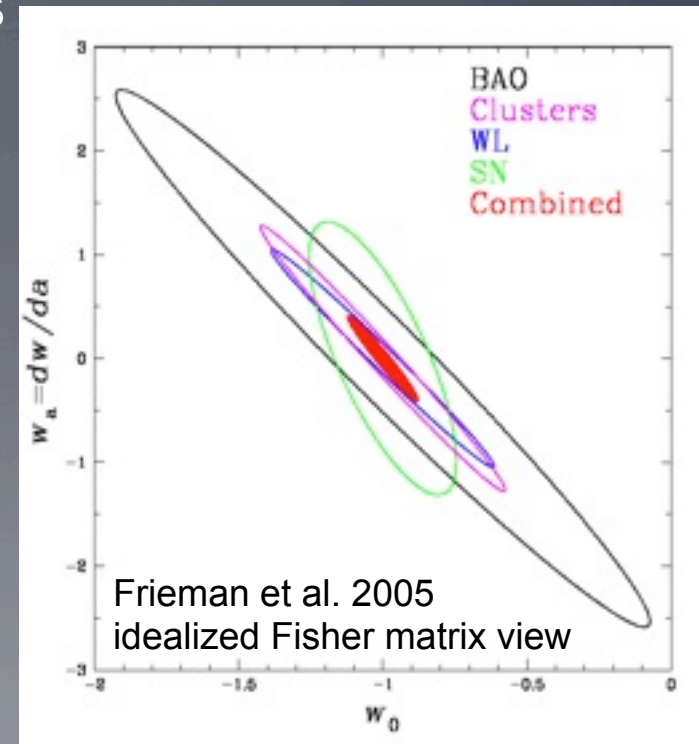


Combining Probes

- Clusters, WL, BAO probe different aspects of structure formation, subject to different systematics
- Combining them improves constraints

But...

- Probe same underlying density field, correlated information
- Shared systematics
- Combining posterior distributions not sufficient, joint analysis required



Joint Likelihood Analysis

likelihood function

number counts: Poisson
2PCF: ~ Gaussian (?)
*improvements needed
for stage IV*

model data vector

self-consistent modeling of all observables
matter power spectrum, halo mass + bias function
+ *selection function, systematics*

$$p(\boldsymbol{\pi} | \hat{\mathbf{d}}) = p(\boldsymbol{\pi}) \mathcal{L}(\hat{\mathbf{d}} | \mathbf{d}(\boldsymbol{\pi}), \mathbf{C})$$

combined data vector

priors

parameters

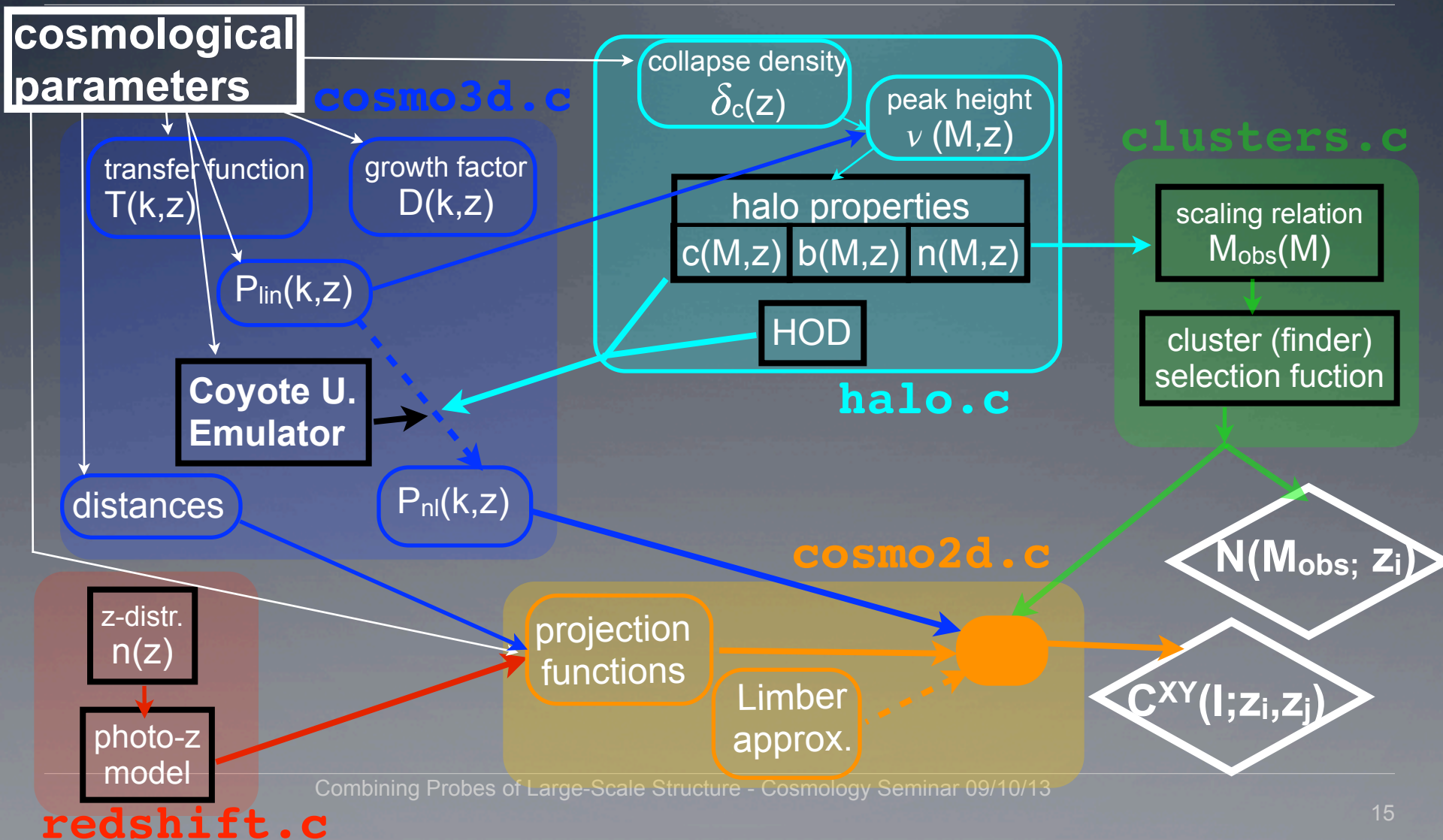
joint covariance

large and complicated,
non-(block) diagonal matrix

Introducing CosmoLike

- Likelihood library for combined probes analyses
 - cosmic shear, galaxy-galaxy lensing, galaxy clustering, cluster abundance + mass self-calibration, CMB cross-correlations
 - covariances, model data vectors including systematic effects
 - optimized for high-dimensional likelihood analyses
- Integrated in DES pipeline, public release in late 2013

CosmoLike: Model Data Vector



Combined Data Vector

- Consider number counts (N), two-point statistics (cosmic shear $\langle \kappa \kappa \rangle$, g-g lensing $\langle \delta \kappa \rangle$, clustering $\langle \delta \delta \rangle$, etc.)

- Number of observables:

Cluster counts	5 richness bins x 5 z-bins	= 25
Cluster lensing	5 x 5 x (source-z bins) x 20 radial bins	> 1000
Cluster clustering	5 x 5 x 20 radial bins	= 250
Galaxy clustering	5 z-bins x 20 radial bins x type bins	> 200
Shear/g-g lensing	2 x 20 radial bins x tomography	~ 1000

→ $n > 2000!$

Joint *Inverse* Covariance

- correlated noise makes inversion difficult
- covariance estimate from data/simulations requires thousands of representative patches N_p

$$\widehat{C}^{-1} \approx \left[1 - \frac{n}{N_p} \right] (\hat{C})^{-1}, \text{ inflates contours}$$

- at least $n + 2$ *independent* realizations

General Covariance Structure

- Consider number counts (N), two-point statistics (e.g., shear $\langle \kappa \kappa \rangle$, g-g lensing $\langle \delta \kappa \rangle$, clustering $\langle \delta \delta \rangle$)

	N	$\langle \delta \delta \rangle$	$\langle \delta \kappa \rangle$	$\langle \kappa \kappa \rangle$
N	Cov (N, N)	Cov ($\langle \delta \delta \rangle, N$)	Cov ($\langle \delta \kappa \rangle, N$)	Cov ($\langle \kappa \kappa \rangle, N$)
$\langle \delta \delta \rangle$	Cov ($\langle \delta \delta \rangle, N$)	Cov ($\langle \delta \delta \rangle, \langle \delta \delta \rangle$)	Cov ($\langle \delta \delta \rangle, \langle \delta \kappa \rangle$)	Cov ($\langle \delta \delta \rangle, \langle \kappa \kappa \rangle$)
$\langle \delta \kappa \rangle$	Cov ($\langle \delta \kappa \rangle, N$)	Cov ($\langle \delta \kappa \rangle, \langle \delta \delta \rangle$)	Cov ($\langle \delta \kappa \rangle, \langle \delta \kappa \rangle$)	Cov ($\langle \delta \kappa \rangle, \langle \kappa \kappa \rangle$)
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General Covariance Structure

- $\text{Cov}(N, N)$: Cluster number counts covariance
 Poisson error + sample variance \rightarrow power spectrum
 (e.g., Lima & Hu '04, Takada & Bridle '07)

	N	$\langle \delta\delta \rangle$	$\langle \delta\kappa \rangle$	$\langle \kappa\kappa \rangle$
N	$\text{Cov}(N, N)$	$\text{Cov}(\langle \delta\delta \rangle, N)$	$\text{Cov}(\langle \delta\kappa \rangle, N)$	$\text{Cov}(\langle \kappa\kappa \rangle, N)$
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General Covariance Structure

- **Cov ($\langle\delta\delta\rangle$, N)**: Covariance of cluster abundance + 2pt statistic of (projected) density field \rightarrow power spectrum, bispectrum (Takada & Bridle '07)
- **Cov (N, N)**: power spectrum

	N	$\langle\delta\delta\rangle$	$\langle\delta\kappa\rangle$	$\langle\kappa\kappa\rangle$
N	Cov (N, N)	Cov ($\langle\delta\delta\rangle, N$)	Cov ($\langle\delta\kappa\rangle, N$)	Cov ($\langle\kappa\kappa\rangle, N$)
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General Covariance Structure

- **Cov ($\langle \delta\delta \rangle$, $\langle \delta\delta \rangle$), etc.:** Covariance of (different) 2pt statistics of (projected) density field

$$\text{Cov}(P(\mathbf{k}_1), P(\mathbf{k}_2)) \approx \underbrace{\frac{2\delta_D(\mathbf{k}_1 + \mathbf{k}_2)}{N_{k_1}} P^2(k_1)}_{\text{Gaussian cosmic variance}} + \underbrace{\frac{\bar{T}(k_1, k_2)}{V_s}}_{\text{non-Gaussian c.v.}} + \underbrace{\frac{\partial P(k_1)}{\partial \rho_L} \frac{\partial P(k_2)}{\partial \rho_L} \sigma^2(\rho_L)}_{\text{sample variance}}$$

- **Cov ($\langle \delta\delta \rangle$, N):** bispectrum, power spectrum
- **Cov (N, N):** power spectrum

	N	$\langle \delta\delta \rangle$	$\langle \delta\kappa \rangle$	$\langle \kappa\kappa \rangle$
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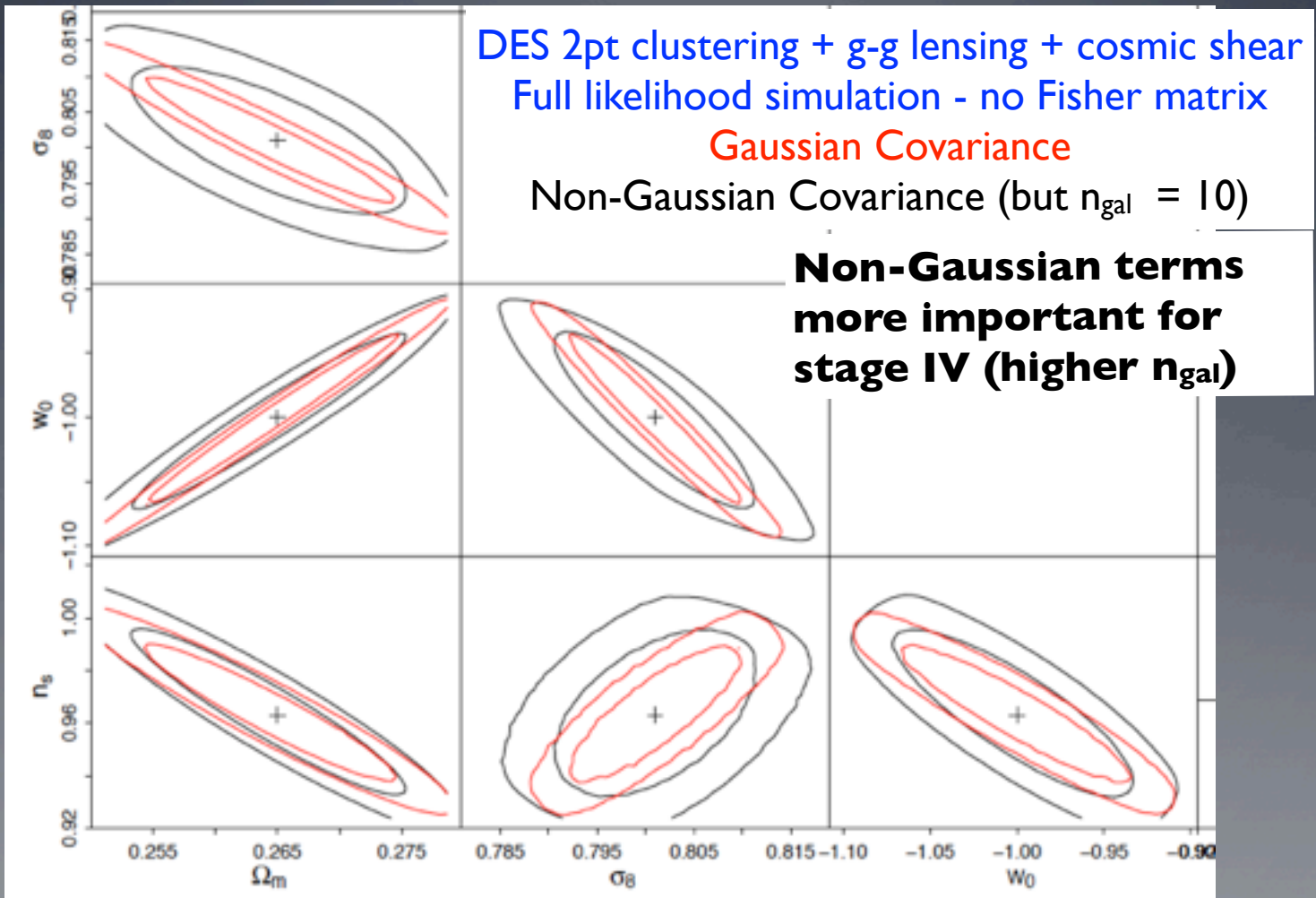
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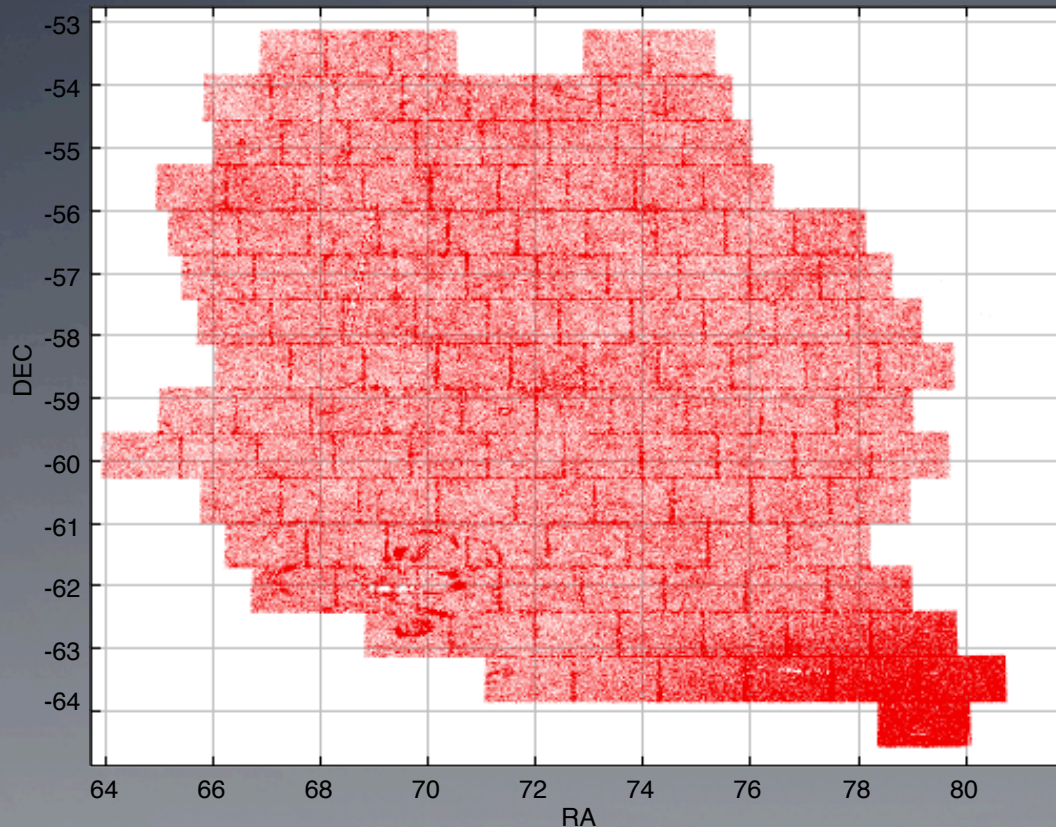
- at least $n + 2$ *independent* realizations
- in practice, combine theoretical templates with matrix regularization
 - for DES, $\mathcal{O}(25)$ simulated realizations sufficient for combined probes covariance

Impact of Non-G. Covariance



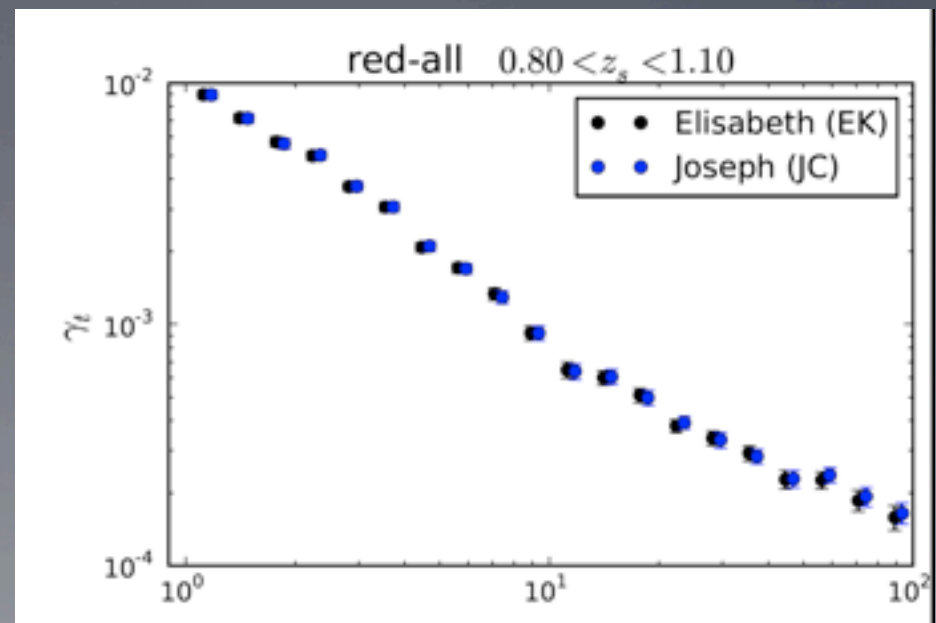
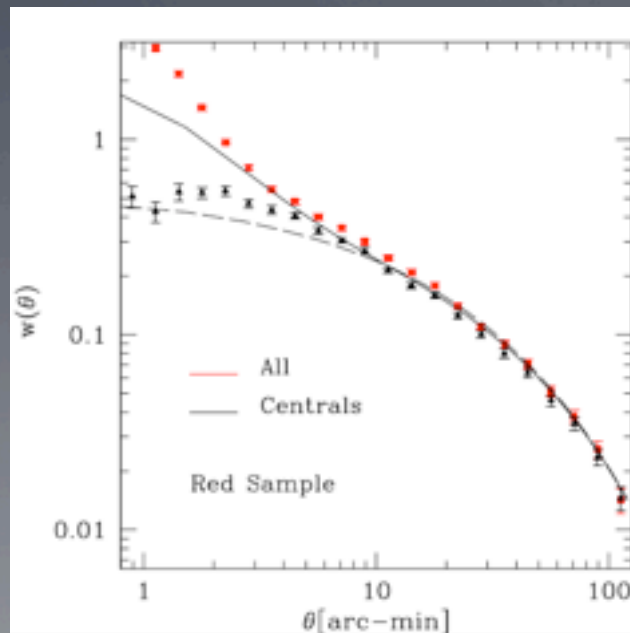
CosmoLike: Applications

- model SPT lensing x DES (galaxies, shear)
 - expect detection in SV data already - catalog cleaning underway...



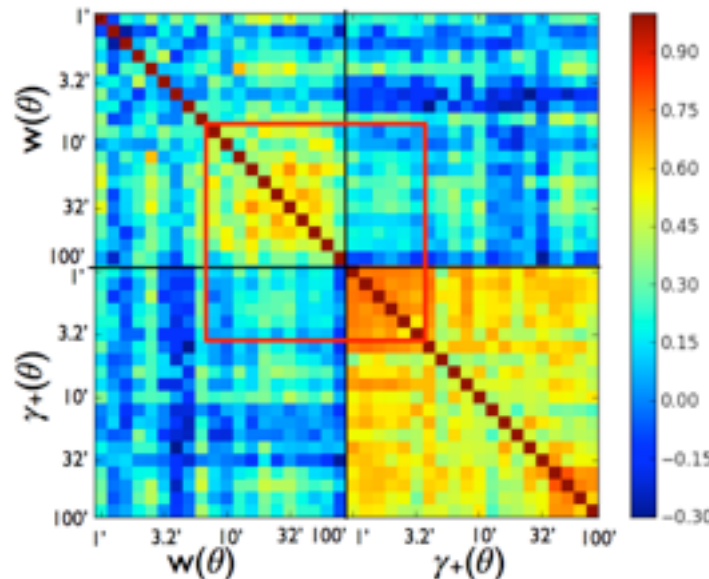
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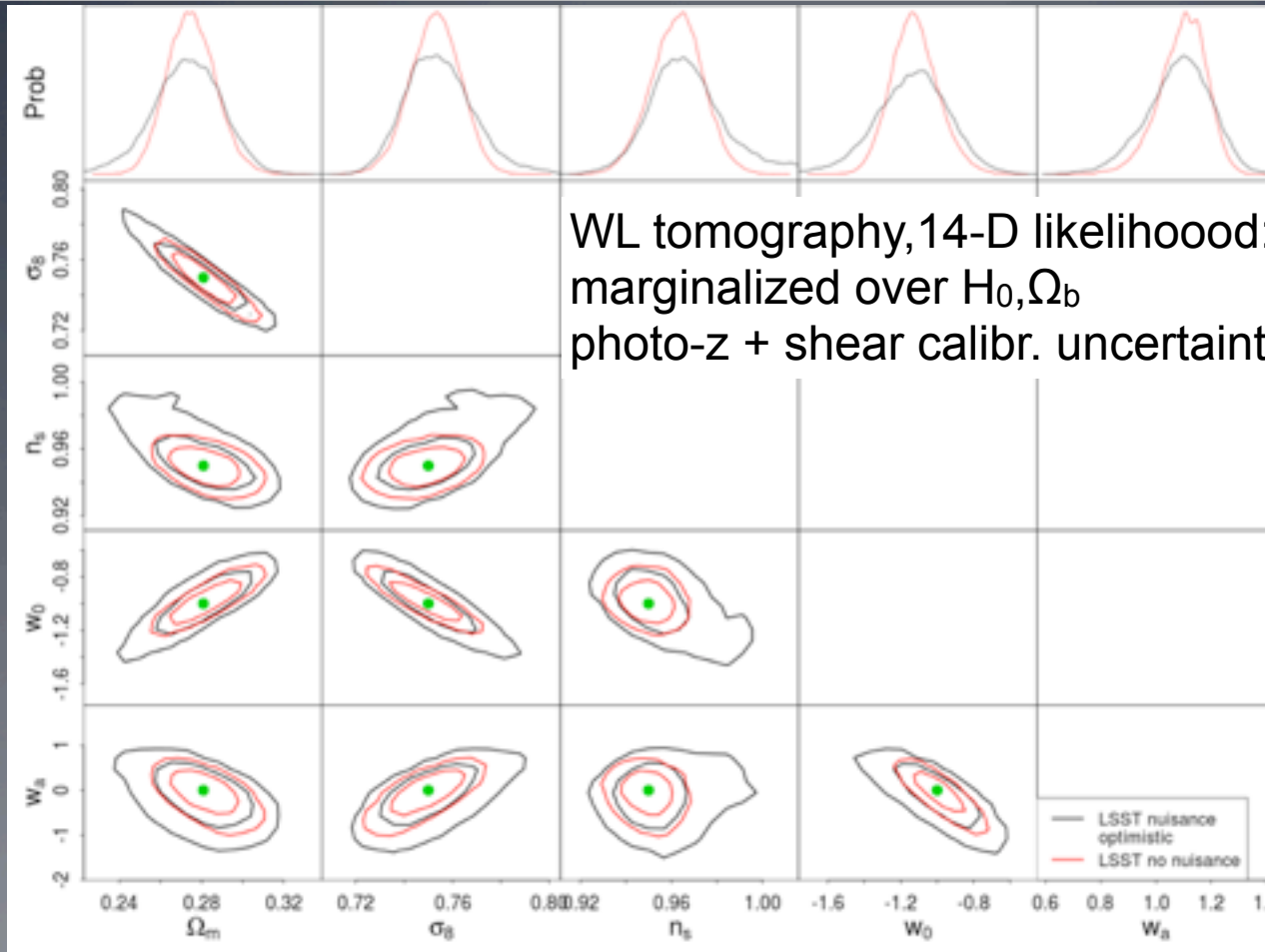
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 - which scales to include? (Yoo & Seljak '12, everything,...?)



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 - tests on DES mocks (EK, Clampitt, Crocce, et al.)
 - which scales to include? (Yoo & Seljak '12, everything,...?)
- explore parameter space of systematic effects:
 - large survey volume, “precision cosmology”
 - limited by systematic uncertainties

Impact of Systematics



EK, Eifler et al. in prep.

Nuisance Parameters

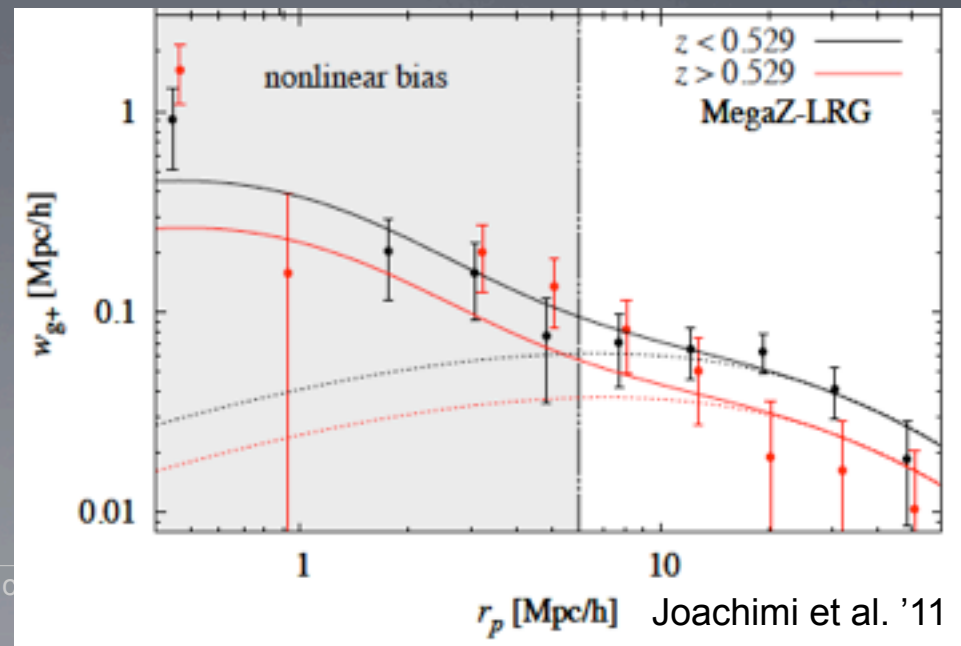
- large survey volume, “precision cosmology”
 - limited by systematic uncertainties
- easy to come up with many parameters
 - galaxy bias: e.g., 5 HOD + b_2 per bin
 - mass - observable relation for clusters
 - 2-3 parameters (mean relation) + scatter parameters, per bin
 - shear calibration, photo-z uncertainties, ...
 - Σ (poll among DES working groups) \sim 500-1000 parameters
- self-calibration + marginalization
 - can be costly (computationally, constraining power)

Combined Probes Approach

- specify data vector (probes included)
- identify (+prioritize) systematic effects
 - find suitable (minimal sets of) parameterizations + limits
 - joint systematics hardest
- possible constraints on nuisance parameters
 - independent observations
 - other observables from same data set
 - split data set
- combine theory, simulations & observations to reduce limits (priors) on nuisance parameters

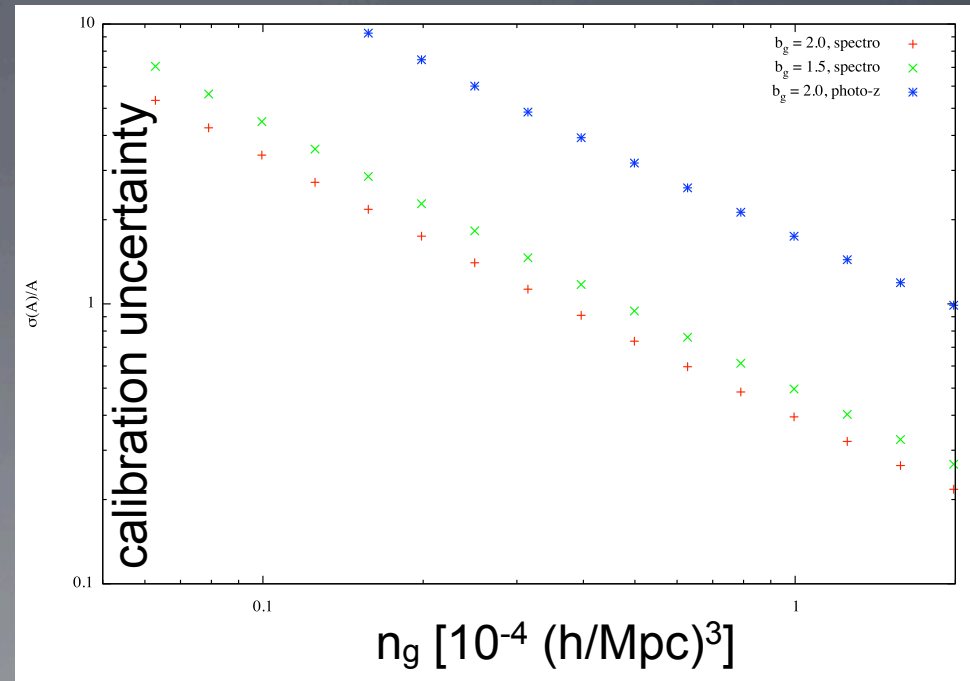
Intrinsic Alignment Calibration

- tidal alignment of galaxies key contaminant for WL
- measured directly with position - shape correlation of low-z galaxies
 - use these observations to calibrate models (Hirata et al. '07, Mandelbaum et al. '11, Joachimi et al. '12)



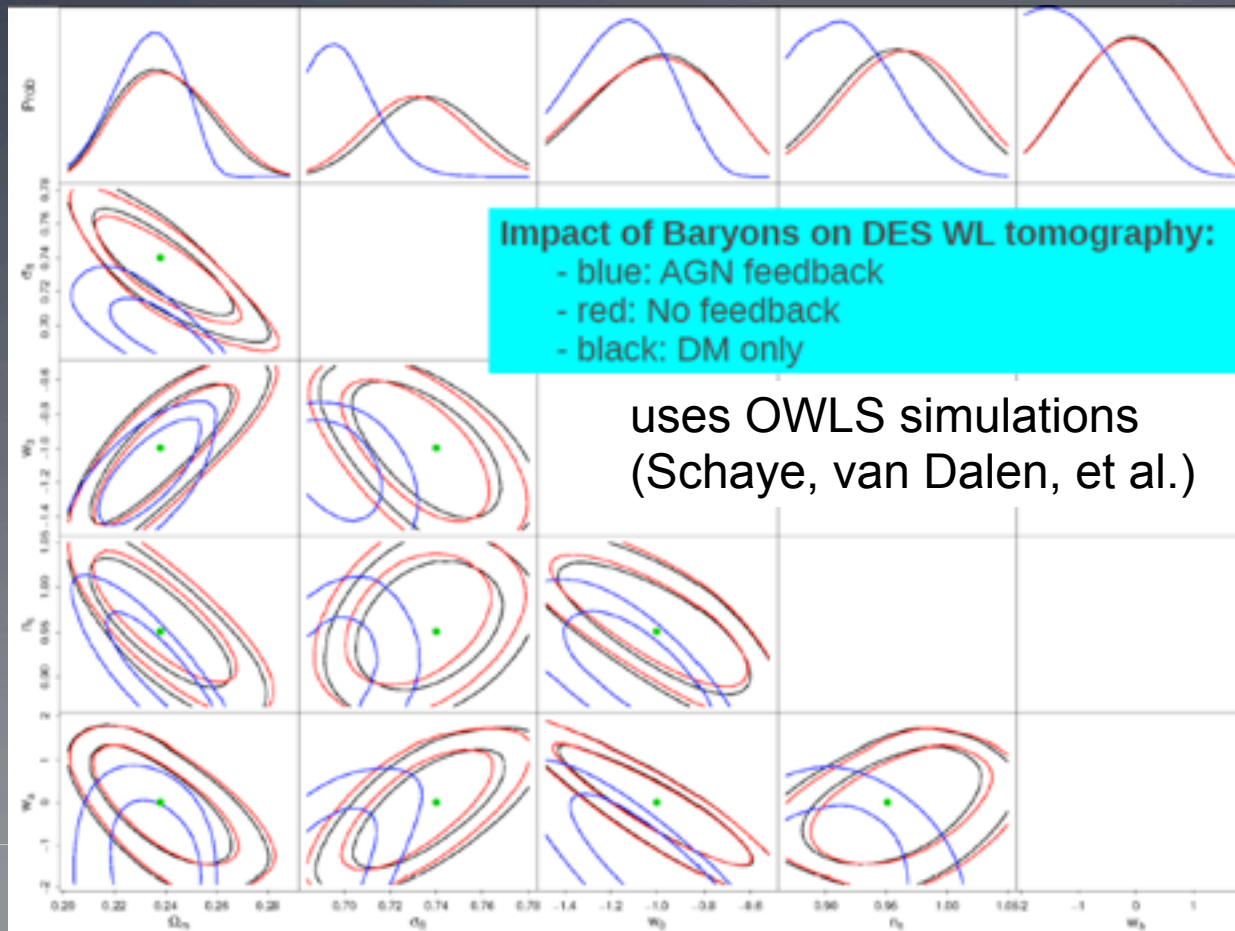
Intrinsic Alignment Calibration

- calibration depends on galaxy sample
 - need to calibrate DES galaxies
- calibration with spectroscopic sample more precise
- optimize follow-up strategy for IA calibration
- currently folding in galaxy properties from SV data, propagation through likelihood (EK, Eifler, Dodelson et al., in prep.)



Baryonic Effects

- baryonic effects (adiabatic contraction, feedback, ...)
key uncertainties on small angular scales



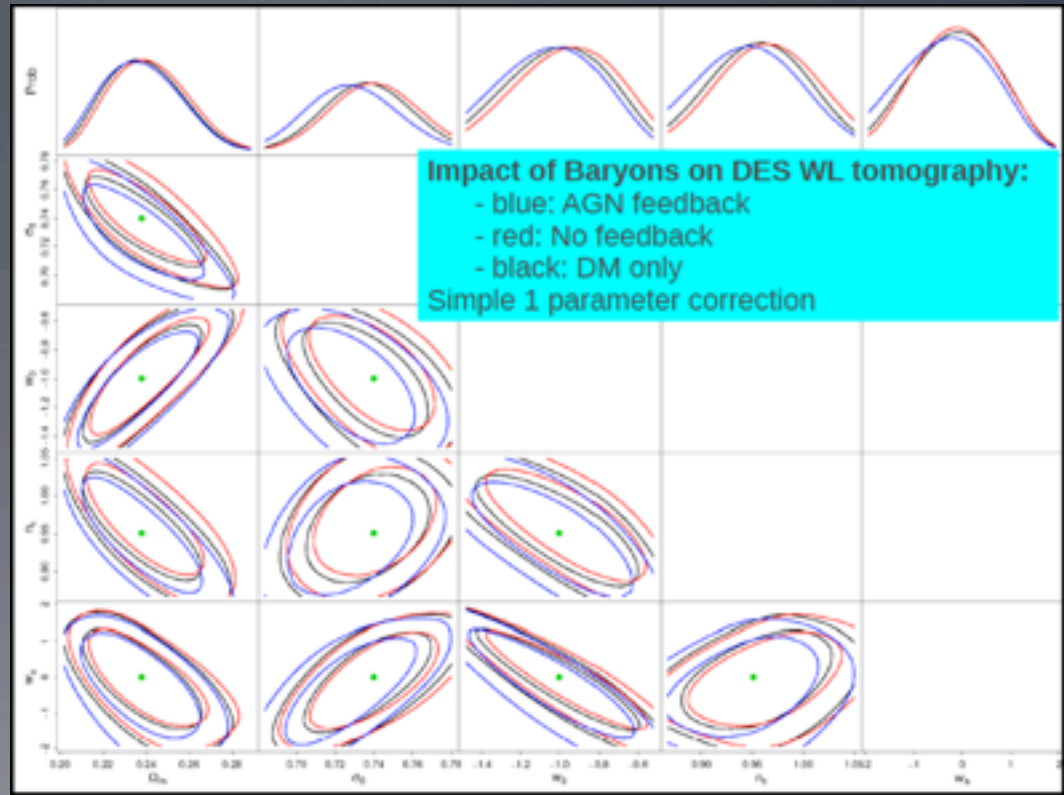
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Baryonic Effects

marginalizing over simple parameterization based on range of simulations reduces bias

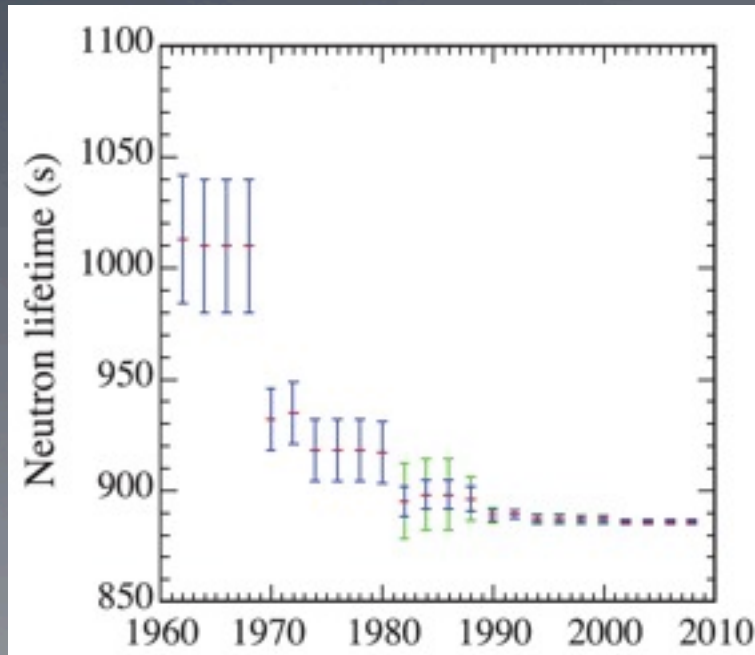
Future work:

- measure stacked halo profiles from SPT data (w/ L. Bleem)
- update parameter range for simulations, run new sims (w/ K. Heitmann & S. Habib)
- feed these into updated marginalization scheme



Experimenter Bias?

- nuisance parameters will outnumber cosmological parameters by far
 - what models + priors to adapt? when is the analysis done?
 - *don't use $w = -1$ to constrain intrinsic alignment model*



a warning from particle physics
Credit: A. Roodman, R. Kessler, Particle
Data Group

Blind Analysis

- Experimenter's bias
 - choice of data samples + selections
 - choice of priors + evaluation of systematics
 - decision to stop work + publish
- Blind Analysis: Method to prevent experimenter's bias
 - hide the answer
 - must be customize for measurement
 - blind, but not dumb
- for DES
 - need to decide on cosmology parameters now
 - steps in unblinding, requirement to publish?

Summary I

- best constraints on cosmology from joint analysis of different probes
 - but individual constraints critical for consistency tests
- conceptually + computationally challenging
 - covariance, joint systematics require advanced modeling
 - nuisance parameters complicate analysis strategy

Outlook

- stage III surveys will improve constraints on DE
 - but, have to learn *a lot* about systematics first...
- for DES, 6-8 cosmological parameters in 5 years
- I'm excited to include detailed DE models, modified gravity parameterizations into the pipeline
 - realistically, in a few years
- with stage III as a training set, much to learn in stage IV (Euclid, LSST, etc.)

Conclusion

likelihood function

number counts: Poisson
2PCF: ~ Gaussian (?)
improvements needed for stage IV

model data vector

self-consistent modeling of all observables
matter power spectrum, halo mass + bias function
+ *selection function, systematics*

$$p(\boldsymbol{\pi} | \hat{\mathbf{d}}) = p(\boldsymbol{\pi}) \mathcal{L}(\hat{\mathbf{d}} | \mathbf{d}(\boldsymbol{\pi}), \mathbf{C})$$

joint covariance

large and complicated,
non-(block) diagonal matrix
use template + regularization

large data vector

**external data
blind analysis**

validate

priors

parameters

~10 for cosmology
XXX for systematics