

# **LARGE SCALE CLUSTERING IN THE SDSS LUMINOUS RED GALAXY SAMPLE**

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**and:**

**Román Scoccimarro, NYU**

**Andreas Berlind, Vanderbilt Uni.**

**Cameron McBride, Vanderbilt Uni.**

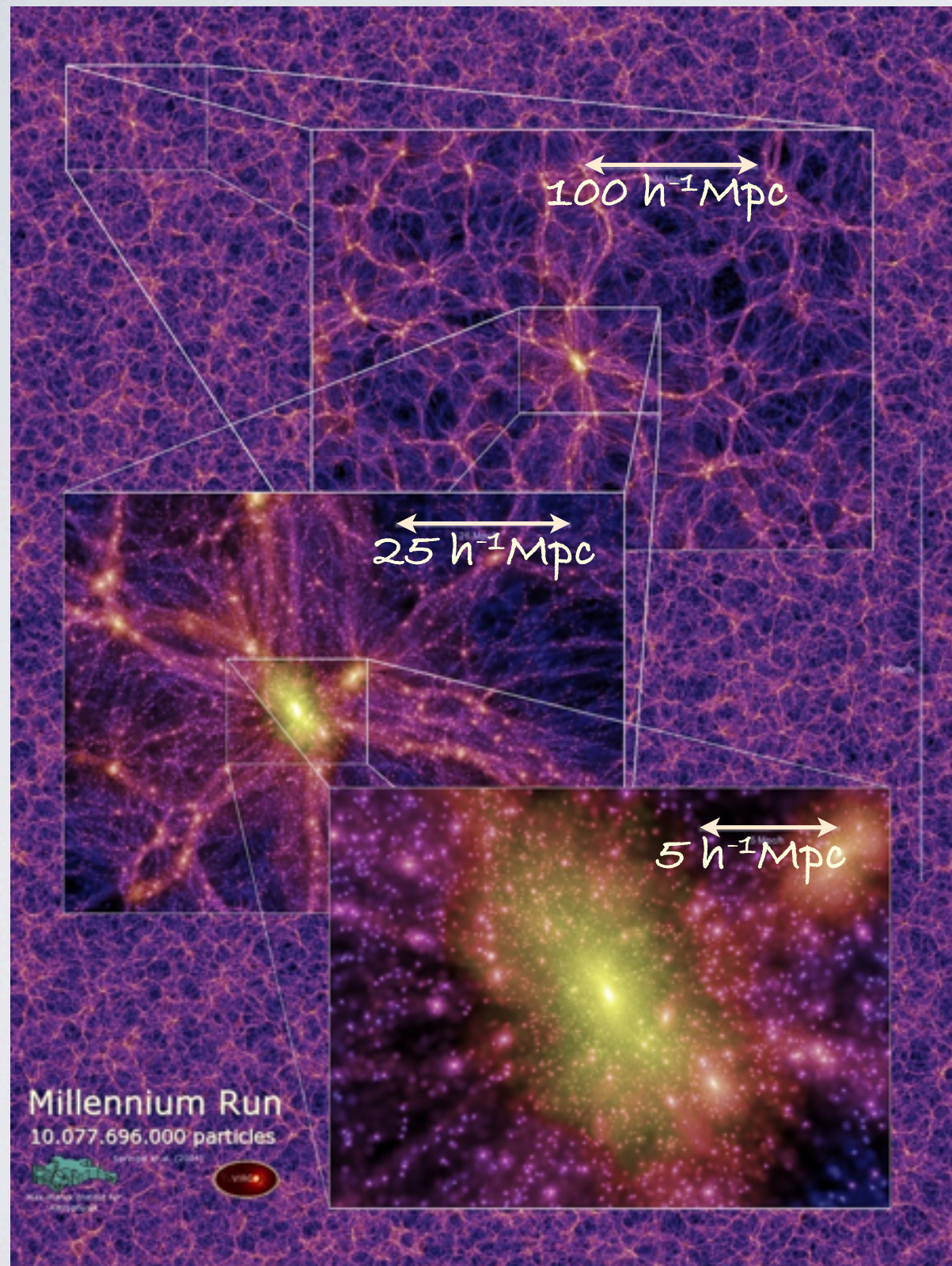


Today I will discuss:

- ☐ Introduction 13 minutes
- ☐ Quantifying Clustering
- ☐ LRGs- Why (should) we like these galaxies so much?
- ☐ The Sloan Digital Sky Survey
- ☐ Baryonic Acoustic Feature 30 minutes
- ☐ Introduction to Redshift Distortions 2 minutes
- ☐ Redshift Distortions in Clustering 5 minutes

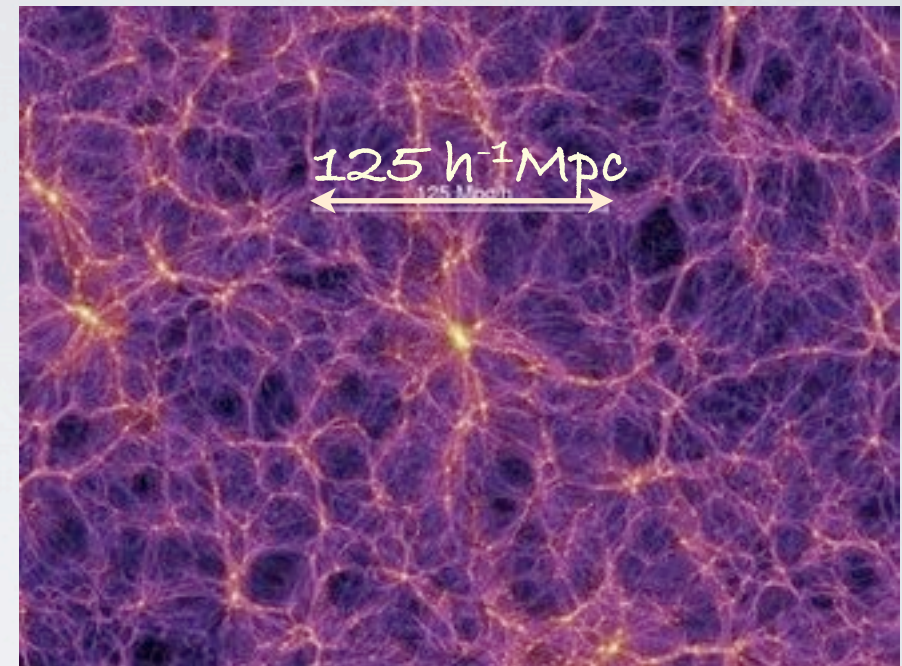


# Large-Scale Structure

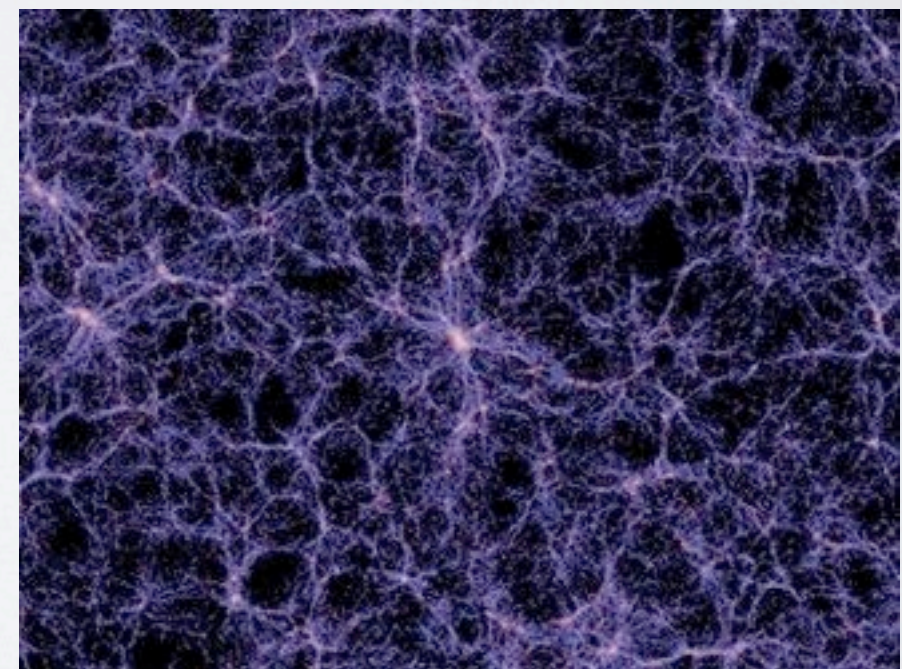


## The Millennium Simulation Project

Dark Matter Distribution



Mock Galaxy Distribution



Springel et al. (2005)



# Quantifying Clustering

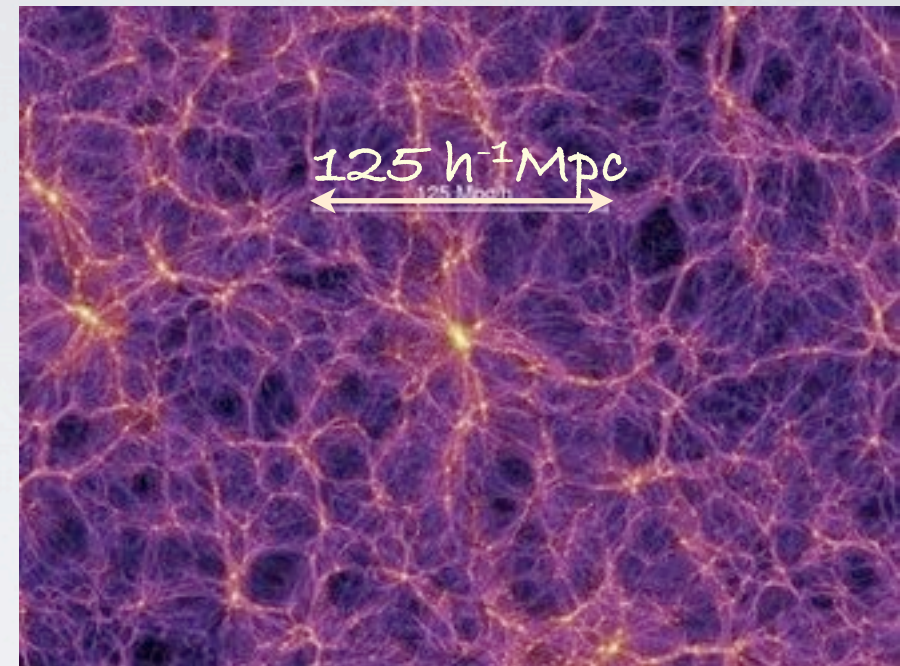
$$\rho(x) = \bar{\rho}(1 + \delta(x))$$

$\rho$  - density  
 $\delta$  - overdensity  
 $\delta \geq -1$

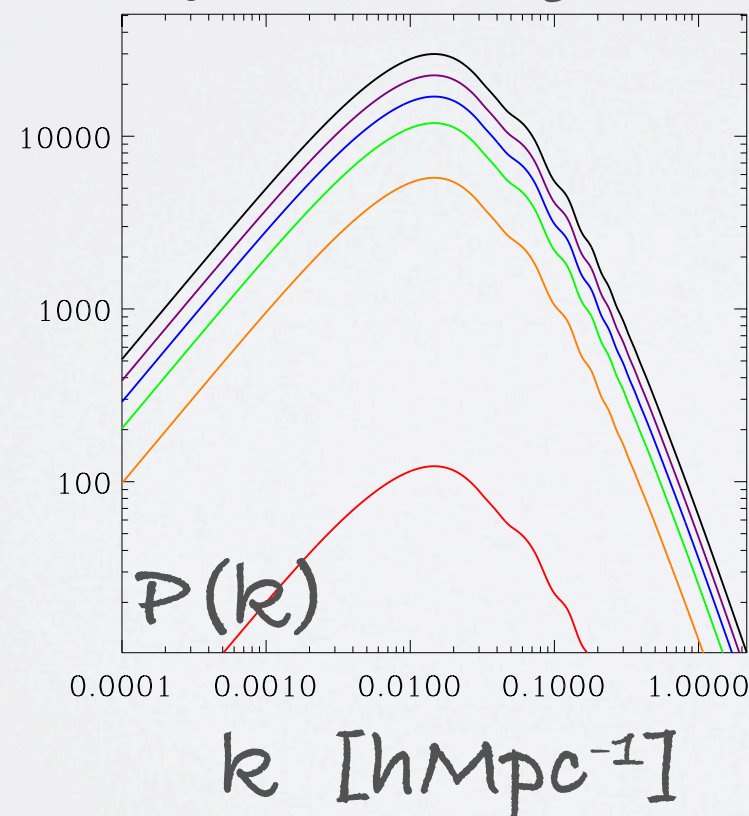
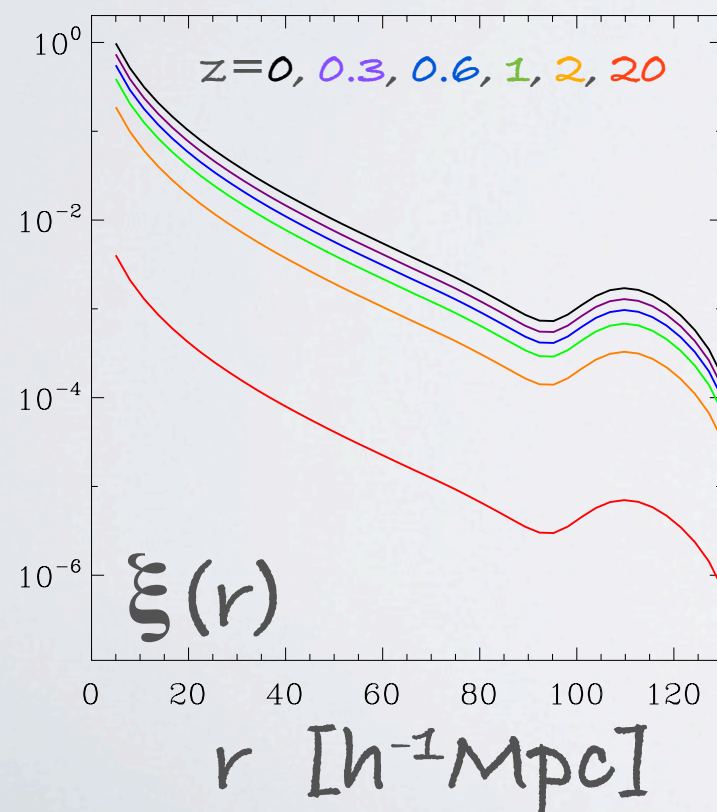
2 point functions

correlation function  $\xi(r) \equiv \langle \delta(x) \delta(x+r) \rangle_{\text{volume}}$

Power Spectrum  $P(k) \equiv \int d^3x e^{-i\mathbf{k} \cdot \mathbf{r}} \xi(r)$



Springel et al. (2005)





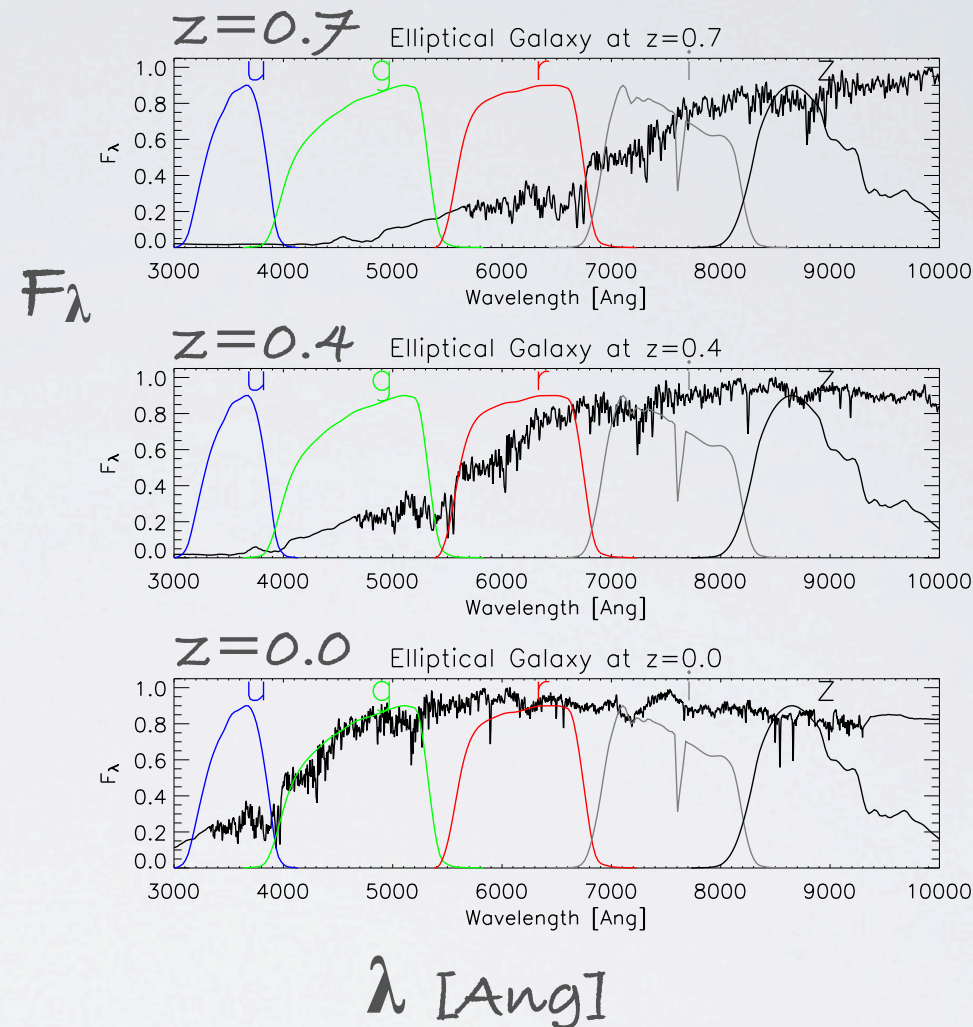
# Luminous Red Galaxies

Padmanabhan et al. (2007)

based on Bruzual&Charlot (2003) model



From a talk by Max Tegmark



- Luminous ➤ Enable large volume limited samples
- Not too rare  $n(z) \sim 3 \cdot 10^{-4} (h \text{Mpc}^{-1})^3$
- Trace Matter well, “bias” (clustering gain)  $b_{\text{Lin}} \sim 2$
- Easy to identify by color cuts, spectra

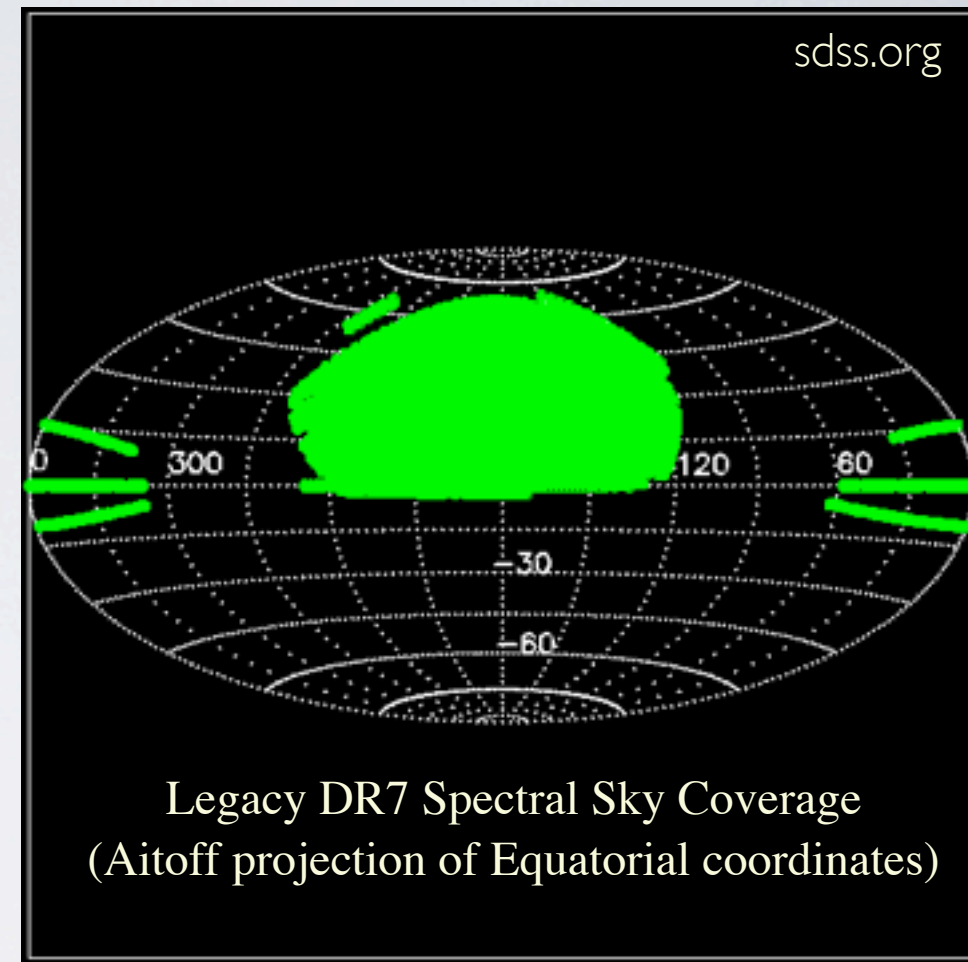
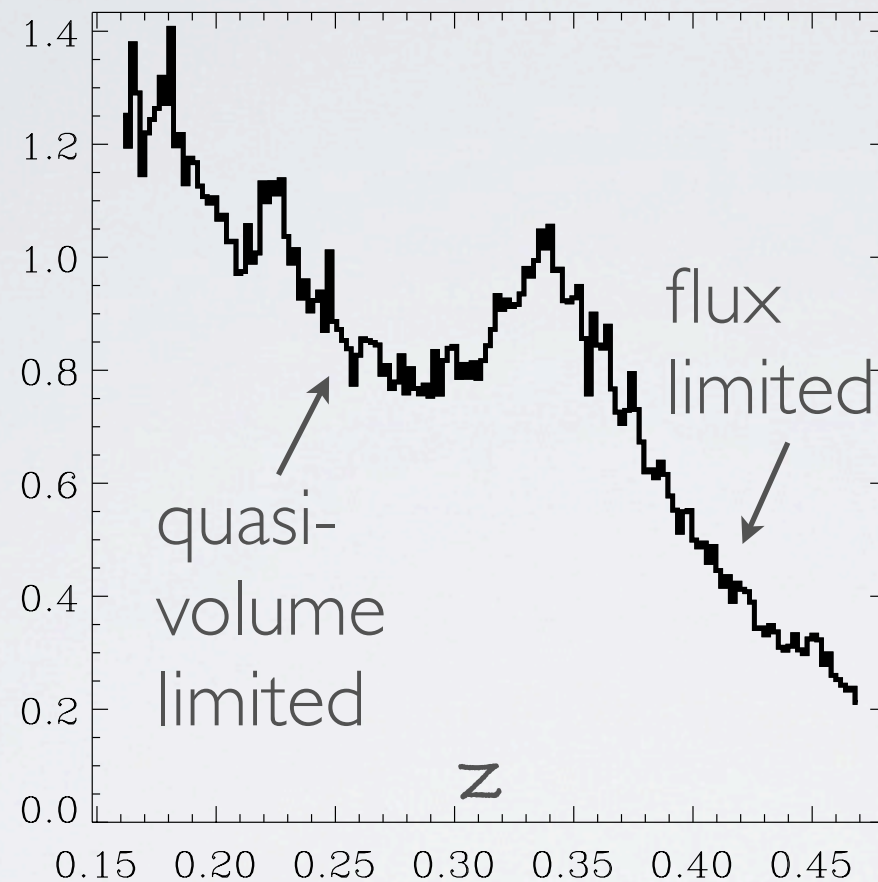
$$\delta_{\text{gal}} \approx b_{\text{Lin}} \delta$$





# The Sloan Digital Sky Survey LRG Sample

$n(z)$   
[ $10^{-4} h^3 \text{Mpc}^{-3}$ ]  
comoving density



- >100,00 LRGs between  $0.16 < z < 0.47$
- Sky Coverage  $\sim 8,000 \text{ degree}^2$
- Comoving Volume  $1.6 h^{-3} \text{Gpc}^3$  of which:  
quasi-volume Limited until  
 $z < 0.36$  ( $0.66 h^{-3} \text{Gpc}^3$ )



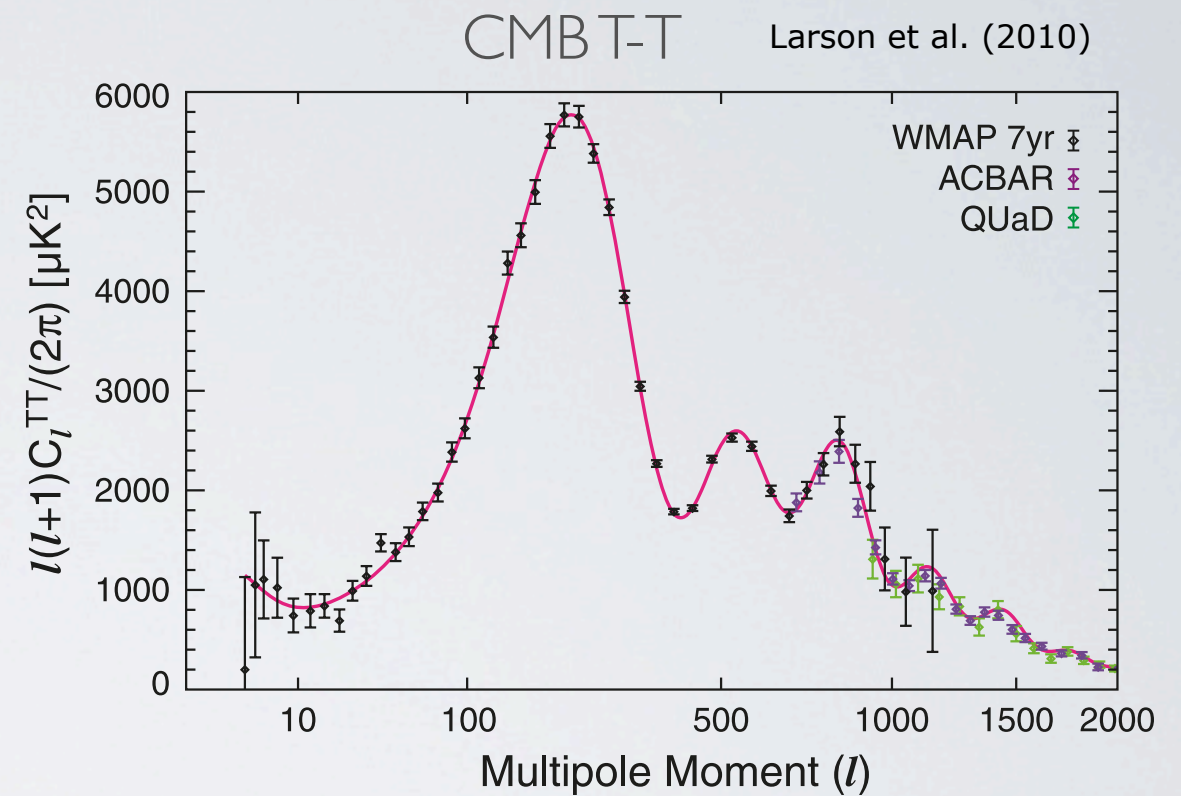
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# The Baryonic Acoustic Feature Linear Theory

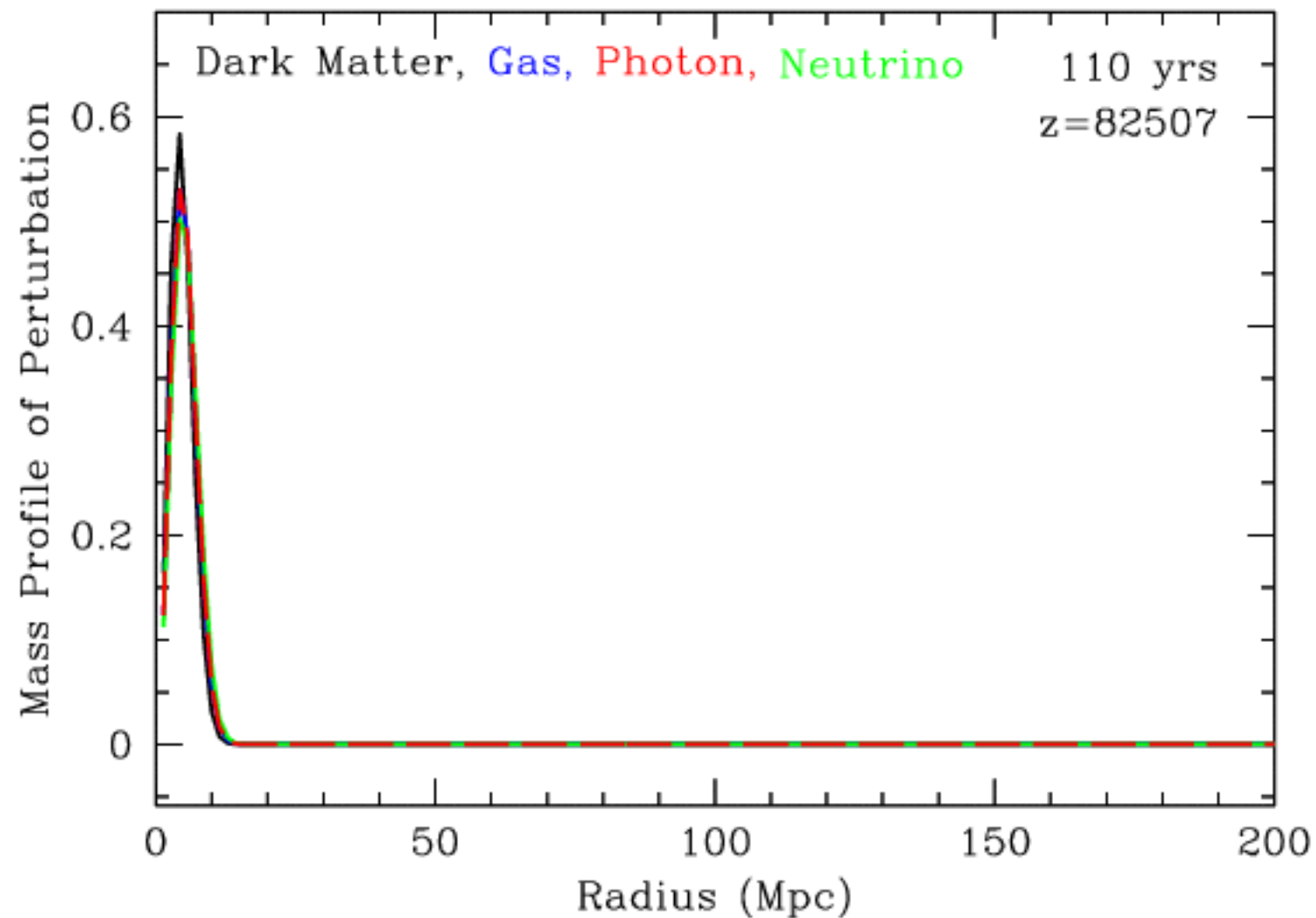
Feature in the early universe:





# Baryonic Acoustic Origins

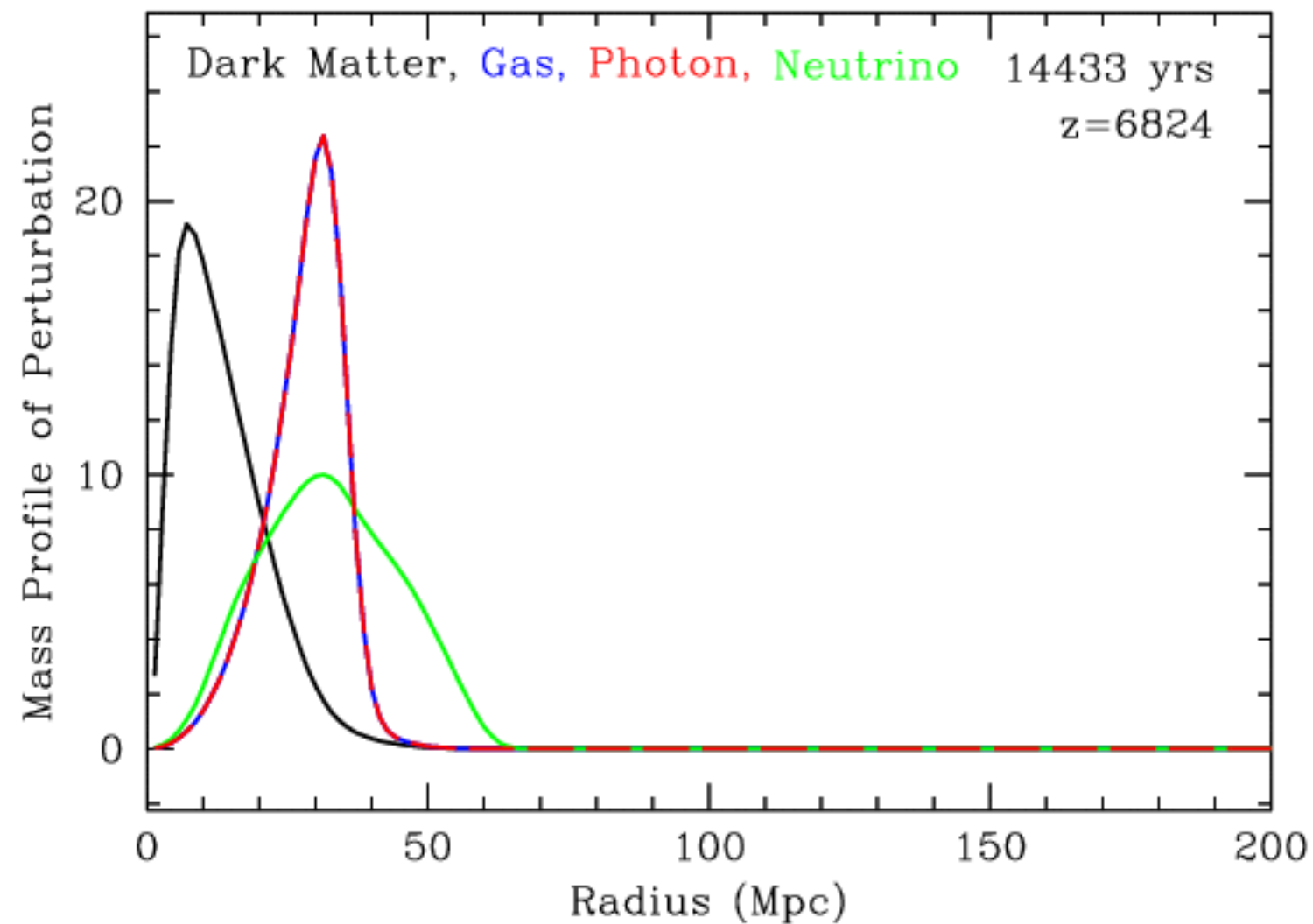
Plots by Daniel Eisenstein





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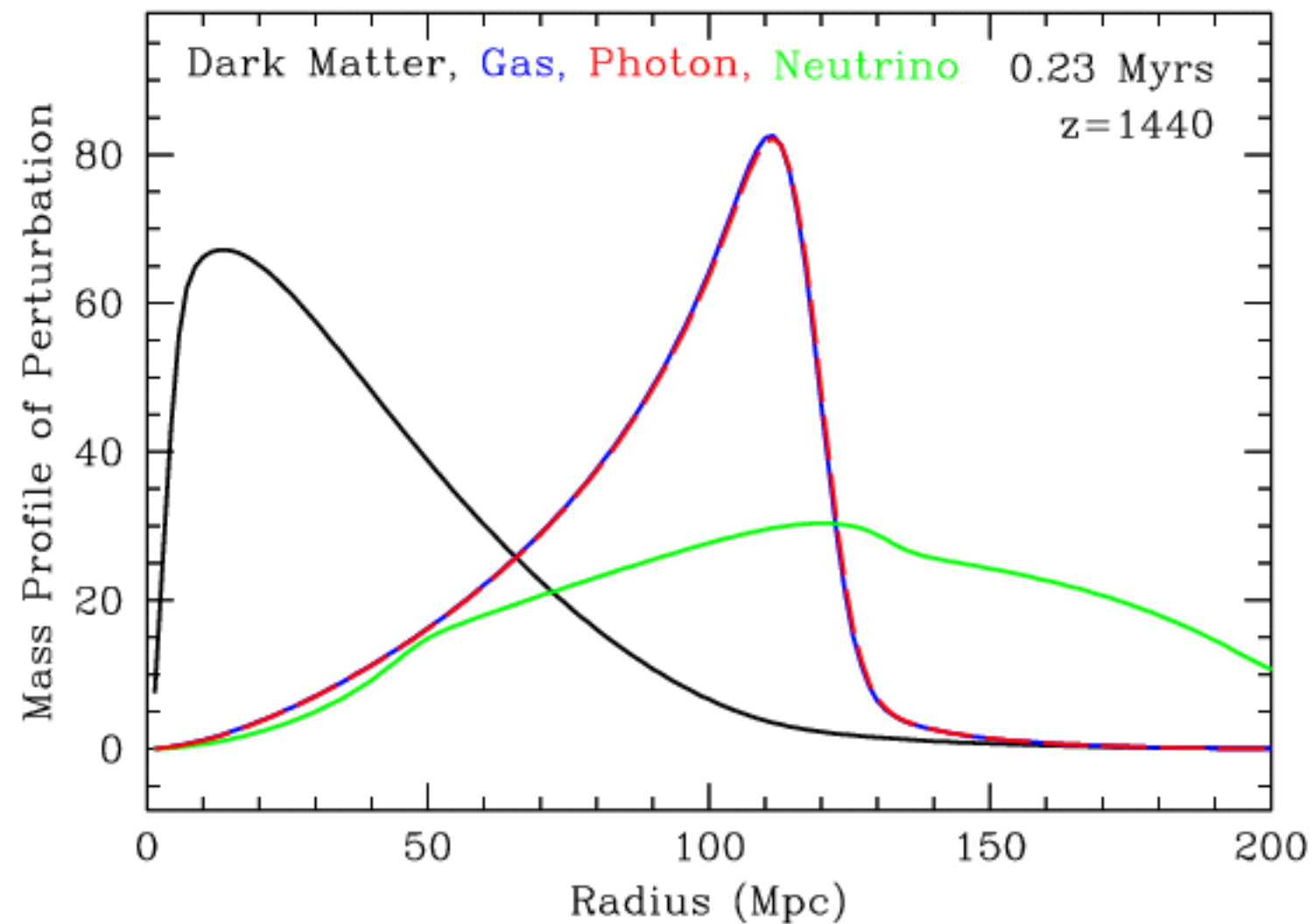
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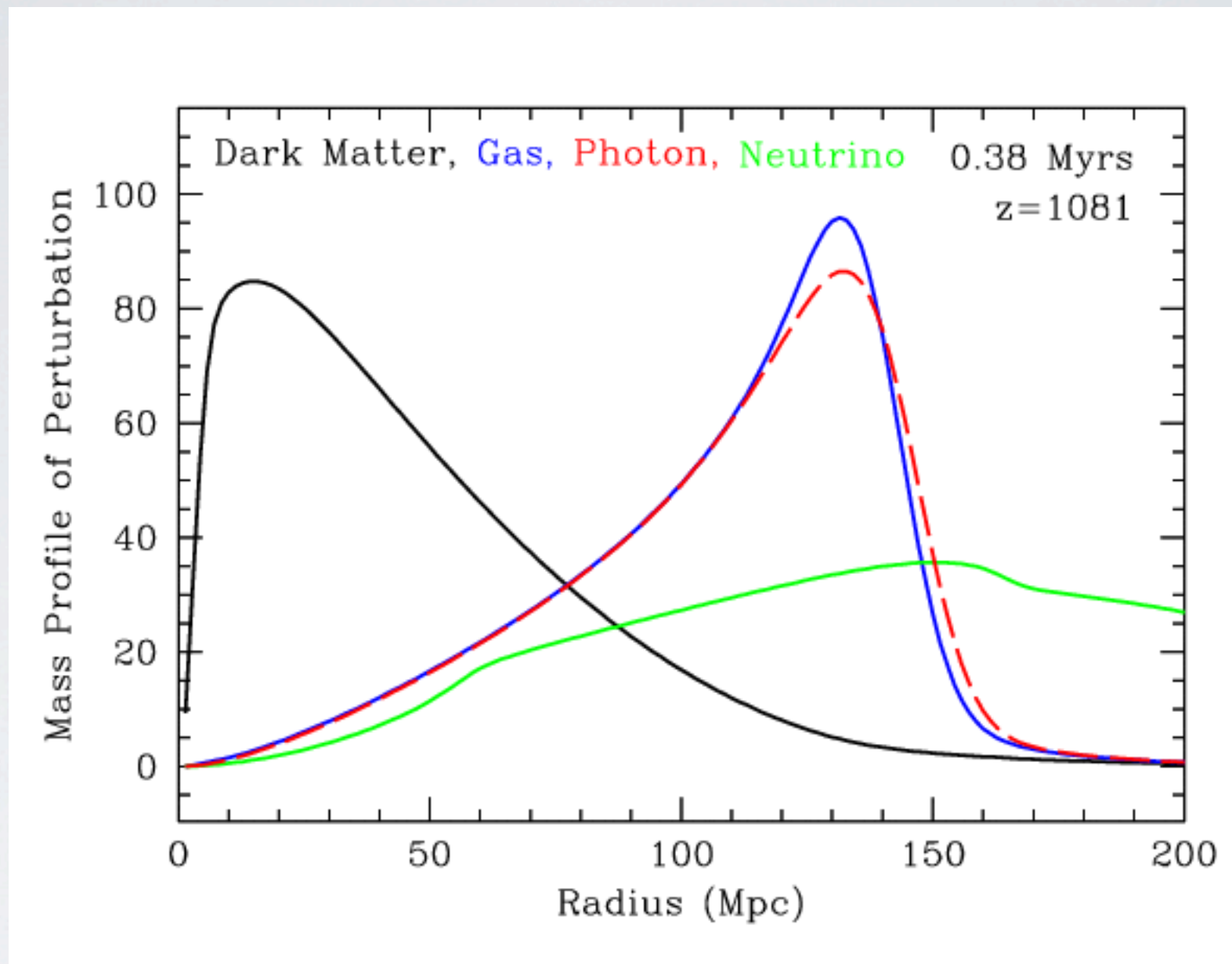
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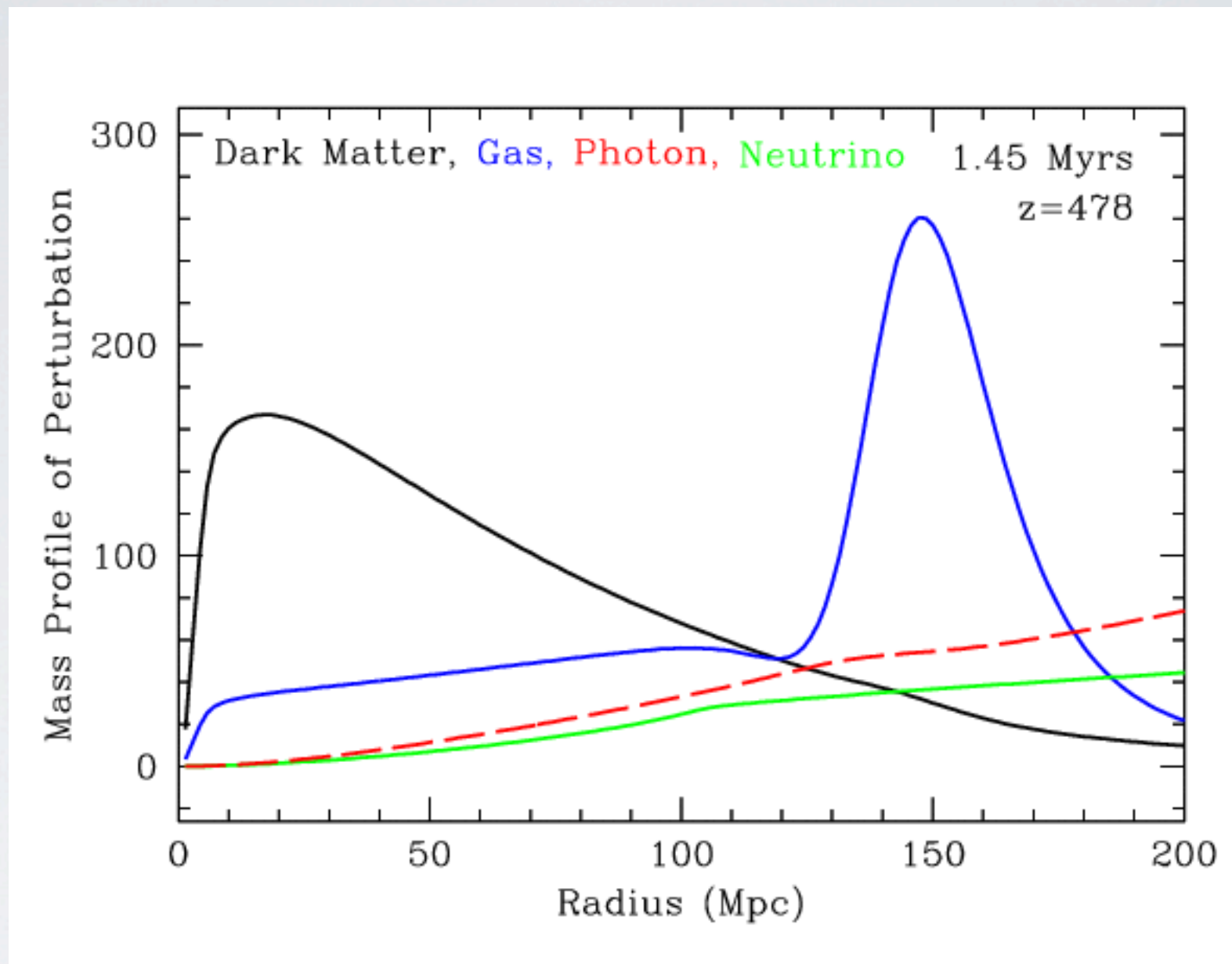
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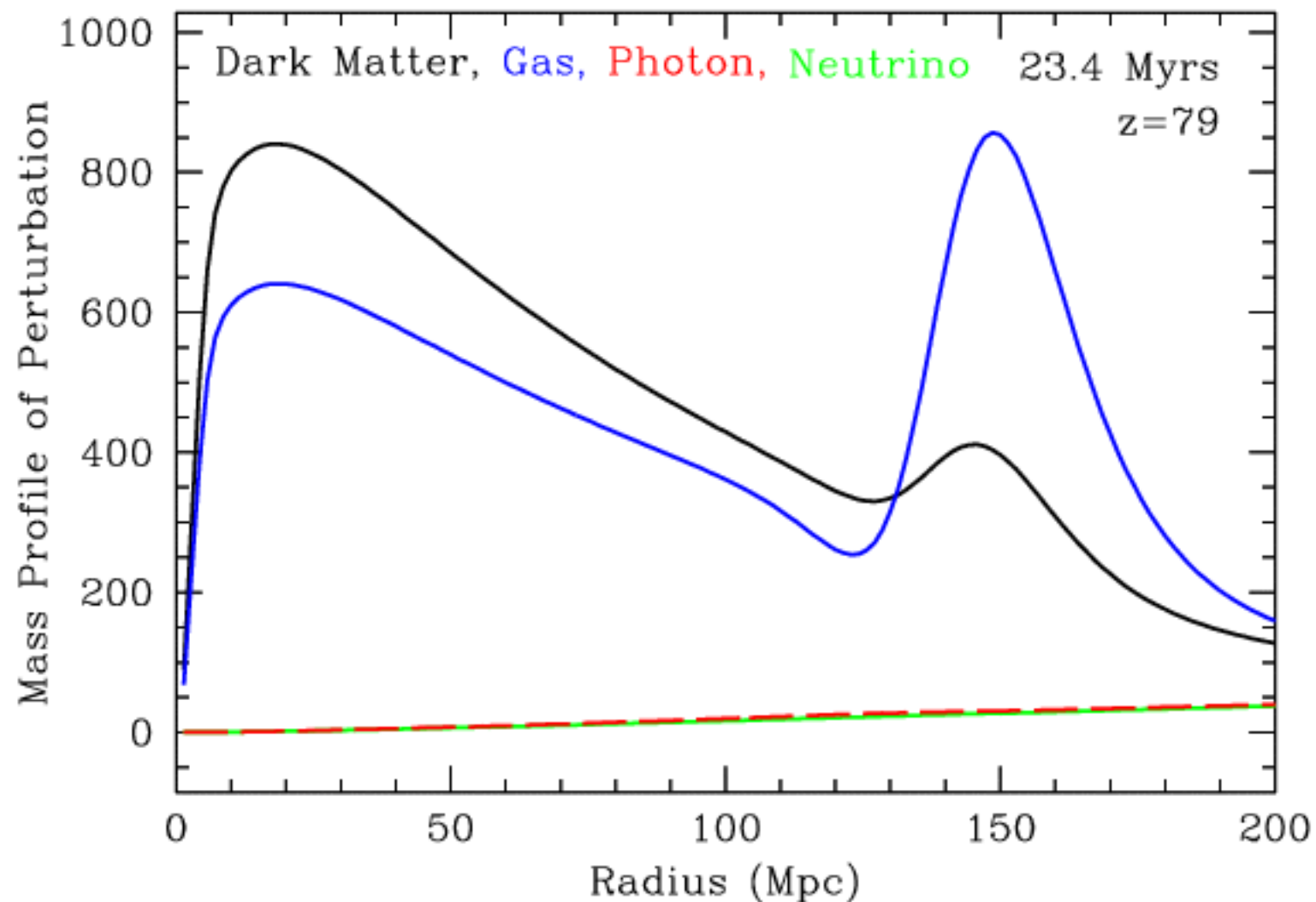
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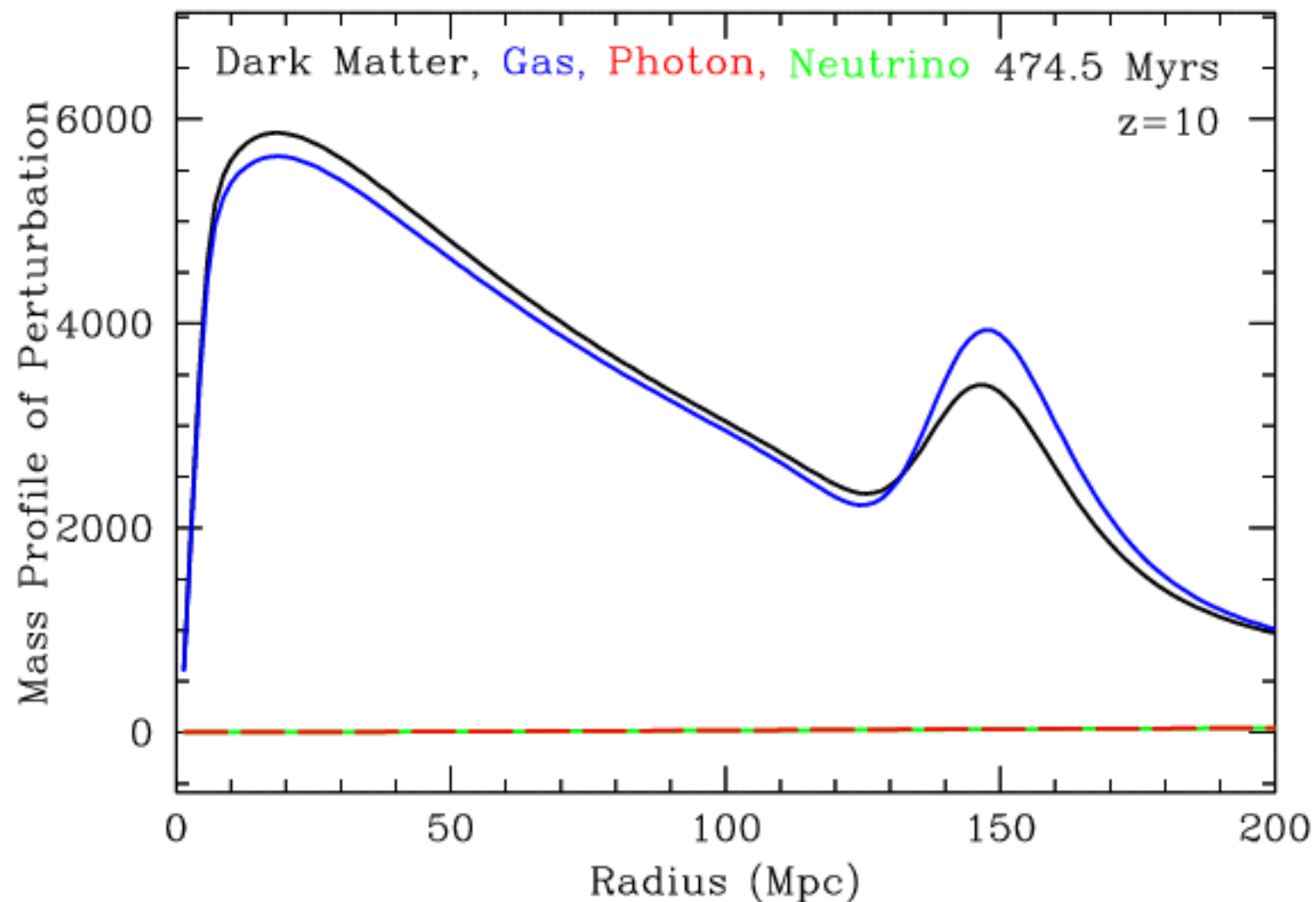
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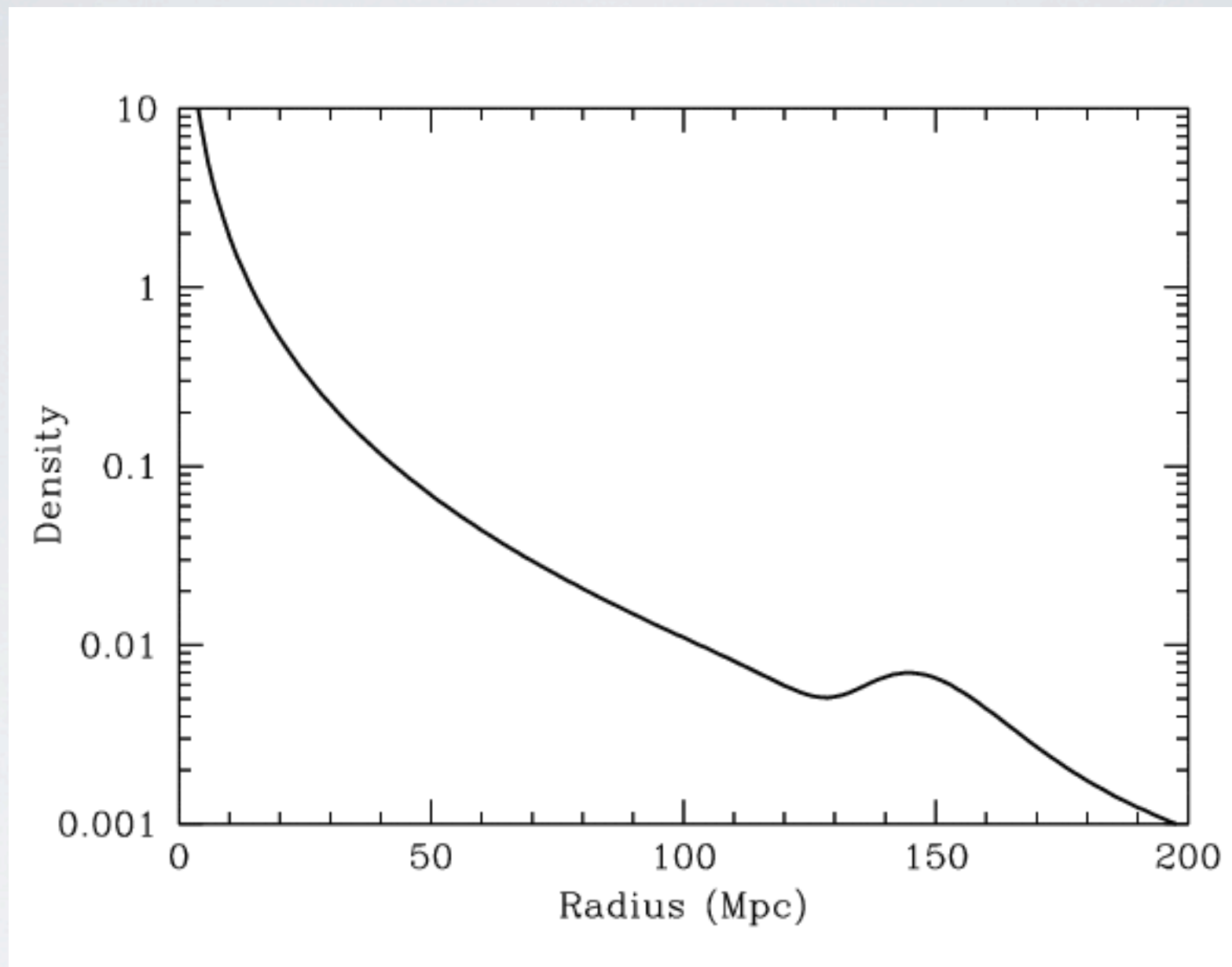
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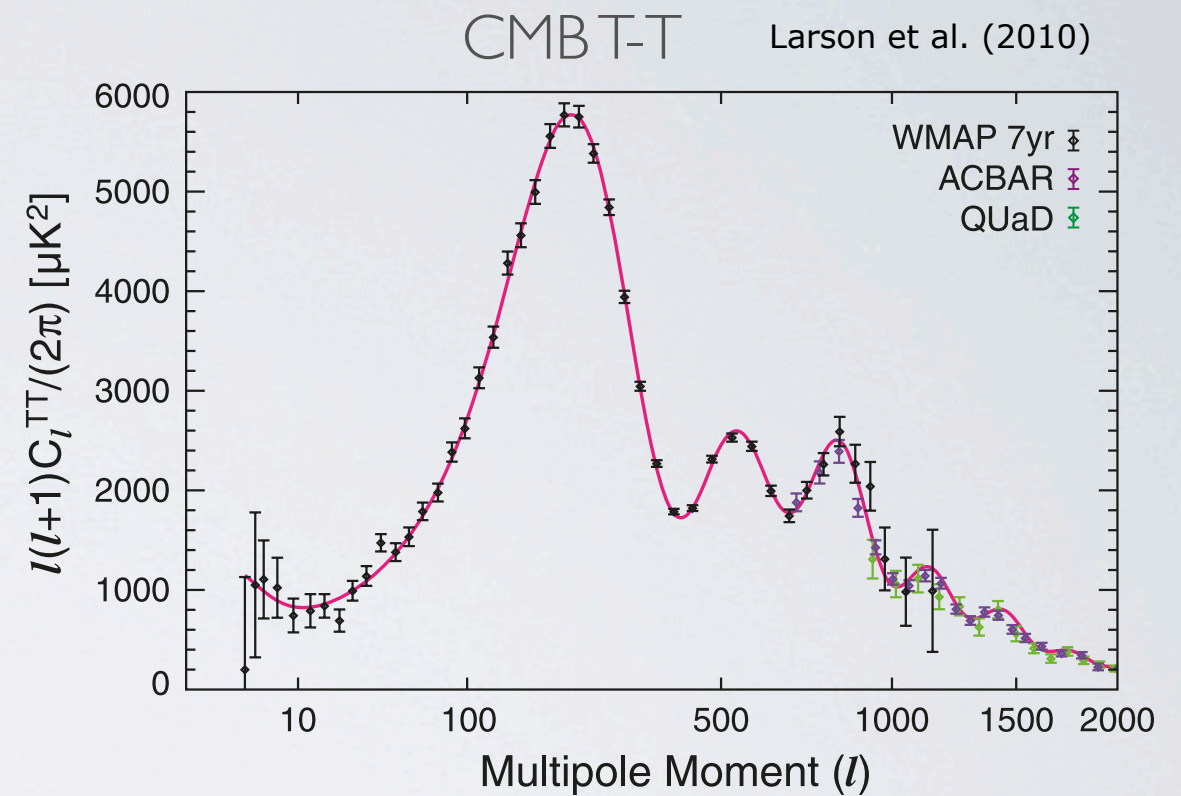
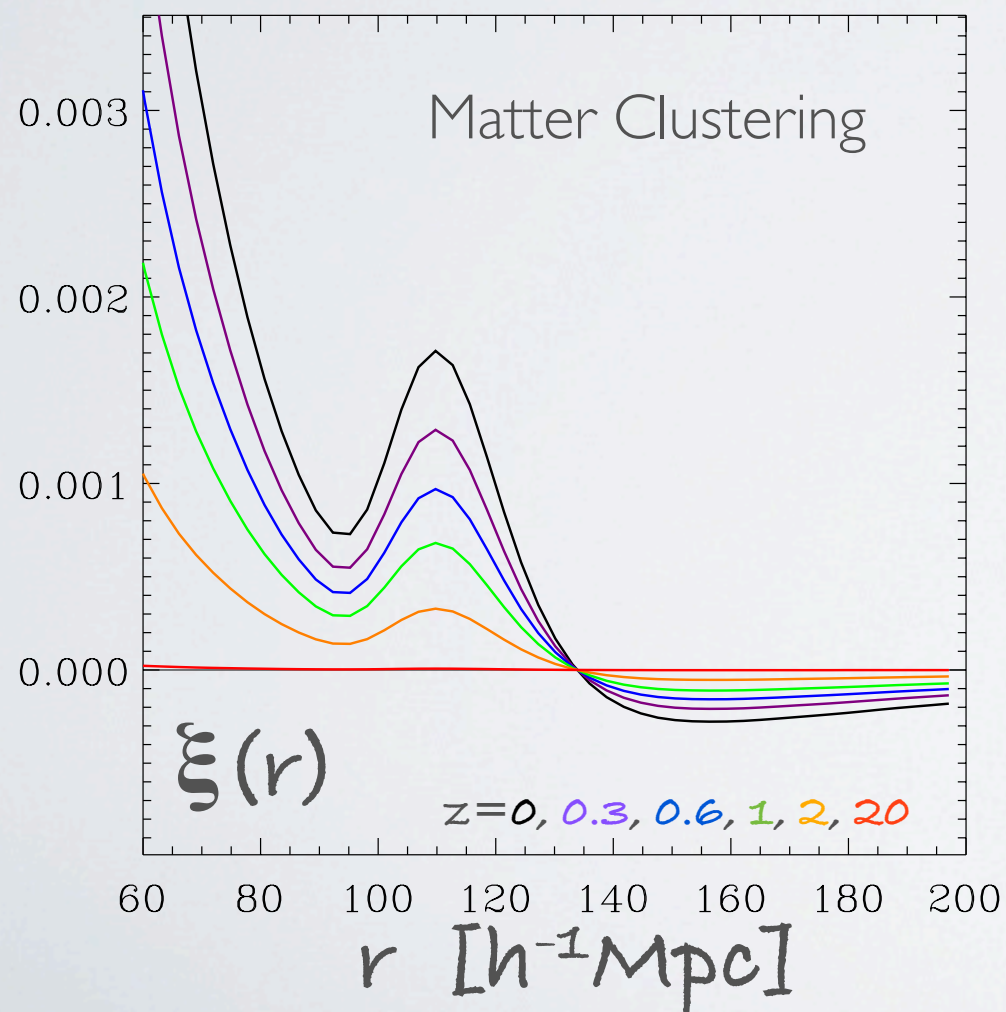




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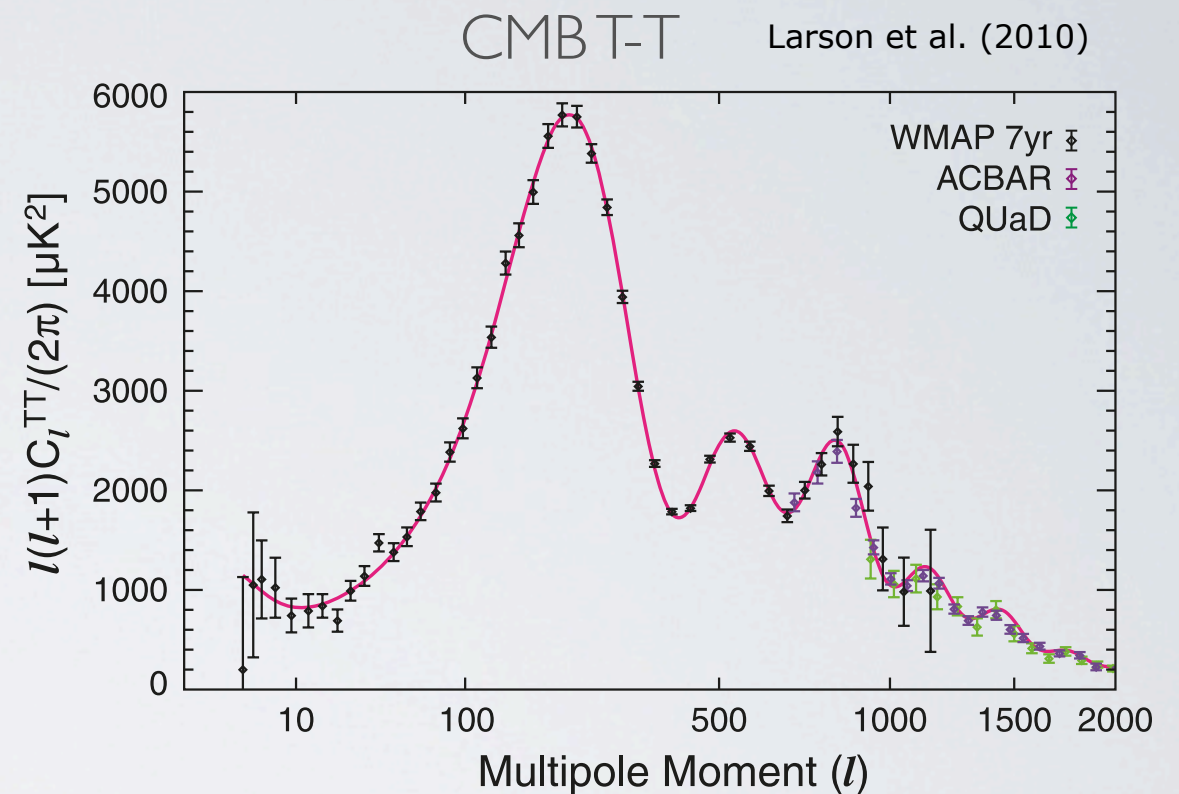
Feature in the early universe:

Feature in the late universe:

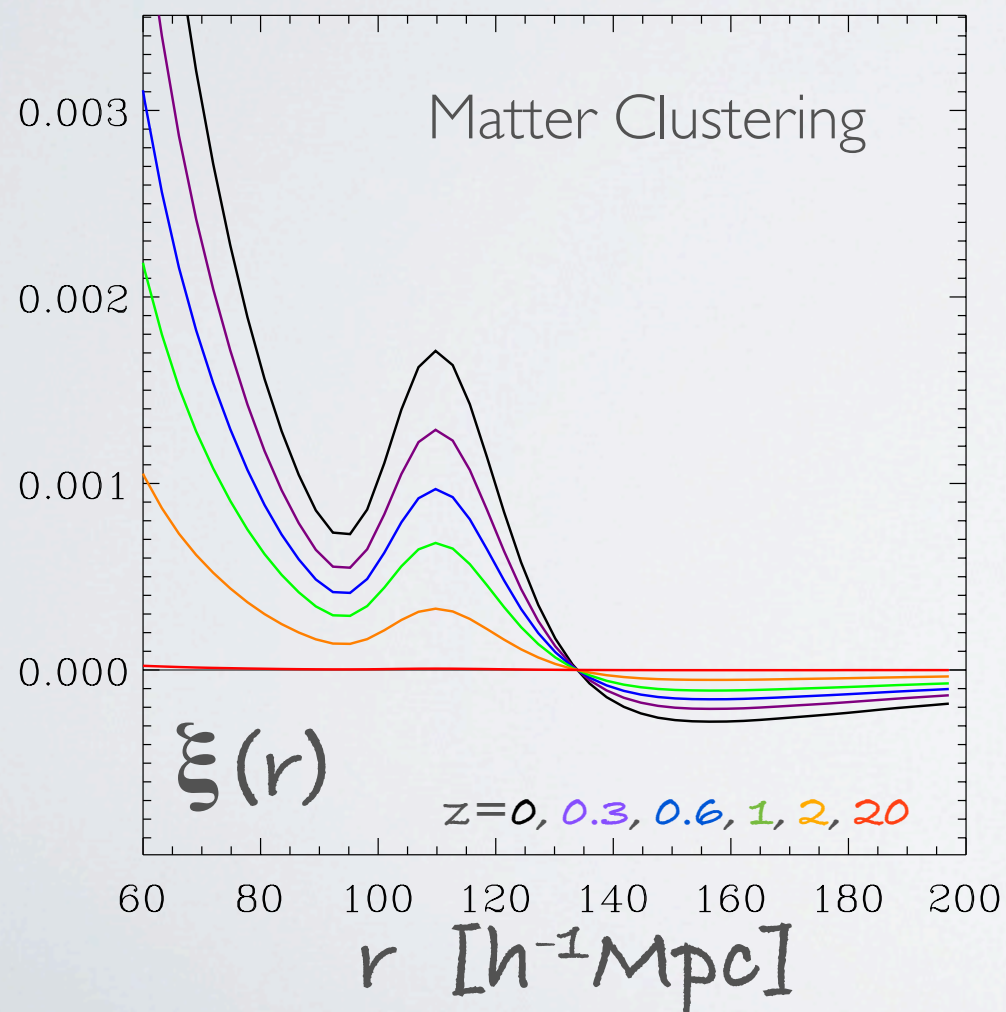


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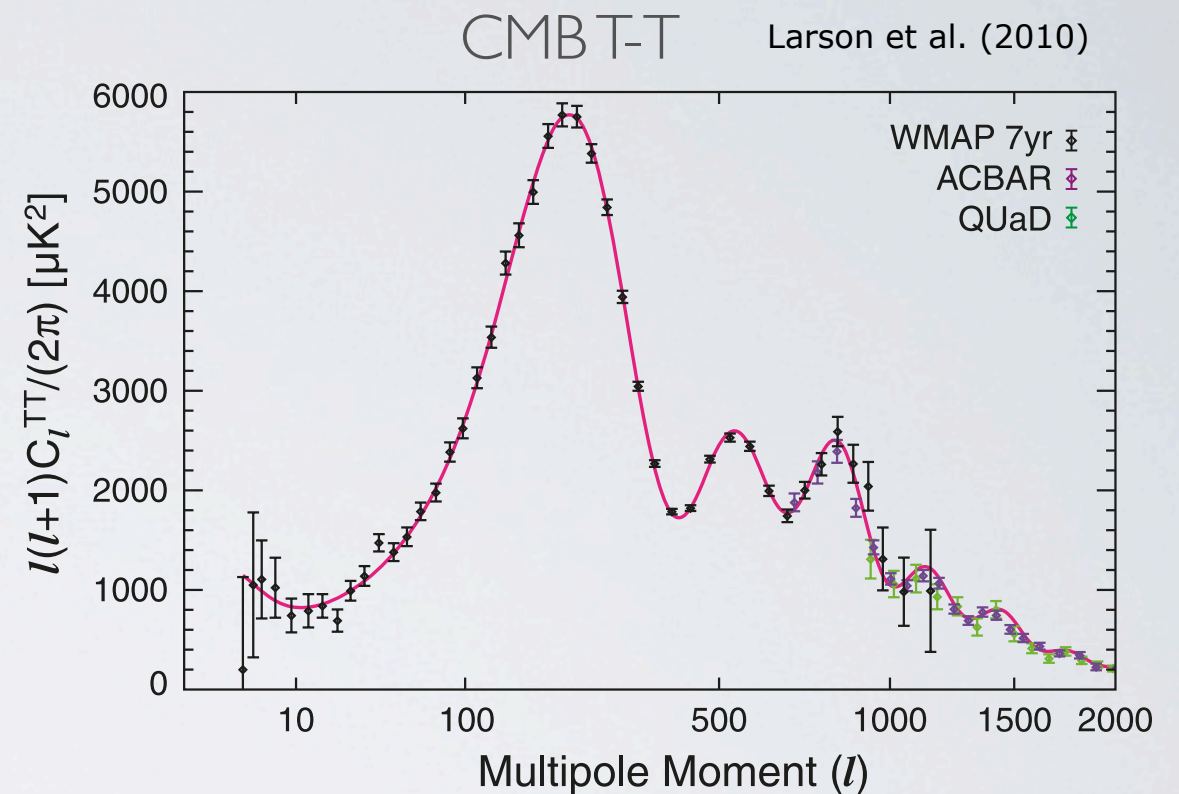
sound horizon

$$r_s(z_{dec}) = \int_0^{\tau_{dec}} c_s d\tau = \int_{\infty}^{z_{dec}} c_s / H(z') dz'$$

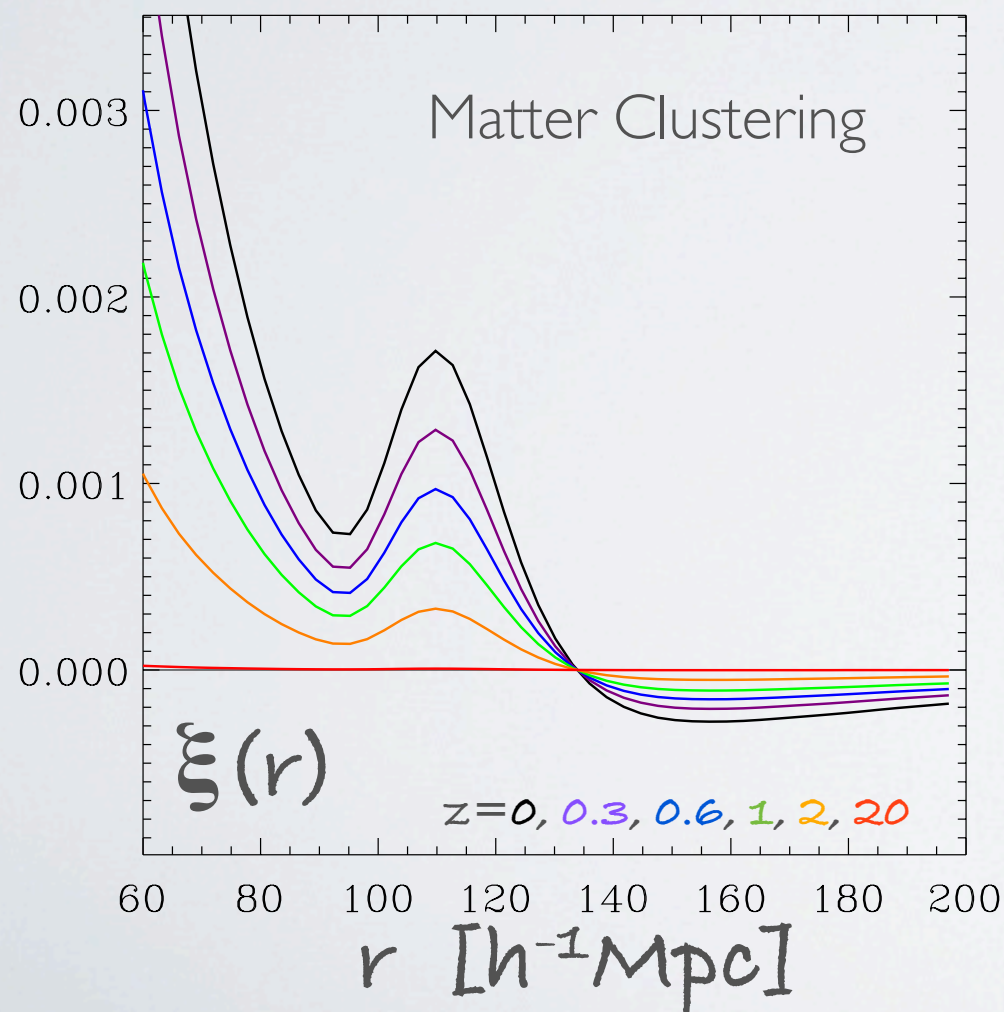


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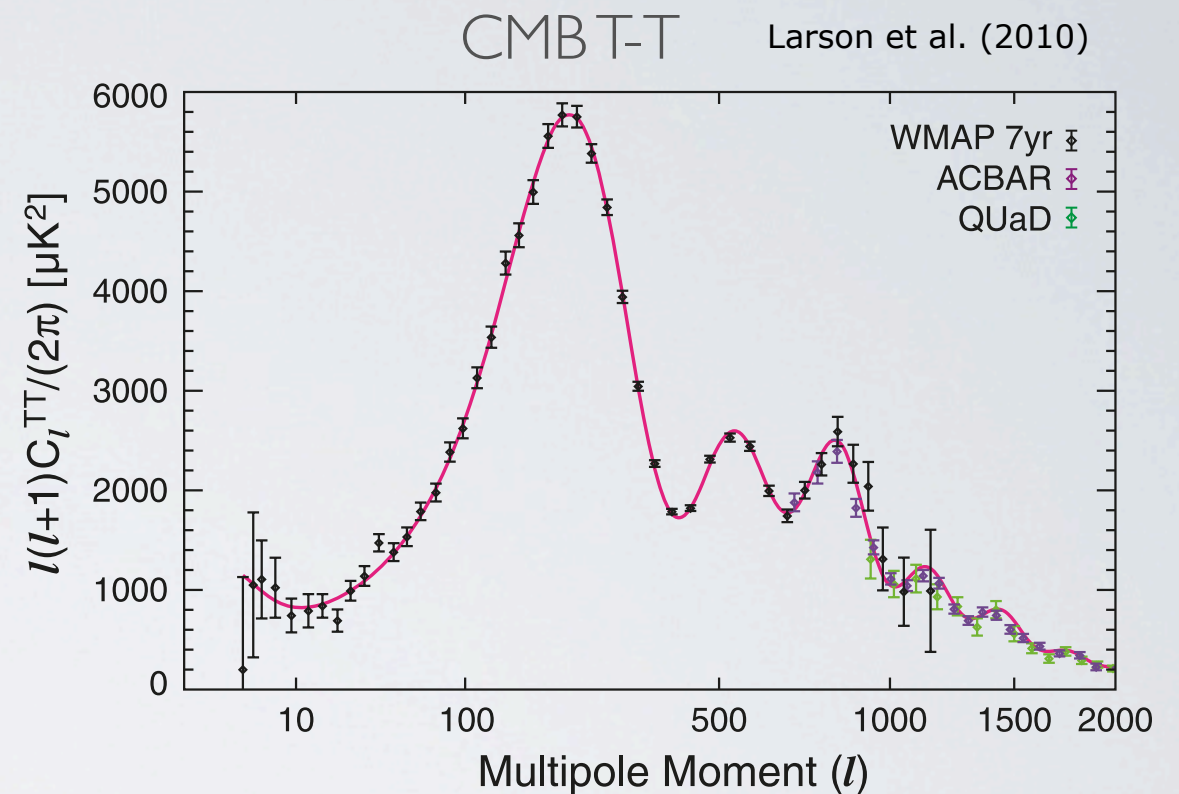
$$r_s(z_{dec}) = \int_0^{\tau_{dec}} c_s d\tau = \int_{\infty}^{z_{dec}} c_s / H(z') dz'$$

$z_{dec}, \tau_{dec}$  conformal time and redshift at photon-baryon decoupling

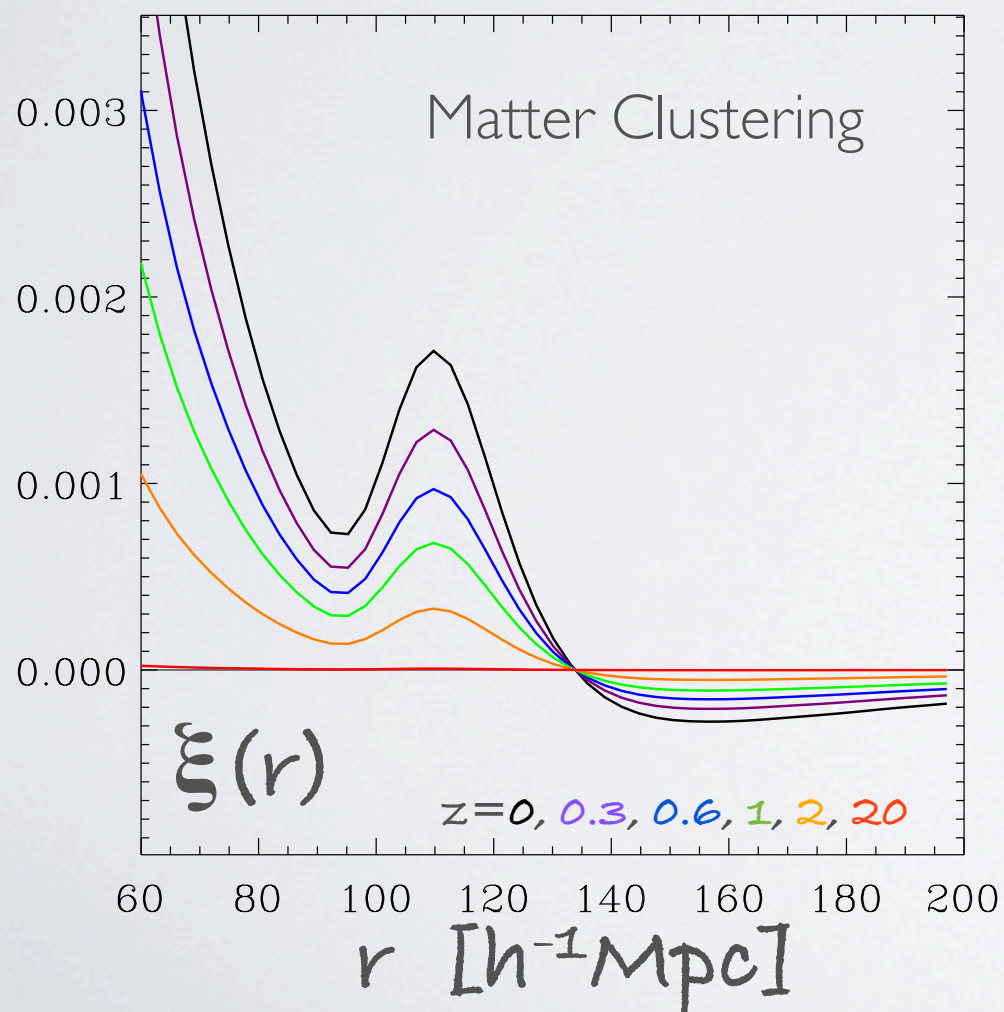
$$d\tau \equiv (1+z) dt = 1/(H(z)) dz$$

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$z_{dec}, \tau_{dec}$  conformal time and redshift at photon-baryon decoupling

$$d\tau \equiv (1+z) dt = 1/(H(z)) dz$$

sound speed  $c_s(z) = c/\sqrt{3(1+R)}$

baryon to photon ratio  $R(z) \equiv 0.75 Q_b / Q_\gamma$

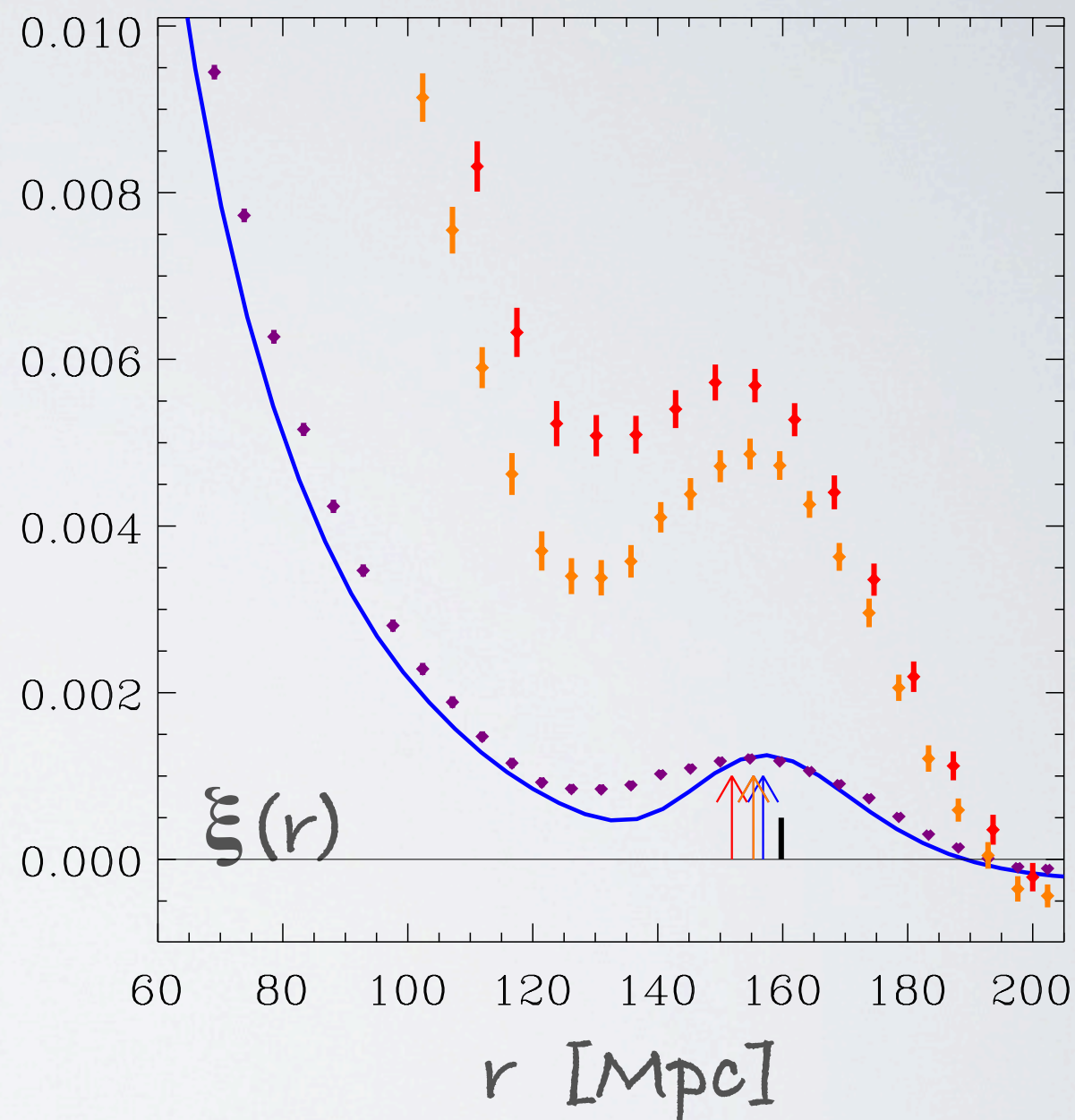


# The Baryonic Acoustic Feature in Late Universe (reality check)

## Deviations from linear theory

(laundry list)

-  Nonlinear clustering
-  Galaxy bias  $\delta_{gal} \approx b_{Lin} \delta$
-  Redshift Distortions
-  Assuming cosmology



galaxies z-space, non-linear  
 galaxies real space, non-linear  
 matter real space, non-linear  
 matter real space, linear



# The Baryonic Acoustic Feature in Late Universe (reality check)

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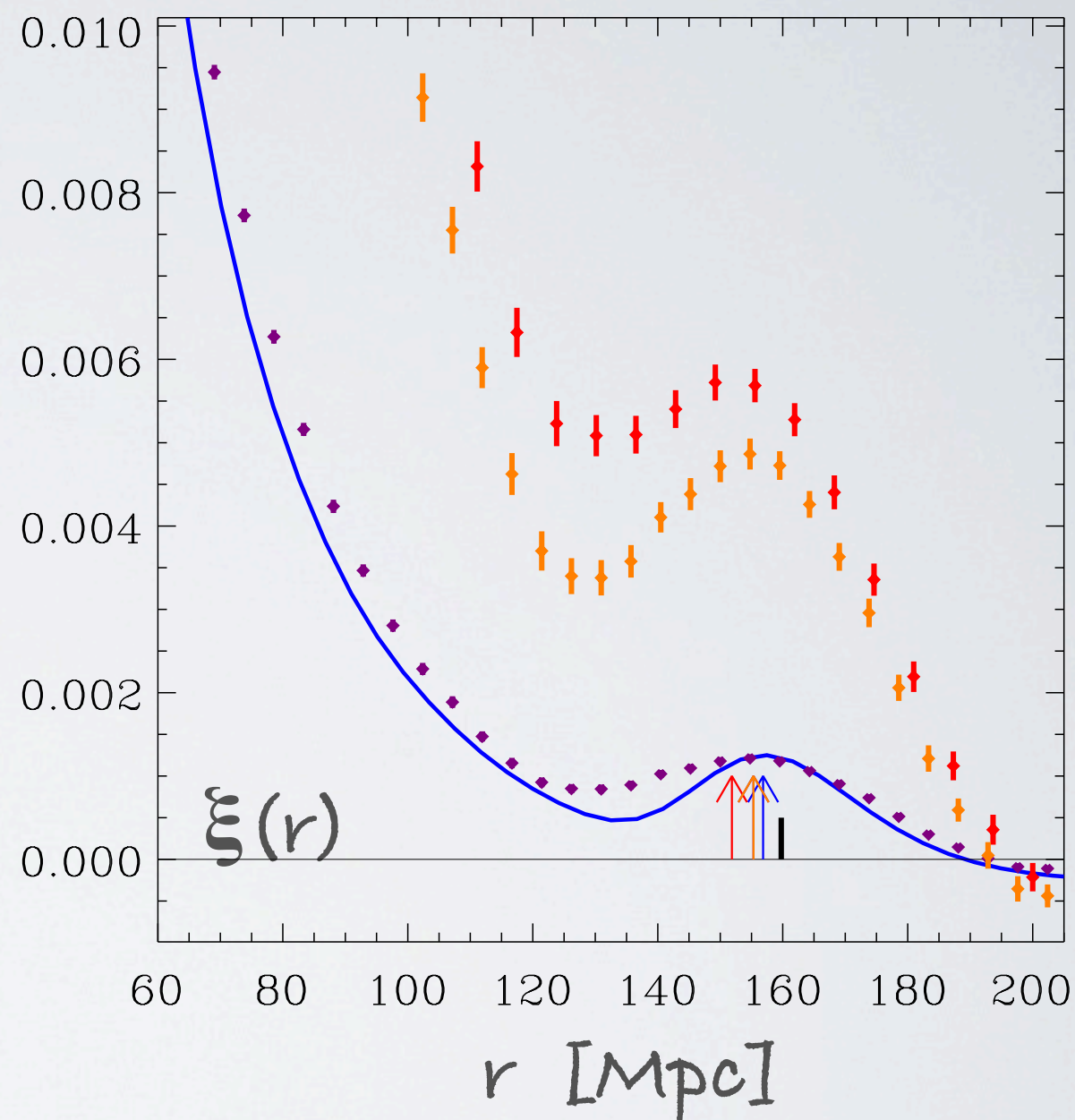
(laundry list)

-  Nonlinear clustering
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S/N ( $\xi / \sigma$ ) depends on

-  Volume of sample
-  Density of sample  $n$

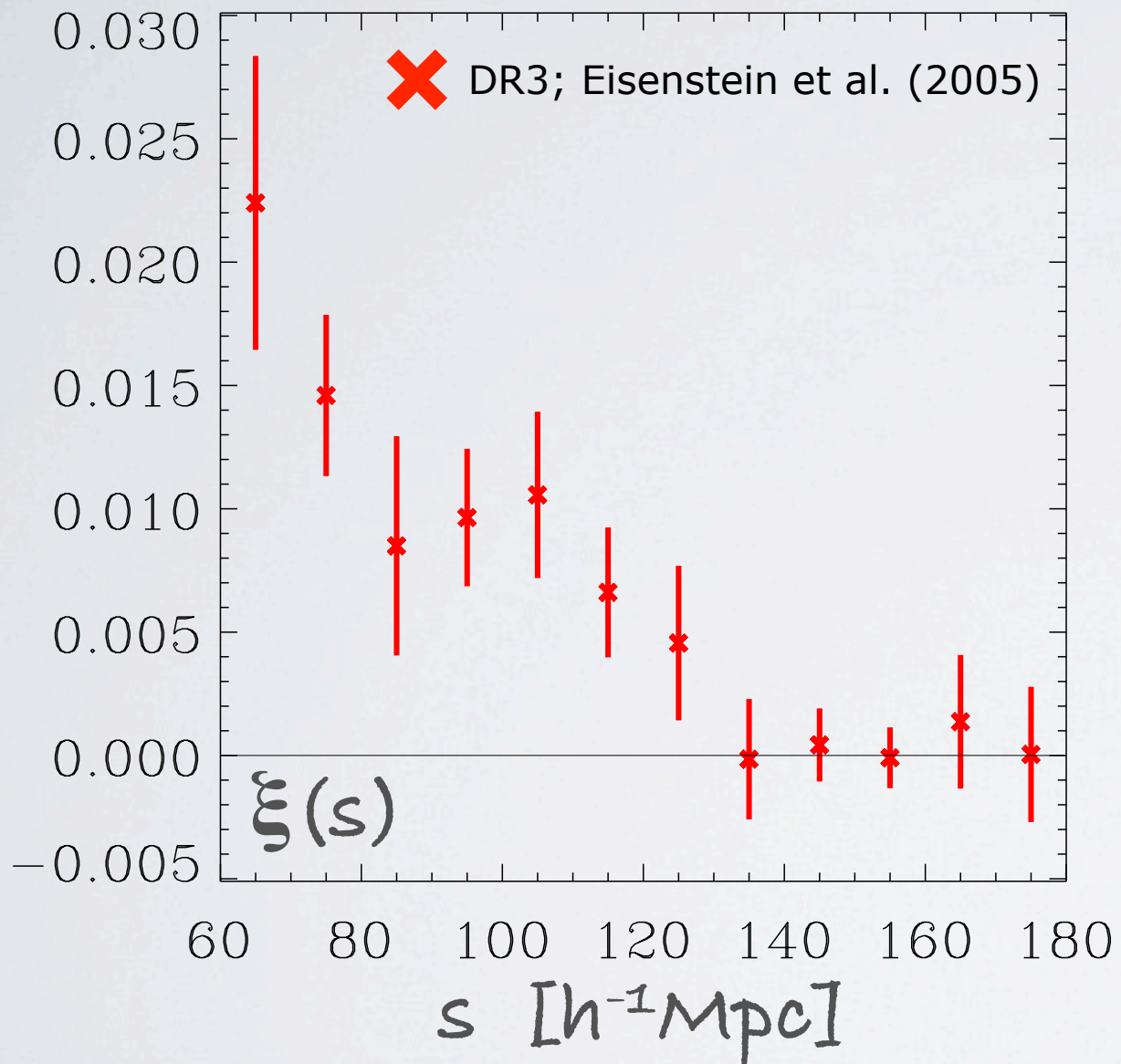
$$\sigma \propto (\sqrt{V}^{-1}) (P(k) + n^{-1})$$





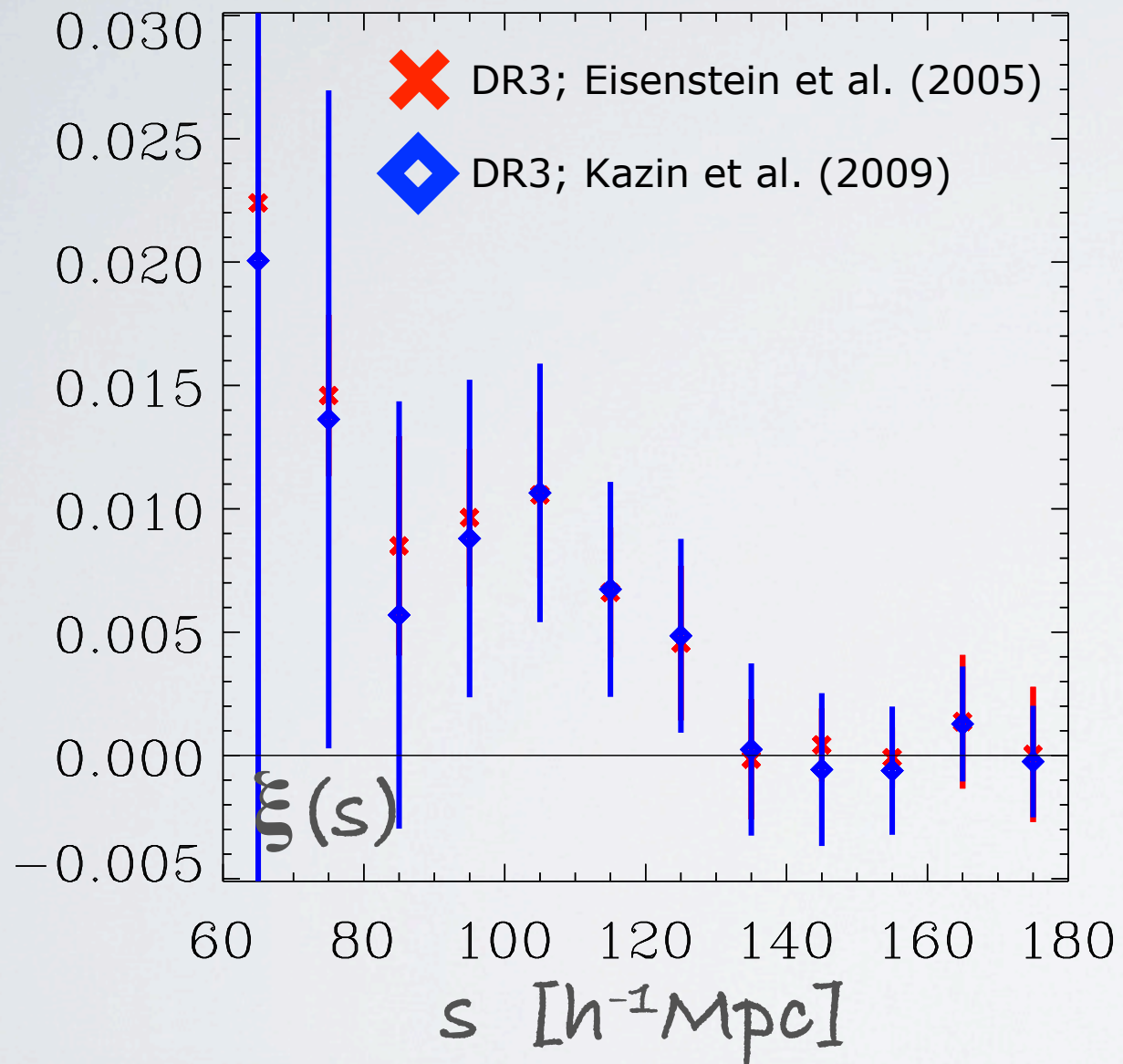
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*2005: Detection!*



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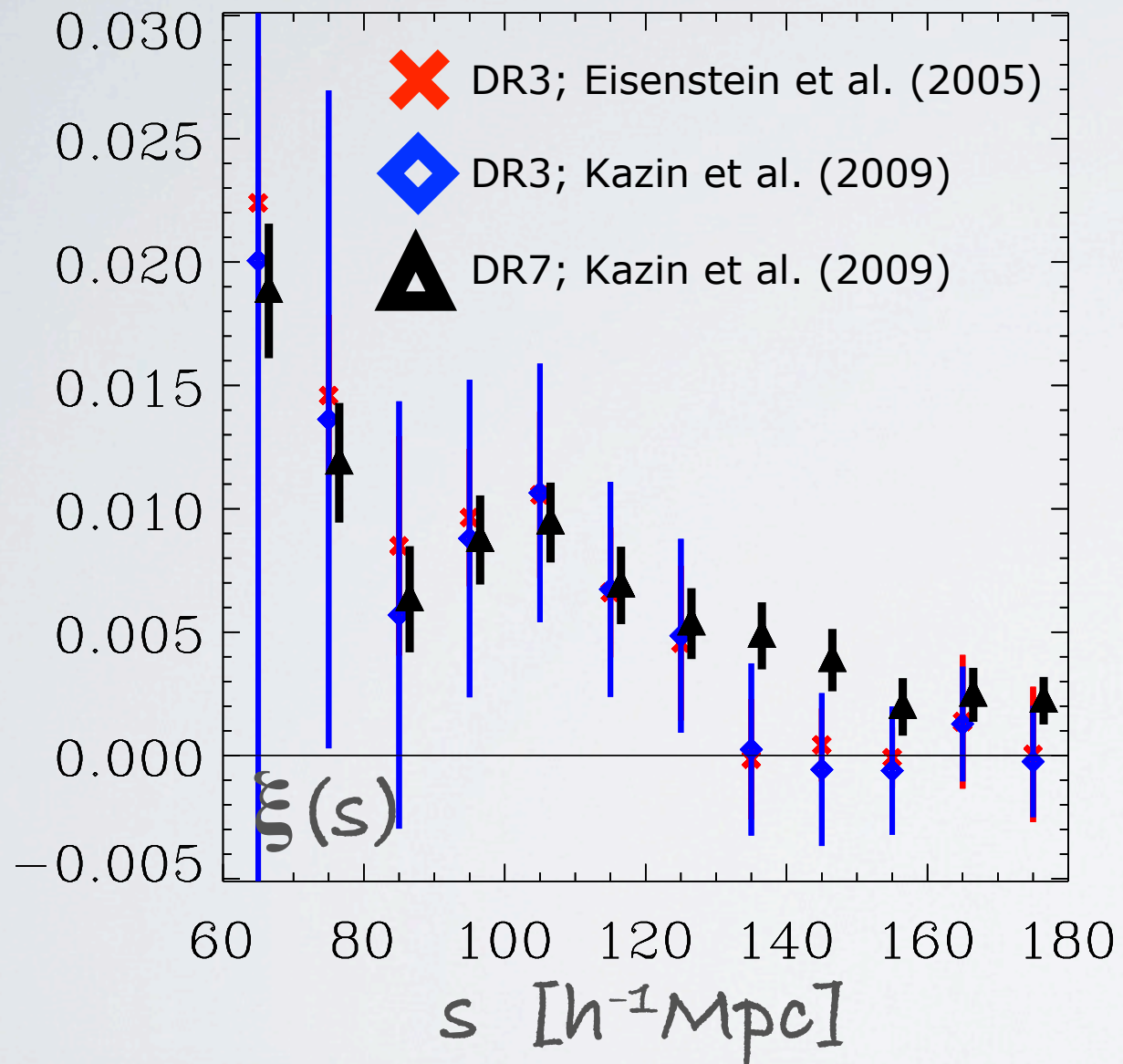
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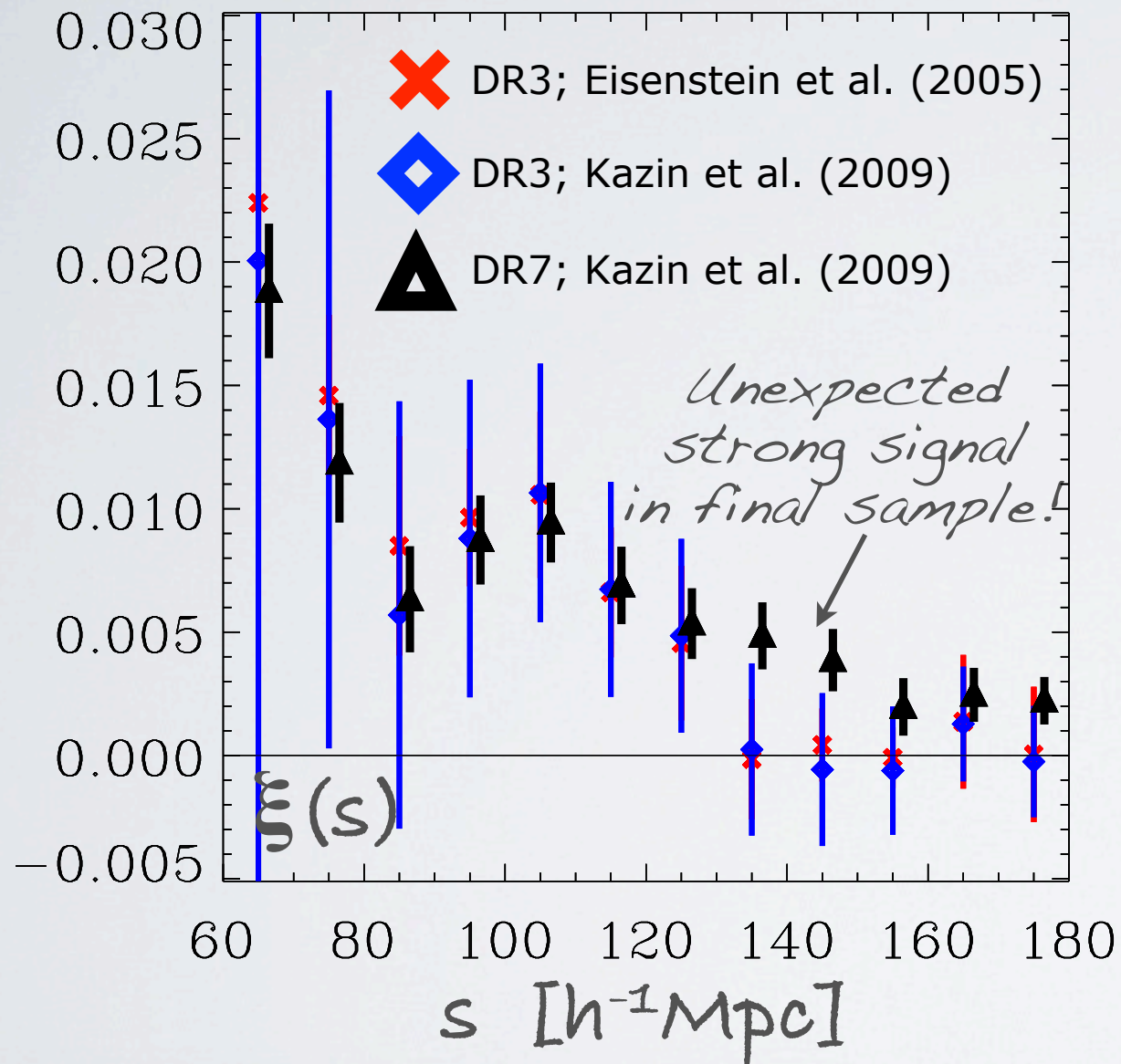
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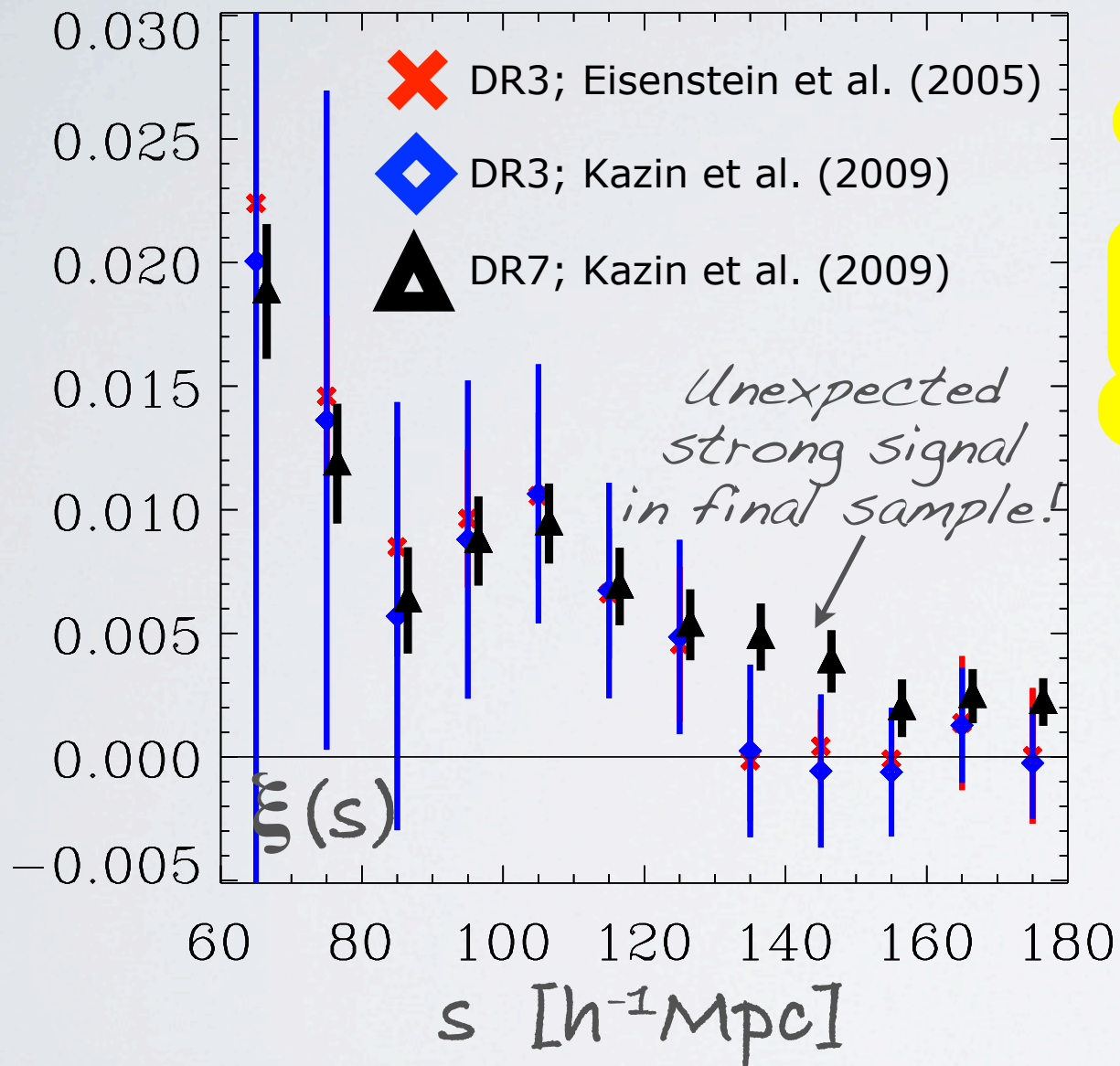


Unexplained strong signal on large scales  
when analyzing volumes larger than DR3



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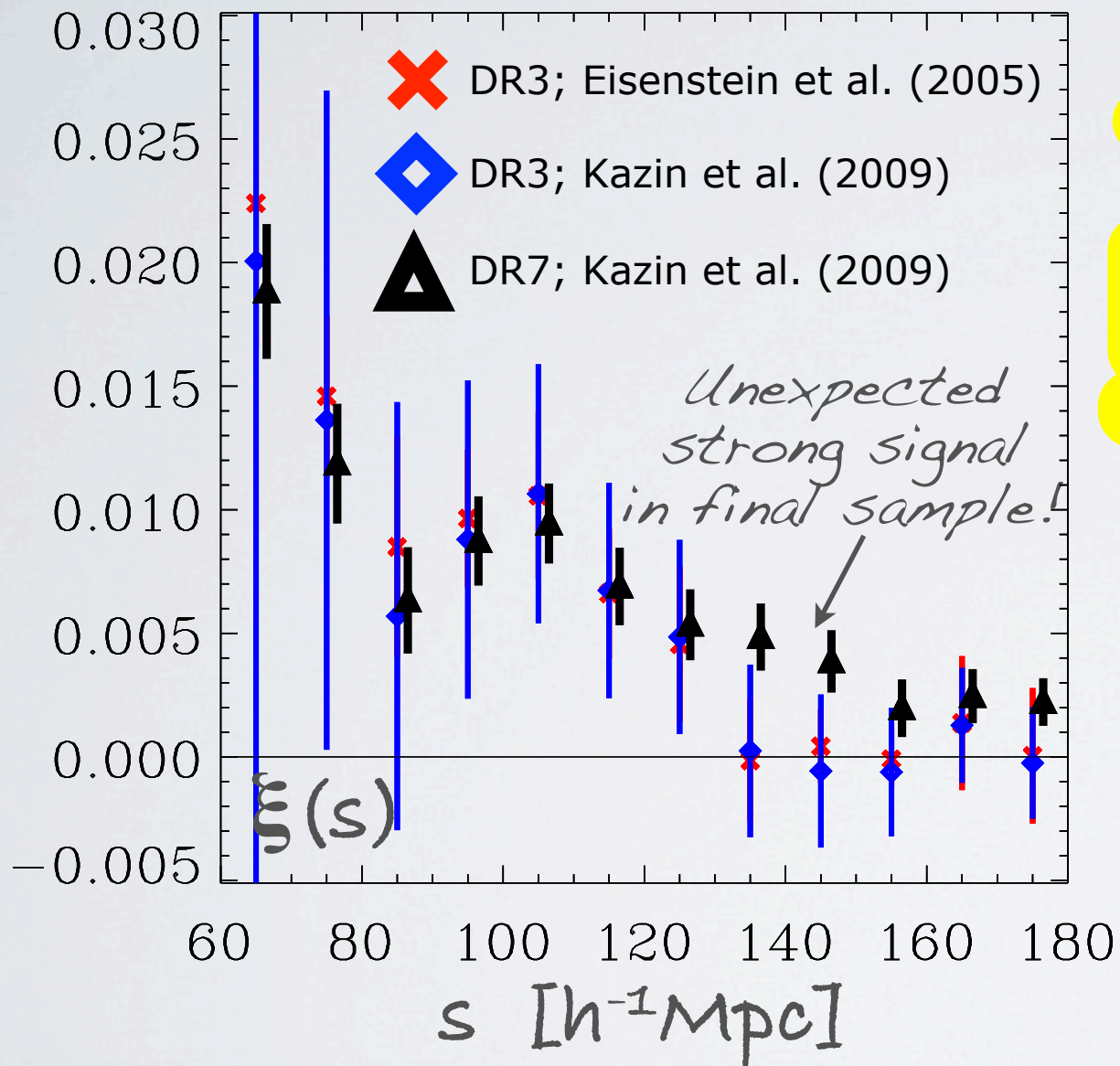
From Blake et al. (2007)

- We measure a hint of excess power relative to the best-fitting cosmological model on the largest scales (the lowest multipole bands in the four redshift slices in Figure 10). If confirmed, this excess power has a range of possible causes: (1) residual systematic errors; (2) cosmic variance; (3) large-scale galaxy biasing mechanisms; (4) new early-Universe physics.

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Unexplained strong signal on large scales when analyzing volumes larger than DR3



Large scale signal difference- Not due to systematics



# LasDamas Mock Simulations

Andreas Berlind  
Michael Busha  
Jeff Gardner  
Cameron McBride  
Román Scoccimarro  
Frank van den Bosch  
Risa Wechsler

$\xi(s \sim \text{BA feature scale})$



$s [h^{-1} \text{Mpc}]$

<http://lss.phy.vanderbilt.edu/lasdamas/>

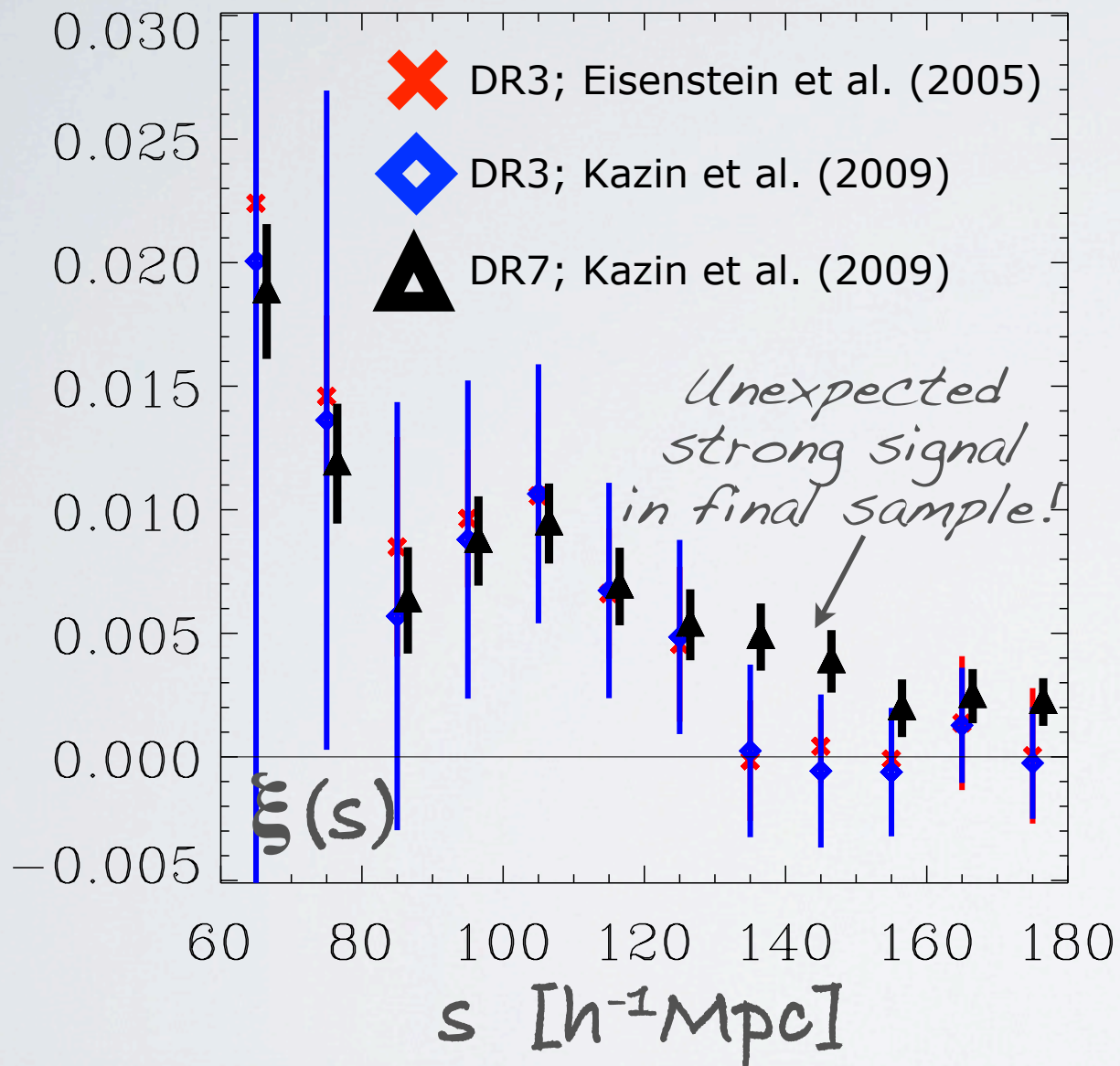
- Large Suite of DM sims
- We use: 160 SDSS-II mock LRG realizations
- Emphasize on many observational effects:
  - Light-cone, z-space
  - SDSS-II geometry
  - Radial selection function
- Results in **most realistic uncertainties** of clustering measurements to date

McBride et al.; in prep.

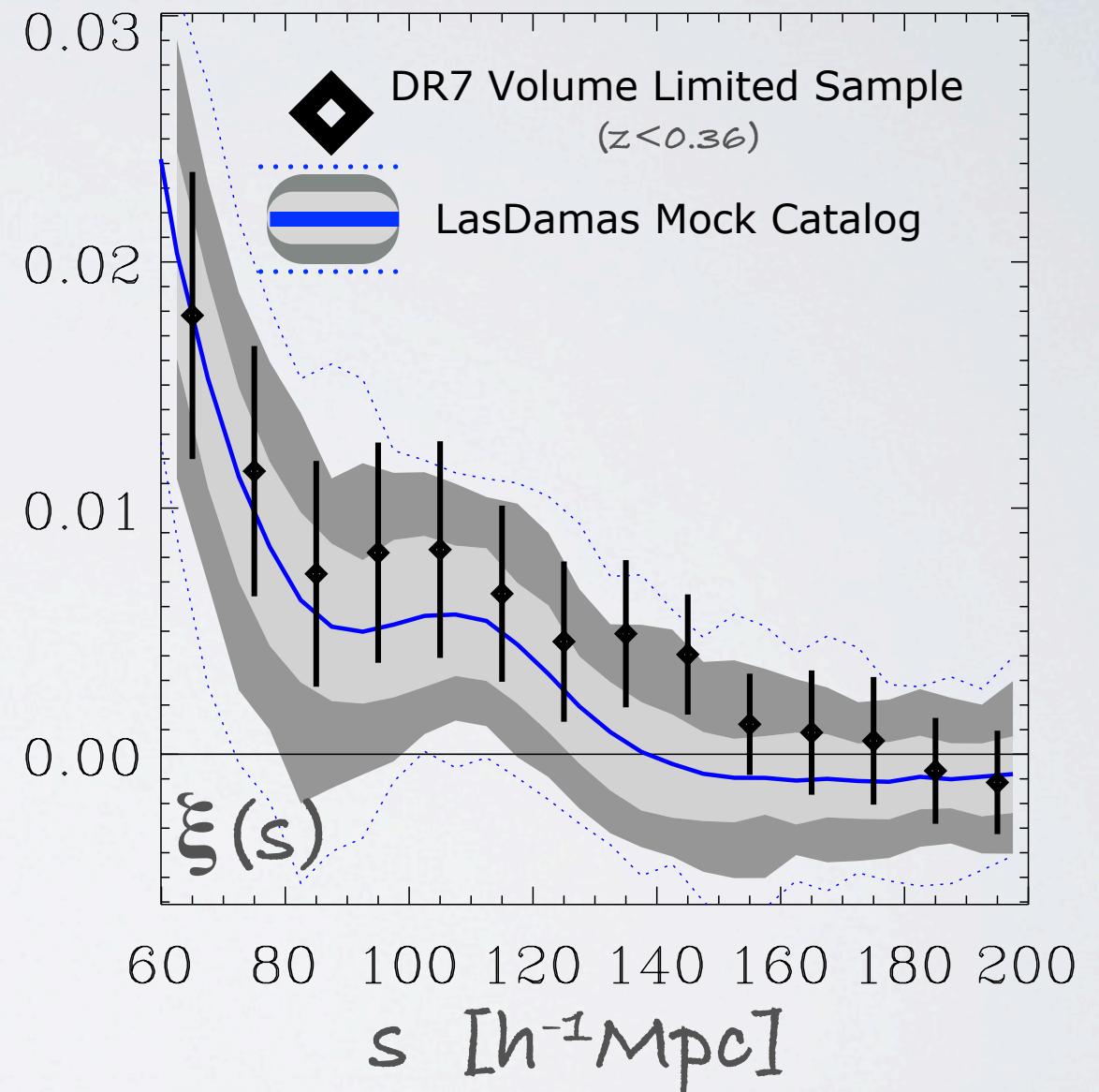


# Baryonic Acoustic Feature in SDSS LRGs MONOPOLE

## SDSS-III (BOSS) Prediction



## SDSS-II Results



Unexplained strong signal on large scales when analyzing larger volumes than DR3

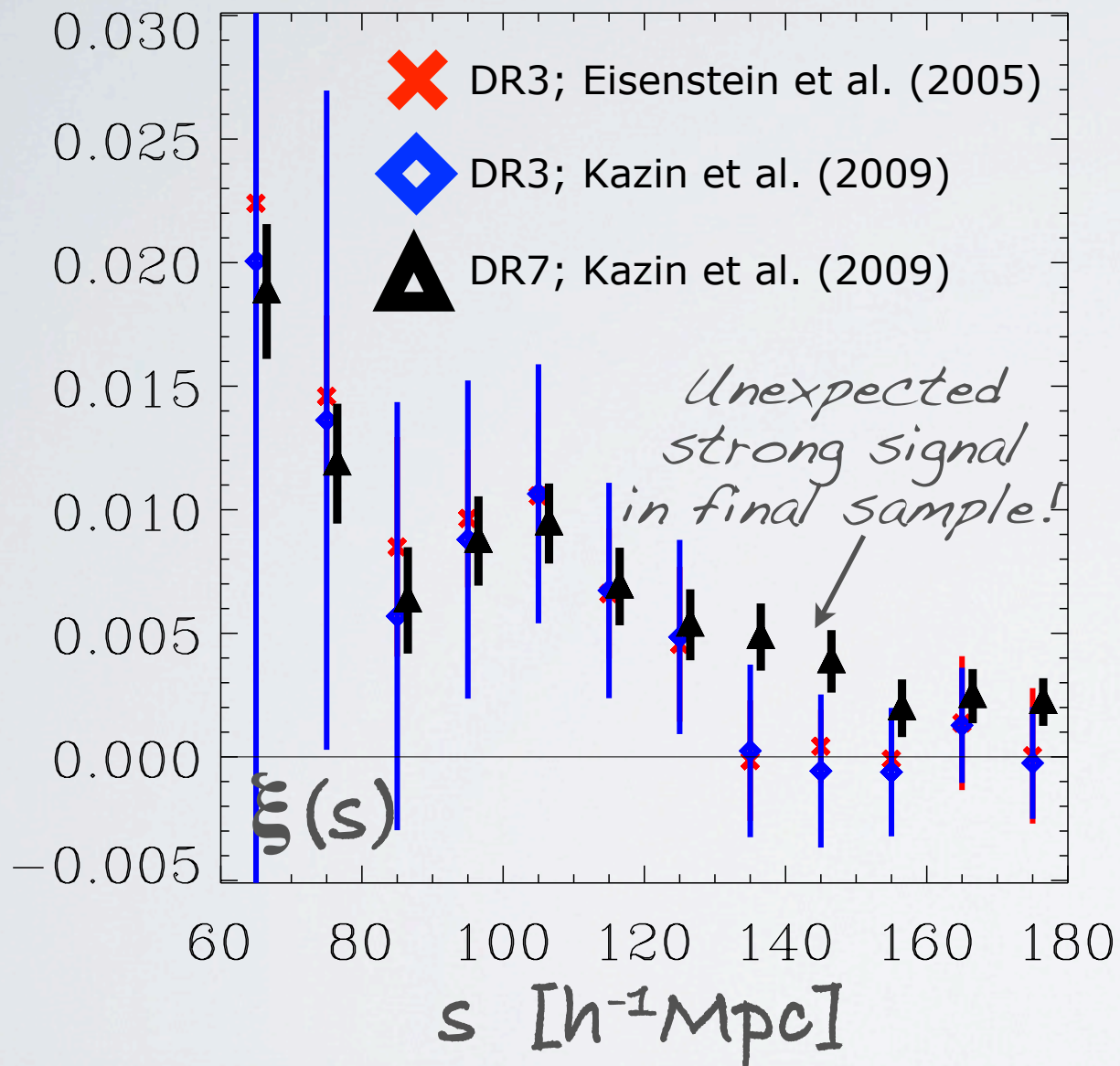


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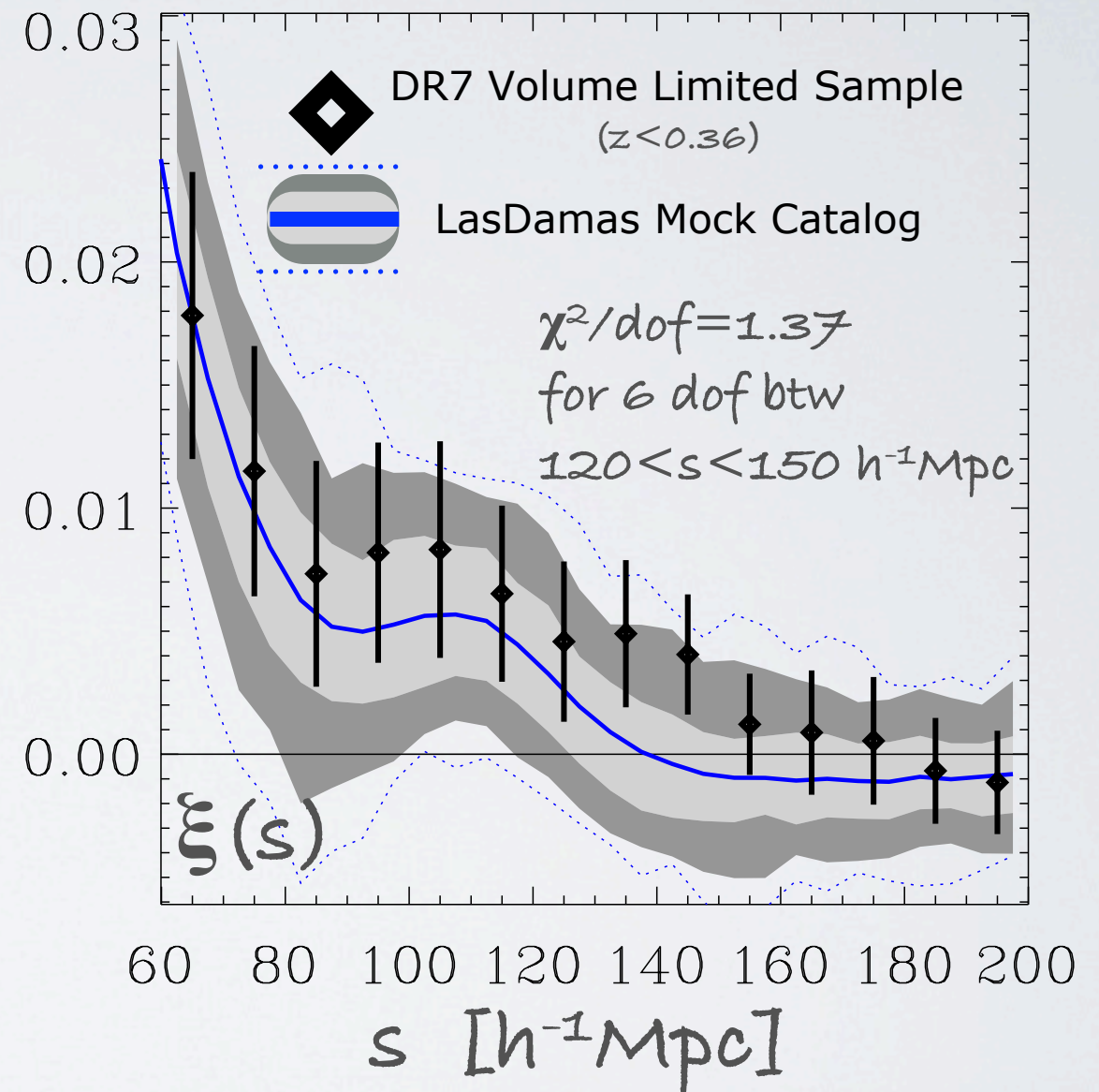


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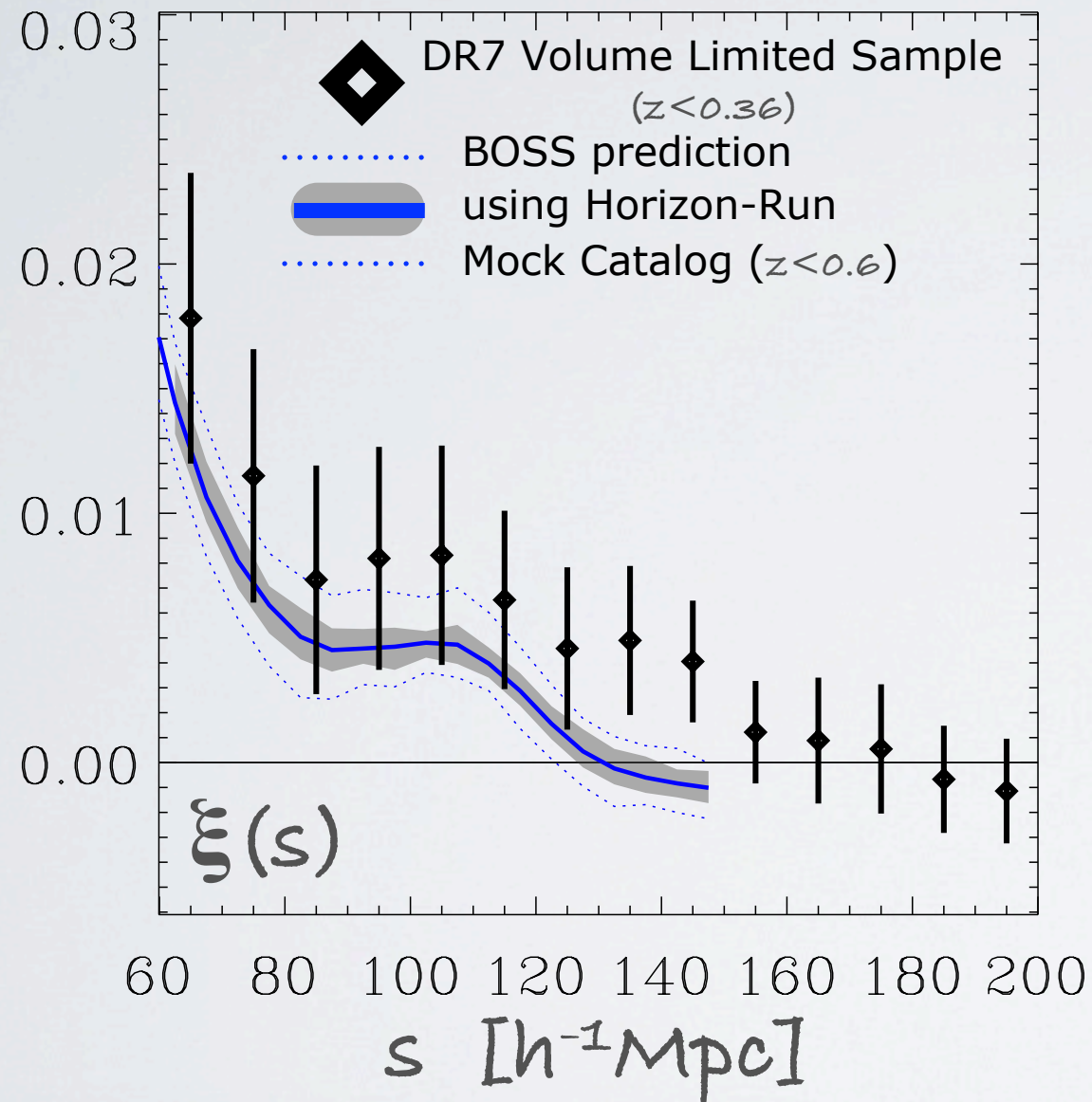
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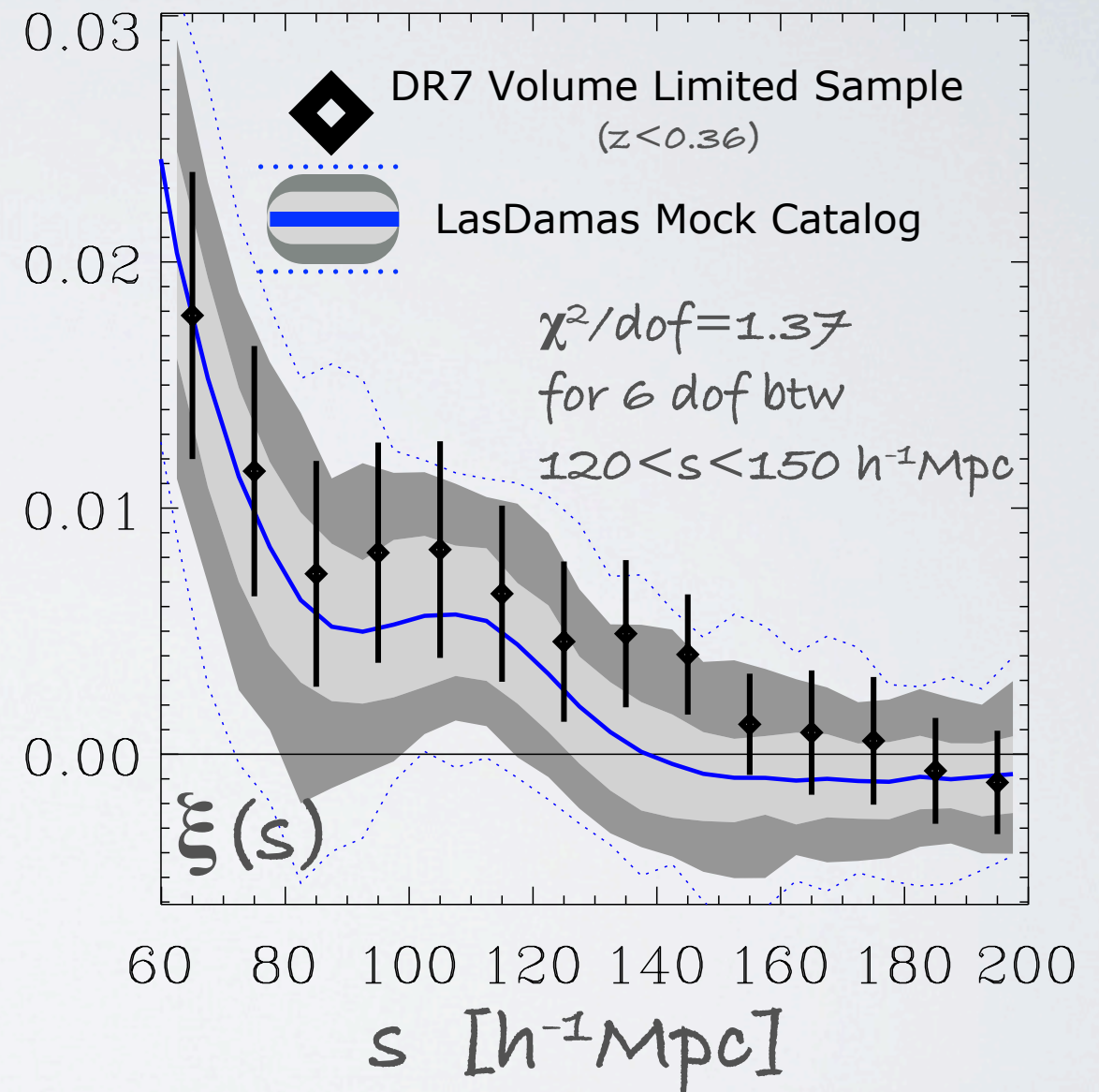
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 $\Lambda$ CDM is consistent with data within  $1.5\sigma$

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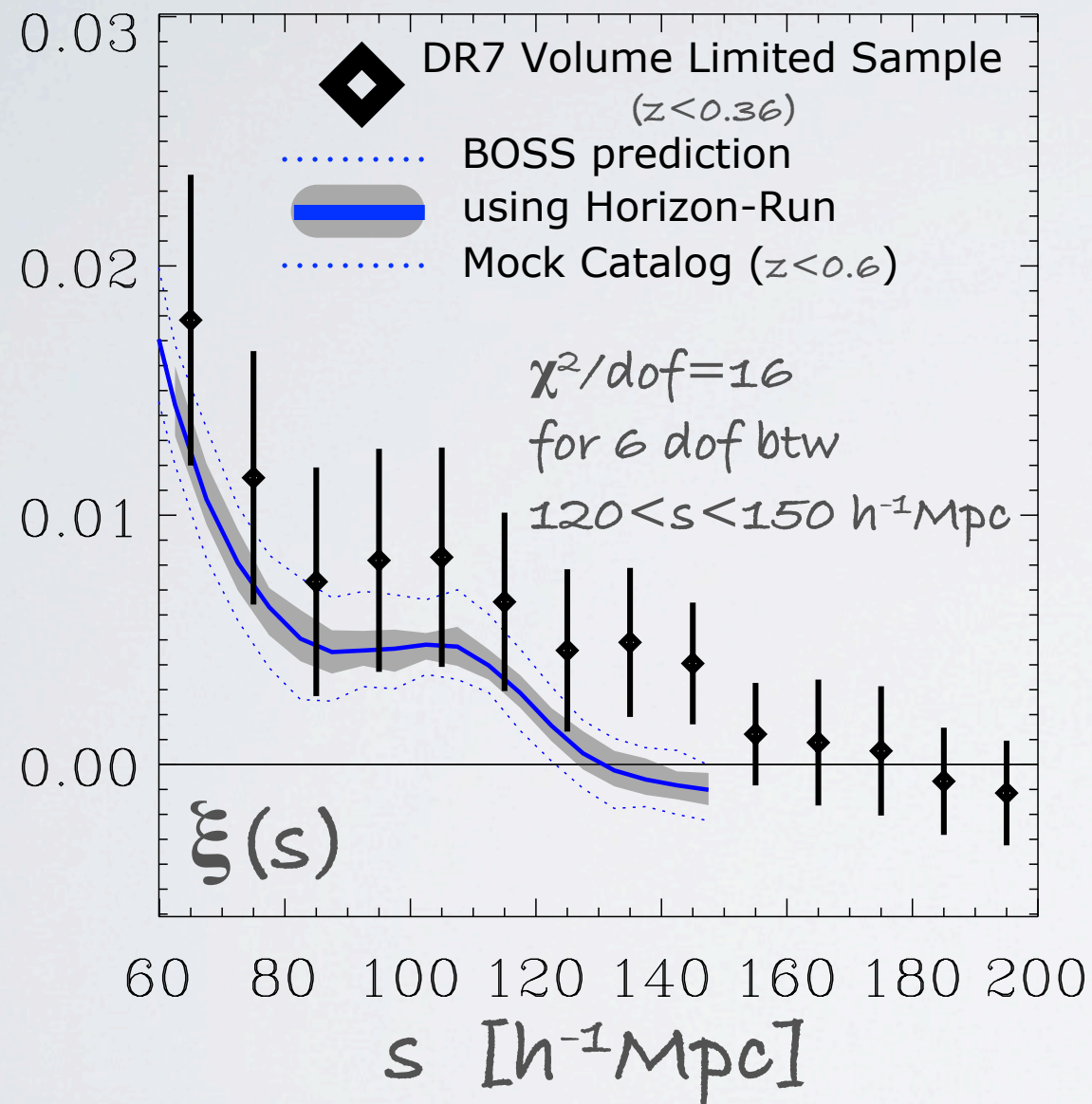


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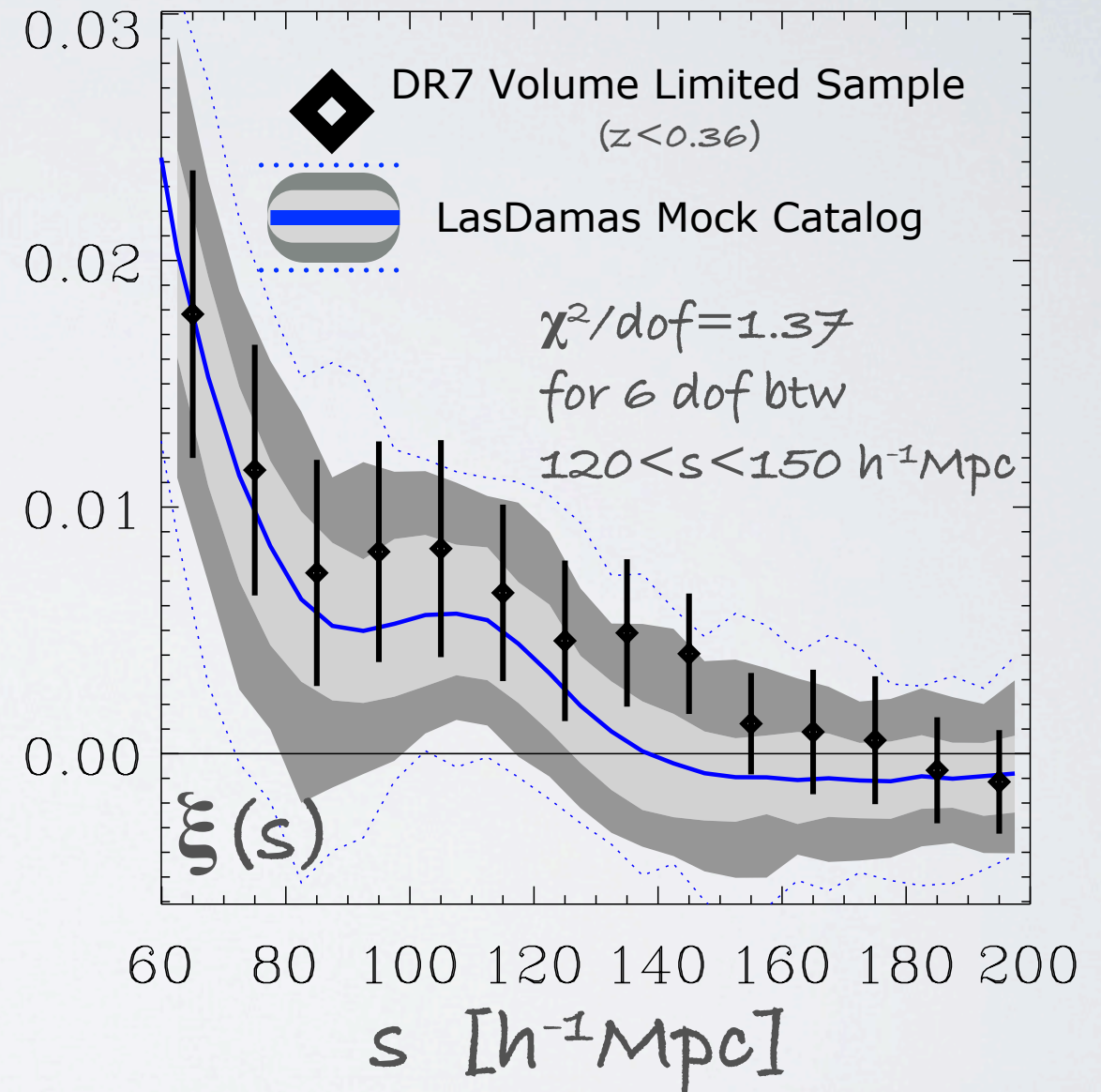


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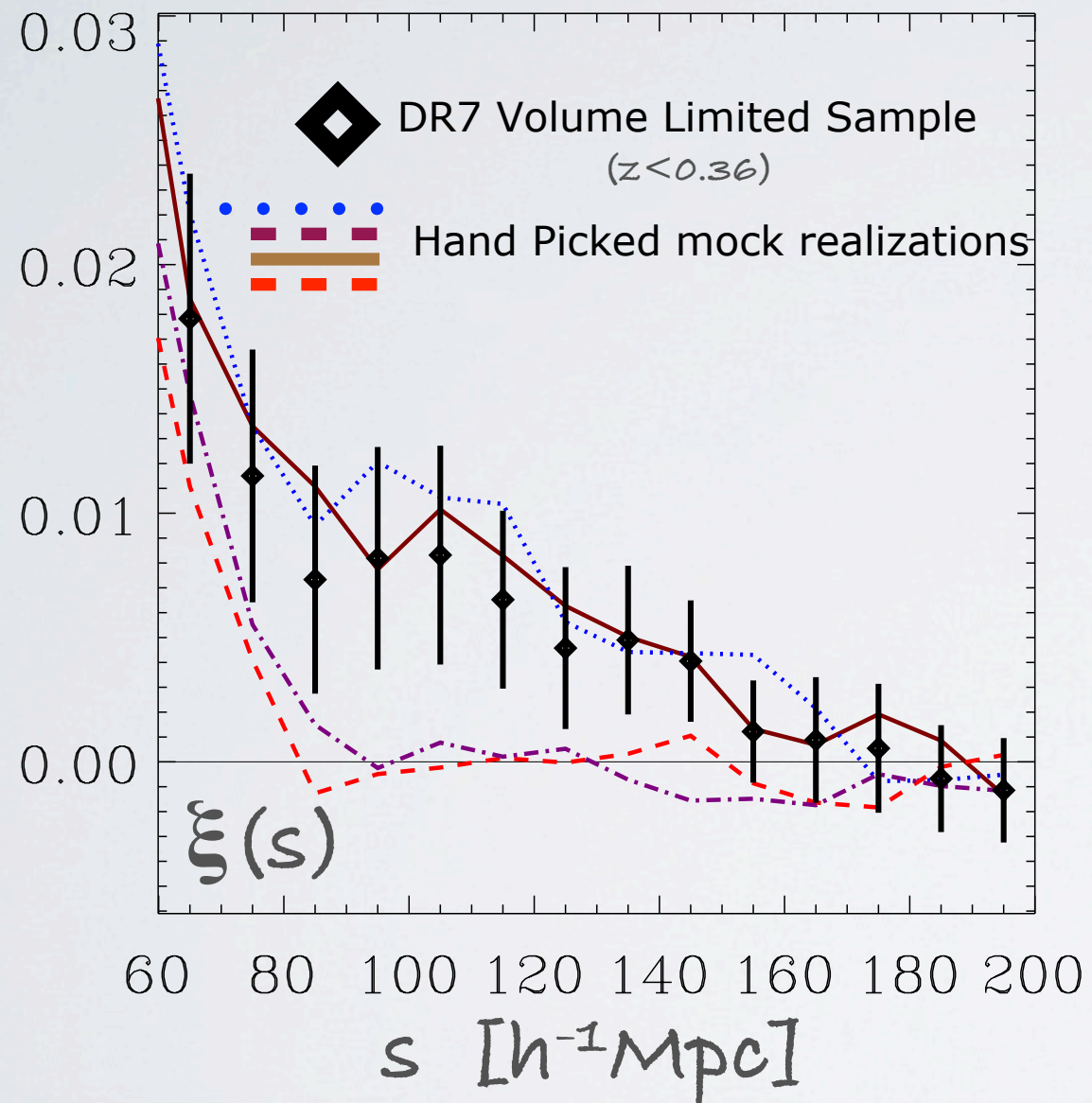


- According to  $\Lambda$ CDM, strong signal should not appear at a high CL
- Large scale signal difference- Not due to systematics
- $\Lambda$ CDM is consistent with data within  $1.5\sigma$

# Baryonic Acoustic Feature in SDSS LRGs MONOPOLE



SDSS-II volume mock catalogs indicate a  $>10\%$  chance of not detecting an apparent signature  
-based on mock catalogs provided by LasDamas (McBride et al.; in prep) and Horizon-Run mocks (Kim et al. 2009)-

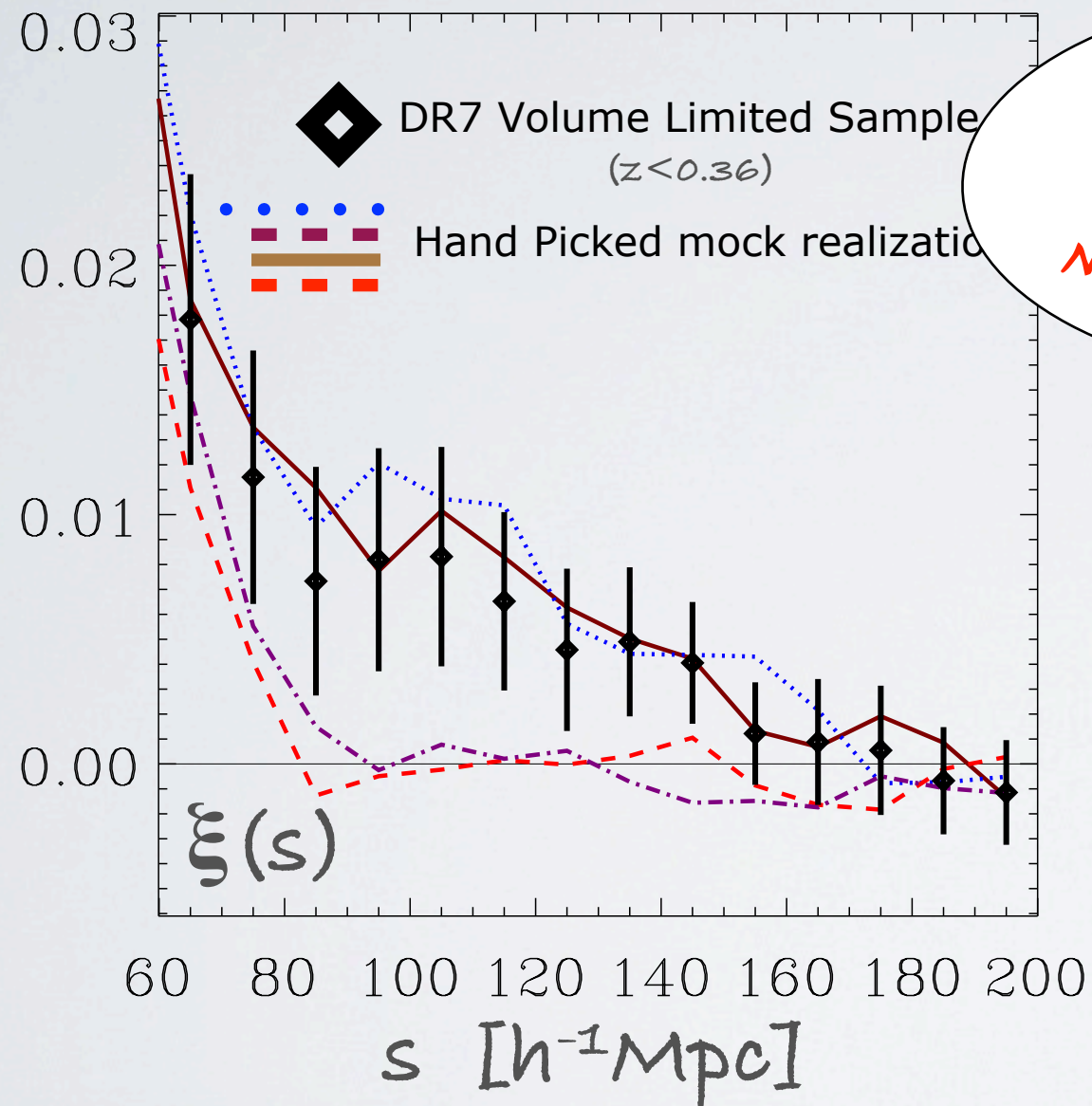




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So,  
do you feel  
*NOT UNlucky?*



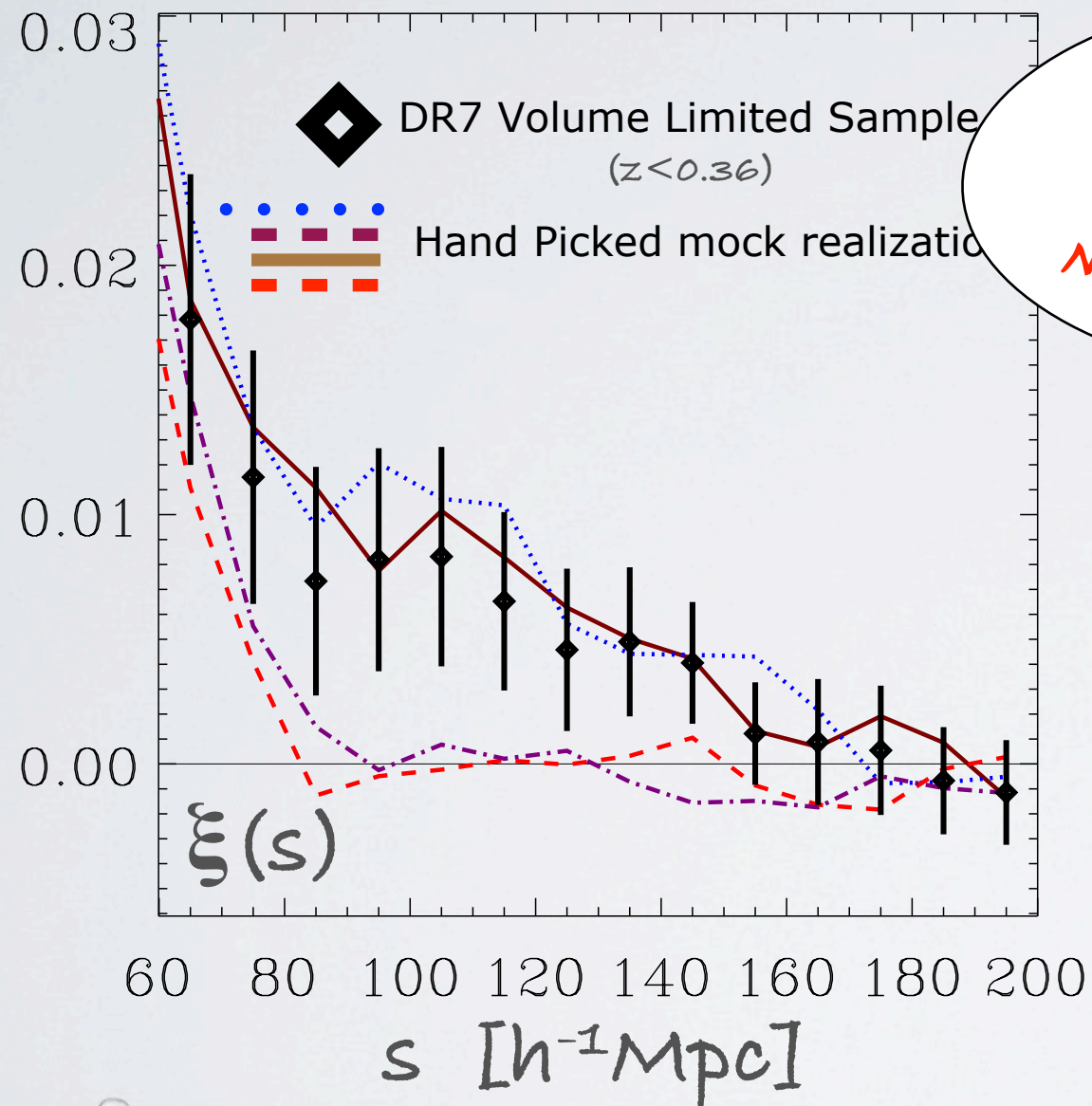
Dirty Harry (1971)



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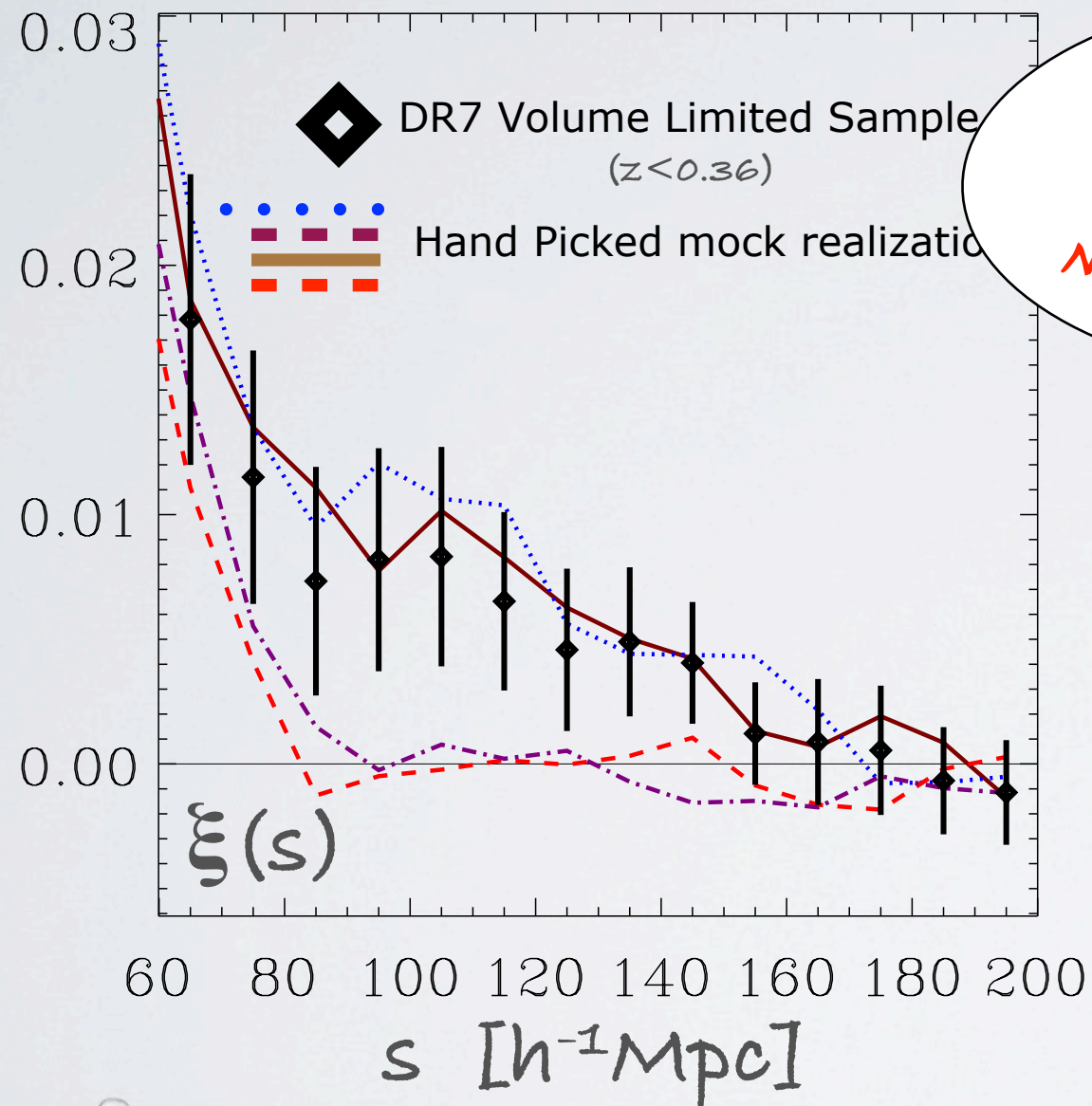
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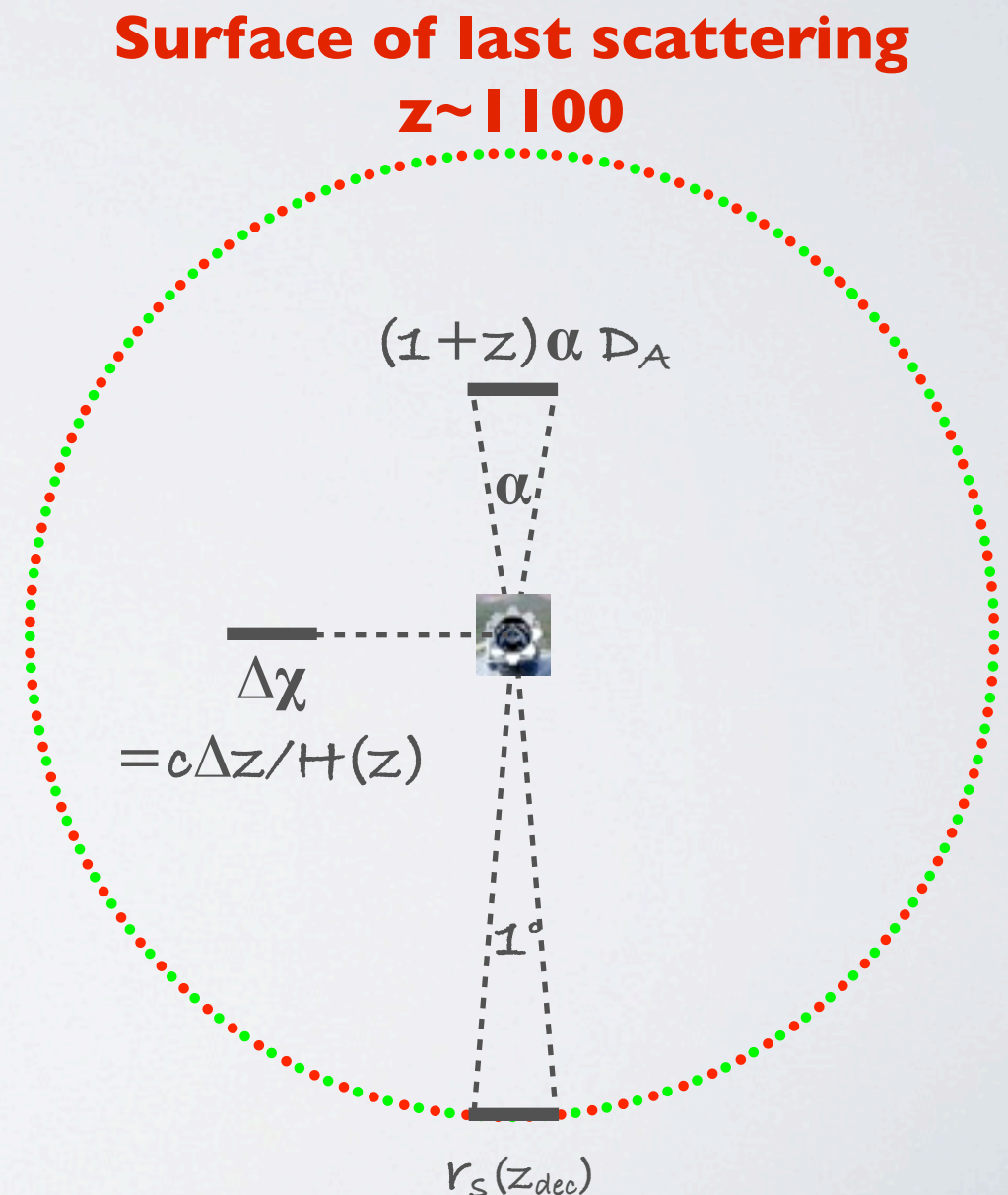


SDSS-II LRGs **do** reveal a Baryonic Acoustic Feature  
in various redshifts and luminosity cuts

# The Baryonic Acoustic Feature as a Standard Ruler

📌 Early Universe ( $z_{\text{dec}} \sim 1090$ ):  
CMB temp fluctuations determines  
 $r_s \sim 147 \text{ Mpc}$  ( $\delta r_s / r_s \sim 1.3\%$ ; Komatsu et al. 2009)

📌 Late Universe :  
Galaxy Clustering ( $z \sim 0.3, 0.6$ )  
QSOs Lyman- $\alpha$  Forest ( $z \sim 2.5$ )





# Baryonic Acoustic Feature on (and off) the defining Line of Sight

$$d = cz/H_0$$

Hubble's Law for proper distance

$$\chi = c \int dz' / H(z') \quad \text{comoving distance} \quad \chi = d(1+z)$$

$$D_A = \chi / (1+z) \quad \text{angular distance (not comoving!)}$$

## measuring

transverse feature  $s_{\perp} = \Delta\alpha D_A (1+z)$

line of sight feature  $s_{||} = \Delta\chi$

## yields ...

$$\int dz' / H(z') = s_{\perp} / \Delta\alpha / c$$

$$H(\langle z \rangle) \sim c \Delta z / s_{||}$$

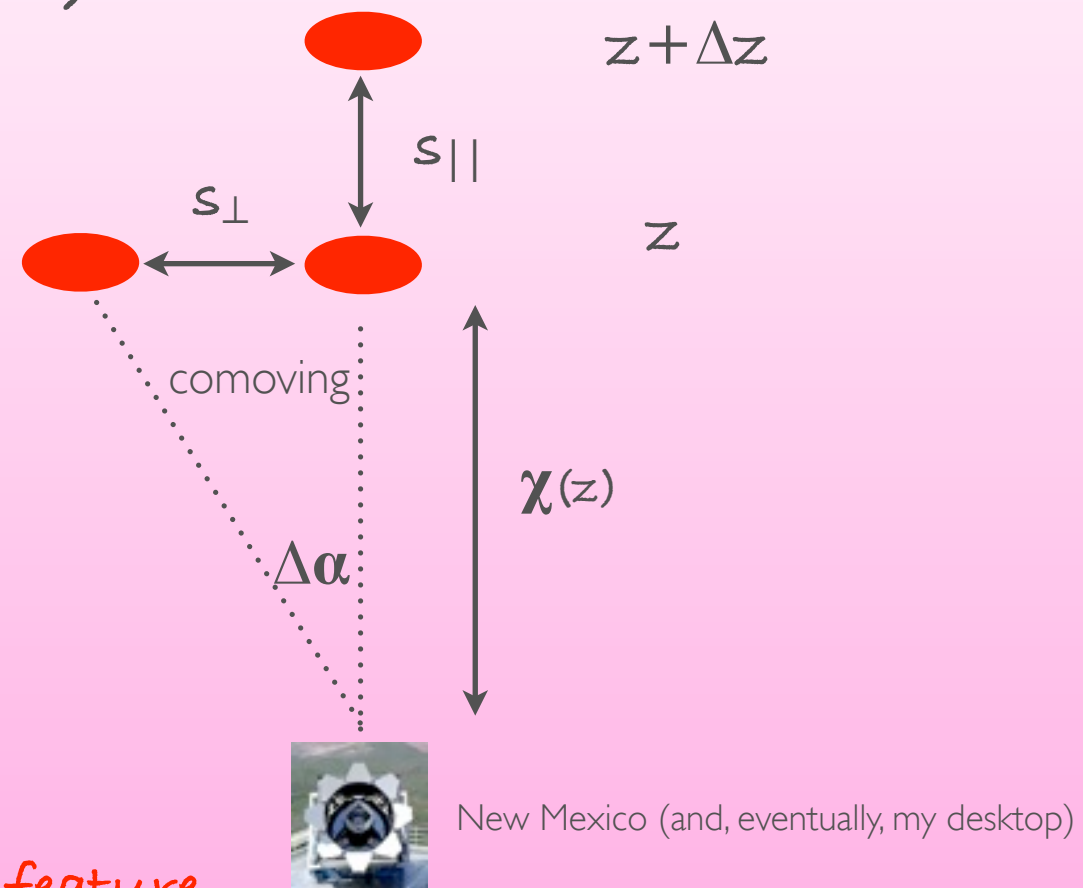
measurable with BA feature  
known knowns...

## meaning

$s_{\perp}$  constrains integral (a lot of degeneracy)

$s_{||}$  constrains  $H$  at a specific redshift!

Can constrain expansion rate!!





BUT....

Line of sight signal is **Noisy**  
(I will show this soon... promise...)

SO....

by using the  
angle averaged signal  
 $\langle \xi \rangle$  (aka monopole),

$$\langle \xi \rangle \equiv \int \xi(s, \theta) \sin(\theta) d\theta$$

we measure the Volume Average (effective) Distance

$$D_V(z) = [(1+z)^2 D_A^2 c / H(z)]^{1/3} \\ \propto [s_{\perp}^2 s_{\parallel}]^{1/3}$$

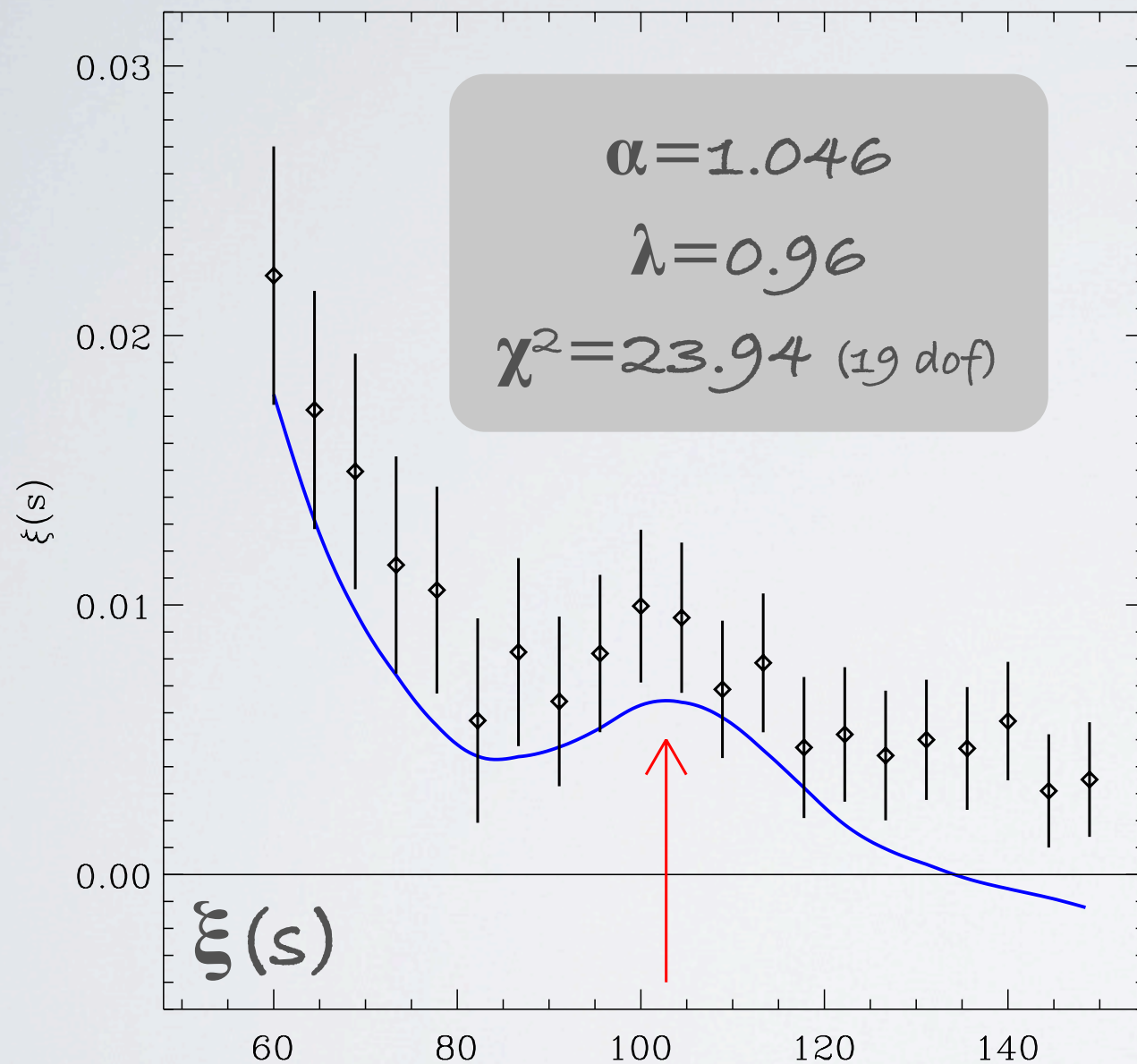
meaning  $\langle \xi \rangle$  constrains  $D_A^2 / H(z)$





# Pinpointing Baryonic Acoustic Feature Peak in SDSS LRGs Monopole

$$\xi_{\text{model}} = \lambda \xi_{\text{NL-theory}}(\alpha \cdot s)$$

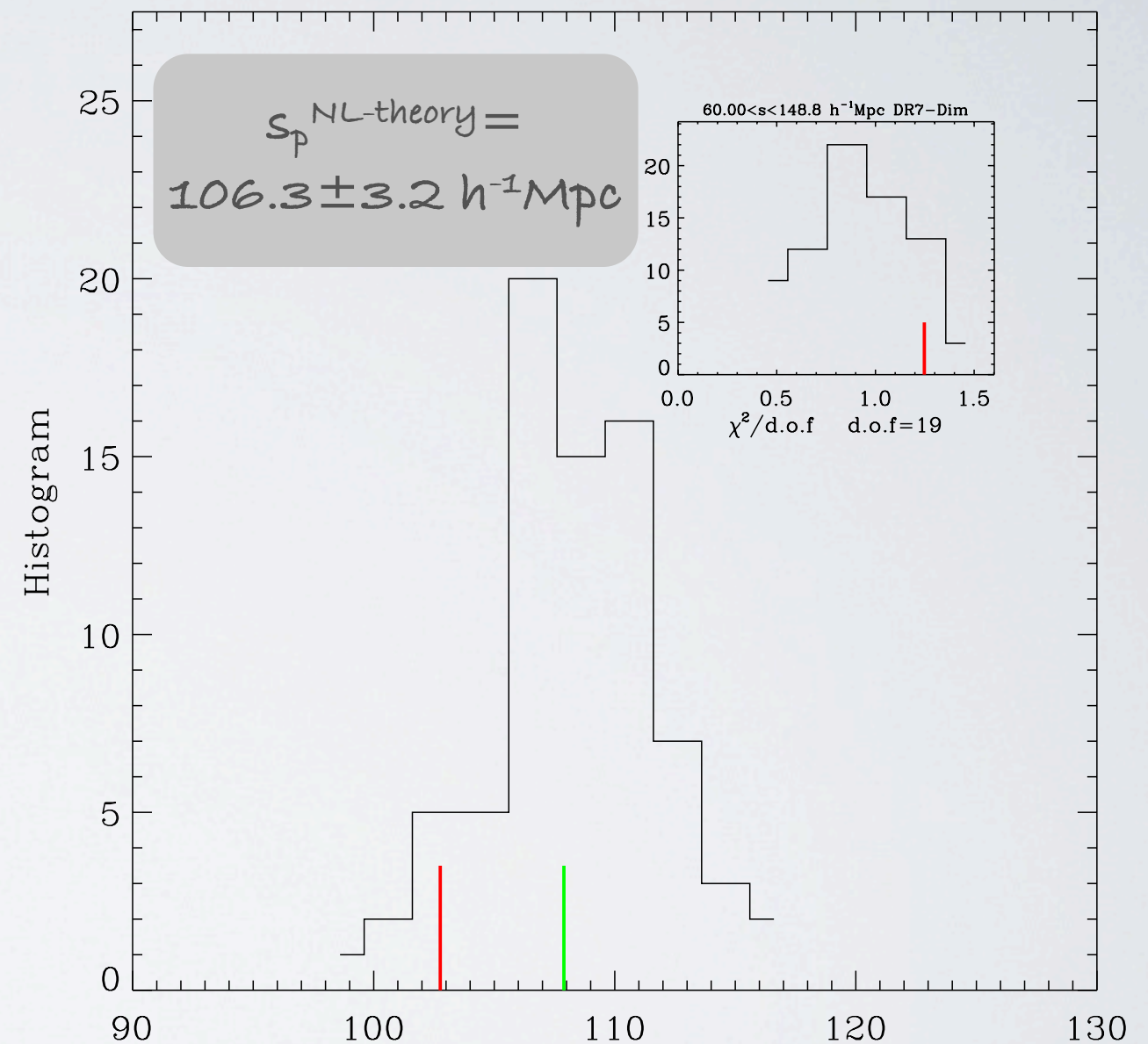


$s$  [ $h^{-1}\text{Mpc}$ ]

Peak position measured at

$$s_p = 101.6 \pm 3.0 \text{ } h^{-1}\text{Mpc}$$

## Peak Position Distribution in mocks



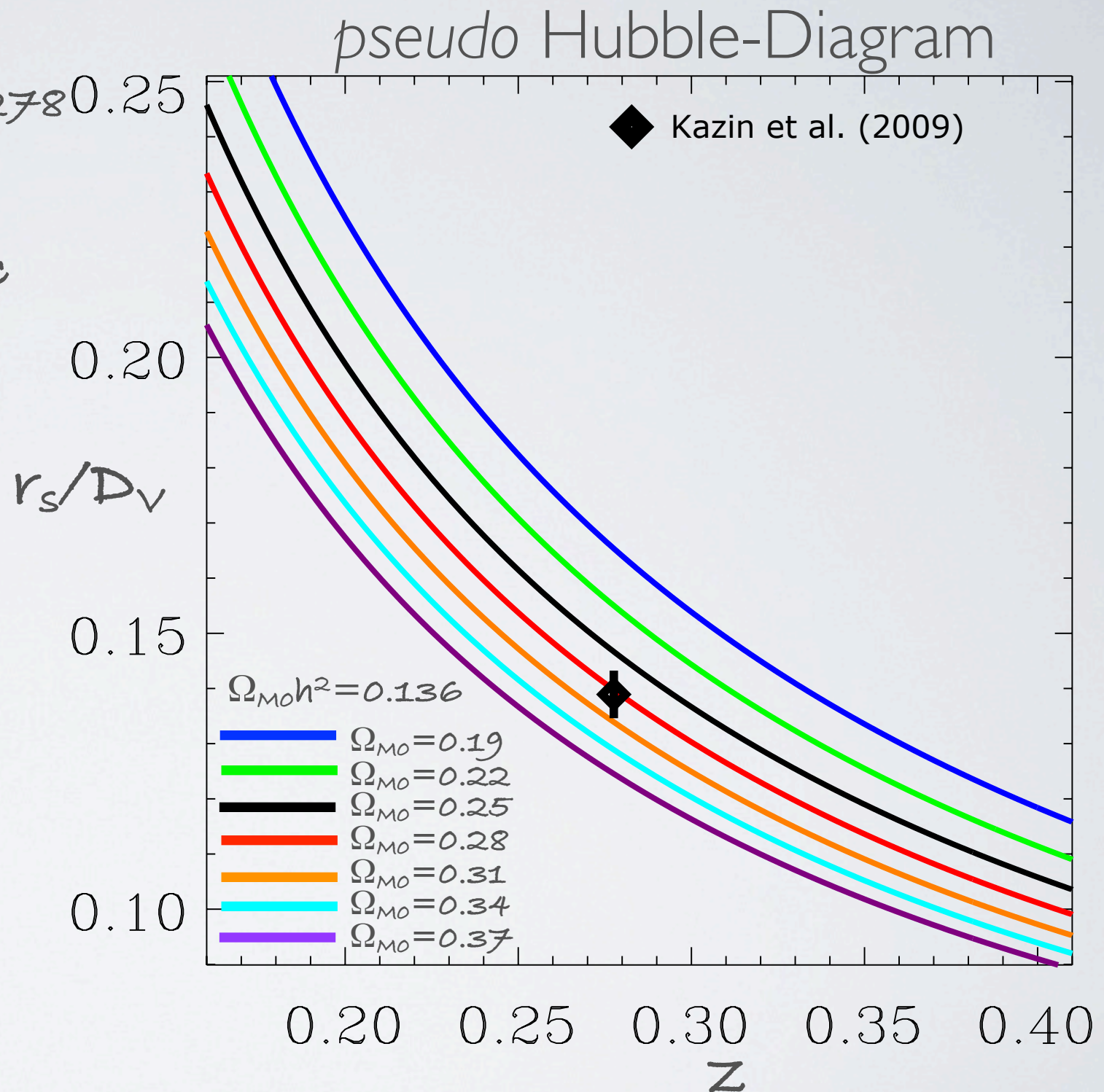
$s_p$  [ $h^{-1}\text{Mpc}$ ]

1σ uncertainties due to sample variance

# Baryonic Acoustic Feature in SDSS LRGs

## Monopole as a Standard Ruler

- Peak position yields  
 $r_s/D_V = 0.1389 \pm 0.043^* @ \langle z \rangle = 0.278$
- Applying  $r_s = 153.3$  Mpc (WMAP5; Komatsu et al.)  
 we obtain:  
 $D_V(\langle z \rangle = 0.278) = 1103 \pm 43$  Mpc
- Consistent with  
 $\Omega_{M0} = [0.25-0.34]$ ,  
 $h = [0.63-0.73]$



\* Method:

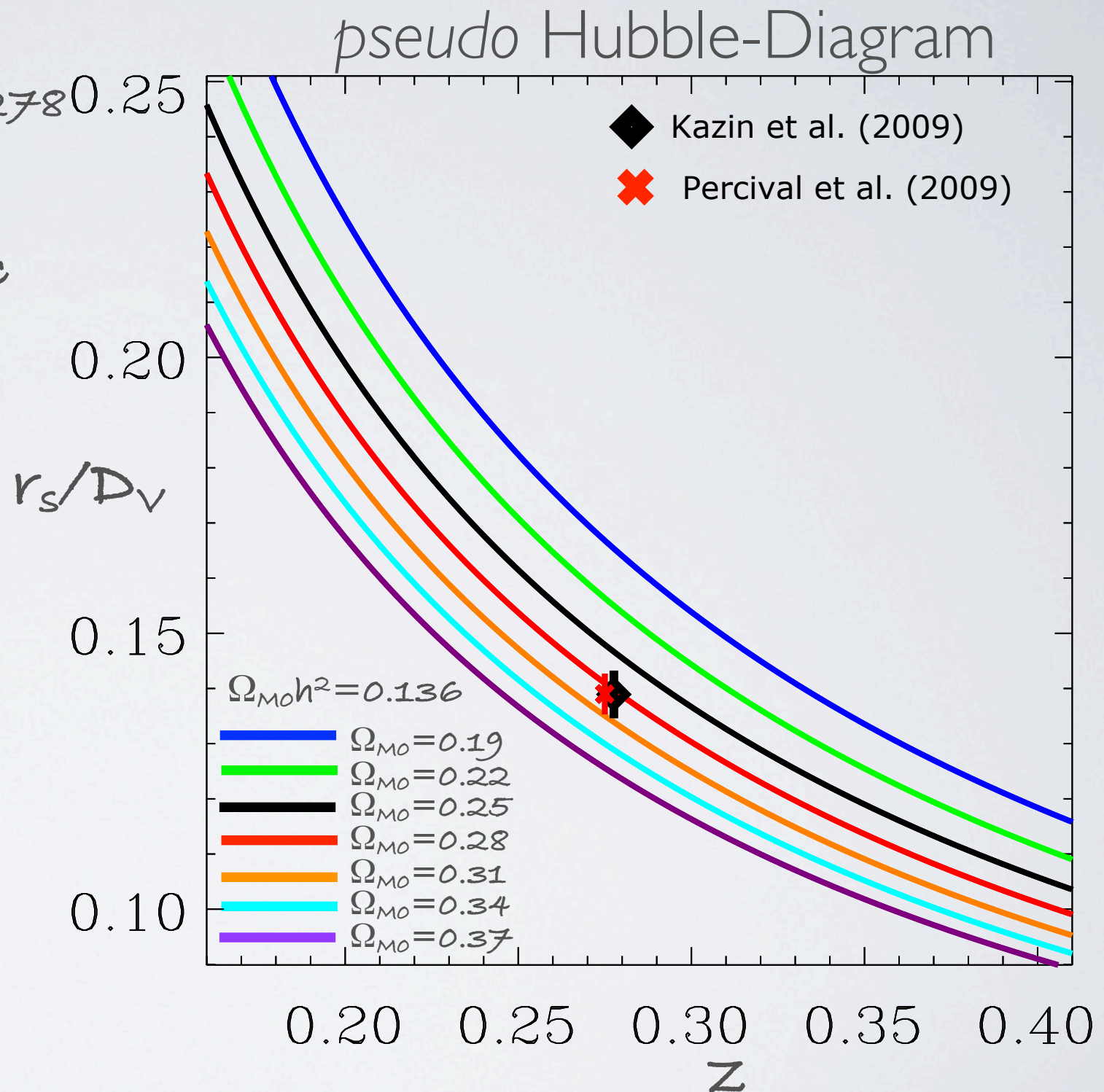
$$(D_V/r_s)^{\text{real}} = (D_V/r_s)^{\text{fiducial}} (s_p^{\text{fiducial}}/s_p^{\text{SDSS}})$$



# Baryonic Acoustic Feature in SDSS LRGs

## Monopole as a Standard Ruler

- Peak position yields  
 $r_s/D_V = 0.1389 \pm 0.043^* @ \langle z \rangle = 0.278$
- Applying  $r_s = 153.3 \text{ Mpc}$  (WMAP5; Komatsu et al.)  
 we obtain:  
 $D_V(\langle z \rangle = 0.278) = 1103 \pm 43 \text{ Mpc}$
- Consistent with  
 $\Omega_{M0} = [0.25-0.34]$ ,  
 $h = [0.63-0.73]$



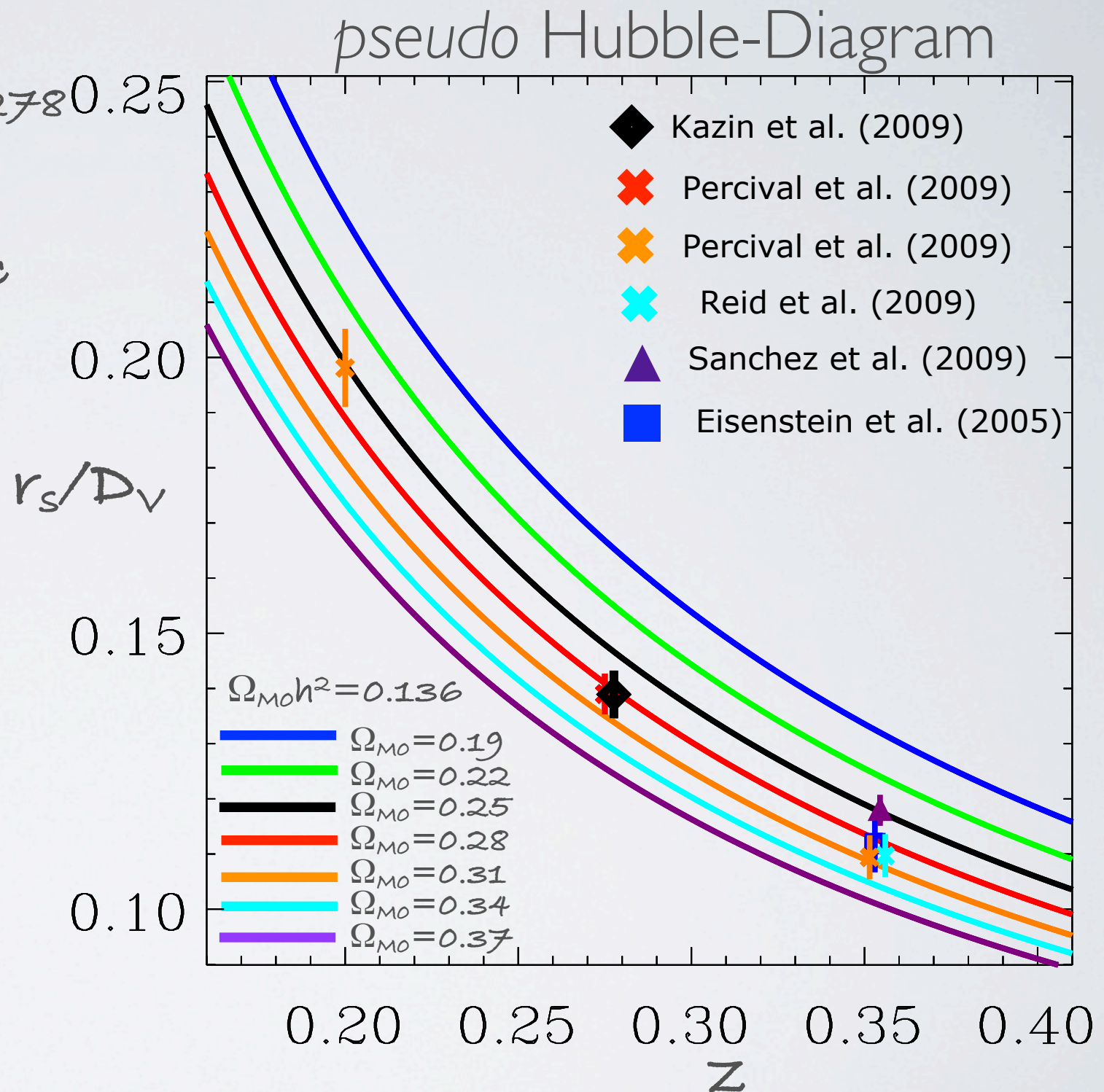
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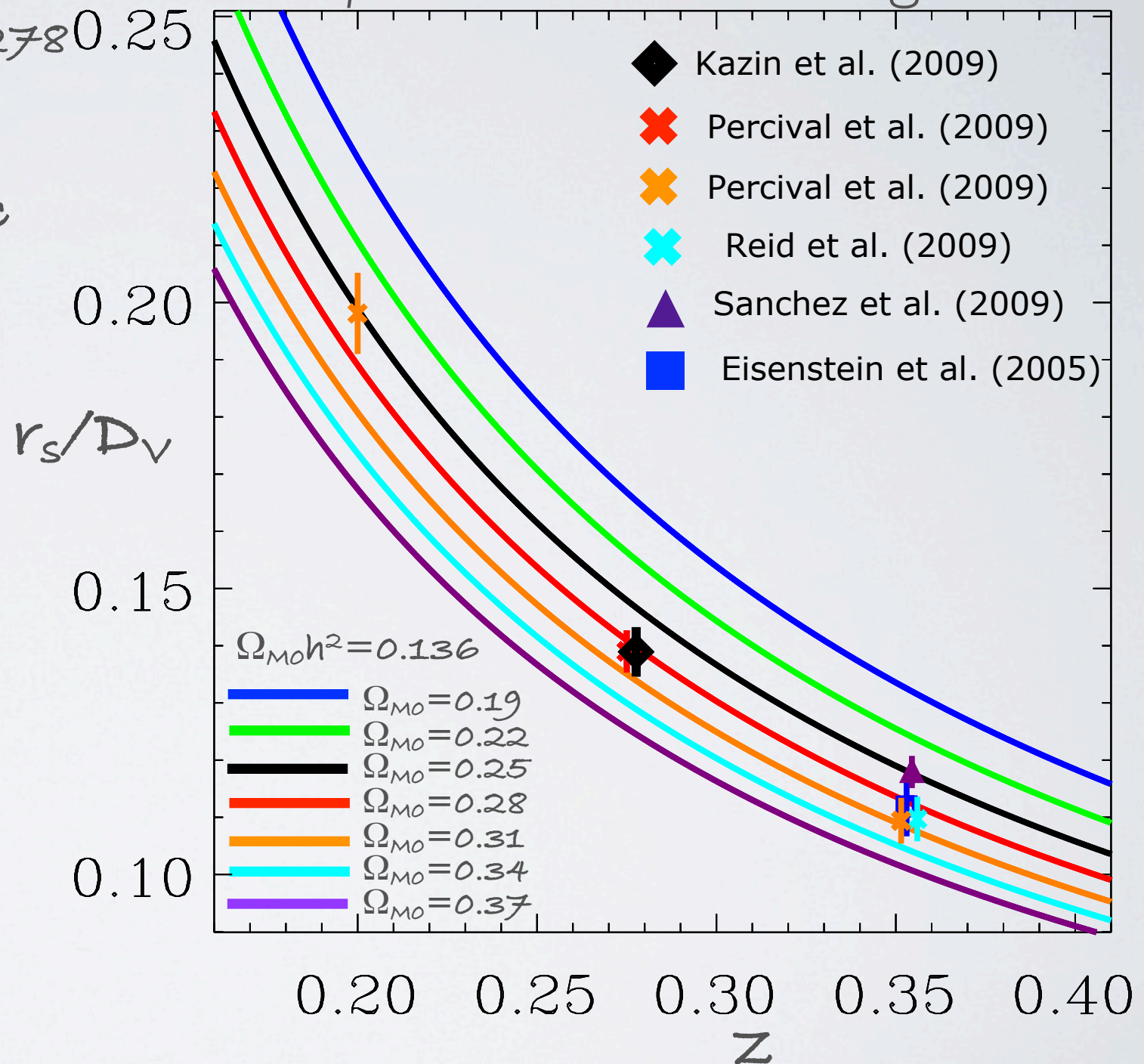
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*pseudo* Hubble-Diagram



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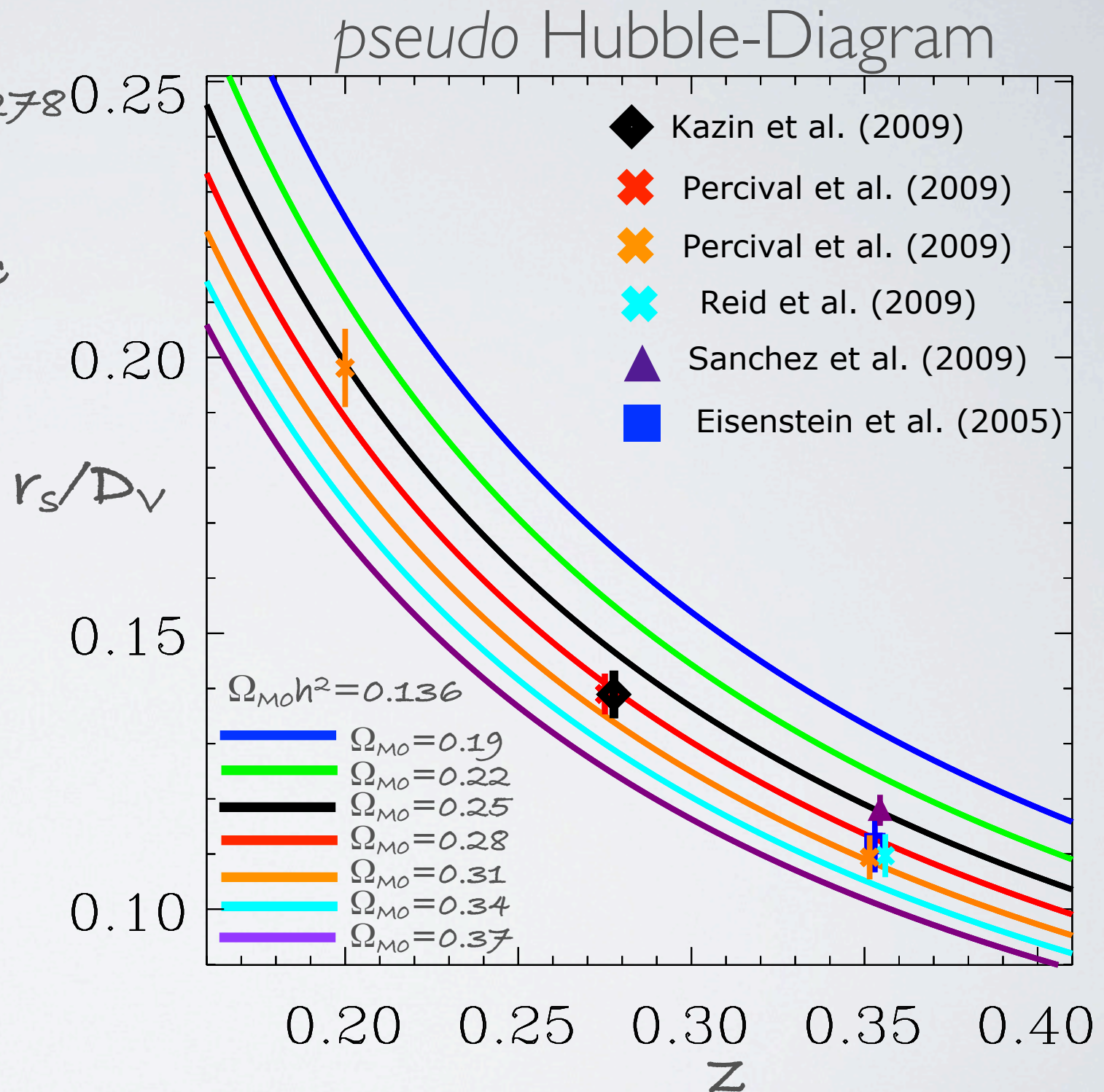
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**Kazin et al. 2009**  
**ApJ 710 (2010) 1444-1461**

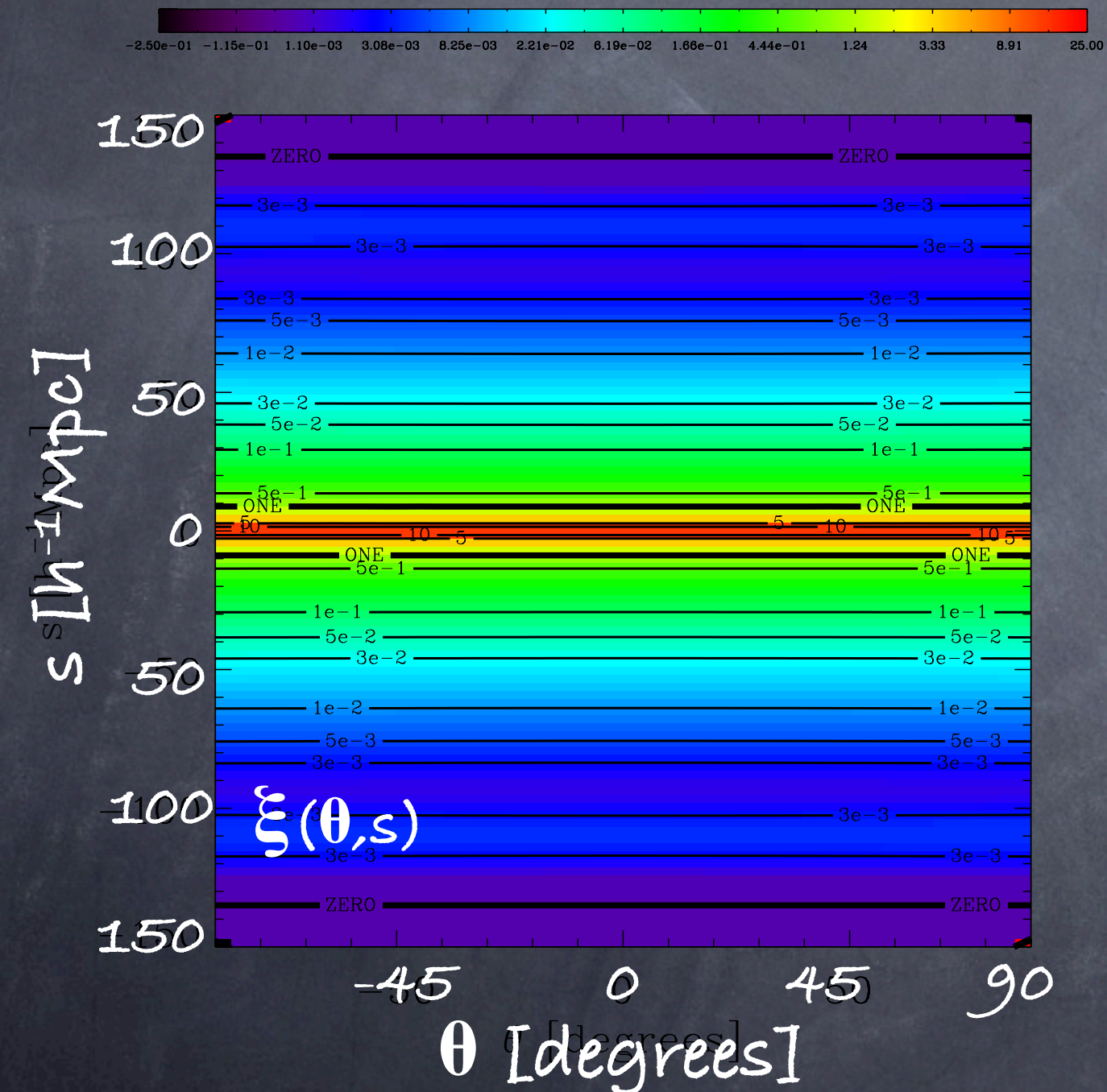
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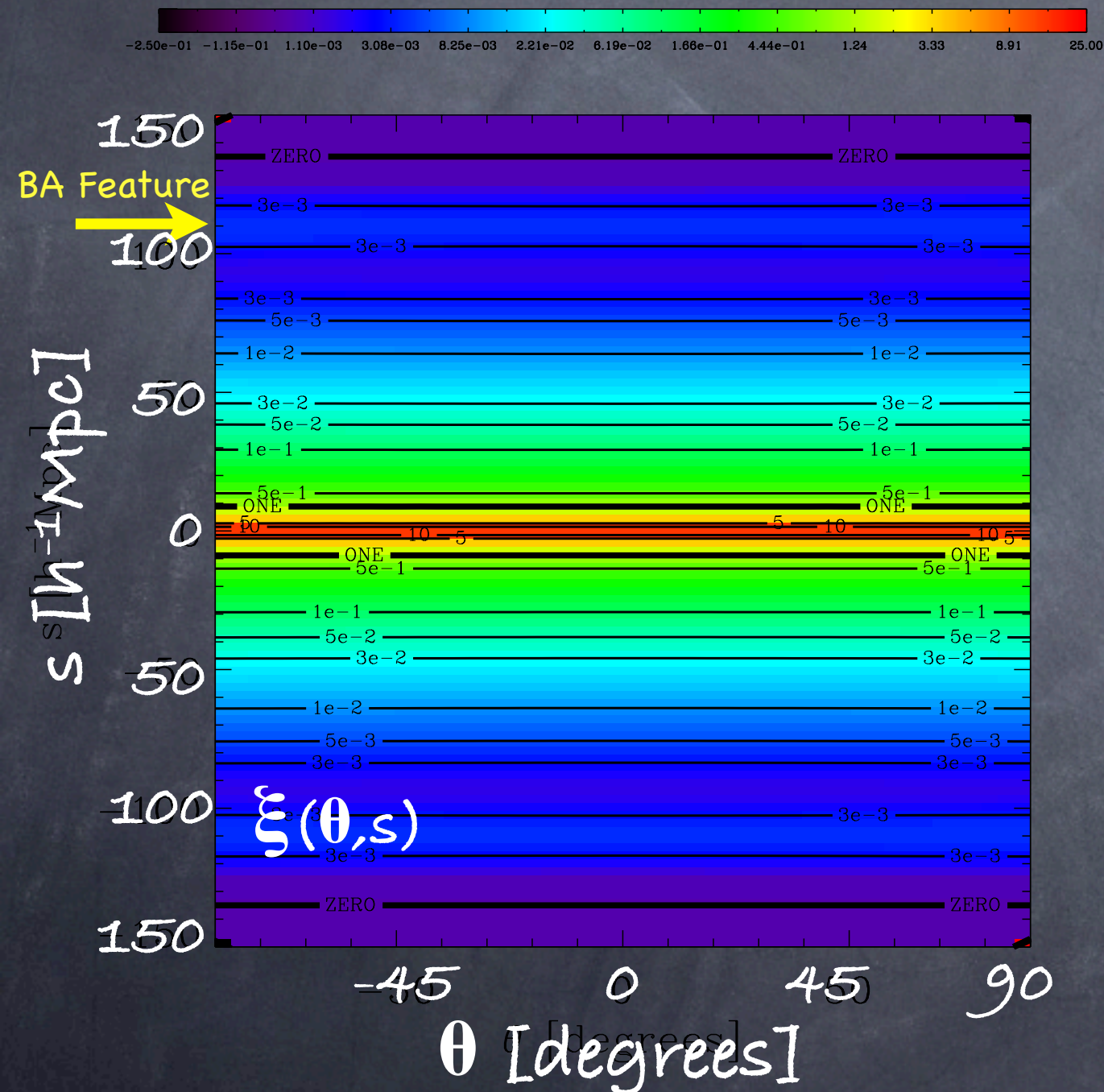


# Clustering as Function of Polar Angle



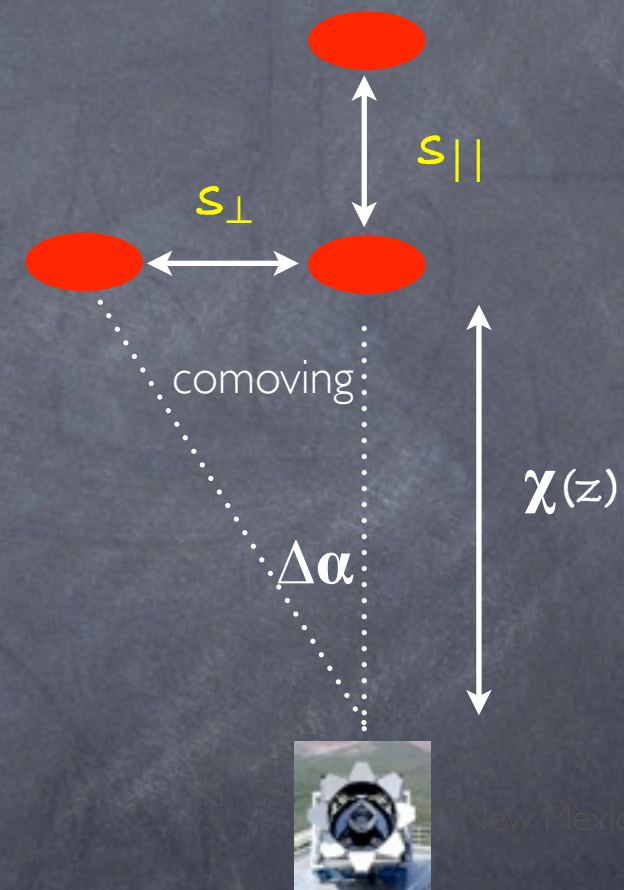
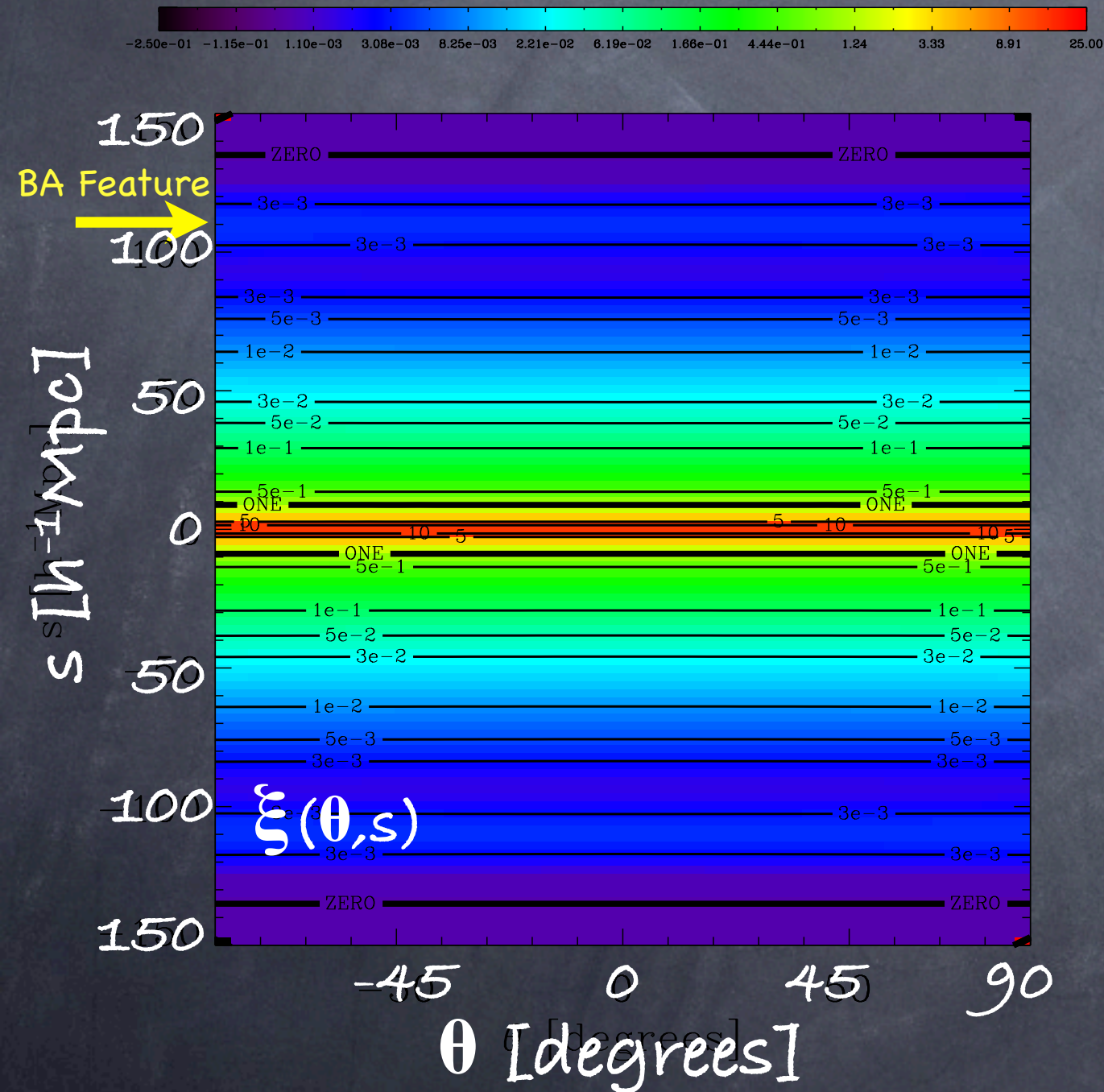


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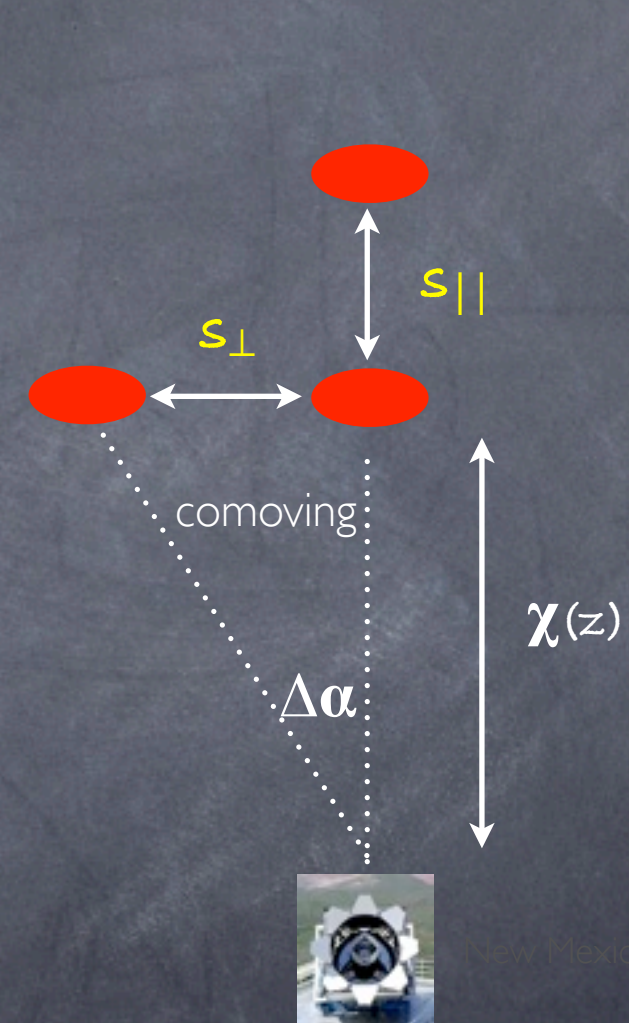
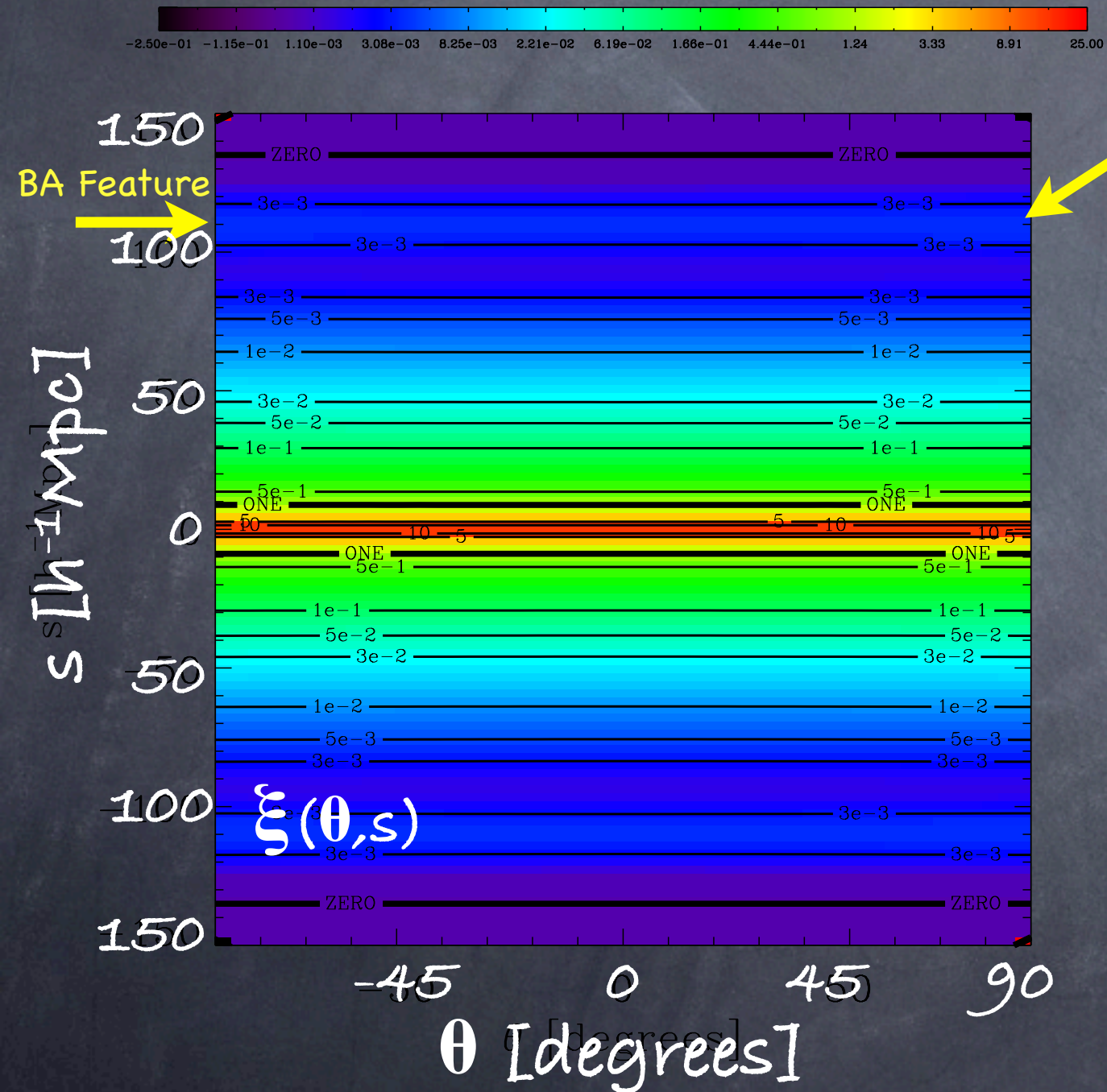
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New Mexico (and, eventually, my desktop)



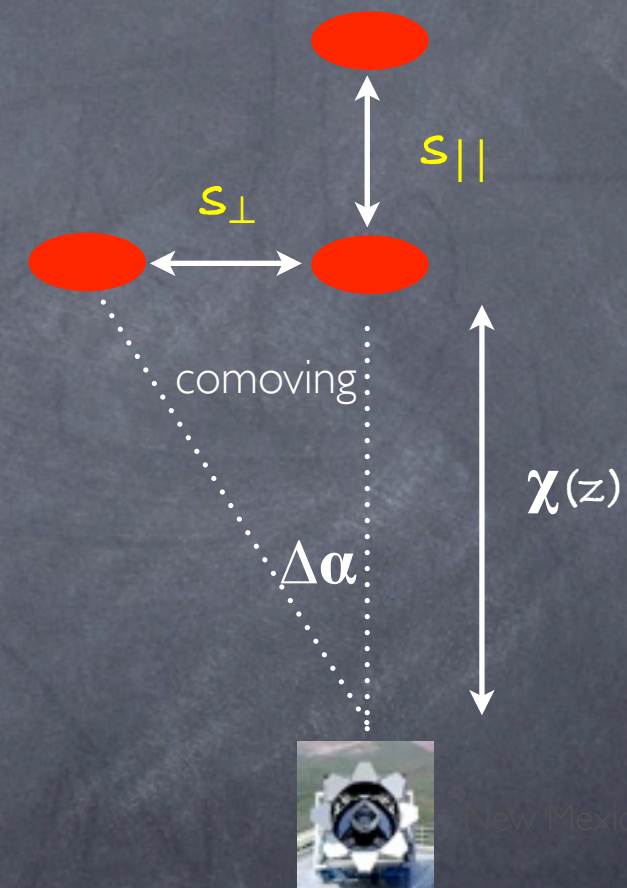
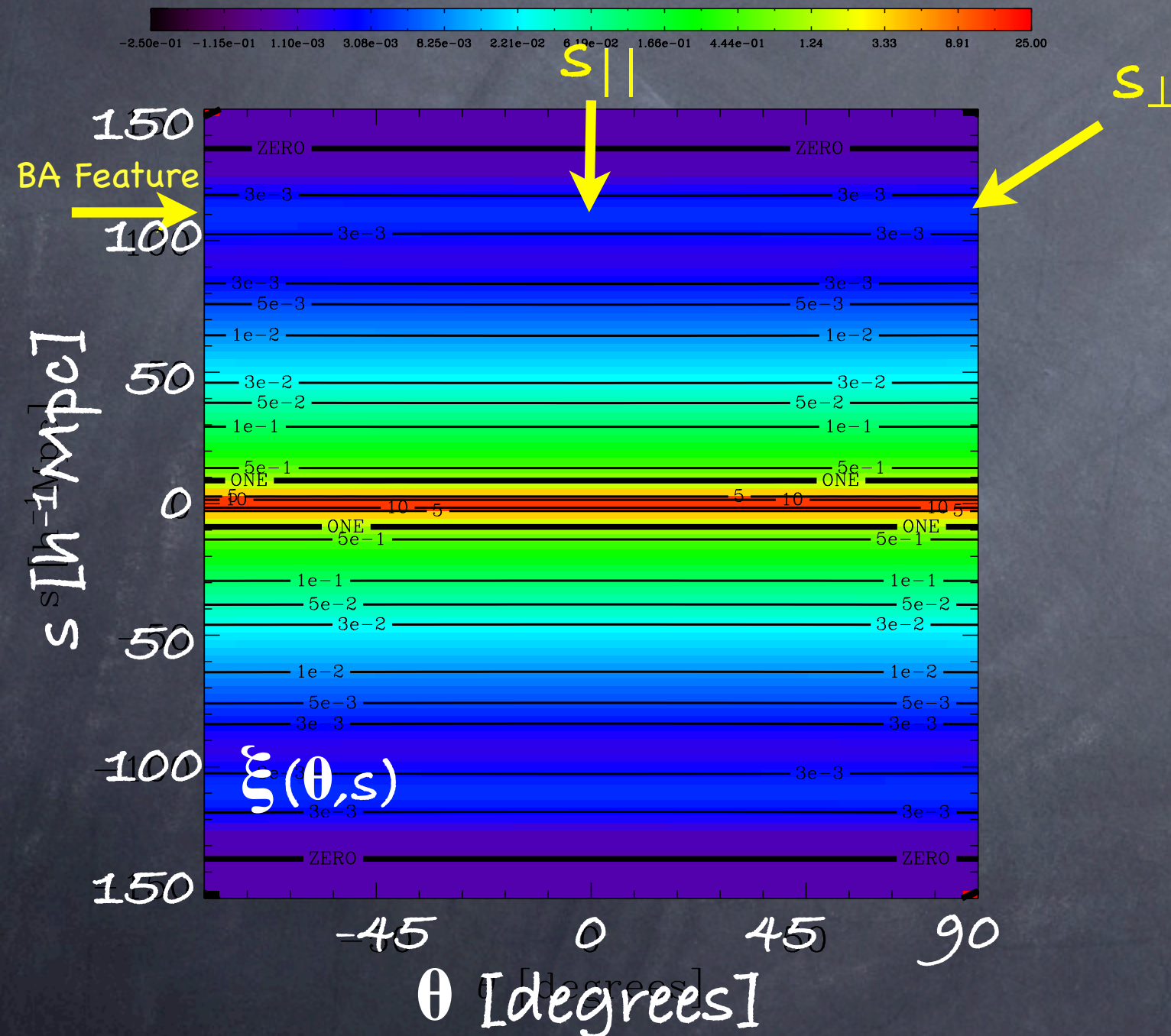
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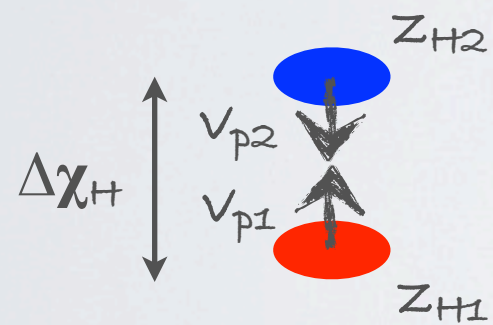


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# Redshift Distortions

Velocity-Dispersion Effect  
(aka Finger of God)  
effects small scales  $\sim$  few Mpc



Real Comoving Space

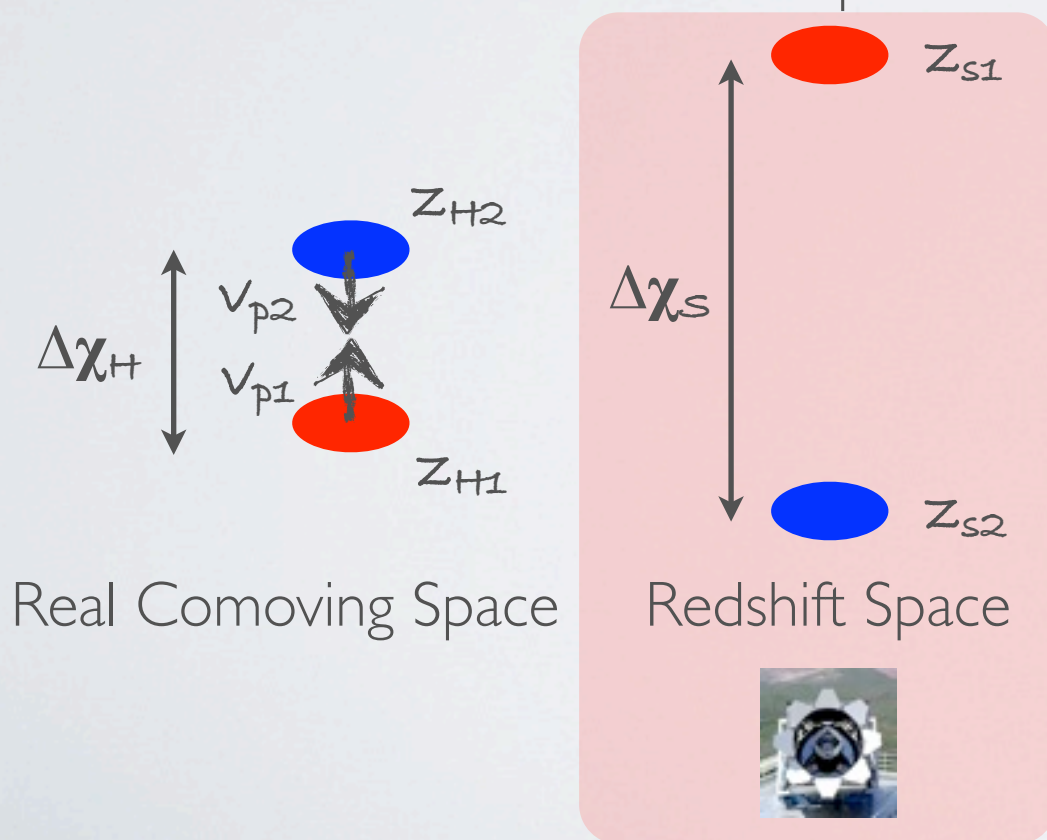
Redshift Space





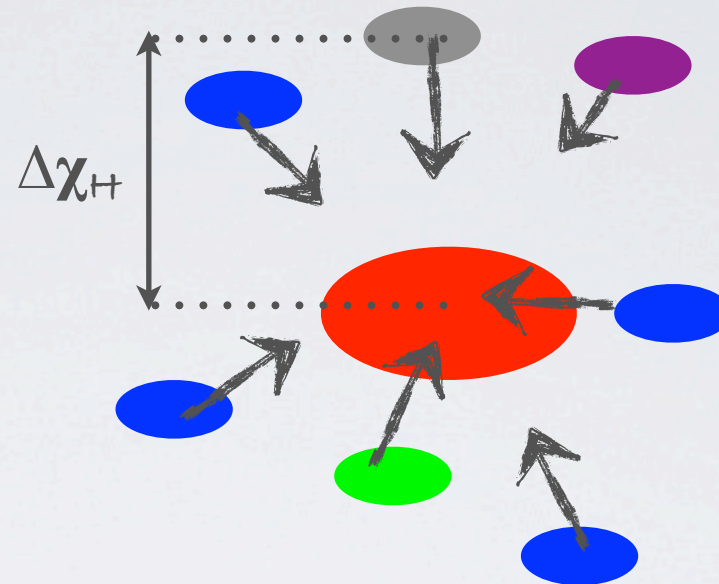
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# Redshift Distortions

Squashing Effect  
effects large scales  $\sim 10's \text{ Mpc}$

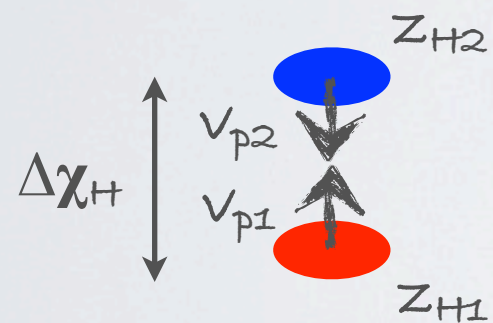


Real Comoving Space

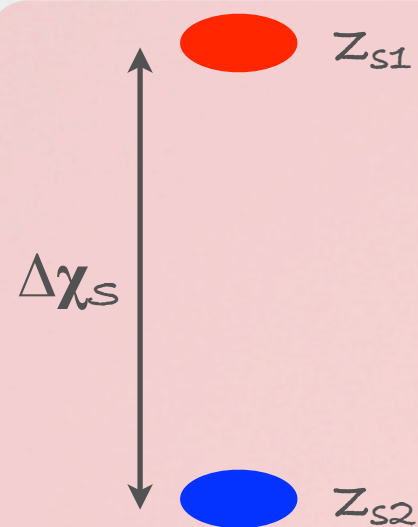
Redshift Space



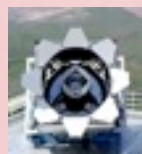
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Real Comoving Space



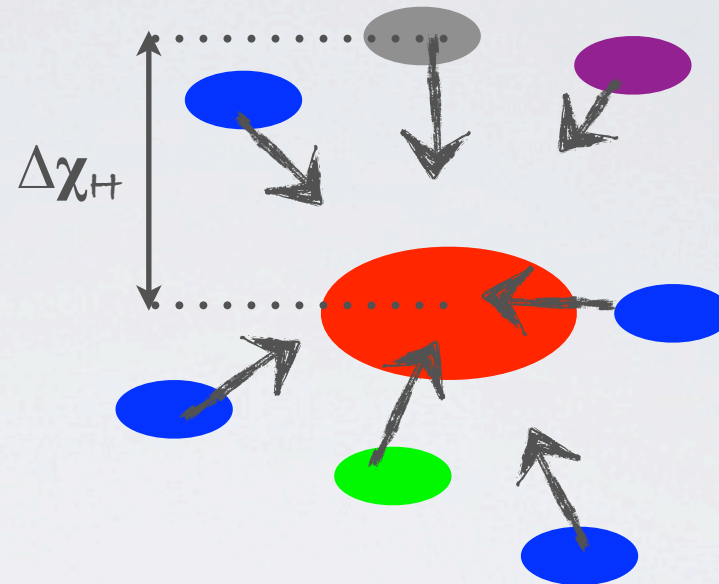
Redshift Space



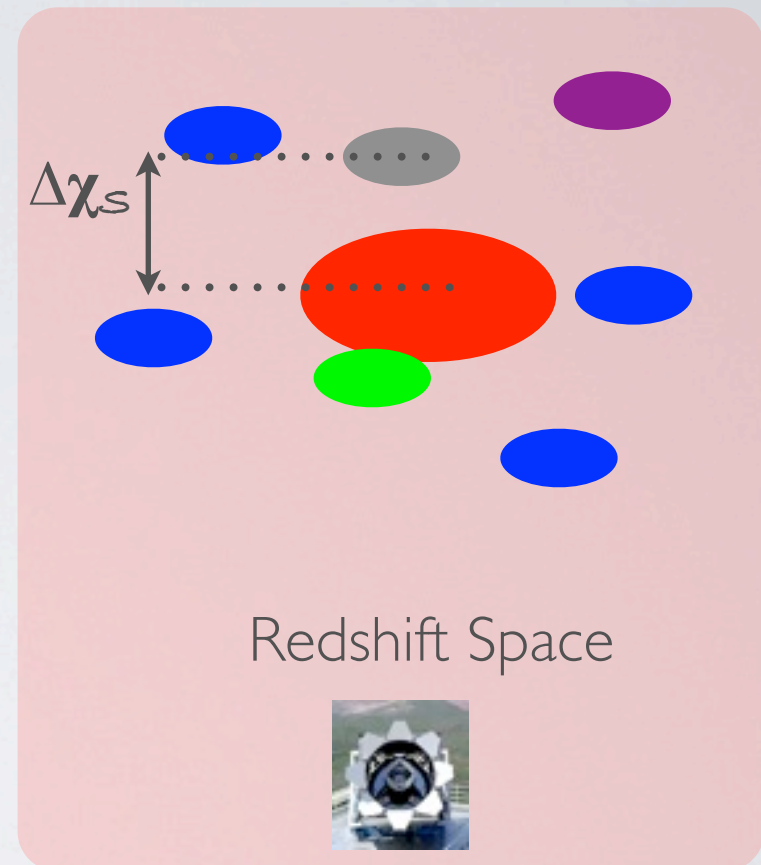


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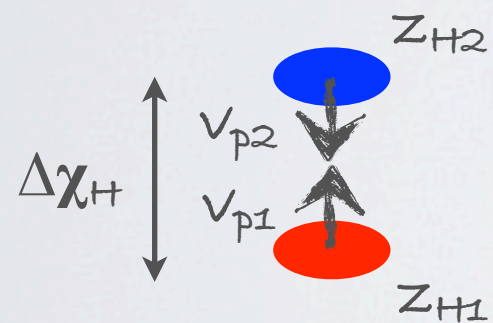


Real Comoving Space

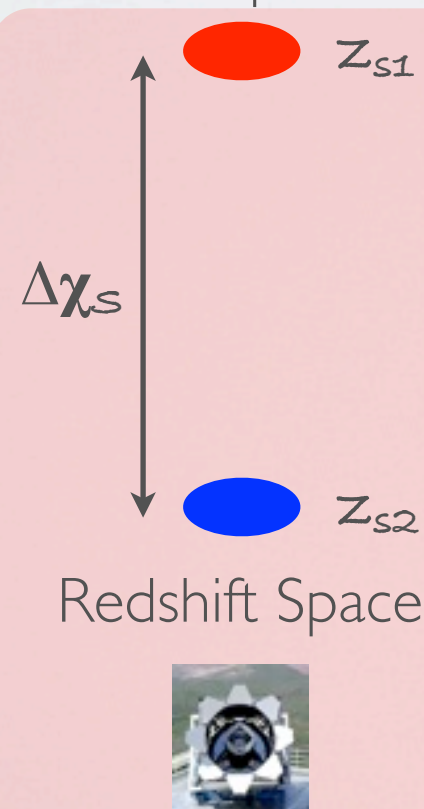


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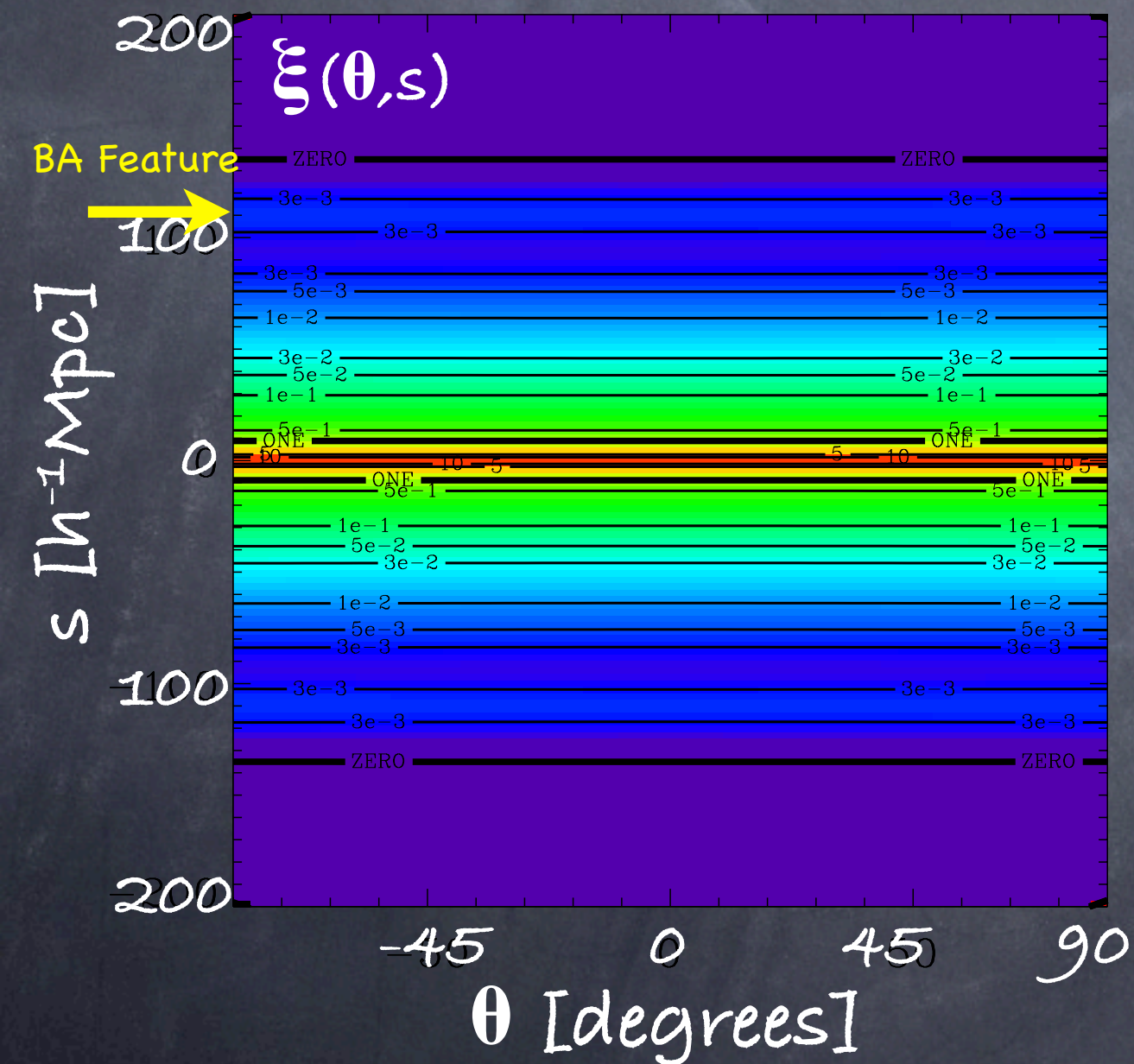
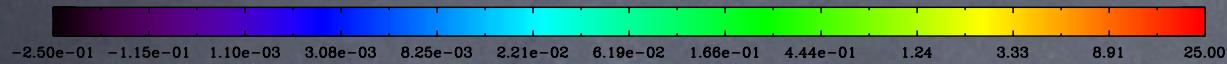
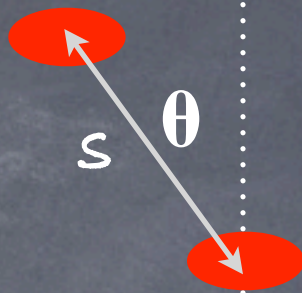
Real Comoving Space



Redshift Space

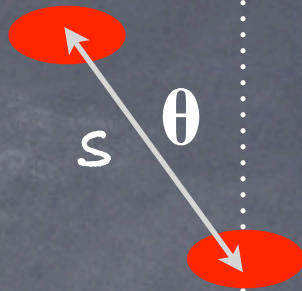


# Clustering as Function of Polar Angle

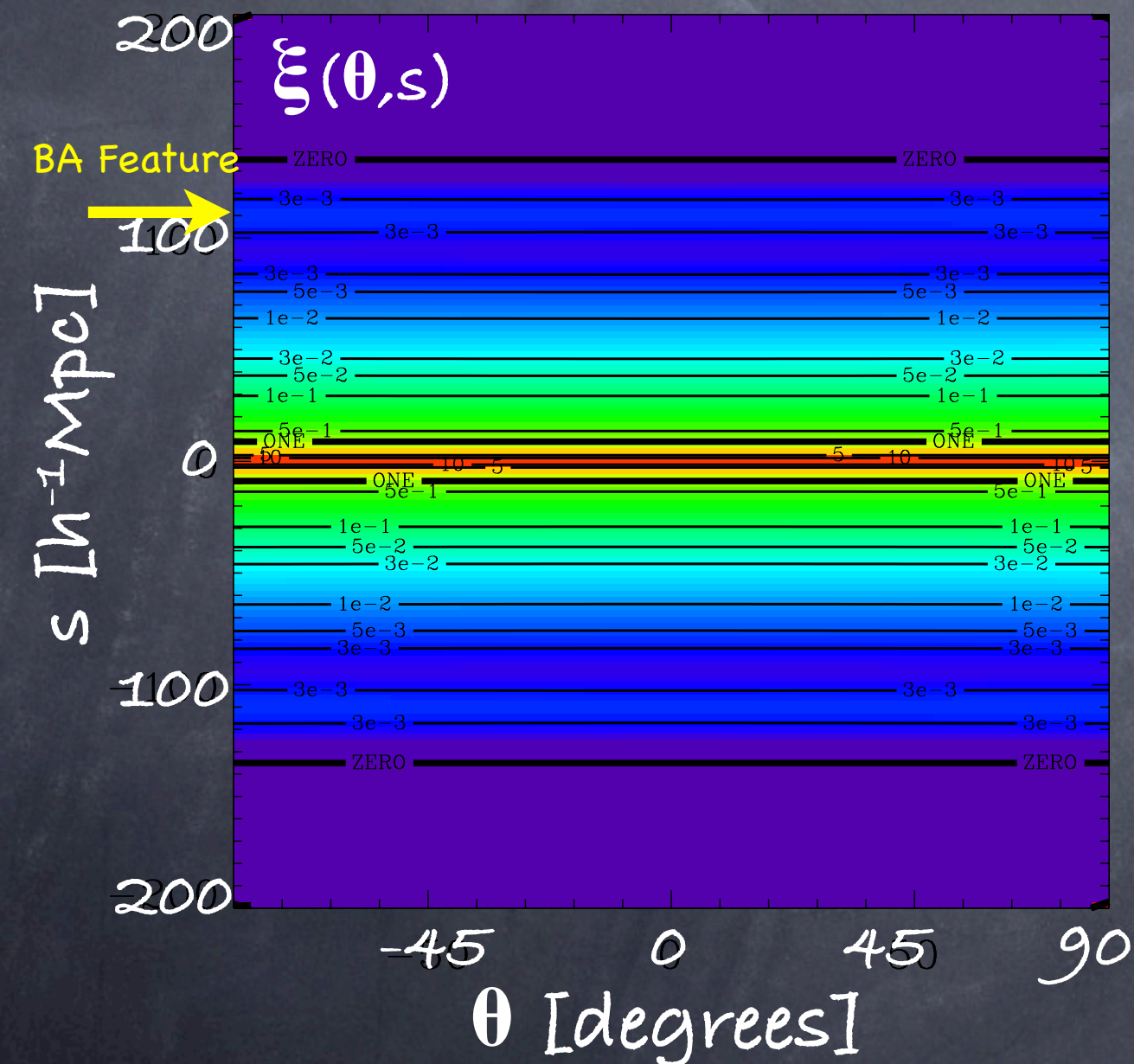
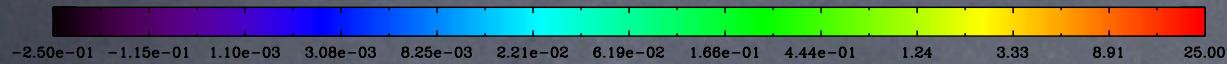




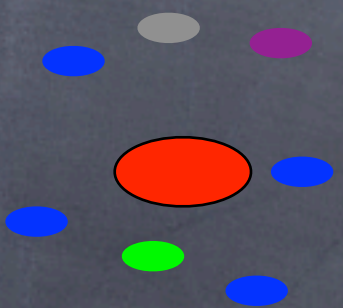
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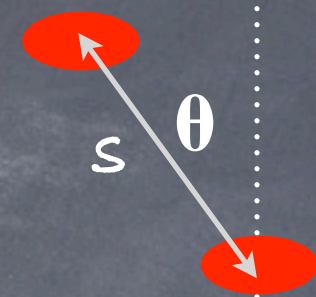
no dynamical distortions  
(linear theory)



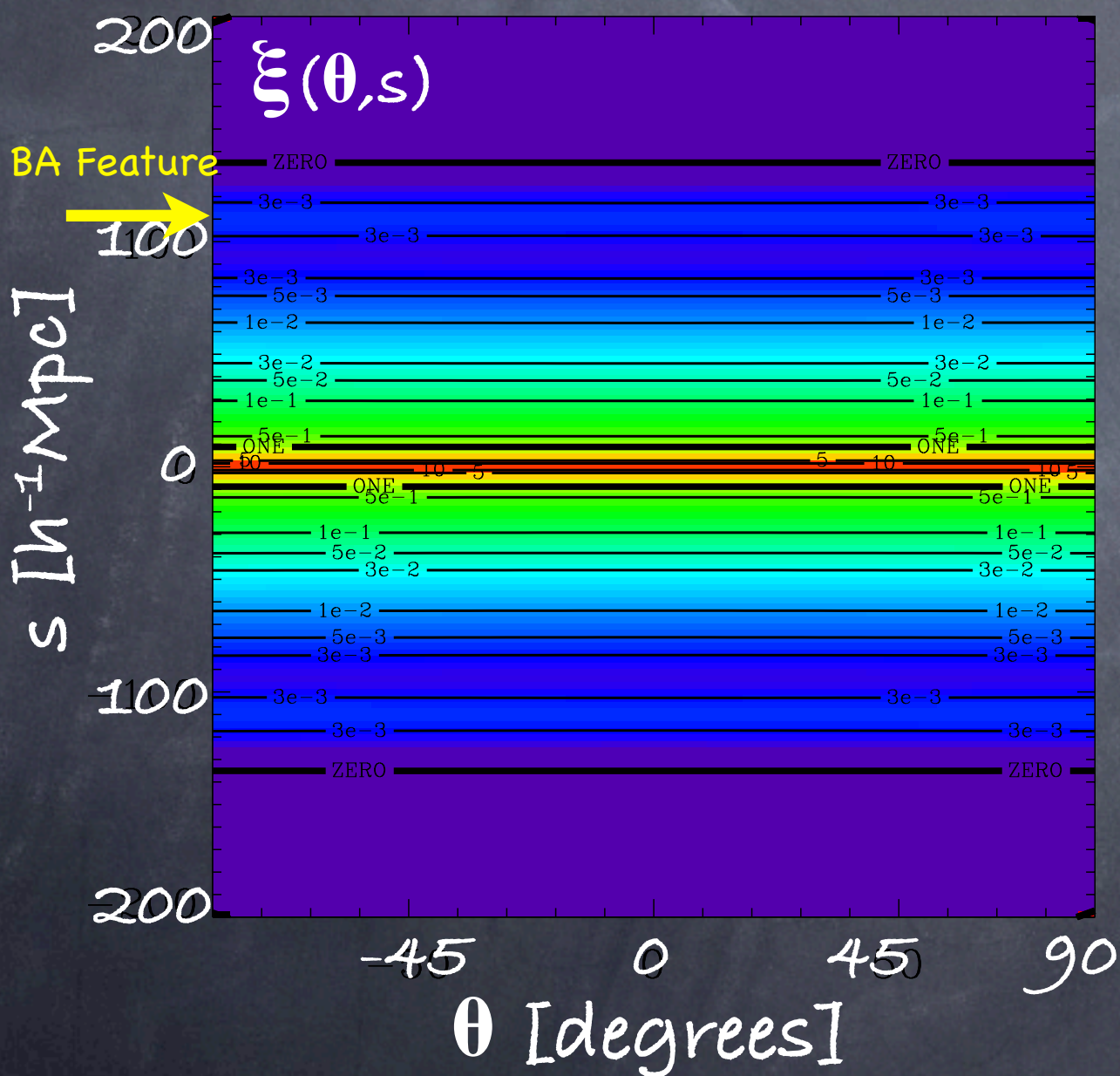
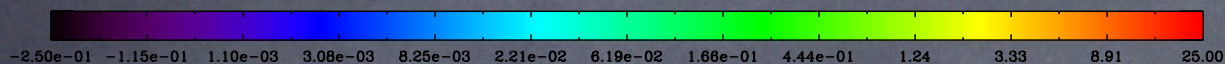




# Clustering as Function of Polar Angle with Squashing Effect



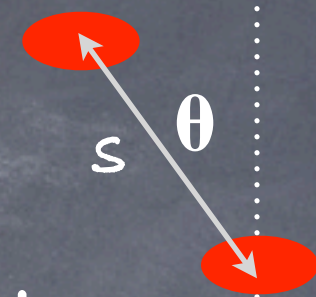
no dynamical distortions  
(linear theory)





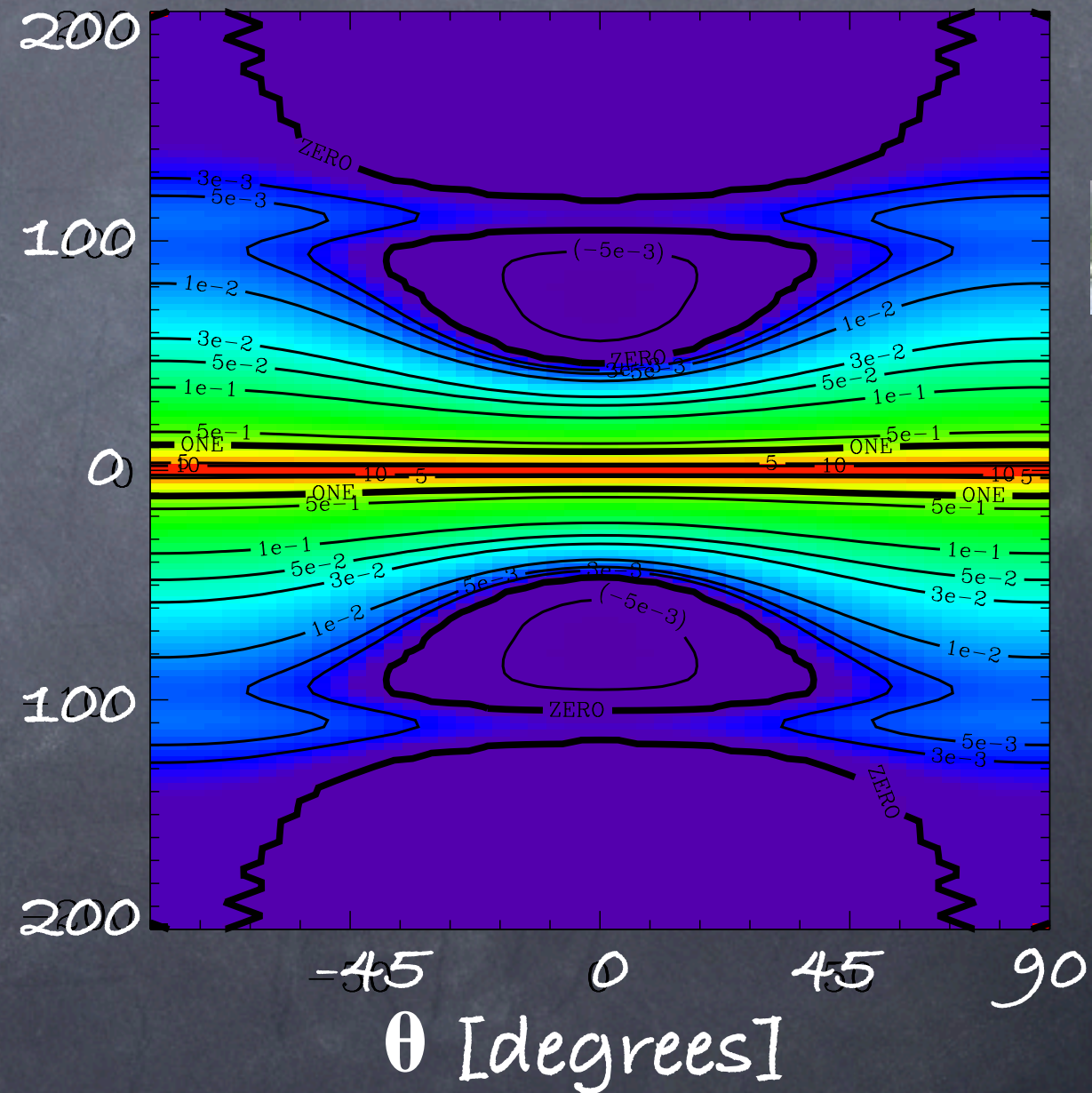
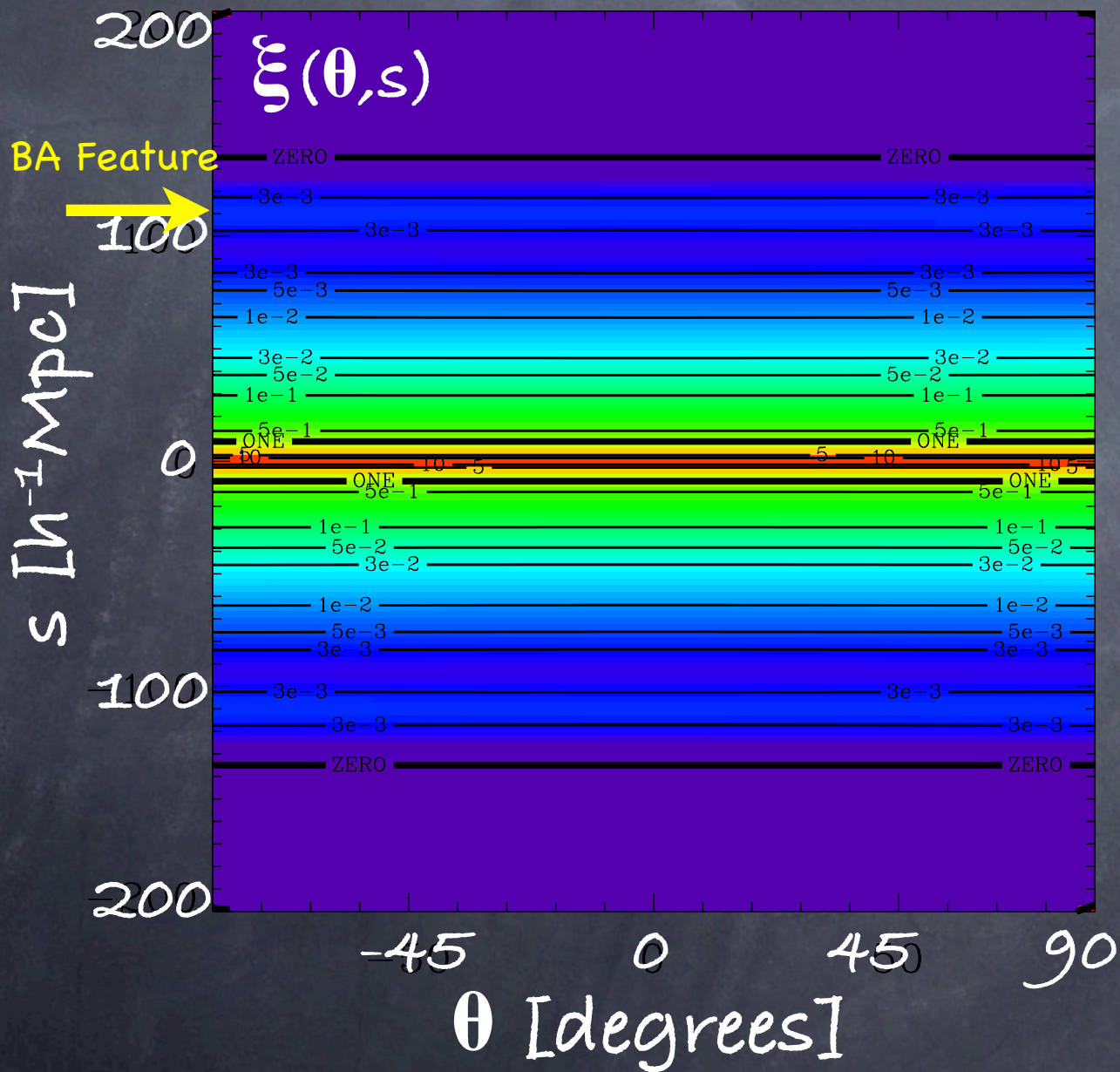
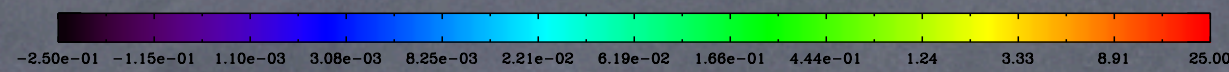
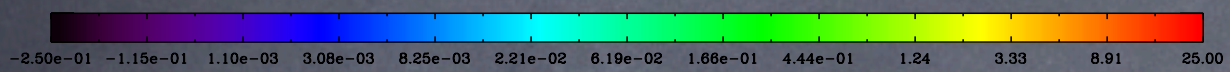


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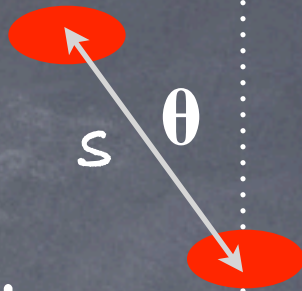
no dynamical distortions  
(linear theory)

squashing effect only  
(linear theory; Matsubara 2004)



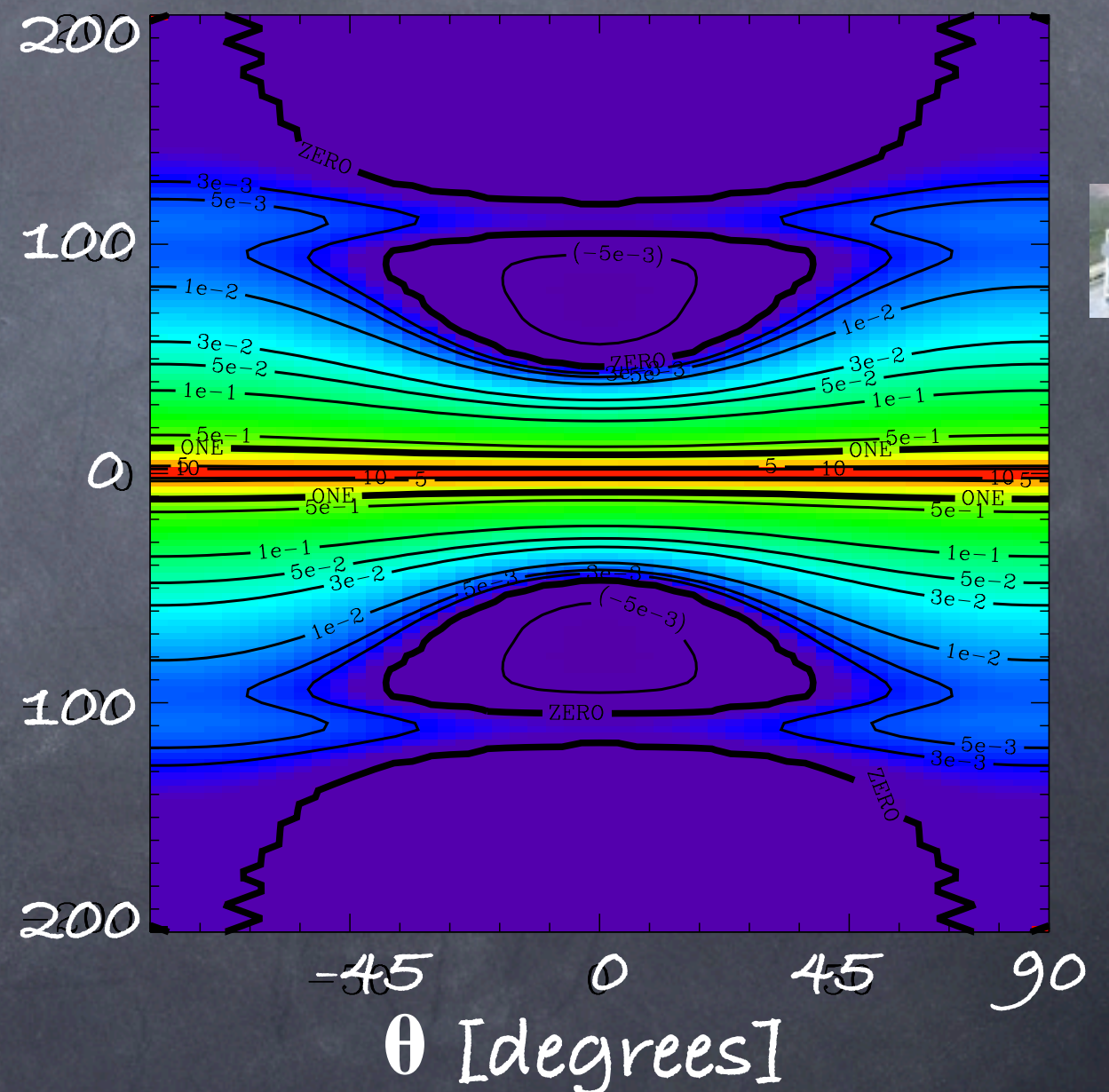
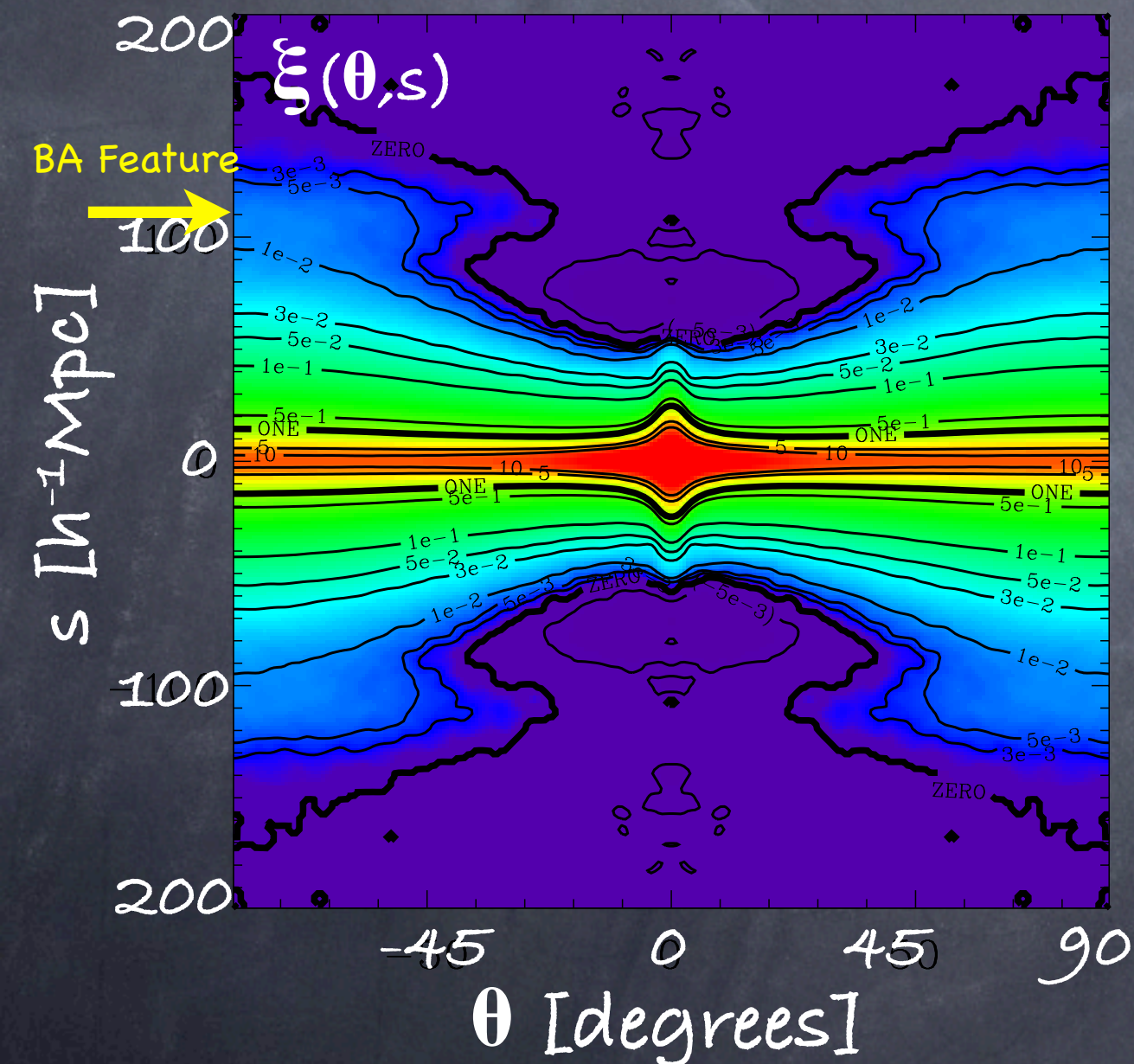
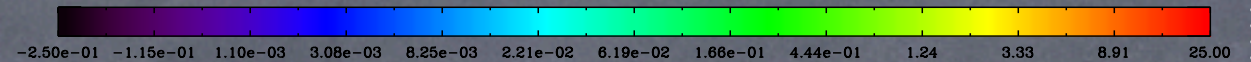
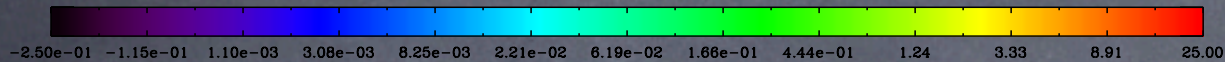


# Clustering as Function of Polar Angle with Squashing Effect



redshift distortions  
(non linear theory; LasDamas mocks)

squashing effect only  
(linear theory; Matsubara 2004)

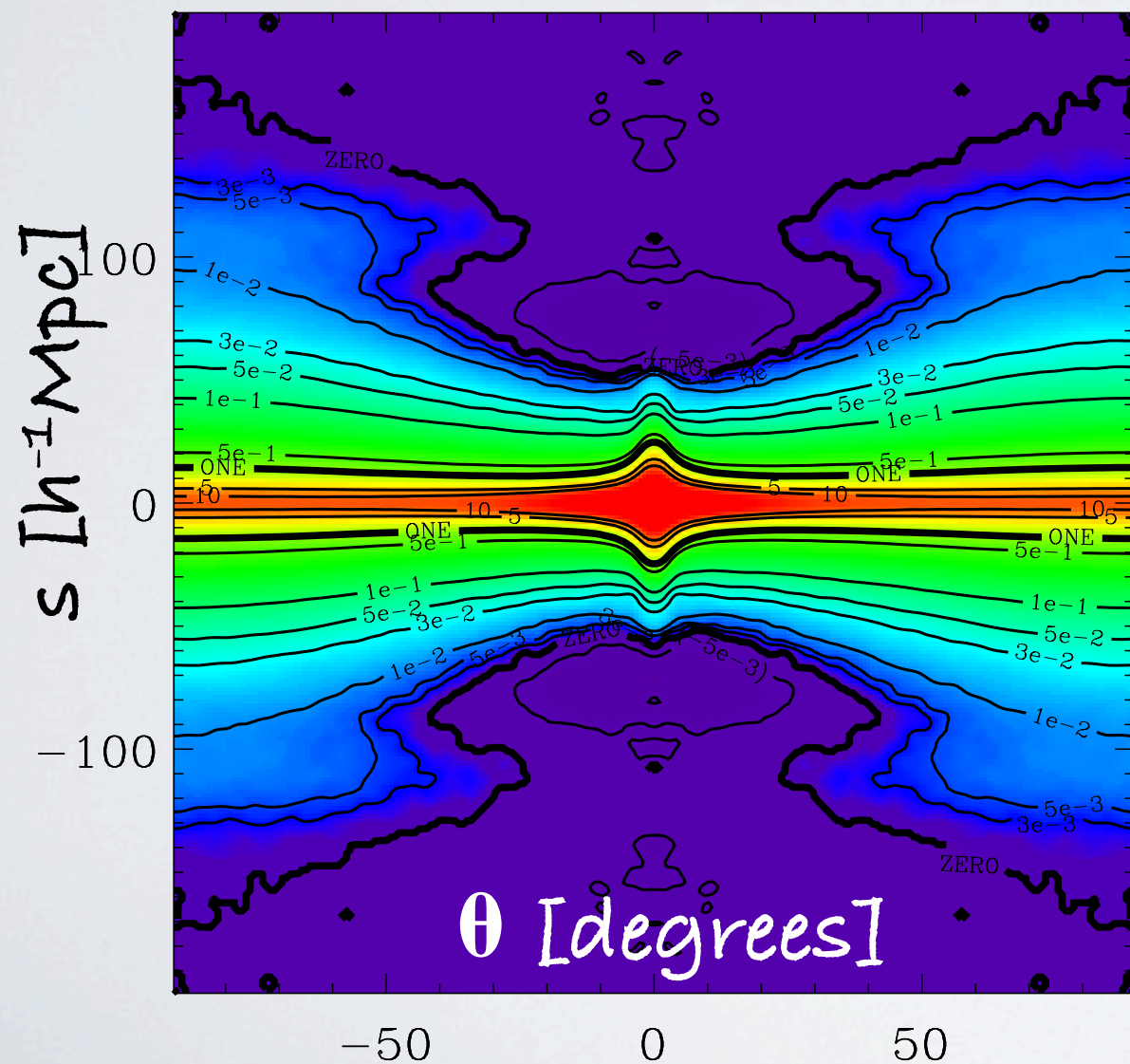
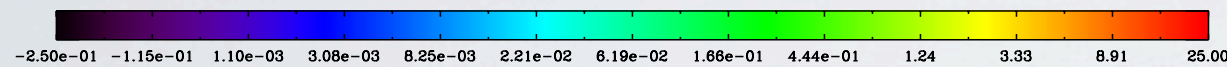




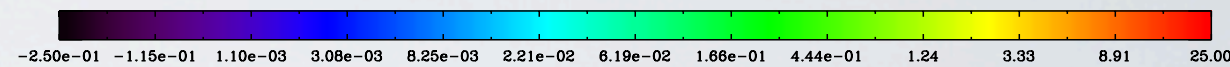
# Baryonic Acoustic Feature in SDSS LRGs

## Line of Sight Detection?

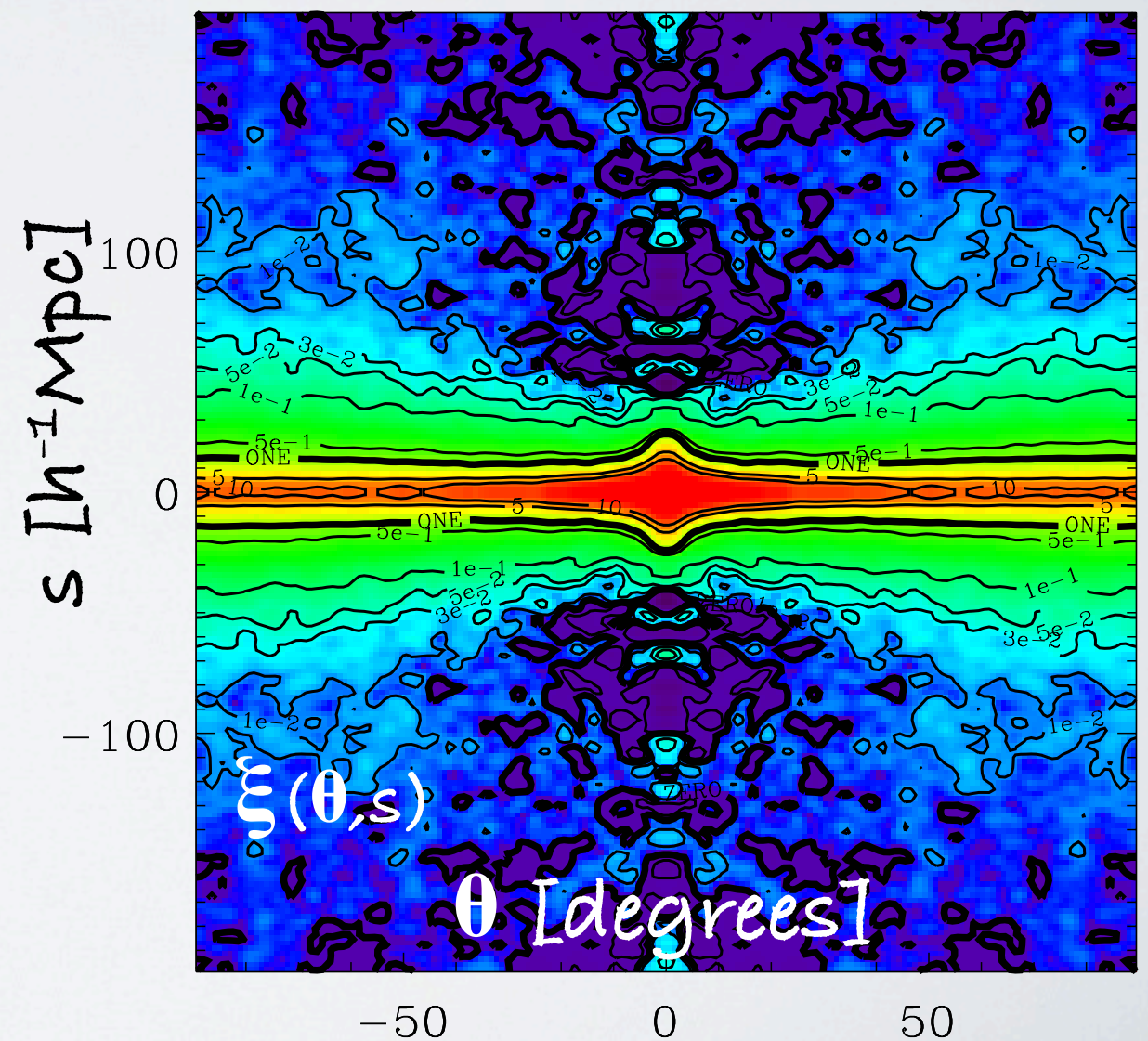
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(non linear theory; LasDamas mocks)



SDSS-II Results



Kazin et al. (in prep.)

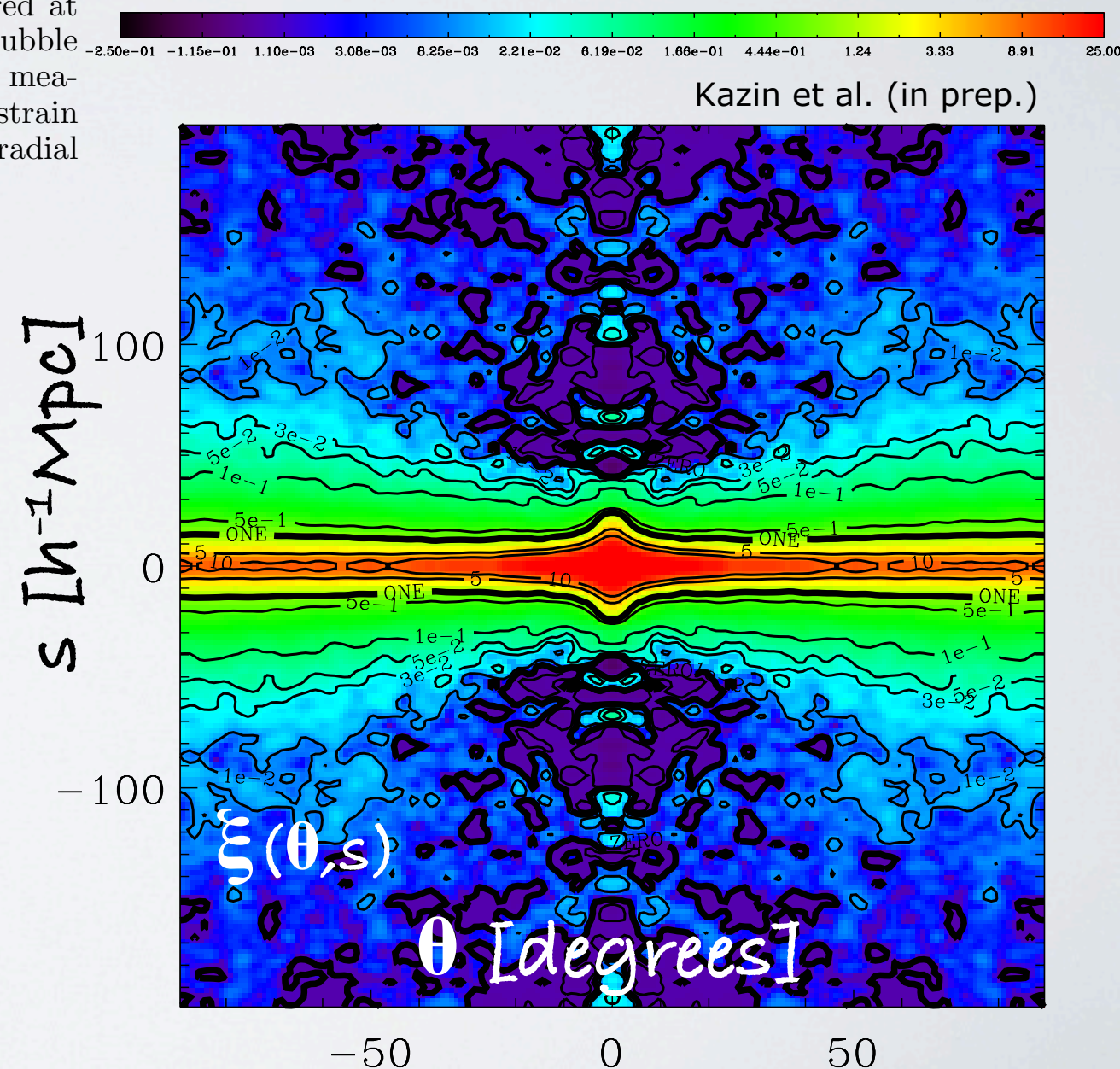


# Baryonic Acoustic Feature in SDSS LRGs Line of Sight Detection?

## ABSTRACT

From Gaztañaga et al. (2008)

We study the clustering of LRG galaxies in the latest spectroscopic SDSS data releases, DR6 and DR7, which sample over  $1 \text{ Gpc}^3/h^3$  to  $z=0.47$ . The 2-point correlation function  $\xi(\sigma, \pi)$  is estimated as a function of perpendicular  $\sigma$  and line-of-sight  $\pi$  (radial) directions. We find a significant detection of a peak at  $r \simeq 110 \text{ Mpc}/h$ , which shows as a circular ring in the  $\sigma - \pi$  plane. There is also significant evidence for a peak along the radial direction whose shape is consistent with its originating from the recombination-epoch baryon acoustic oscillations (BAO). A  $\xi(\sigma, \pi)$  model with no radial BAO peak is disfavored at  $3.2\sigma$ , whereas a model with no magnification bias is disfavored at  $2\sigma$ . The radial data enable, for the first time, a direct measurement of the Hubble parameter  $H(z)$  as a function of redshift. This is independent from earlier BAO measurements which used the spherically averaged (monopole) correlation to constrain an integral of  $H(z)$ . Using the BAO peak position as a standard ruler in the radial





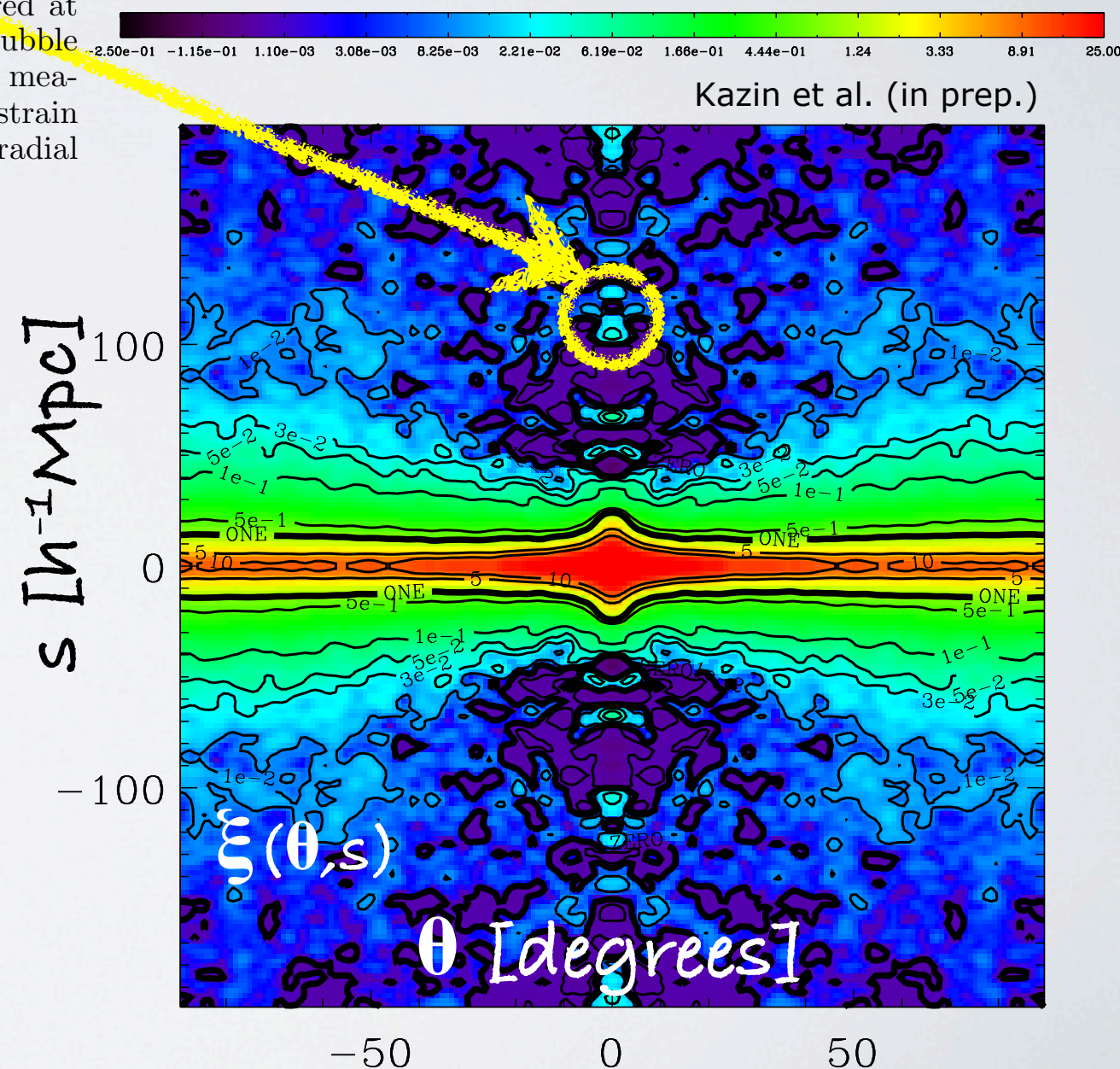
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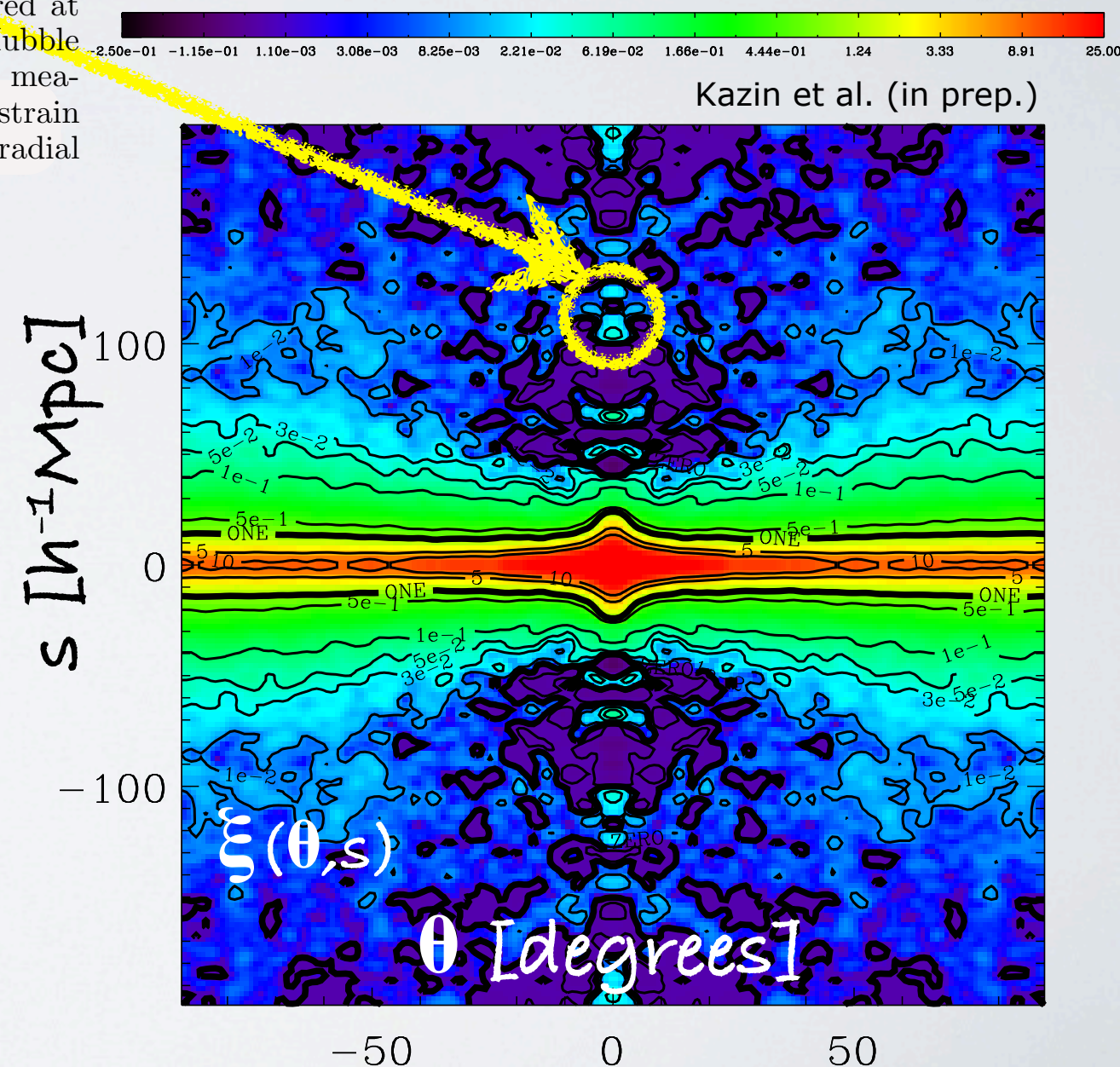
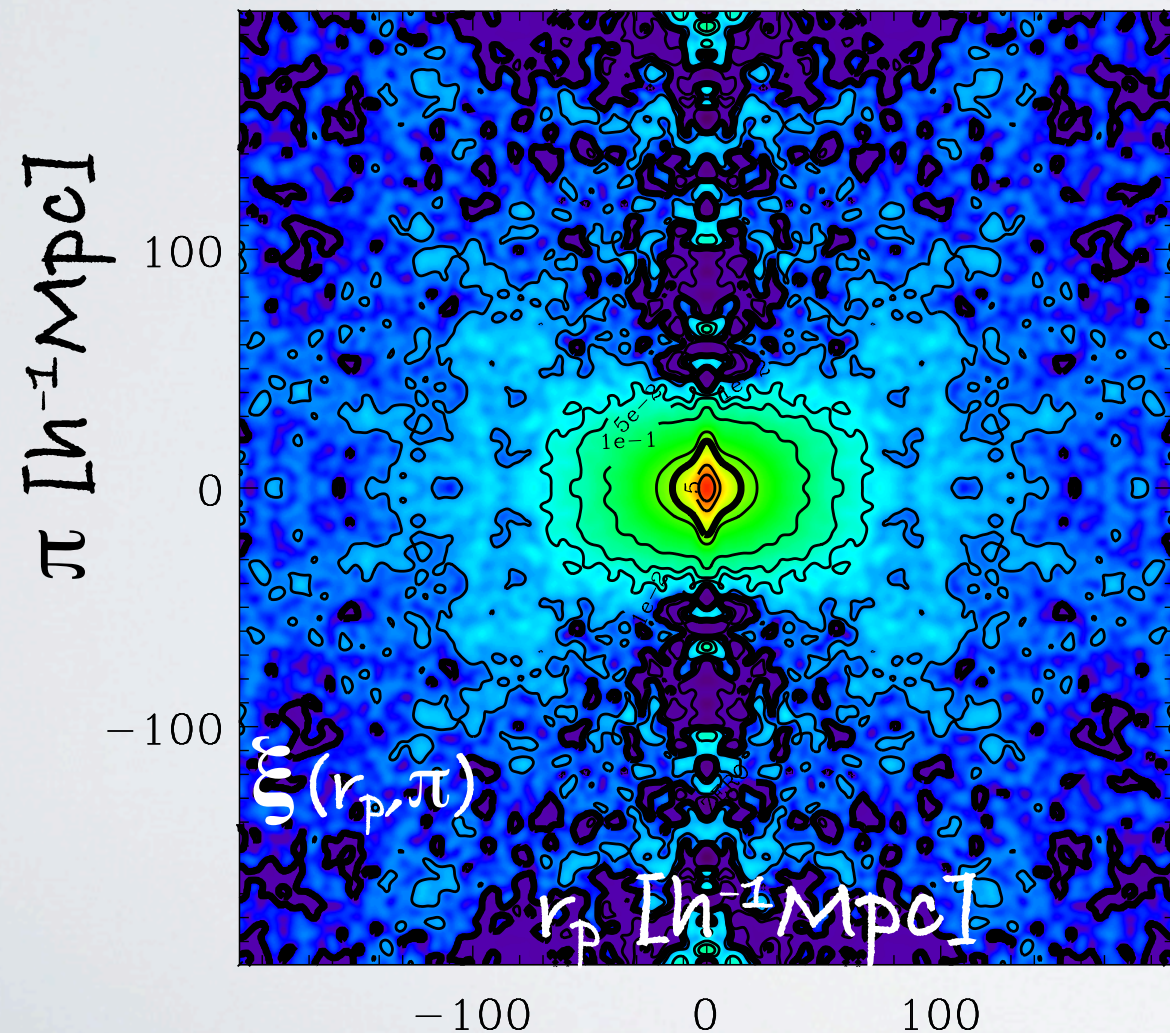
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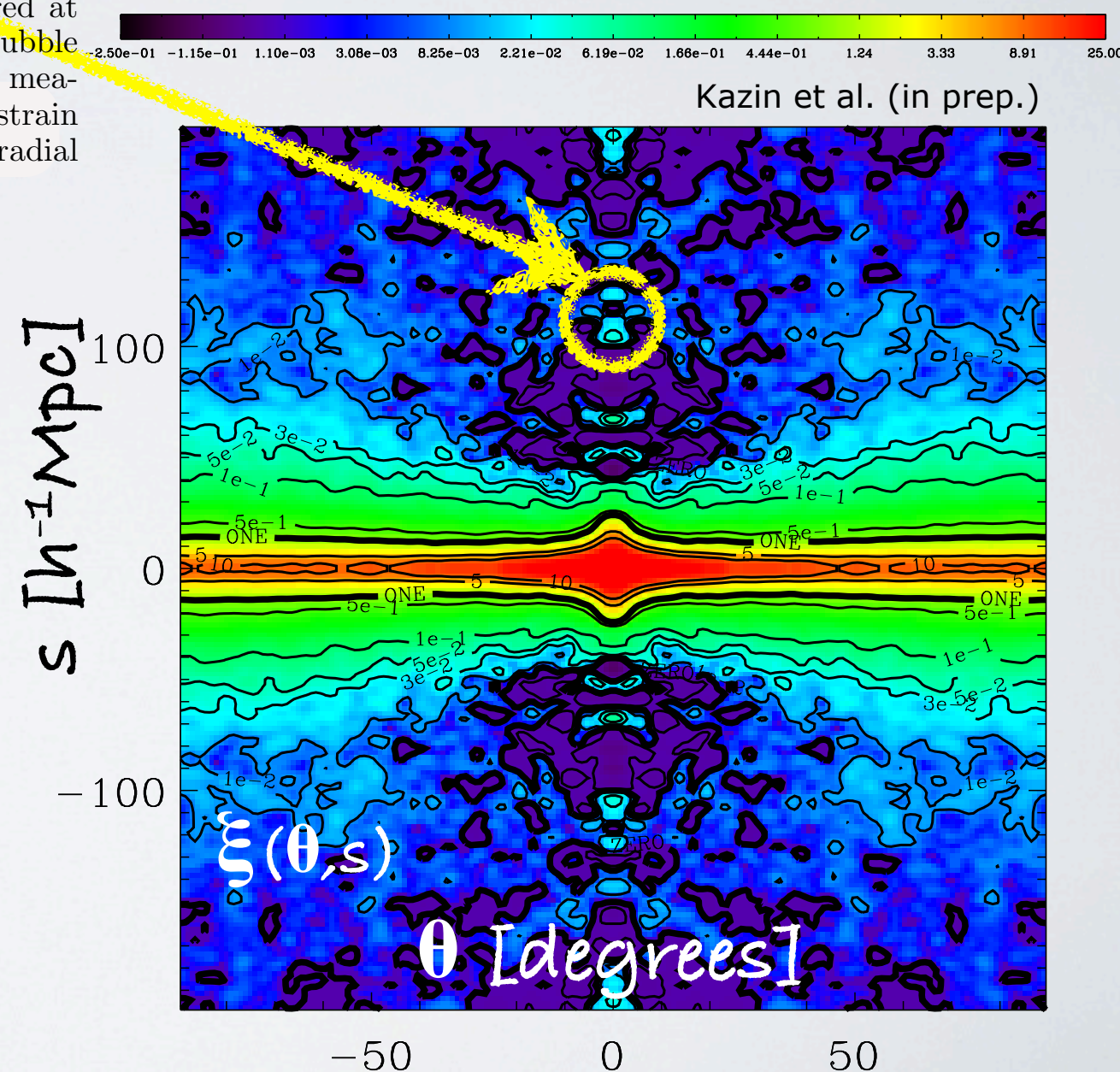
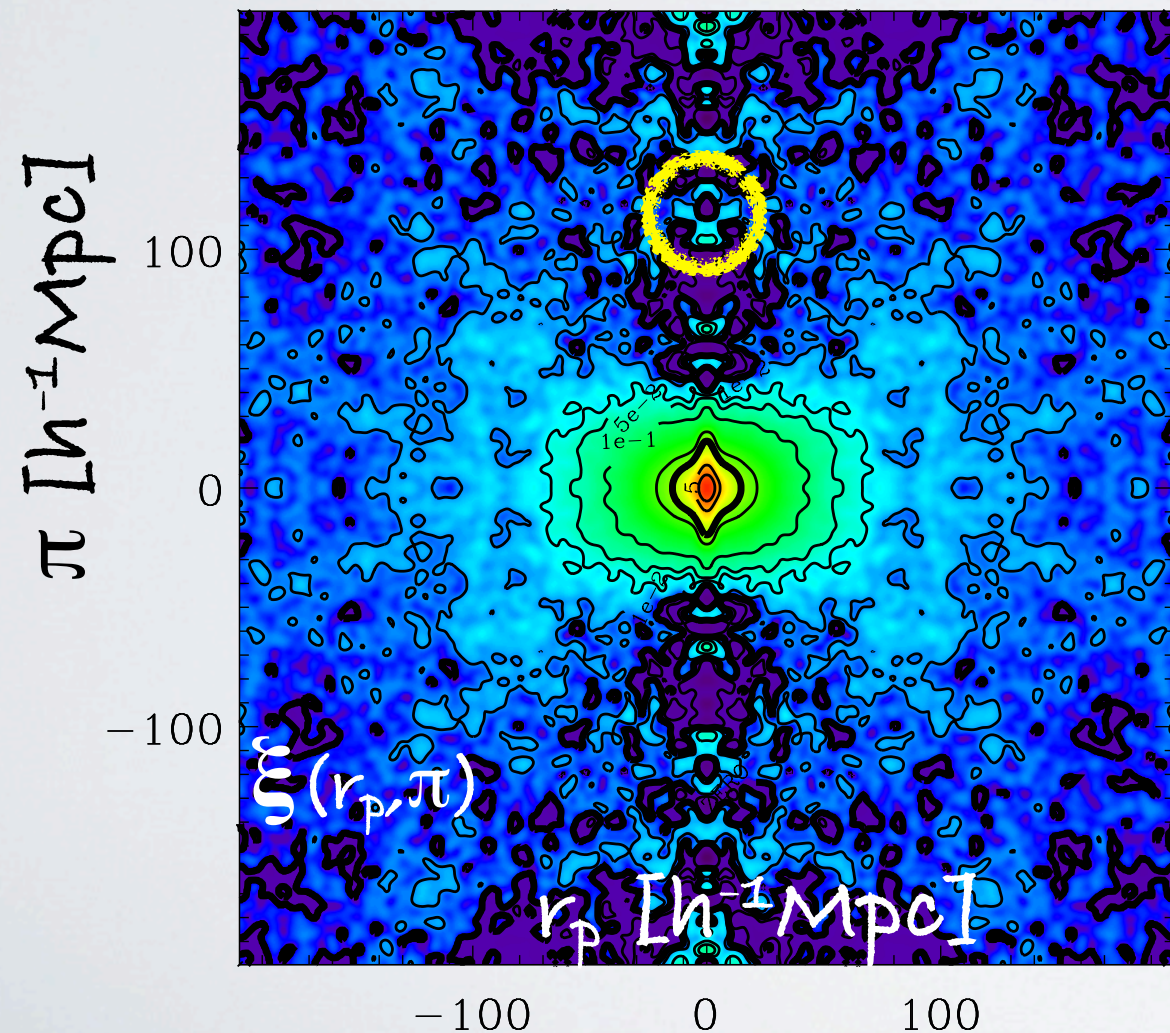
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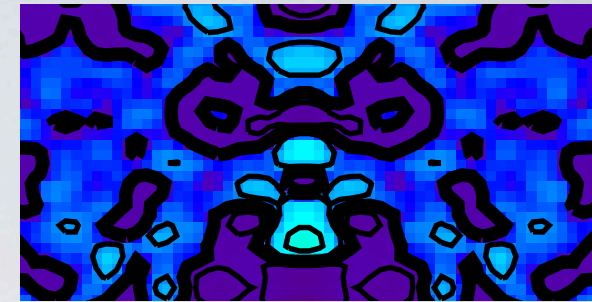
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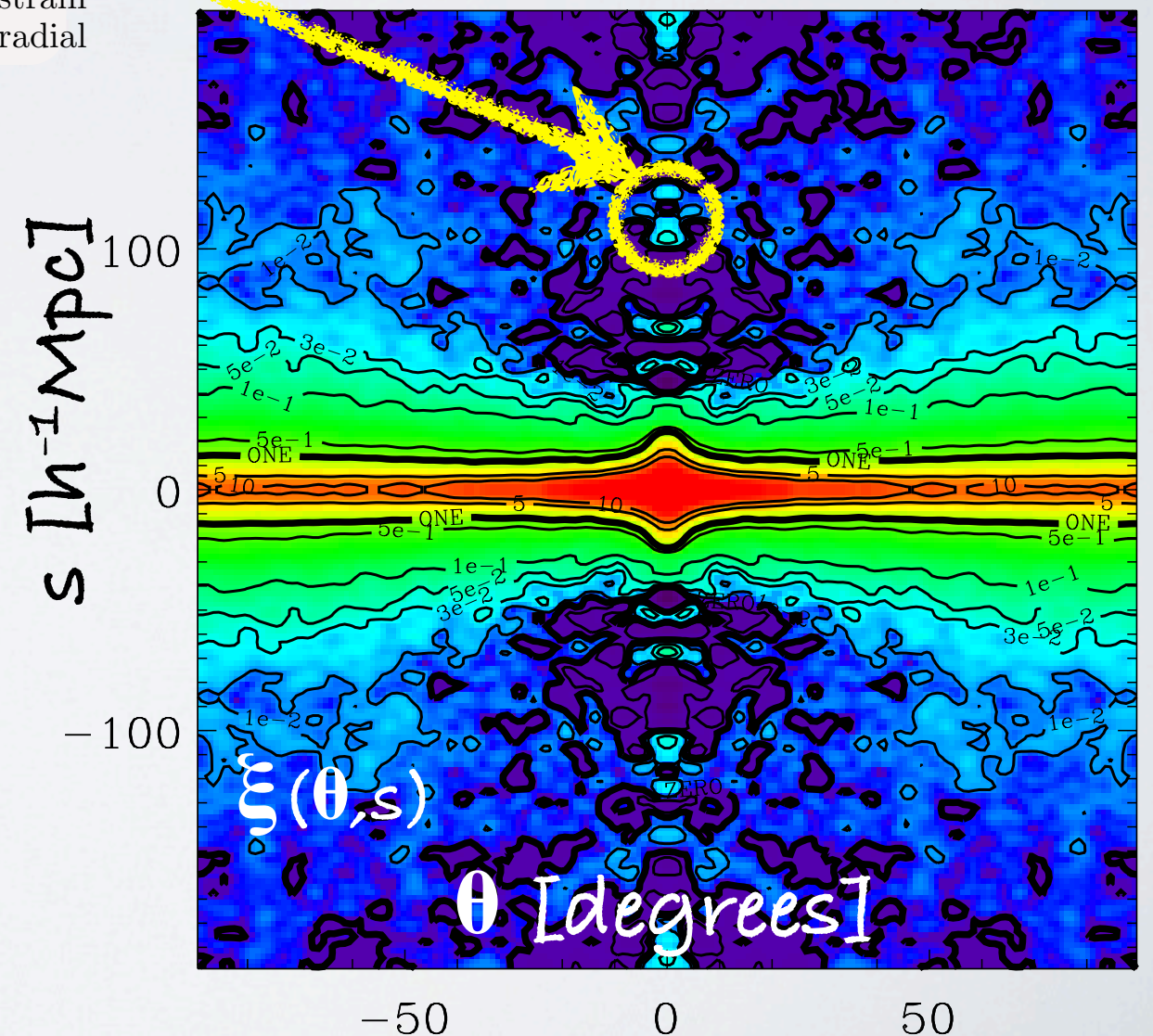
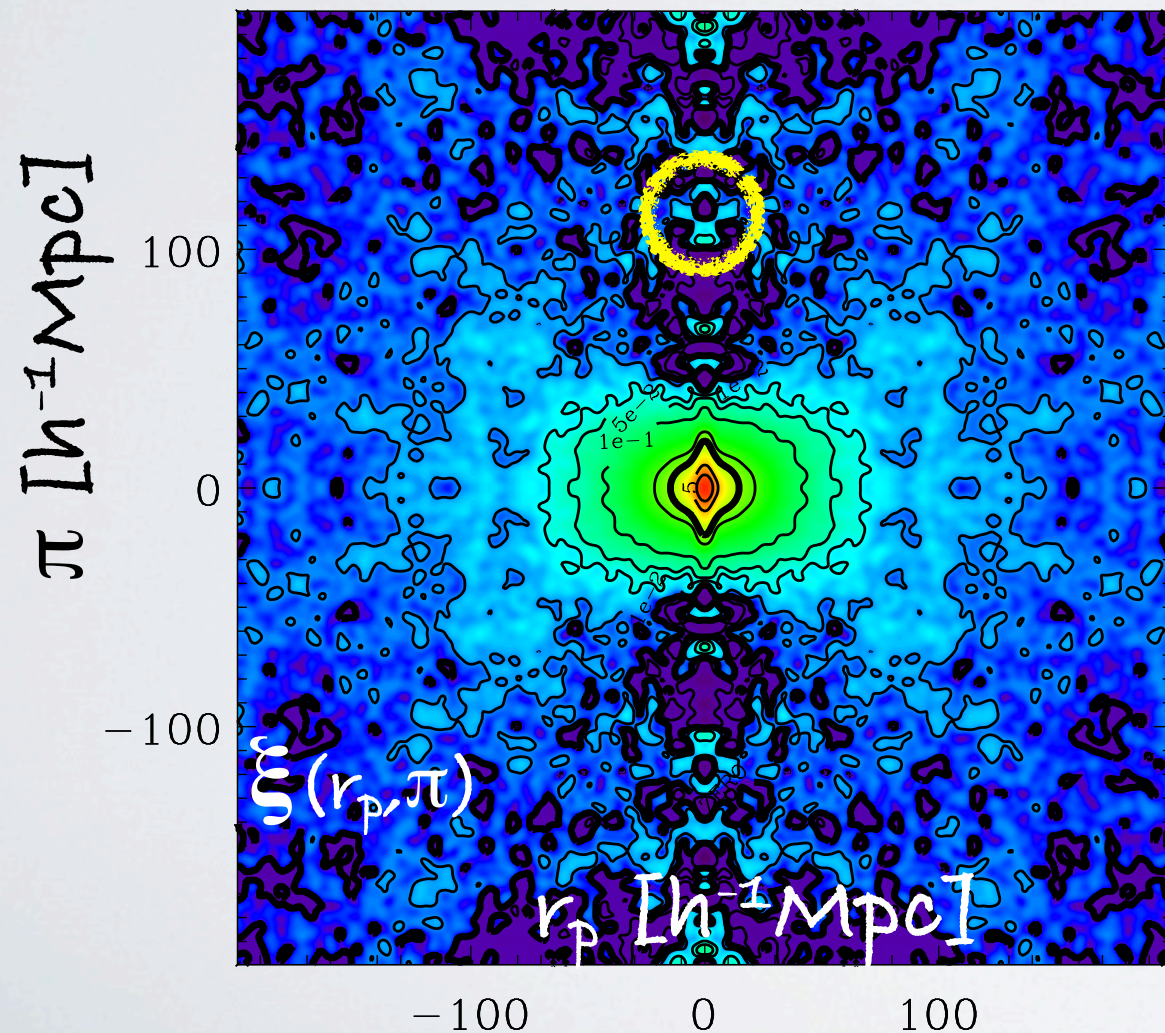
From Gaztañaga et al. (2008)



Full LRG sample



Kazin et al. (in prep.)





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### ABSTRACT

We study the clustering of LRG galaxies in the latest spectroscopic SDSS data releases, DR6 and DR7, which sample over  $1 \text{ Gpc}^3/h^3$  to  $z=0.47$ . The 2-point correlation function  $\xi(\sigma, \pi)$  is estimated as a function of perpendicular  $\sigma$  and line-of-sight  $\pi$  (radial) directions. We find a significant detection of a peak at  $r \simeq 110 \text{ Mpc}/h$ , which shows as a circular ring in the  $\sigma - \pi$  plane. There is also significant evidence for a peak along the radial direction whose shape is consistent with its originating from the recombination-epoch baryon acoustic oscillations (BAO). A  $\xi(\sigma, \pi)$  model with no radial BAO peak is disfavored at  $3.2\sigma$ , whereas a model with no magnification bias is disfavored at  $2\sigma$ . The radial data enable, for the first time, a direct measurement of the Hubble parameter  $H(z)$  as a function of redshift. This is independent from earlier BAO measurements which used the spherically averaged (monopole) correlation to constrain an integral of  $H(z)$ . Using the BAO peak position as a standard ruler in the radial

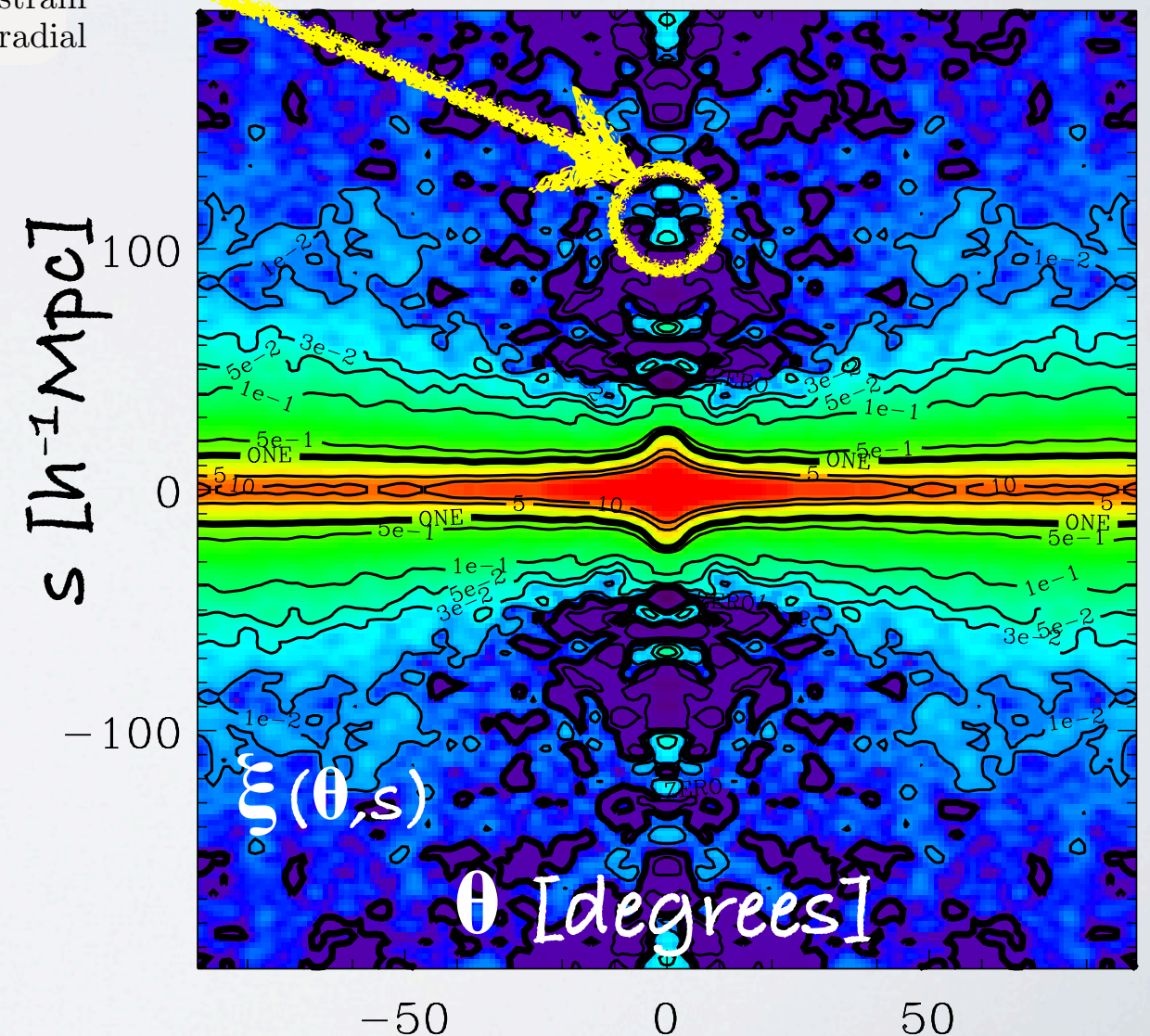
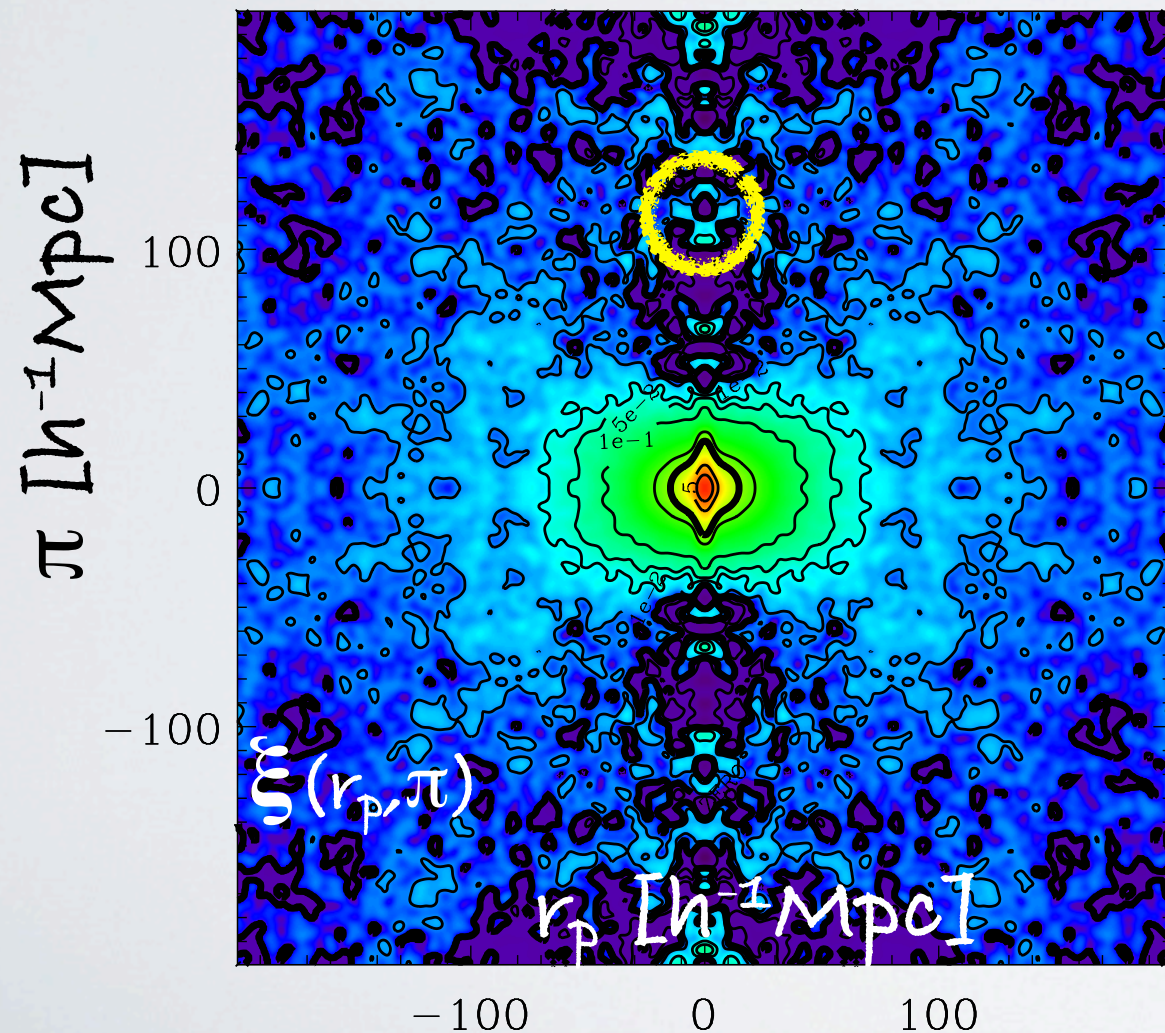
From Gaztañaga et al. (2008)

Volume Limited sample



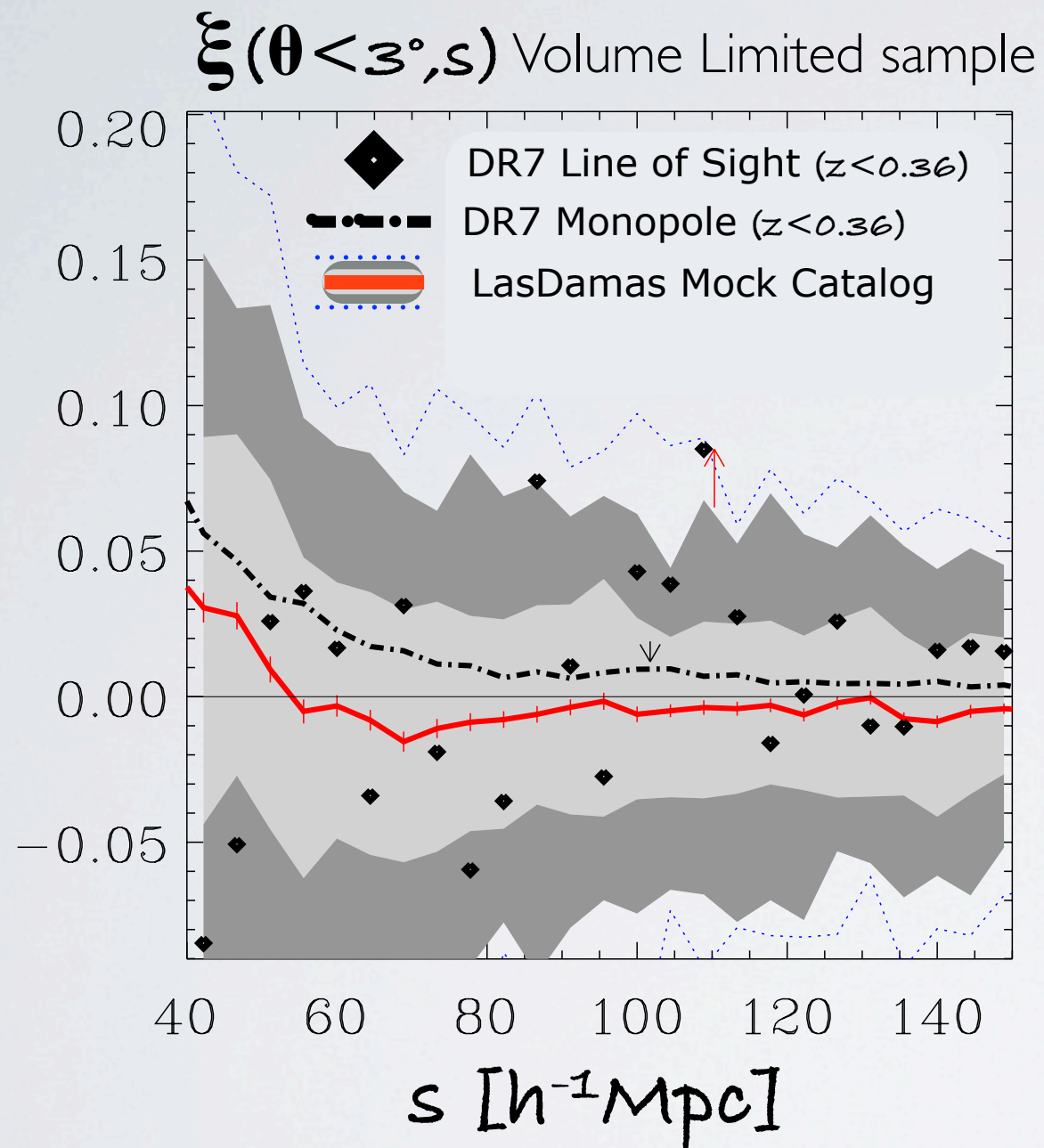
Full LRG sample

Kazin et al. (in prep.)



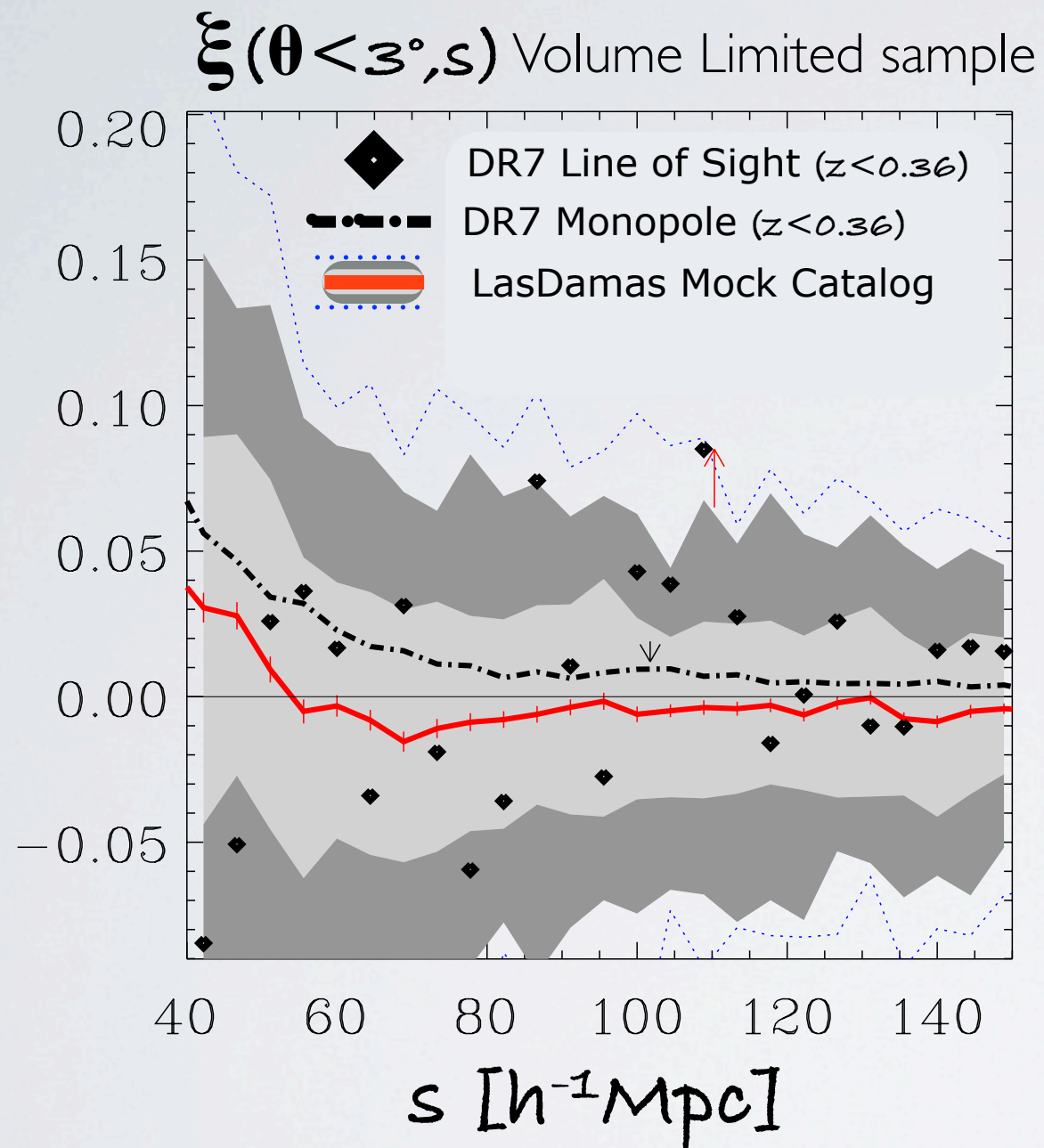


# Baryonic Acoustic Feature in SDSS LRGs Line of Sight Detection?





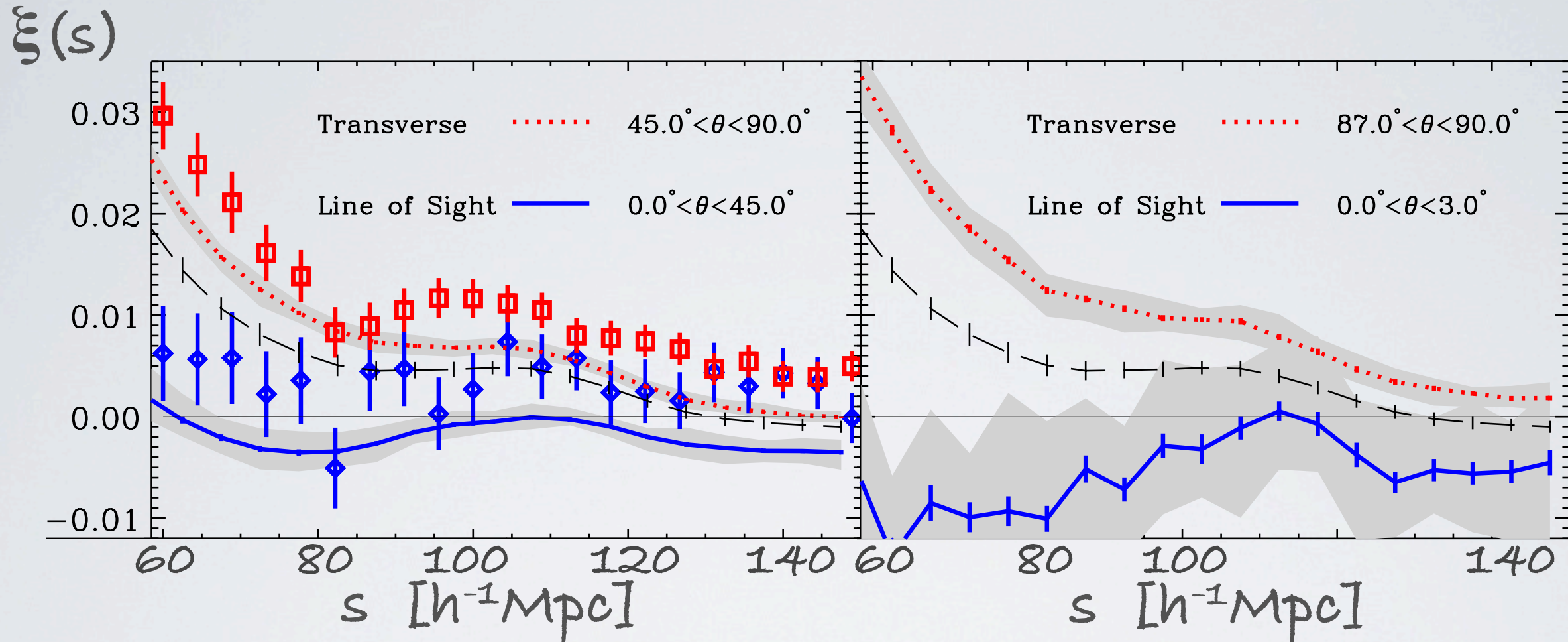
# Baryonic Acoustic Feature in SDSS LRGs Line of Sight Detection?



- SDSS-II does not contain enough modes to measure the line of sight BA feature at  $\theta < 3^\circ$
- The strong signal at  $110 \text{ h}^{-1}\text{Mpc}$ , although unlikely, is consistent with being noise

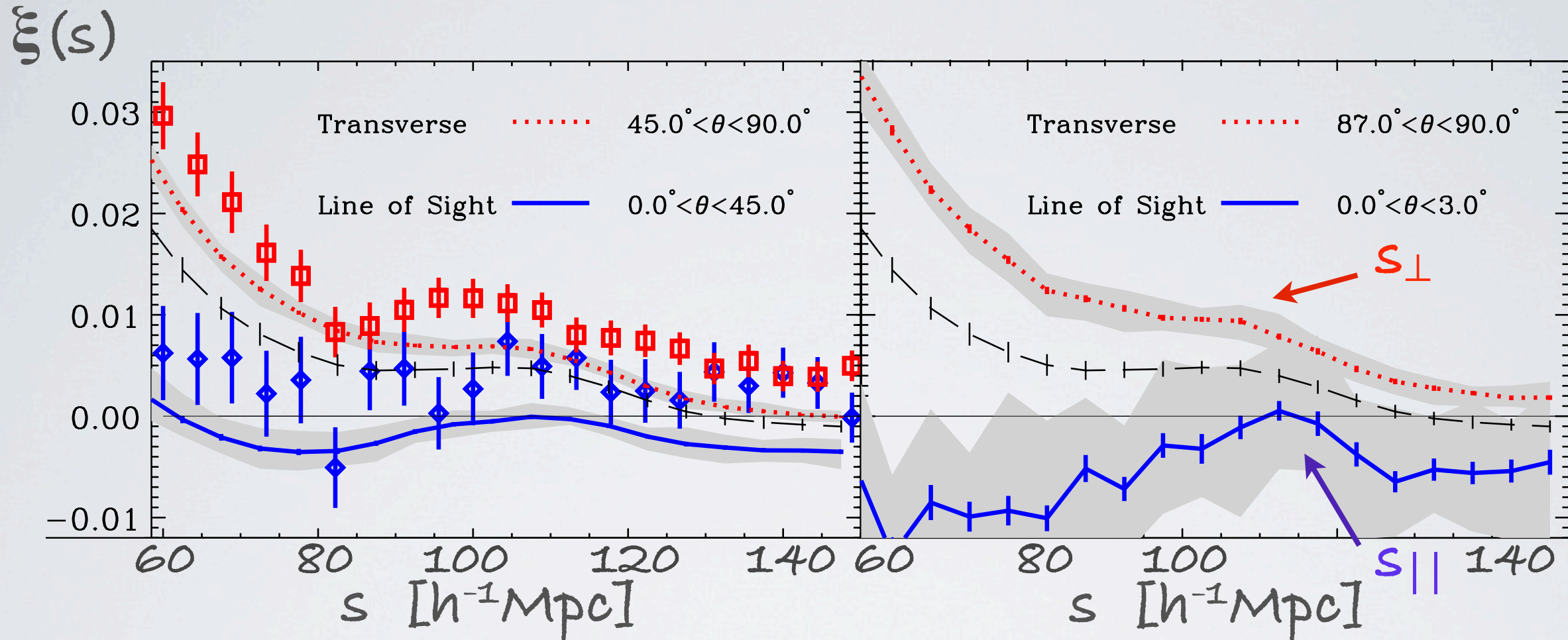


# Baryonic Acoustic Feature in BOSS LRGs in Line of Sight and Transverse Directions





# Baryonic Acoustic Feature in BOSS LRGs in Line of Sight and Transverse Directions

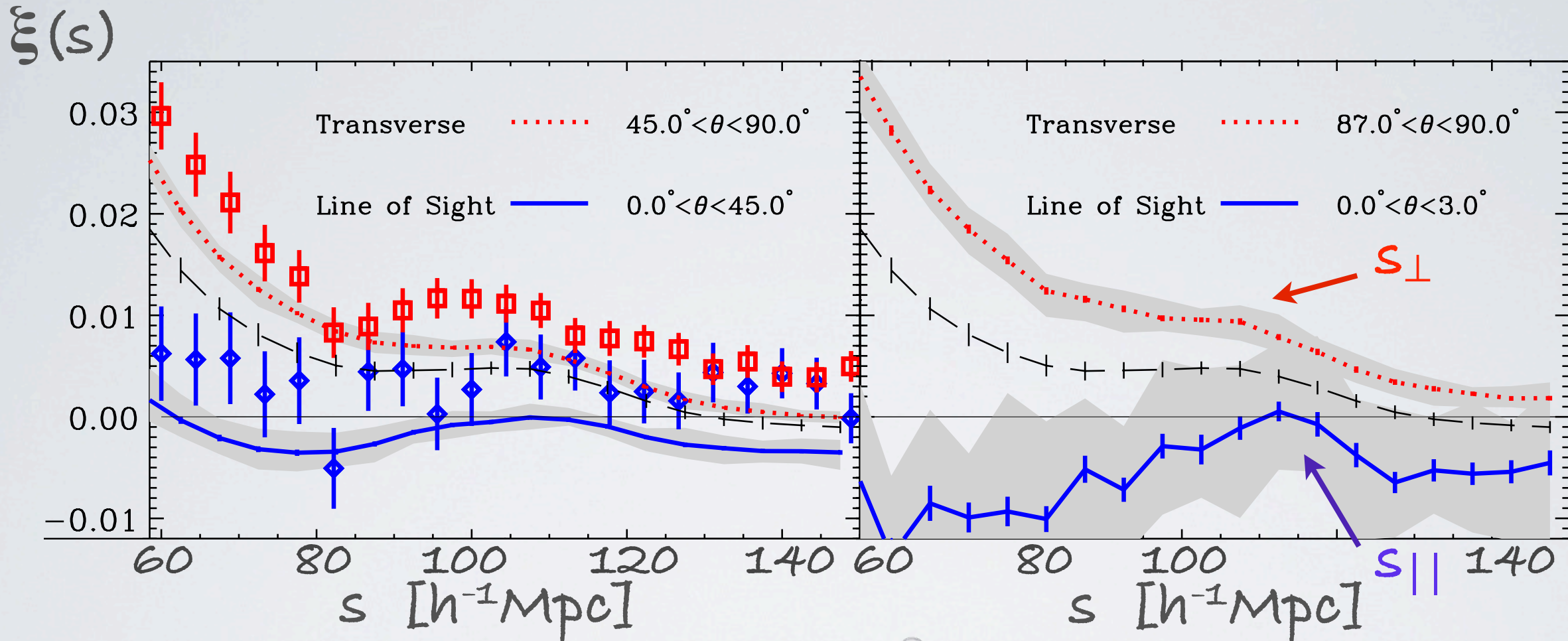


$$\int dz' / H(z') = s_\perp / \Delta\alpha / c$$

$$H(\langle z \rangle) \sim c \Delta z / s_{||}$$



# Baryonic Acoustic Feature in BOSS LRGs in Line of Sight and Transverse Directions



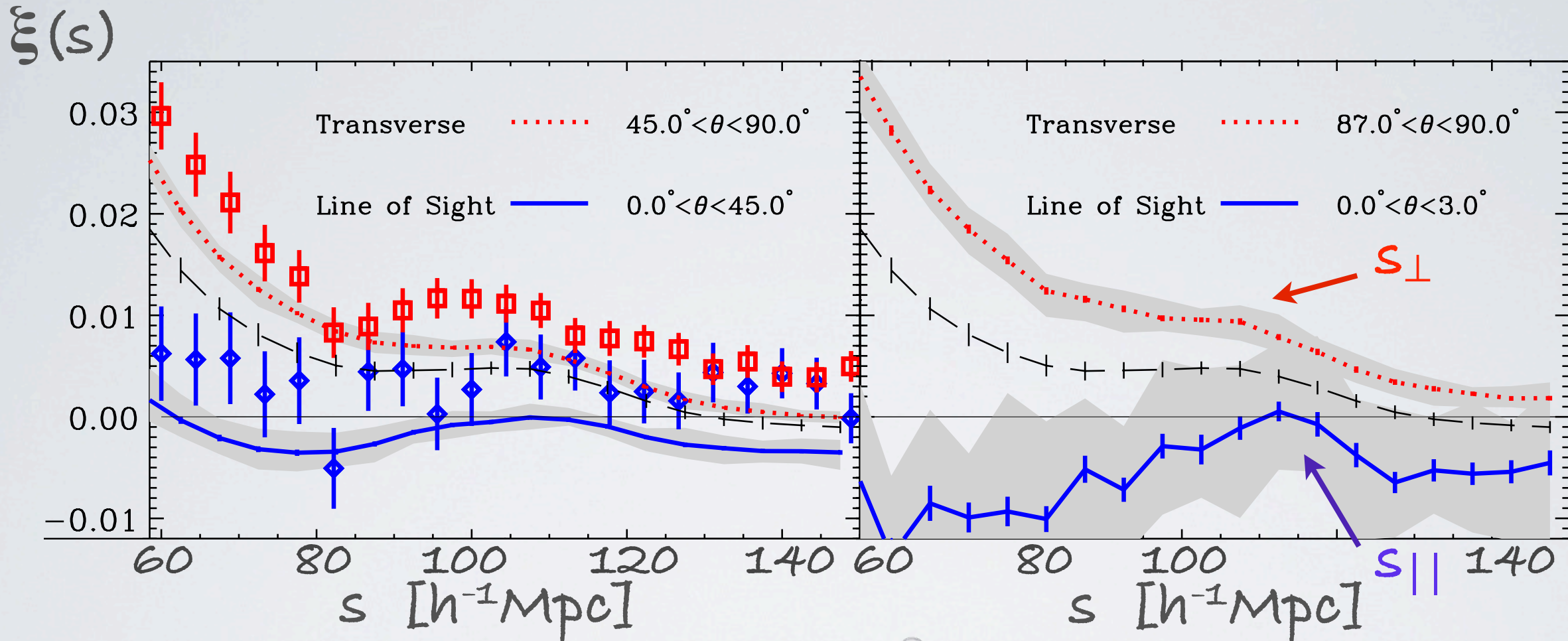
- The strong SDSS-II signal at 110 h<sup>-1</sup>Mpc is predicted to be ruled out by BOSS
- BOSS *does contain* enough modes to measure the line of sight BA feature, although for  $r_p < 5.5$  h<sup>-1</sup>Mpc the signal is noisy.

$$\int dz' / H(z') = s_\perp / \Delta\alpha / c$$

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# Baryonic Acoustic Feature in BOSS LRGs in Line of Sight and Transverse Directions



- The expected separation btw line-of-sight and transverse signals for large  $\Delta\theta$  raise optimism for disentangling  $H(\langle z \rangle)$  and  $D_A(\langle z \rangle)$

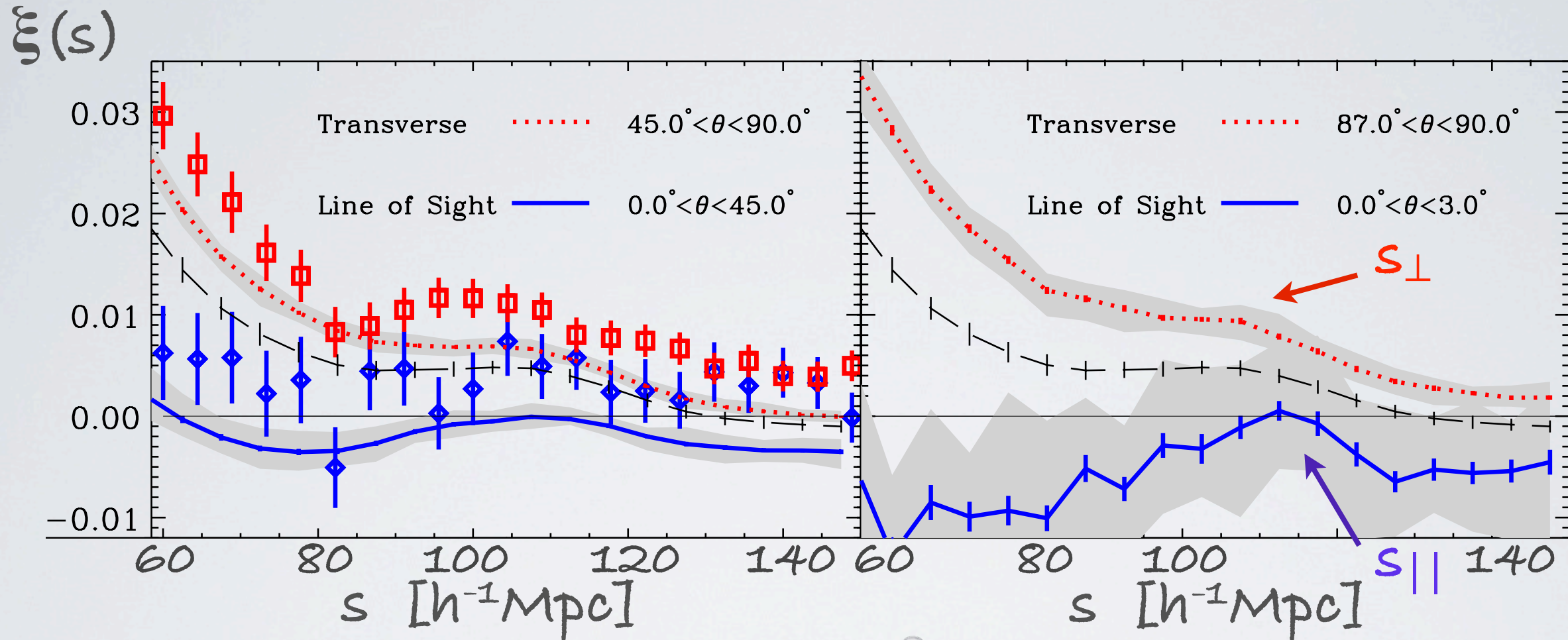
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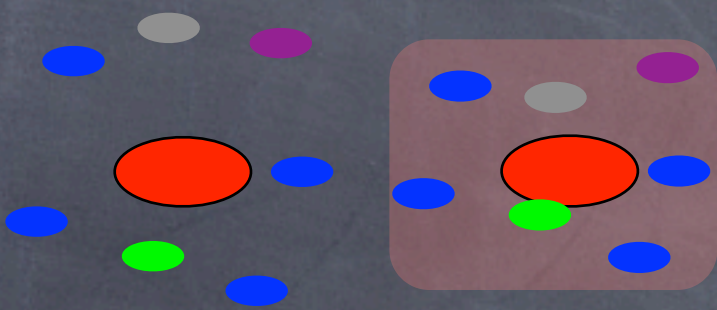
$$H(\langle z \rangle) \sim c \Delta z / s_{||}$$

**Kazin et al.  
coming very soon...**

Today I will discuss:

- ☐ Introduction 13 minutes
- ☒ Quantifying Clustering
- ☒ LRGs- Why (should) we like these galaxies so much?
- ☒ The Sloan Digital Sky Survey
- ☒ Baryonic Acoustic Feature 30 minutes
- ☐ Introduction to Redshift Distortions 2 minutes
- ☐ Redshift Distortions in Clustering 5 minutes





# Quantifying the Squashing Effect

Kaiser 1987: conservation of number of objects when going from real-space to z-space

$$n(s)d^3s = n(r)d^3r$$

where

$$\mu \equiv \cos(\theta)$$

$$f \equiv d\ln(D_1)/d\ln(a)$$

and

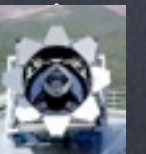
overdensity  $\delta(a) \approx D_1 \delta_{\text{initial}}$   $D_1$ -linear growth factor

$a = 1/(1+z)$  expansion factor

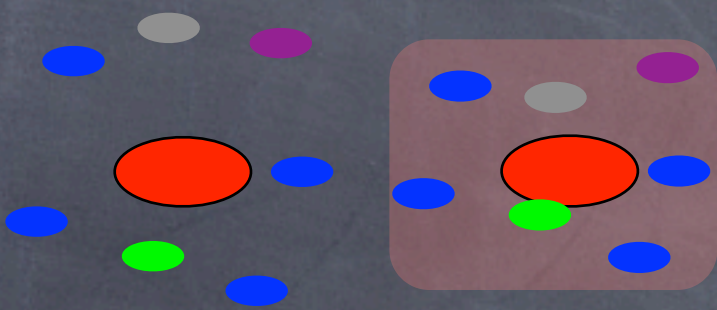
$$P^{(s)}(k, \mu) = (1 + f\mu^2)^2 P(k)$$

z-space  
matter

real space  
matter







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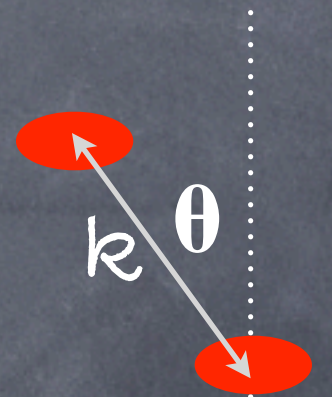
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z-space  
matter

real space  
matter



$$P^{(s)}_{\text{gal}}(k, \mu) = (1 + \beta\mu^2)^2 P_{\text{gal}}(k)$$

z-space  
tracer

real space  
tracer

$$= (b + f\mu^2)^2 P(k)$$

real space  
matter

$$\beta \equiv f/b_1$$

where

$$\delta_{\text{gal}} \approx b_1 \delta$$





# Extracting information from the Squashing Effect



Kaiser 1987:  $\beta \equiv f(z)/b_1 \approx \Omega_M^\gamma(z)/b_1$

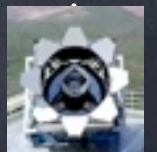
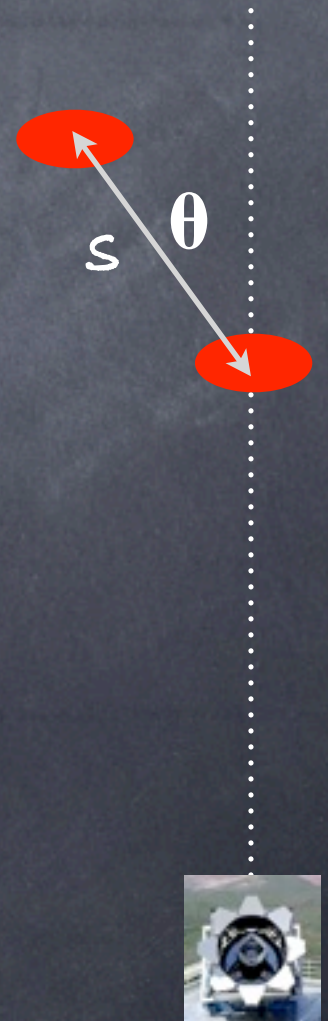
growth index  
 $\Lambda$ CDM:  $\gamma \sim 0.56$

DGP:  $\gamma \sim 0.68$

So:  $\beta \leftrightarrow \Omega_M$

Or:  $\beta \leftrightarrow \text{gravity (through } \gamma; \text{ Linder 2005)}$

Or:  $\beta \leftrightarrow \text{break (bias)} \sigma_8 \text{ degeneracy}$





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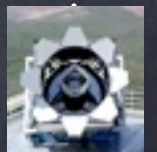
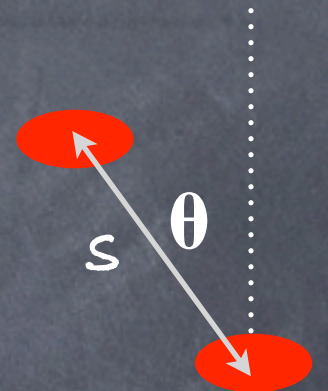
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Or:  $\beta \leftrightarrow$  break (bias)  $\sigma_8$  degeneracy

Quadrupole Test: No dependence on scale!

$$Q \equiv \frac{\text{quadrupole/monopole}}{P_2(k)/P_0(k)} = (4/3\beta + 4/7\beta^2) / (1 + 2/3\beta + 1/5\beta^2)$$





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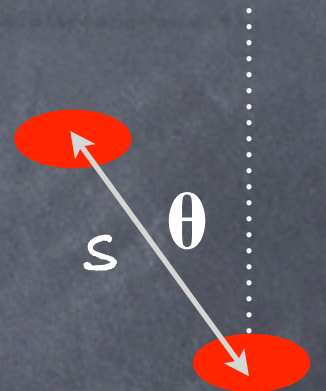
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In configuration space (Hamilton 1992):

$$Q = \frac{\xi_2(s) / [ \xi_0(s) - \langle \xi_0(s) \rangle ]}{(4/3\beta + 4/7\beta^2) / (1 + 2/3\beta + 1/5\beta^2)}$$

where  $\xi_l(s) = (2l+1)/2 \int \xi(\mu', s) \mathcal{L}_l(\mu') d\mu'$



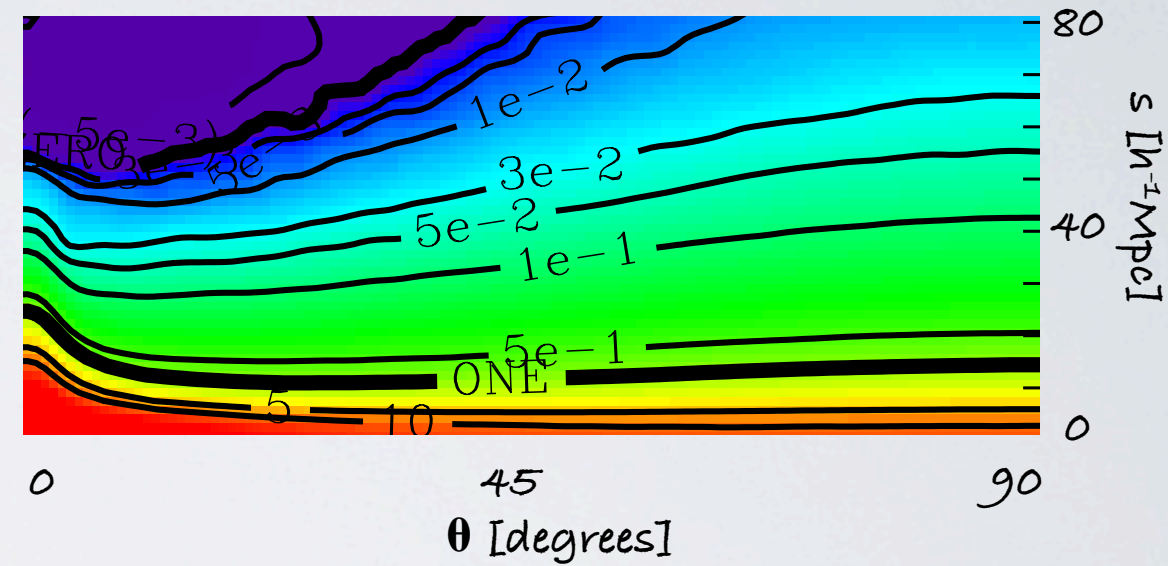


# $\beta$ through the Quadrupole Test

## Non-Linear Theory

$$Q = \xi_2(s) / [\xi_0(s) - \langle \xi_0(s) \rangle] = (4/3\beta + 4/7\beta^2) / (1 + 2/3\beta + 1/5\beta^2)$$

$$\xi(\theta, s)$$



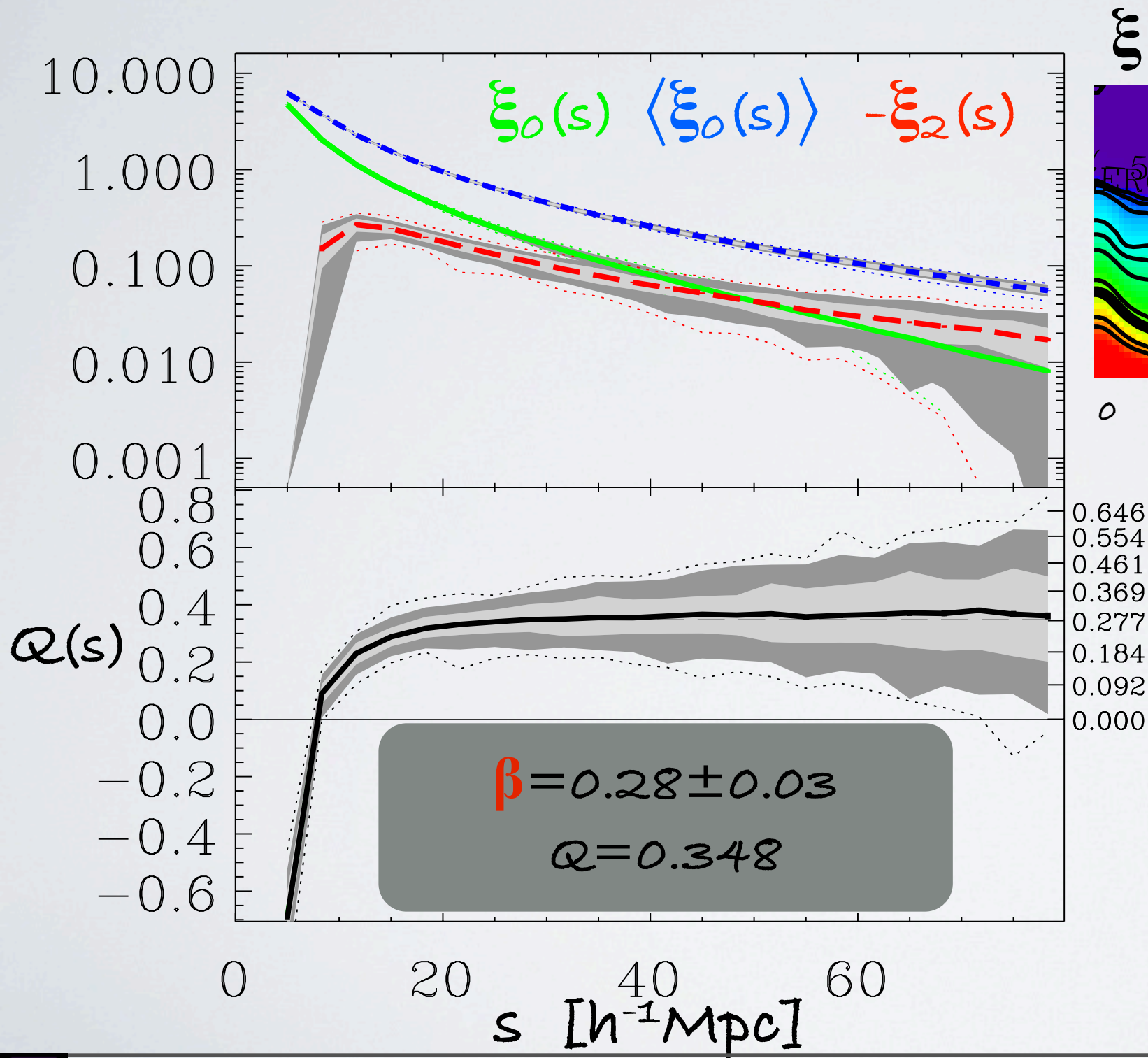
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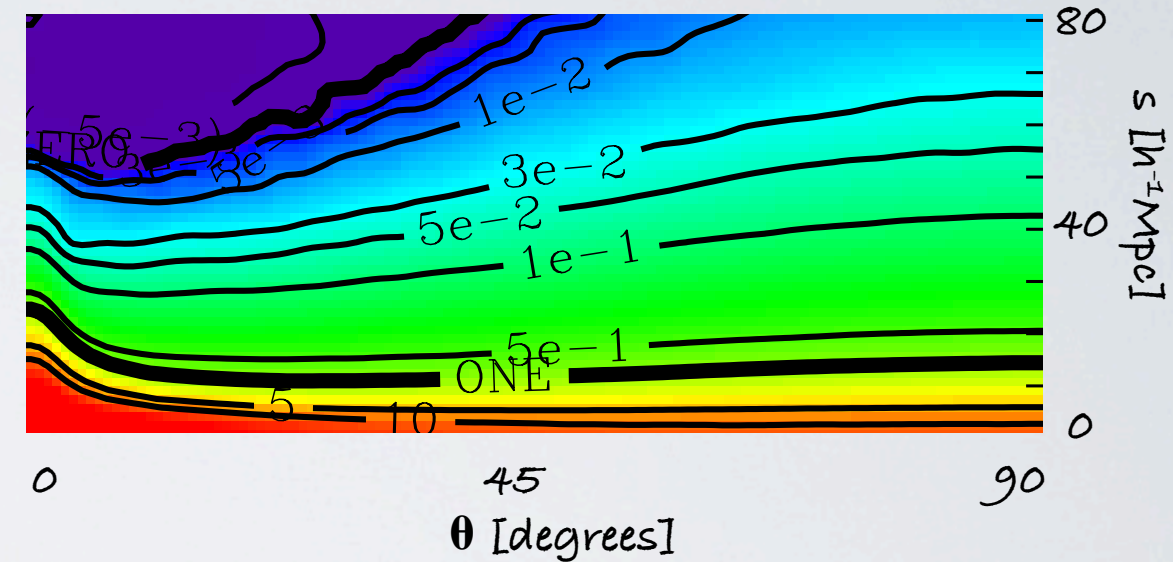
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$\xi(\theta, s)$



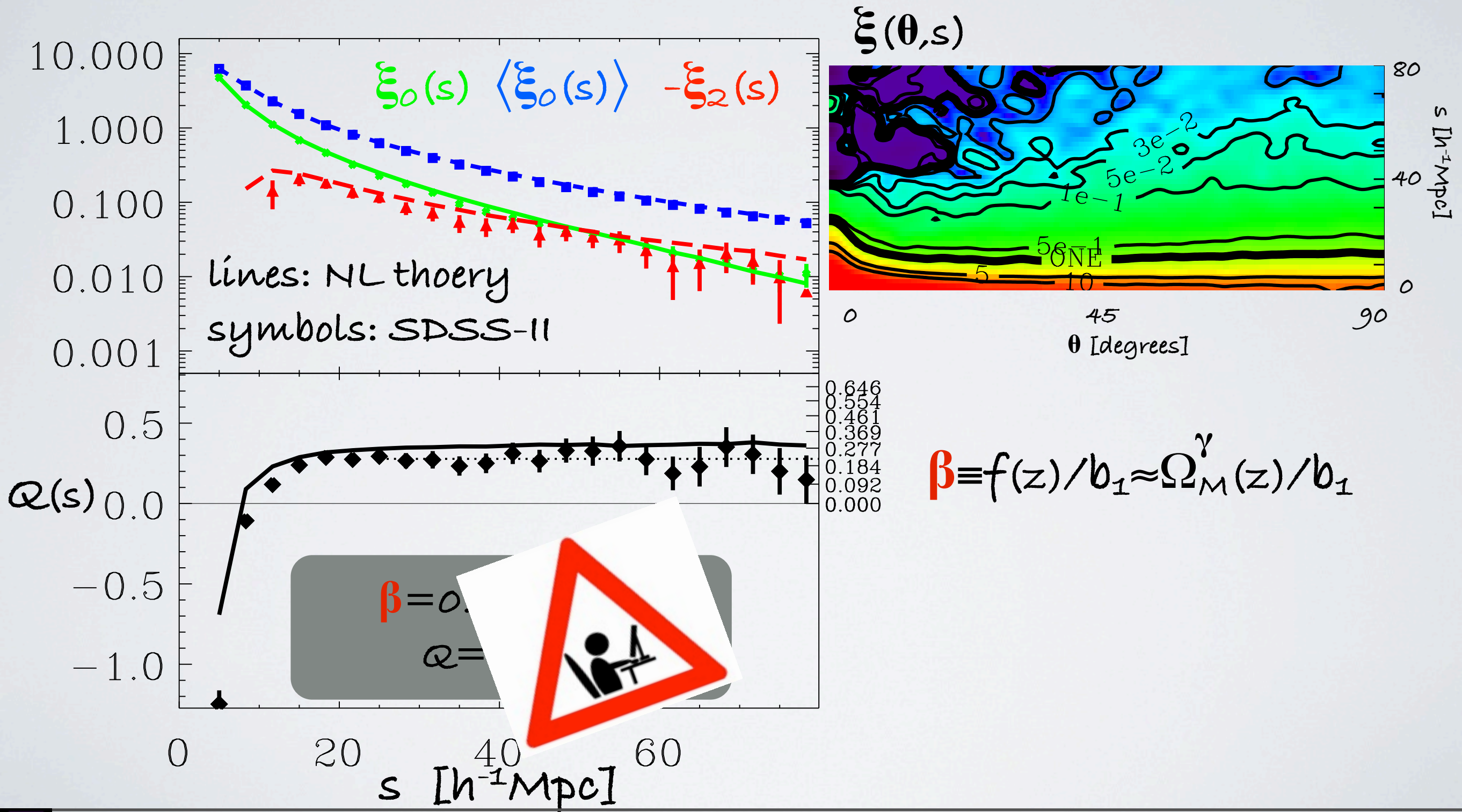
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# $\beta$ through the Quadrupole Test

## SDSS-II Results

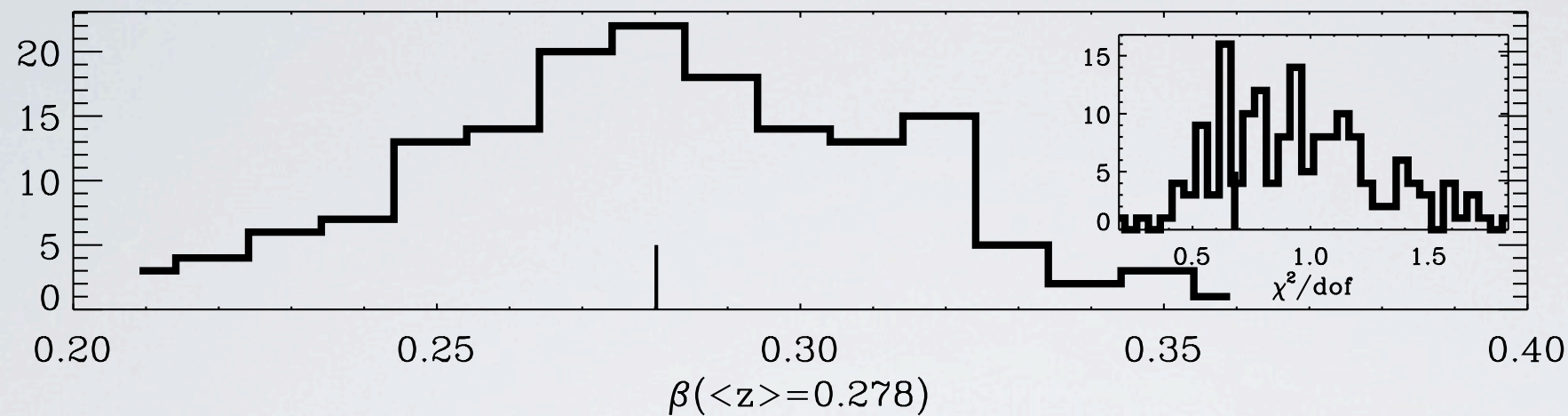
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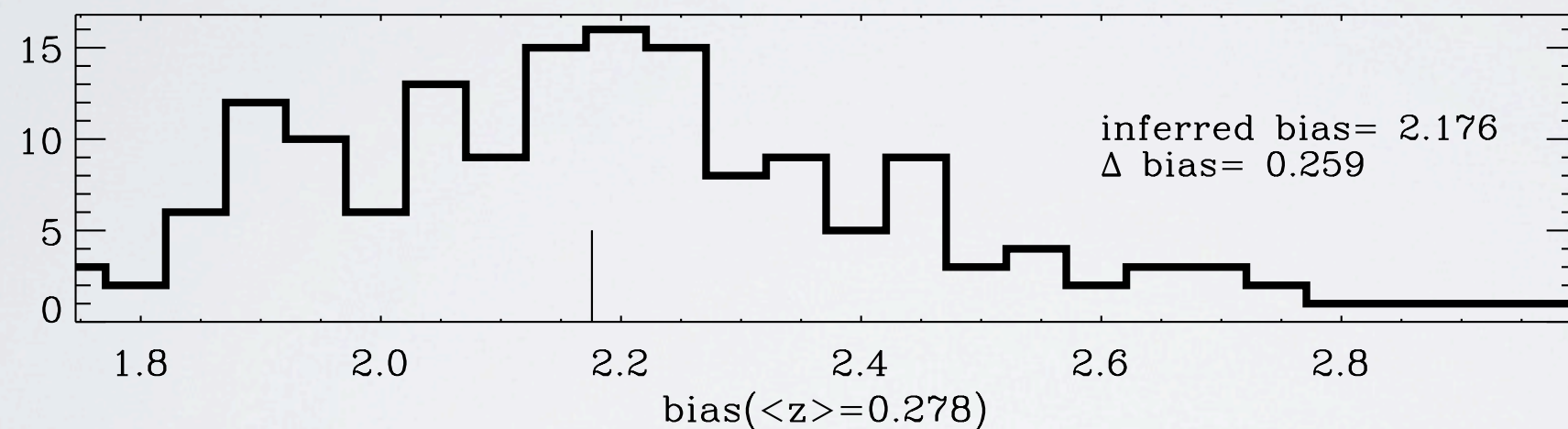


# Quadrupole Test- Cosmological Significance

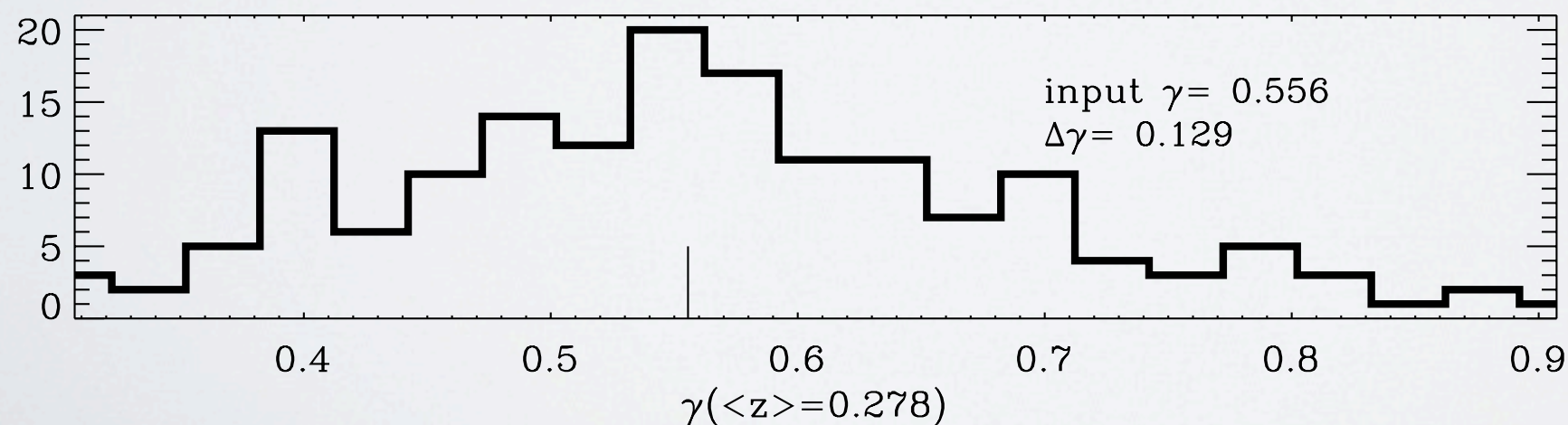
$$\beta \equiv f(z)/b_1 \approx \Omega_M^\gamma(z)/b_1$$



$$\sigma_\beta/\beta \sim 10\%$$



$$\sigma_{\text{bias}}/\text{bias} \sim 10\%$$

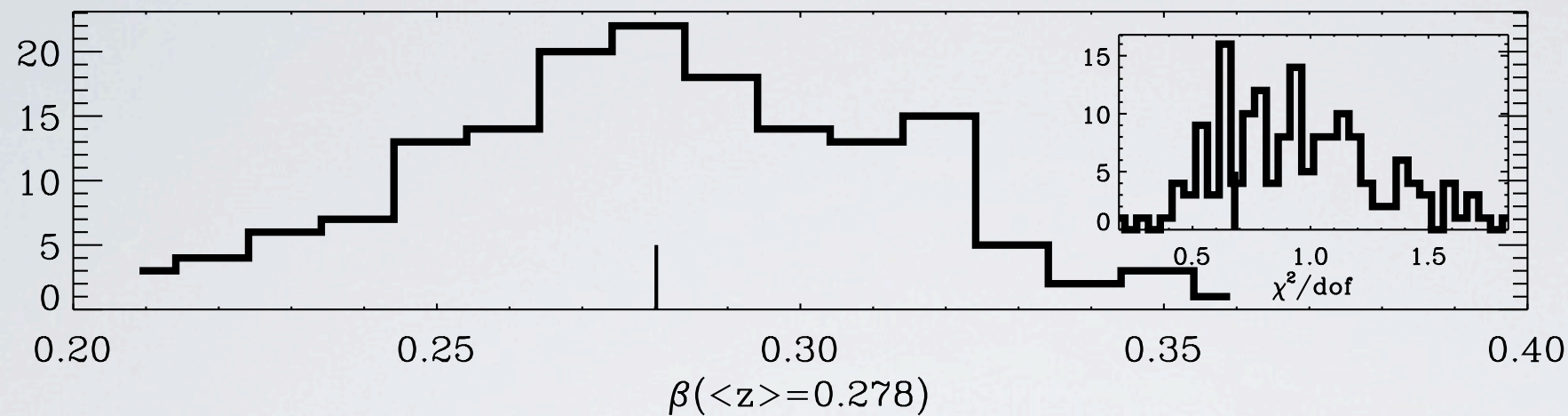


$$\sigma_\gamma/\gamma \sim 25\%$$

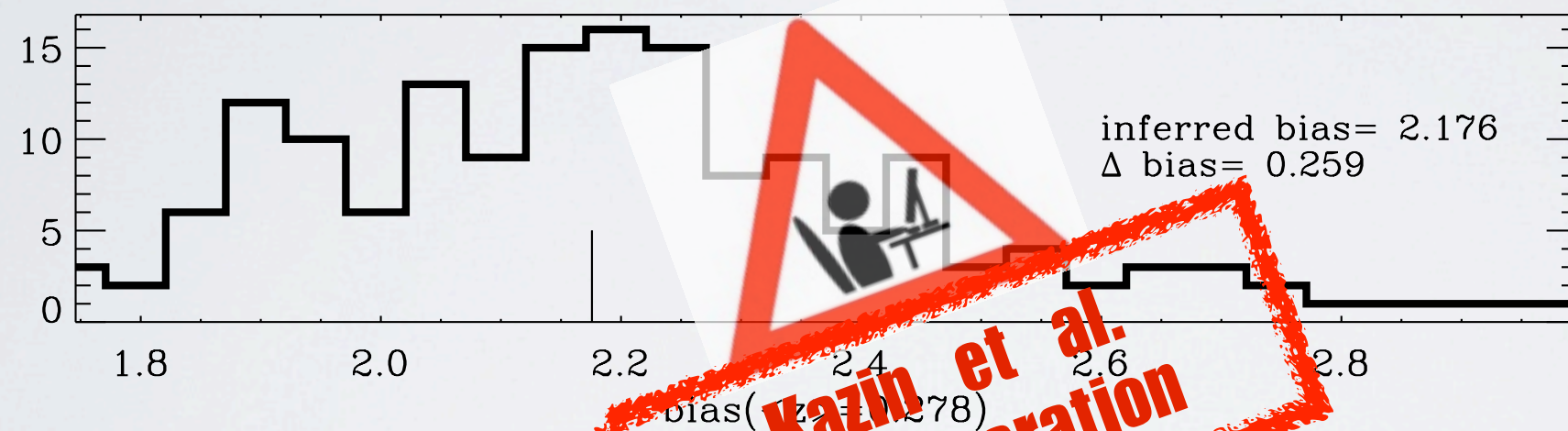


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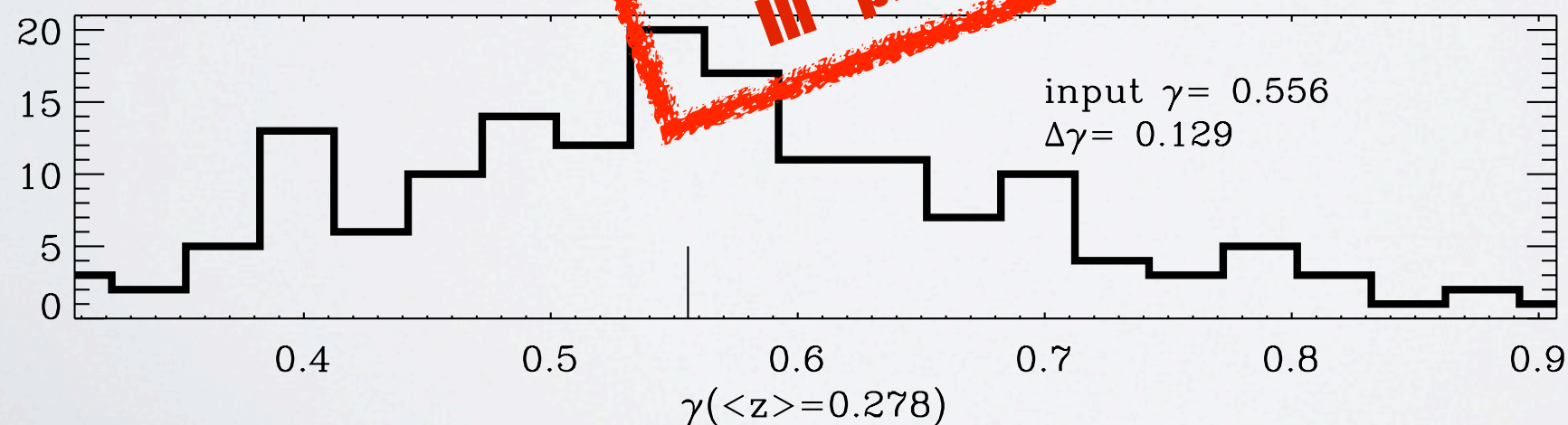
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$$\sigma_{bias}/bias \sim 10\%$$



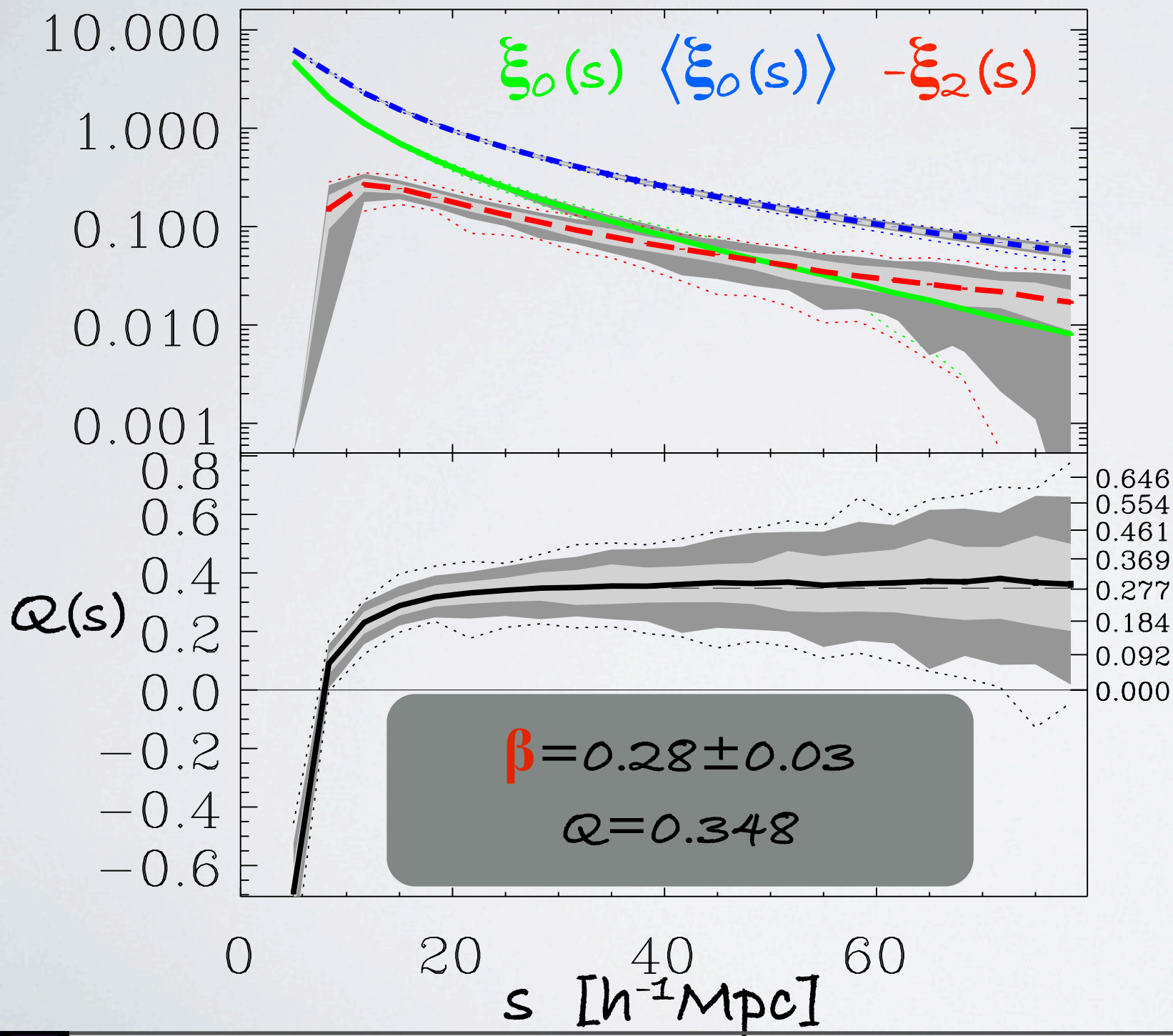
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SDSS-II

$$\sigma_\beta / \beta \sim 10\% - 15\%$$

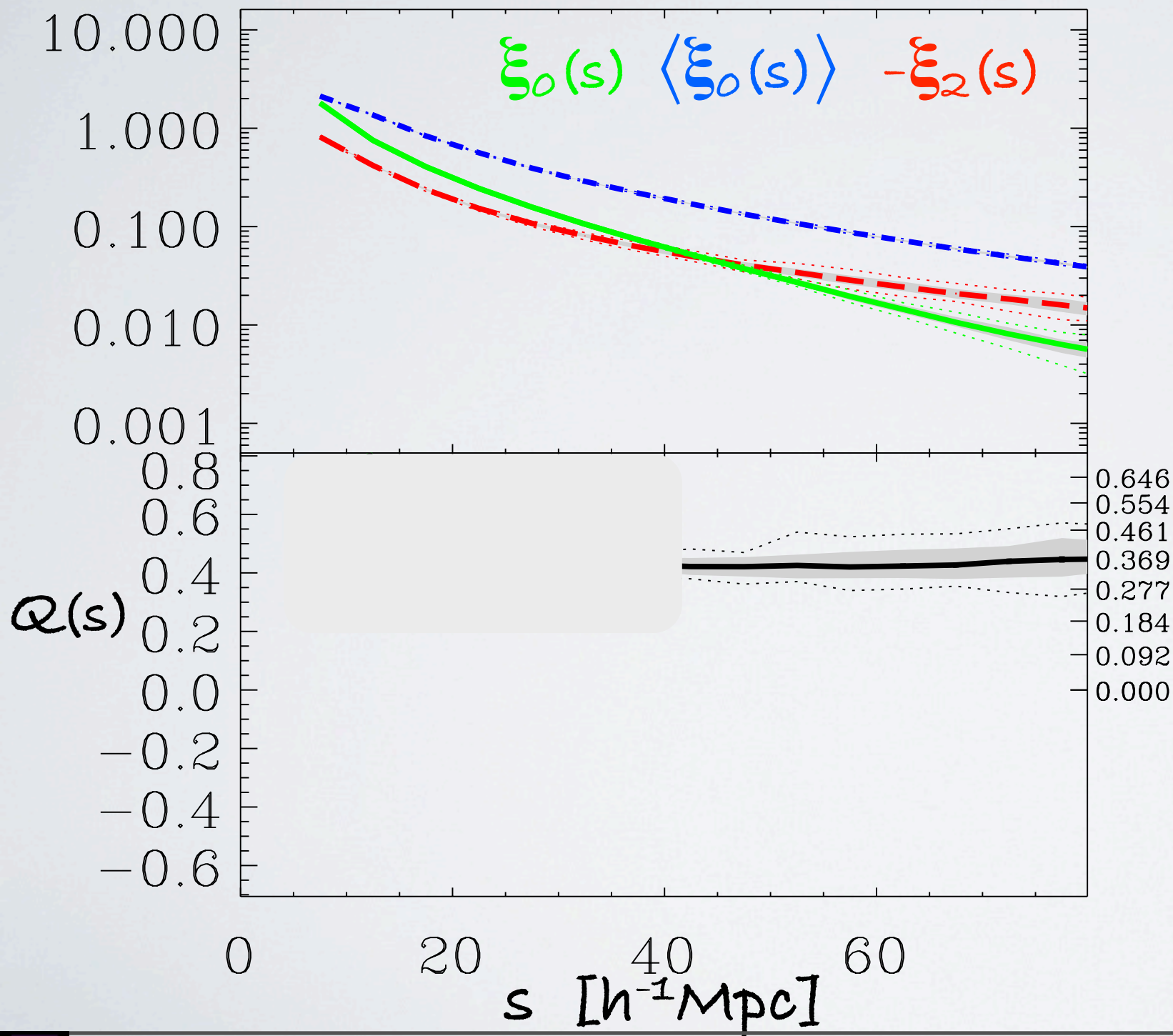
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SDSS-III

$$\sigma_\beta / \beta \sim 7\%$$

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# Summary

- ☒ Baryonic Acoustic Feature in SDSS-II  $\xi$  Monopole
  - ☒ Apparent in LRG clustering, and consistent with  $\Lambda$ CDM cosmology.
  - ☒ Can be used to measure distance to  $z \sim 0.28$  at accuracy of 3%
  - ☒ Prediction: Strong signal at  $s \sim 130 h^{-1} \text{Mpc}$  will not appear in BOSS
- ☒ Baryonic Acoustic Feature in Line of Sight  $\xi$ 
  - ☒ Not measurable in SDSS-II due to lack of modes
  - ☒ Will be noisy in BOSS when restricting to thin angular slice ( $\theta < 3^\circ$ )
  - ☒ Using wider wedges- BOSS will be able to be distinguished from transverse signal, enabling disentanglement of  $H(z)$  and  $D_A(z)$
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  - ☒ Yields  $\sigma_\beta/\beta \sim 10\%$  @  $z \sim 0.28$  (sample variance)
  - ☐ Cosmological constraints

“All astronomers do these days is count photons, galaxies and citations”, M.R.B



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$\xi$ ,  $c_{ij}$  results as well as LRG sample may be obtained here!  
<http://cosmo.nyu.edu/~eak306/LSS.html>



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*Thank You!*

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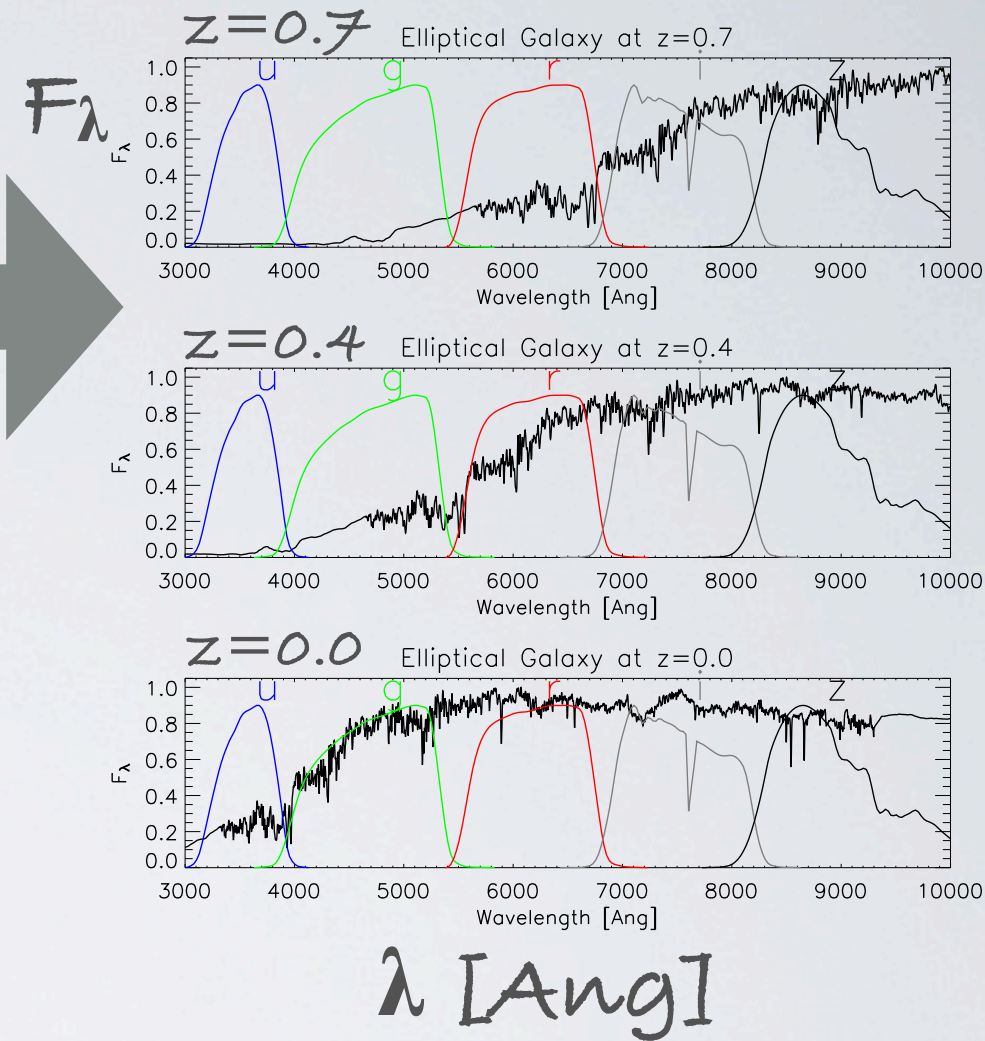
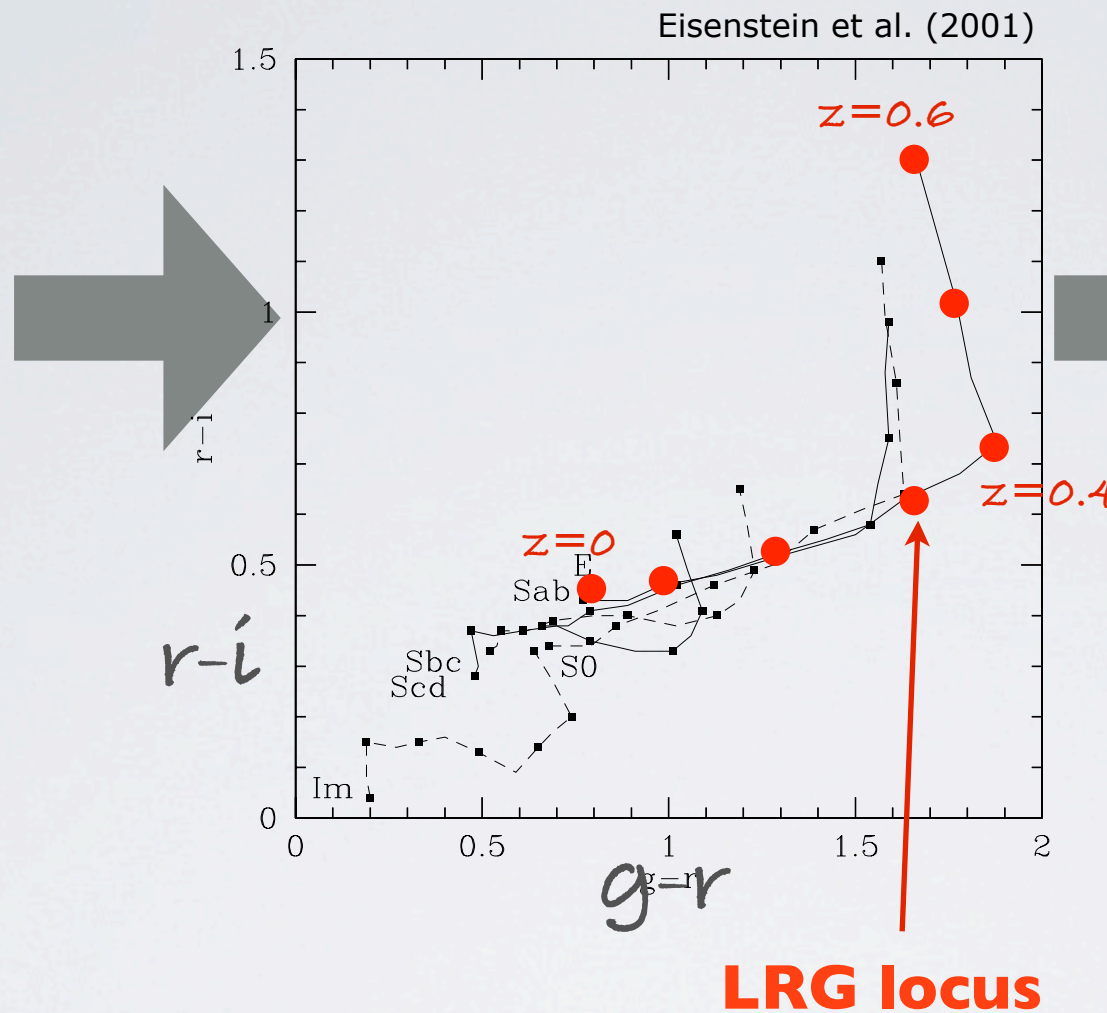
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# Luminous Red Galaxies

Padmanabhan et al. (2007)

based on Bruzual&Charlot (2003) model



- Luminous ➤ Enable large volume limited samples
- Not too rare  $n(z) \sim 3 \cdot 10^{-4} (h\text{Mpc}^{-1})^3$
- Trace Matter well, “bias” (clustering gain)  $b_{\text{Lin}} \sim 2$
- Easy to identify by color cuts, spectra

$$\delta_{\text{gal}} \approx b_{\text{Lin}} \delta$$



# Some Cosmography

Hubble Equation;  
assumptions:  
low  $z$ 's  
 $v_H \ll c$

$$cz = v_H = H_0 d = H_0 \chi / (1+z)$$

Comoving  
distances  
generalized

$$\chi(z) = c \int_0^z dz' / H(z')$$

Assuming flat  $\Lambda$ CDM

expansion rate

$$H(z) = H_0 \{ \Omega_M (1+z)^3 + \Omega_\Lambda f(z) \}^{0.5}$$

where

$$f(z) \equiv \exp \left[ 3 \int_0^z dz' (1+w(z')) / (1+z') \right]$$

equation of state  $w \equiv P_\Lambda / \rho_\Lambda$



# Some Cosmography

more

$$\chi(z) = c \int_0^z dz' / H(z')$$

comoving distance

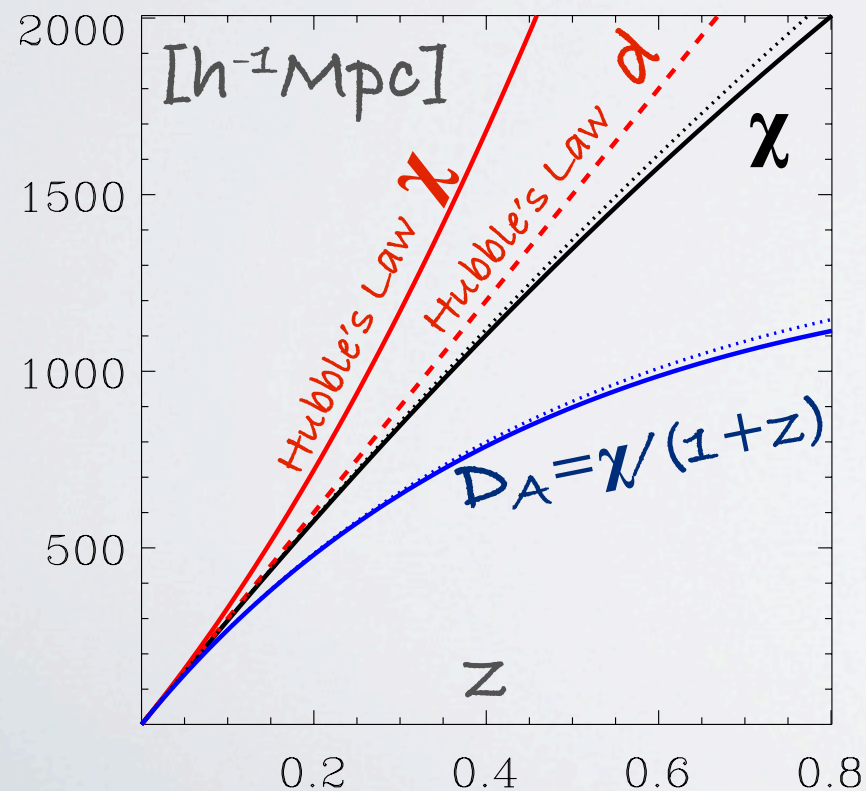
$$D_A = \frac{\sin\{\sqrt{-\Omega_K} \chi\}}{(1+z) \sqrt{-\Omega_K}}$$

angular distance (not comoving!)

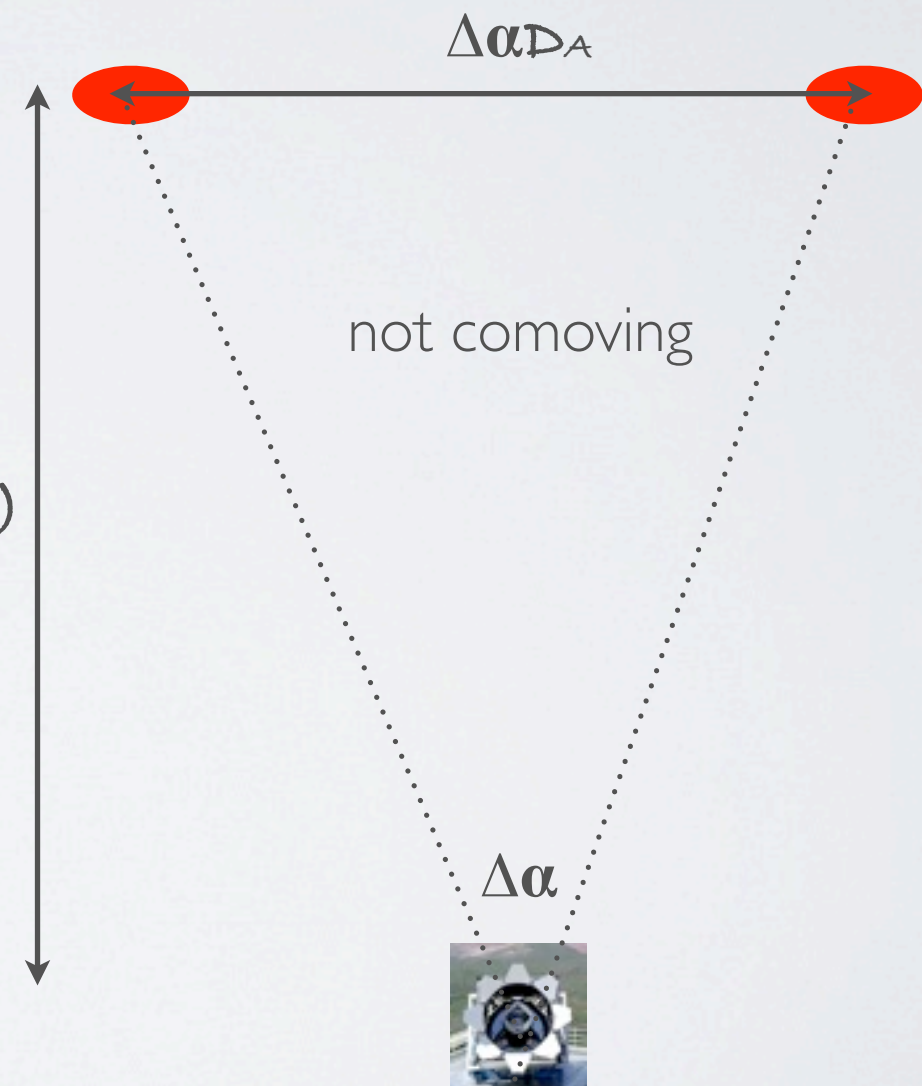
$\Omega_K > 0$  open universe  
 $\Omega_K < 0$  closed

assuming flat universe  $\Omega_K \Rightarrow 0$

$$\approx \frac{\chi}{(1+z)}$$



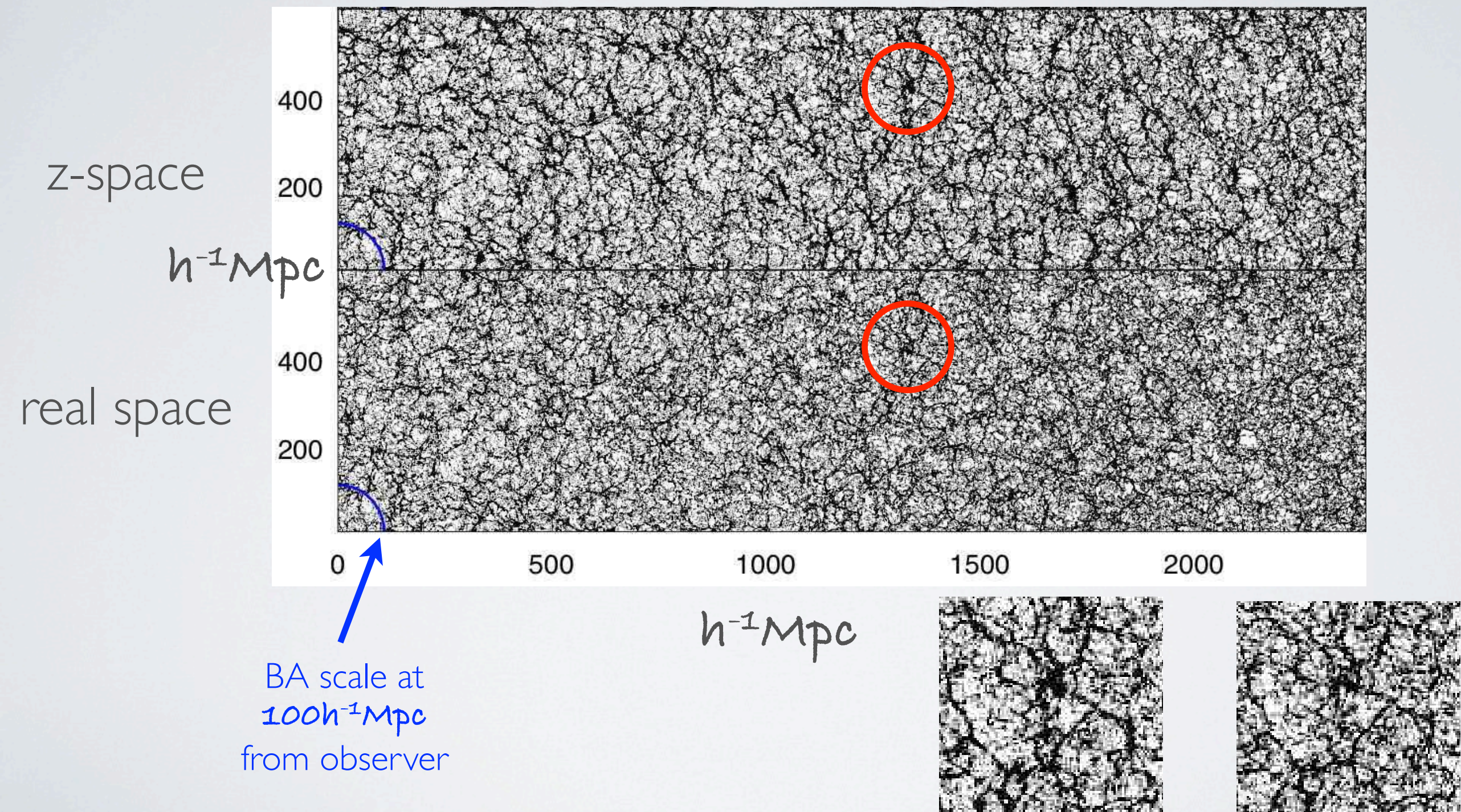
$$D_A = \chi / (1+z)$$





# Redshift Distortions

Dark Matter Simulation  
Benítez et al. (2008)





# The Alcock&Paczynski Effect

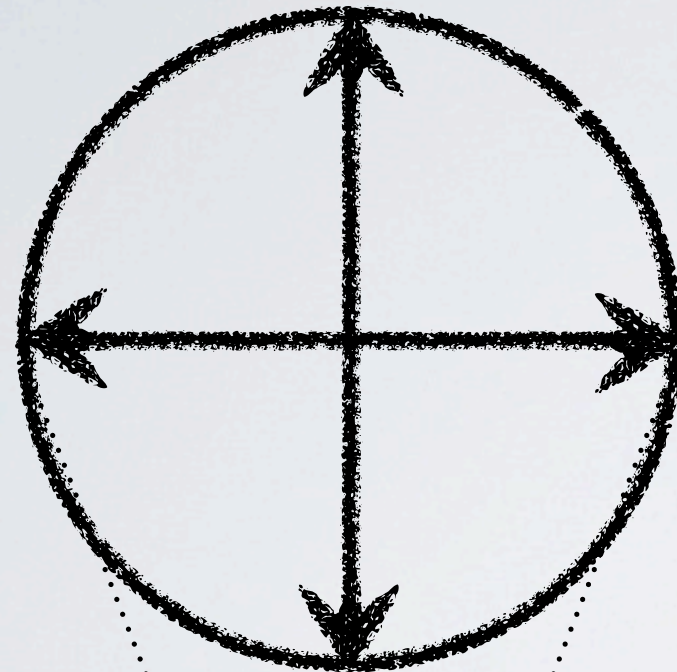
$\longleftrightarrow \alpha z$   
 $\updownarrow \Delta z$

Real Space

$$\frac{\Delta z}{\alpha z} = 1$$

Redshift Space  $\frac{\Delta z}{\alpha z} > 1$

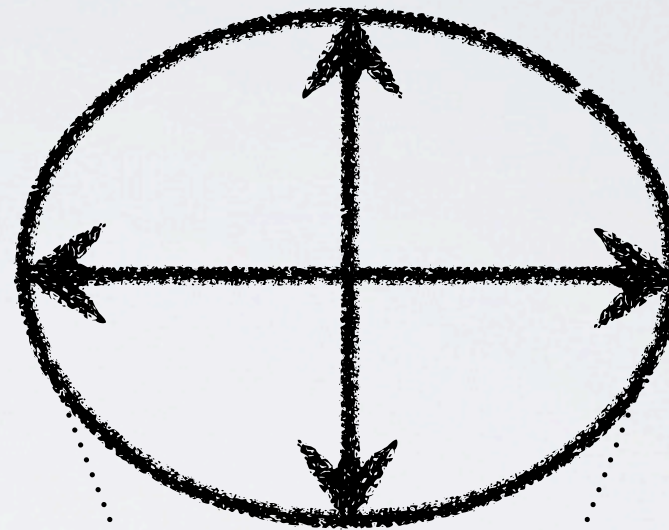
$$\frac{\Delta z}{\alpha z} < 1$$



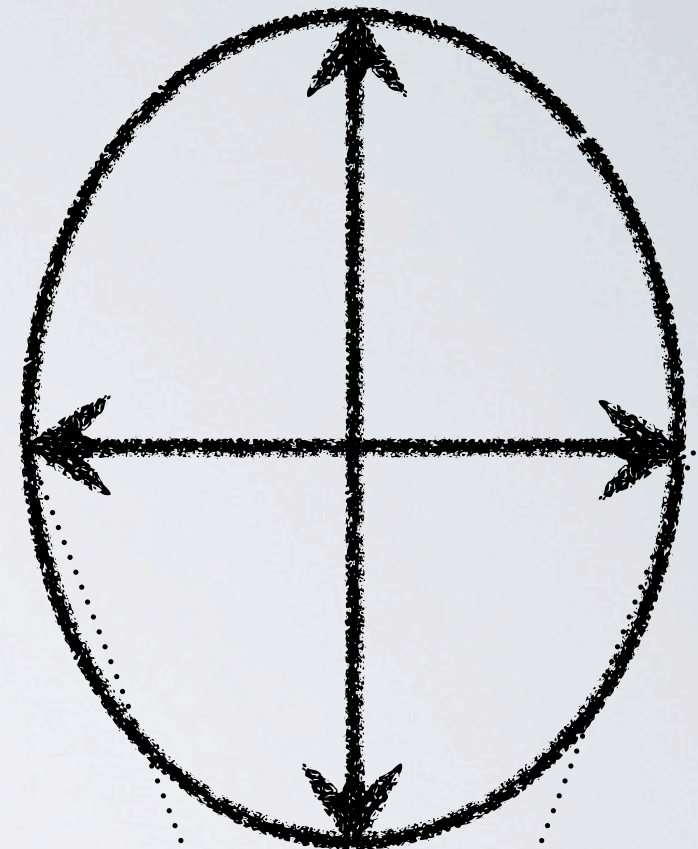
$H(z + \Delta z)$

$H(z)$

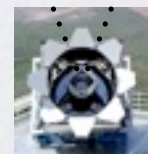
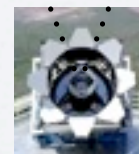
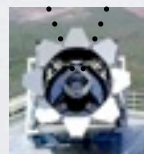
$H(z - \Delta z)$



$\alpha$

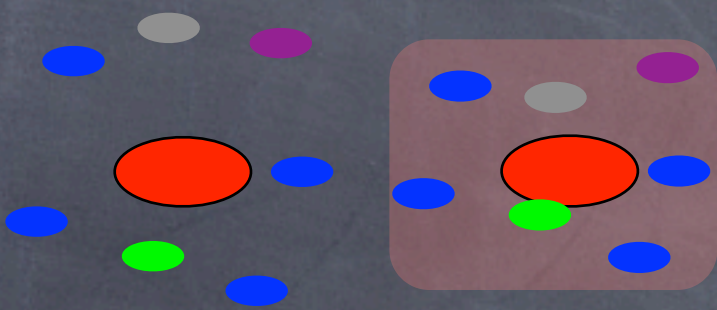


$\alpha$



$$\frac{\Delta z}{\alpha z} = z^{-1} [\Omega_{\Lambda} + \Omega_{M0} (1+z)^3]^{1/2} \int_1^{z+1} dy (\Omega_{\Lambda} + \Omega_{M0} y^3)$$





# Quantifying the Squashing Effect

Kaiser 1987: Spherical Harmonics

$$P_{gal}^{(s)}(k, \mu) = (1 + \beta \mu^2)^2 P_{gal}(k)$$

$$P_{gal}^{(s)}(k, \mu) = \mathcal{L}_0(\mu) P_0^{(s)}(k) + \mathcal{L}_2(\mu) P_2^{(s)}(k) + \mathcal{L}_4(\mu) P_4^{(s)}(k)$$

where

$$P_l(k) = 0.5(2l+1) \int P(\mu', k) \mathcal{L}_l(\mu') d\mu'$$

Legendre Polynomials

$$\mathcal{L}_0(\mu) = 1$$

$$\mathcal{L}_2(\mu) = 0.5(3\mu^2 - 1)$$

$$\mathcal{L}_4(\mu) = 0.125(35\mu^2 - 30\mu + 3)$$

and

$$\mu \equiv \cos(\theta)$$

$$f \equiv d \ln(D_1) / d \ln(a)$$

$$\beta \equiv f / b_1$$

$$\delta_{gal} \approx b_1 \delta$$

observables!

$$P_0^{(s)}(k) = B_0(\beta) P_{gal}(k)$$

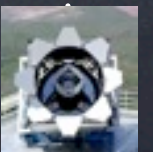
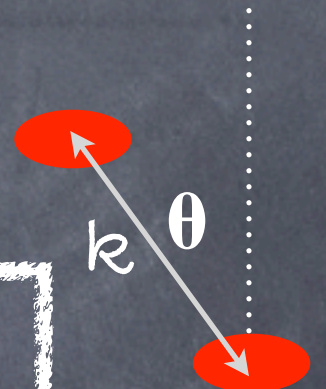
$$P_2^{(s)}(k) = B_2(\beta) P_{gal}(k)$$

$$P_4^{(s)}(k) = B_4(\beta) P_{gal}(k)$$

$$B_0(\beta) \equiv (1 + 2/3 \beta + 1/5 \beta^2)$$

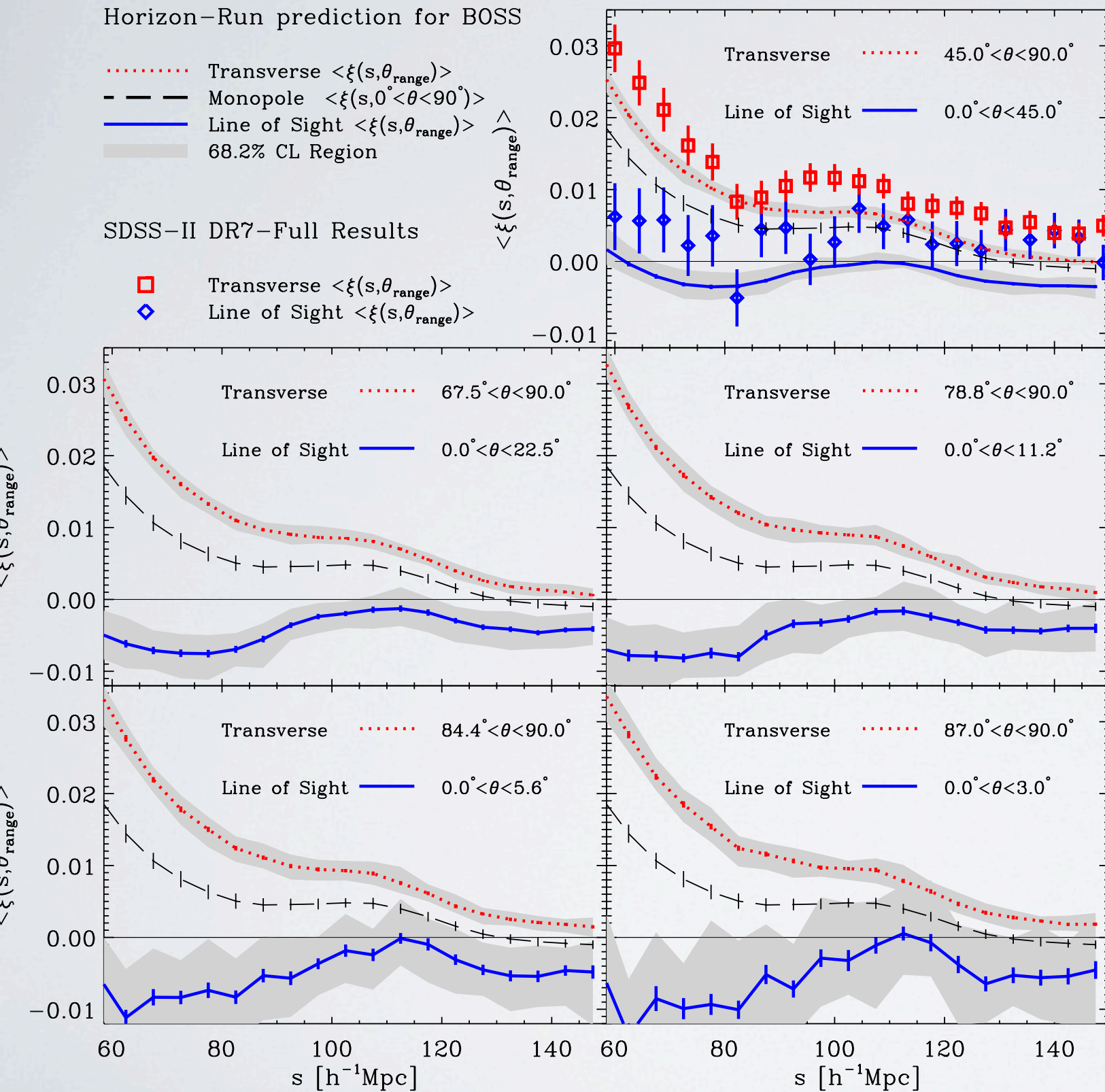
$$B_2(\beta) \equiv (4/3 \beta + 4/7 \beta^2)$$

$$B_4(\beta) \equiv 8/35 \beta^2$$



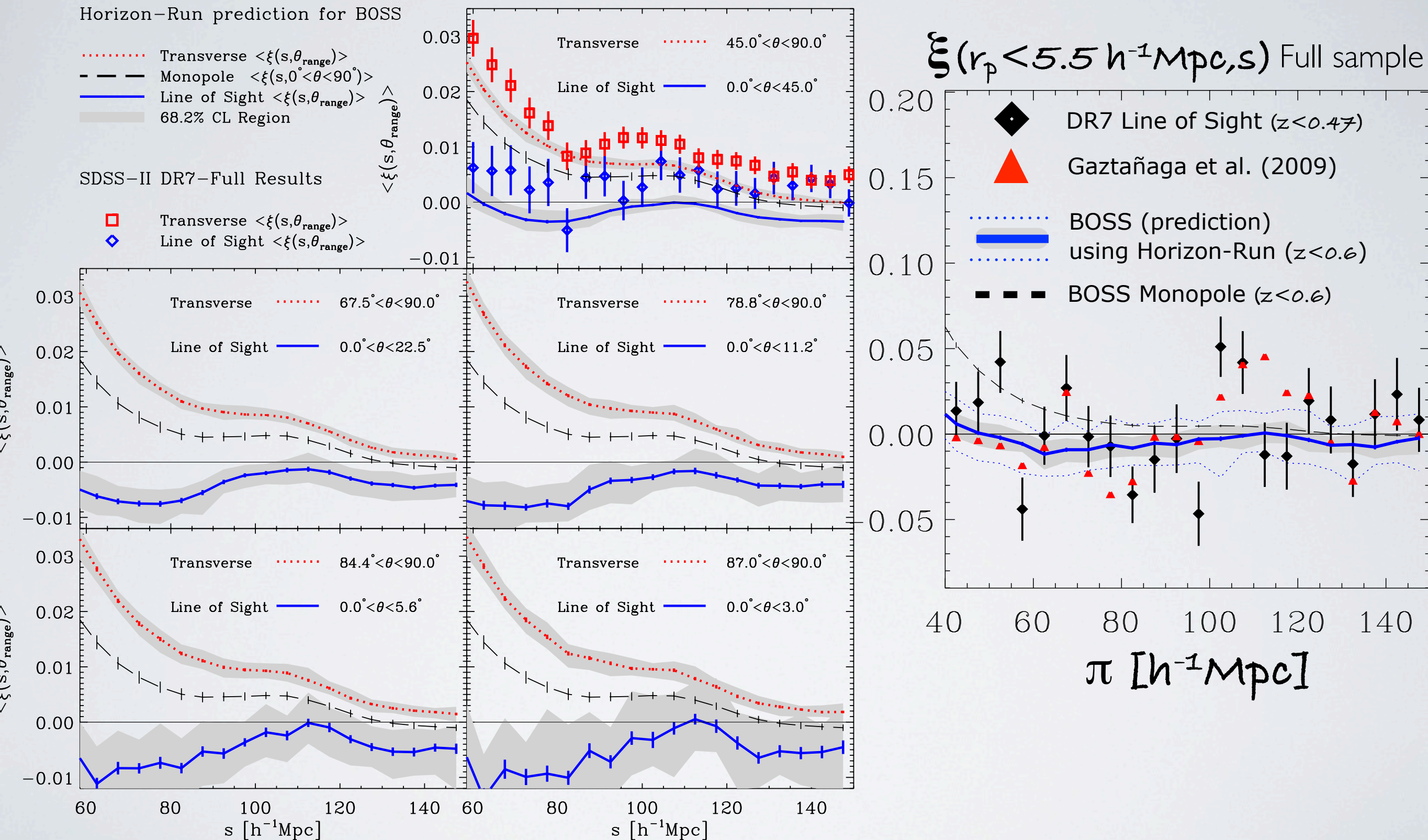


# What Should We Expect from BOSS?





# What Should We Expect from BOSS?









dotted: NL theory  
solid: SDSS-II

