

VOID DYNAMICS

CONSTRAINTS ON COSMOLOGY AND GRAVITY

NICO HAMAUS

in collaboration with

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GUILHEM LAVAUX, BENJAMIN WANDELT,
STÉPHANIE ESCOFFIER, GIORGIA POLLINA,
BEN HOYLE, JOCHEN WELLER**



1 VOIDS IN THEORY

2 VOIDS IN SIMULATIONS

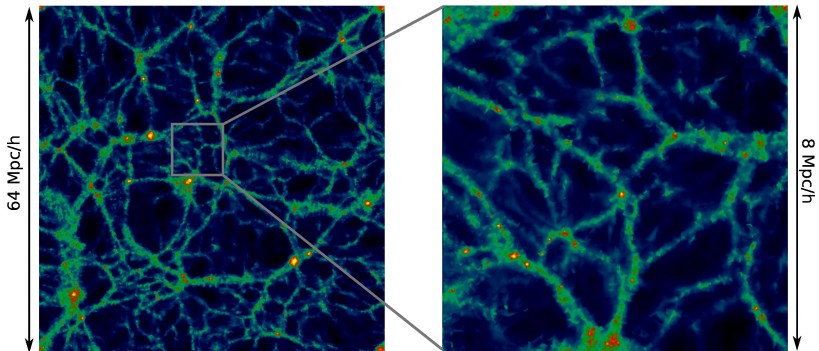
ARXIV: 1307.2571, 1403.5499, 1409.3580, 1507.04363

3 VOIDS IN OBSERVATIONS

ARXIV: 1602.01784

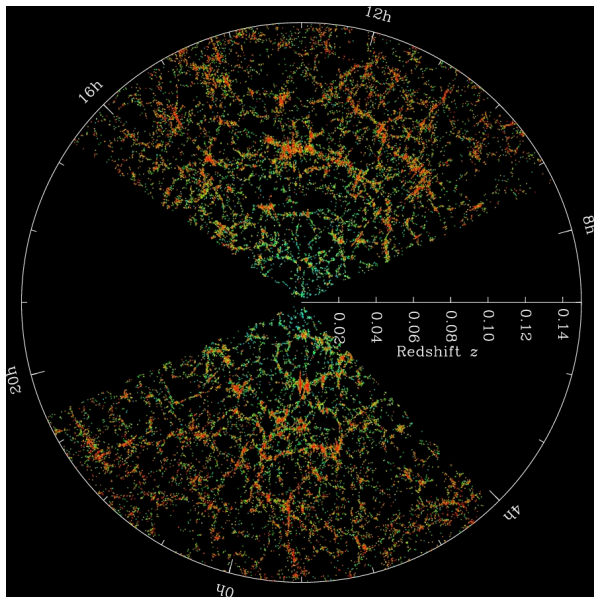
4 CONCLUSIONS

THE COSMIC WEB



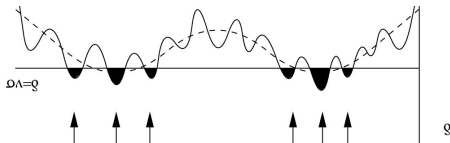
Aragon-Calvo, Szalay (2013)

SDSS GALAXIES



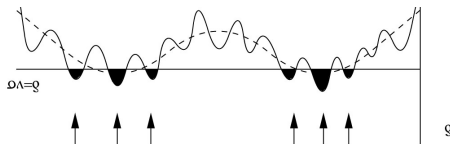
DEFINITION OF VOIDS

Search for local minima in density field

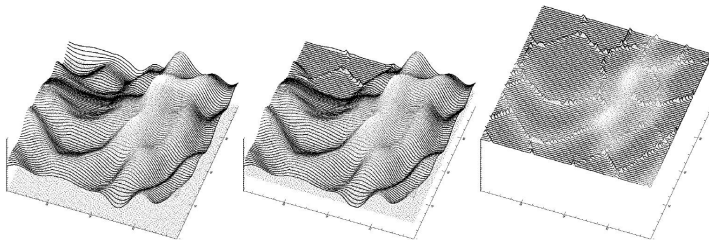


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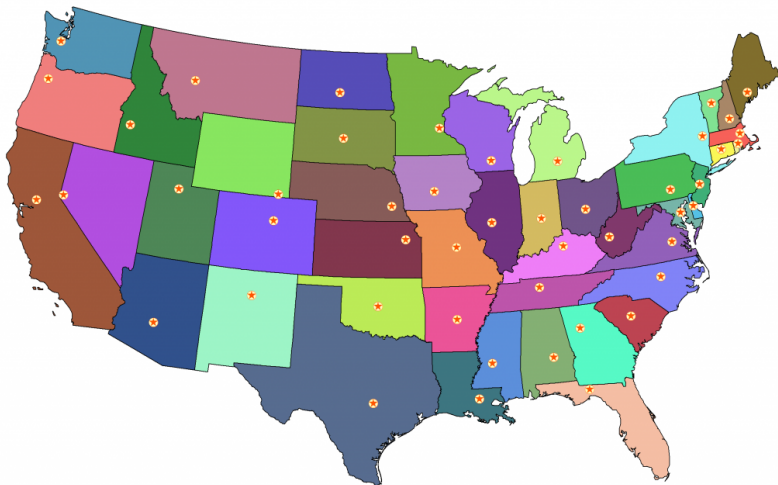
and raise a density threshold until a ridge is reached



Watershed algorithm, Platen et al. (2007)

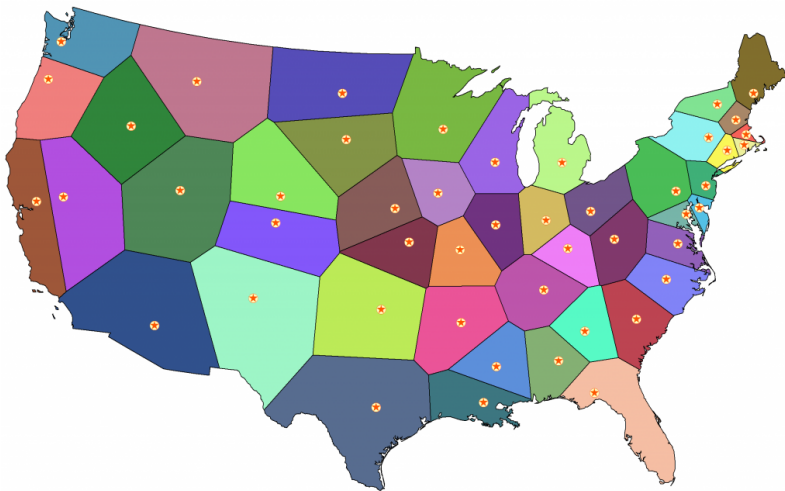
DEFINITION OF VOIDS

Define density field via **Voronoi tessellation** of tracer particles



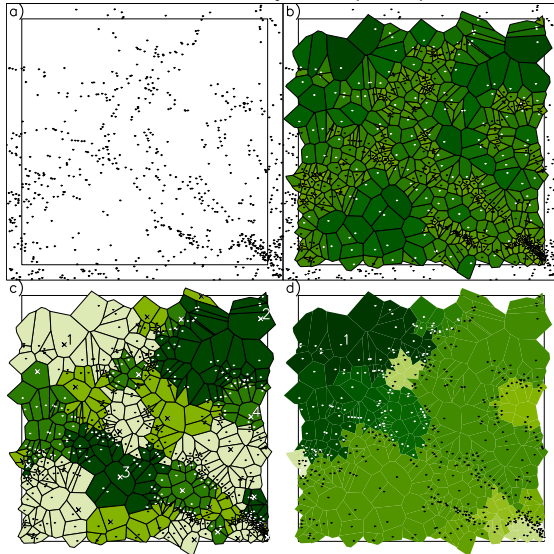
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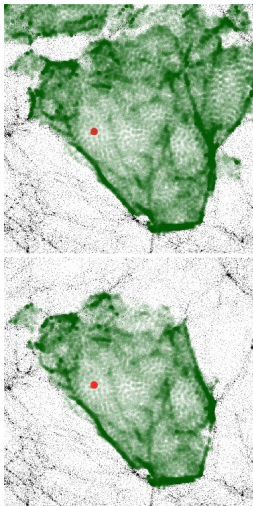


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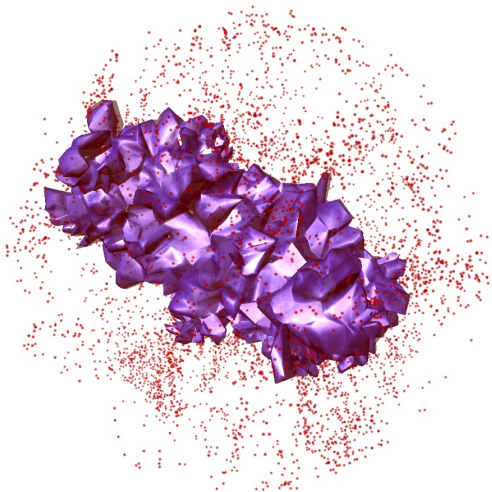
ZOBOV, Neyrinck (2008)



DEFINITION OF VOIDS

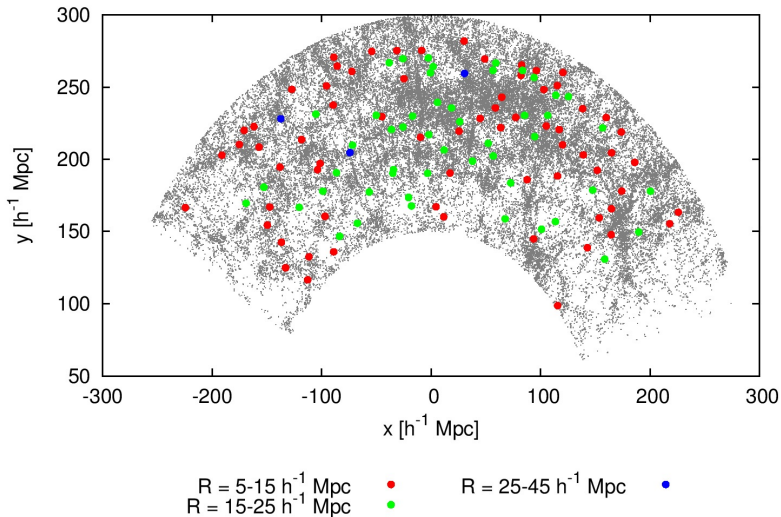


Neyrinck (2008)



Sutter, Lavaux, Wandelt, Weinberg (2012)

OBSERVED VOIDS (SDSS)



Sutter et al. (2012)

VOID PROFILE

Estimate density and velocity profile by “stacking” tracer particles around void centers

$$\rho_v(r) = \frac{3}{4\pi} \sum_i \frac{m_i(\mathbf{r}_i)}{(r + \delta r)^3 - (r - \delta r)^3}$$

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MASS CONSERVATION TO LINEAR ORDER

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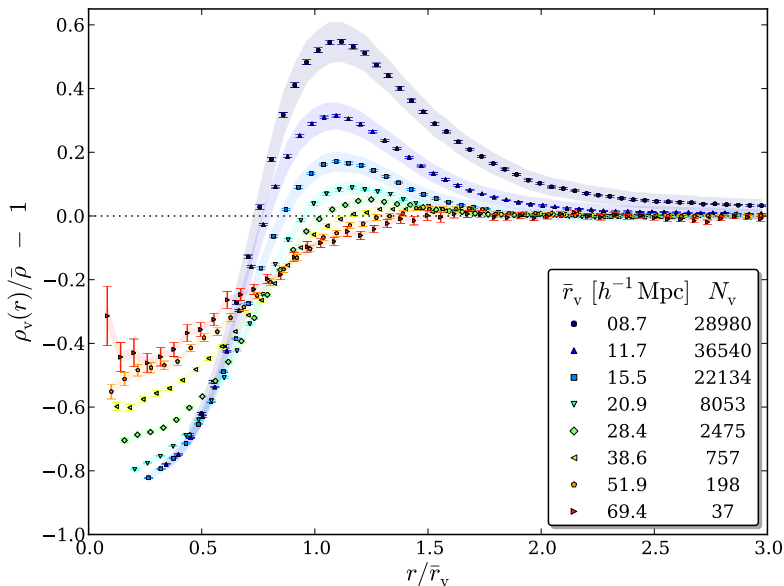
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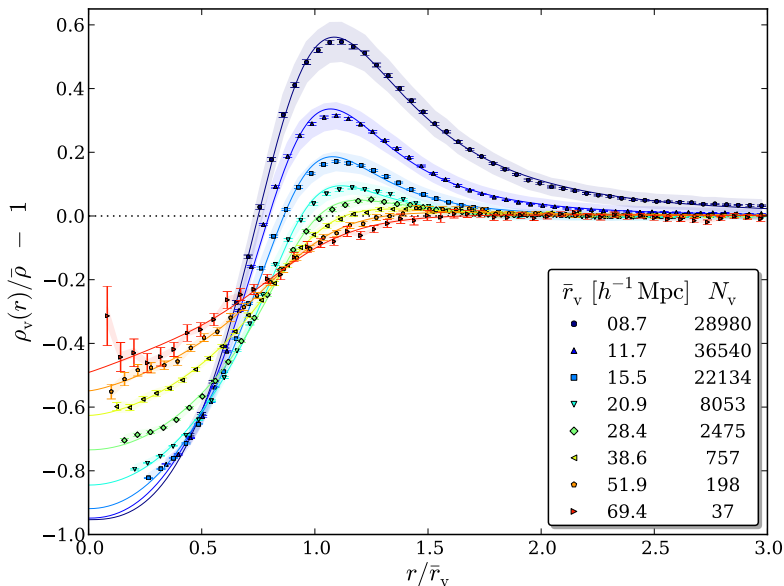
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In General Relativity: $f(z) = \Omega_m^{0.55}(z)$

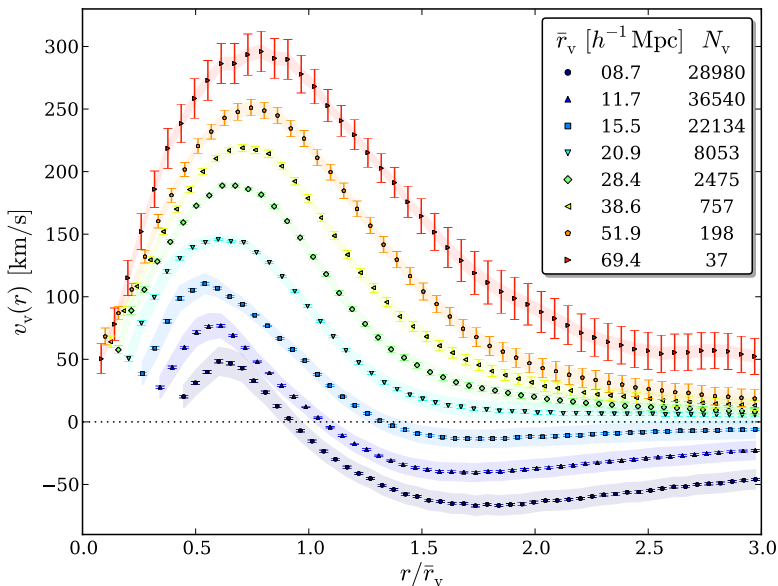
VOID PROFILE: DENSITY



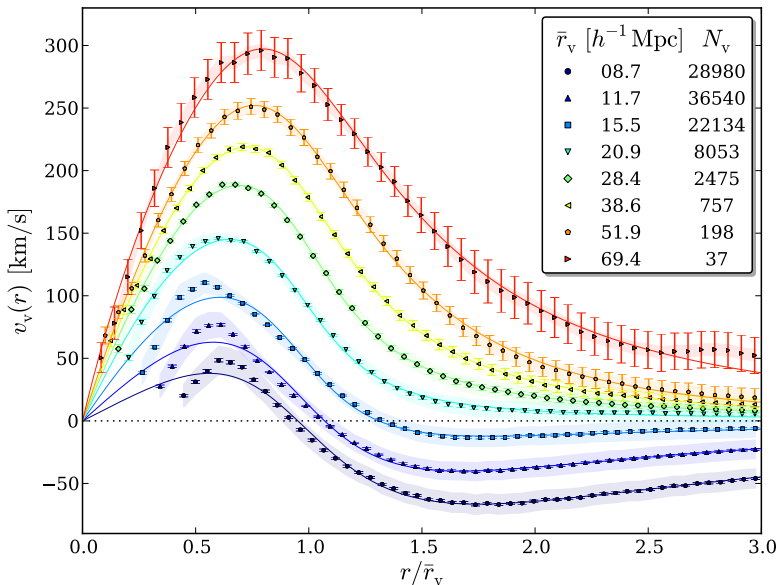
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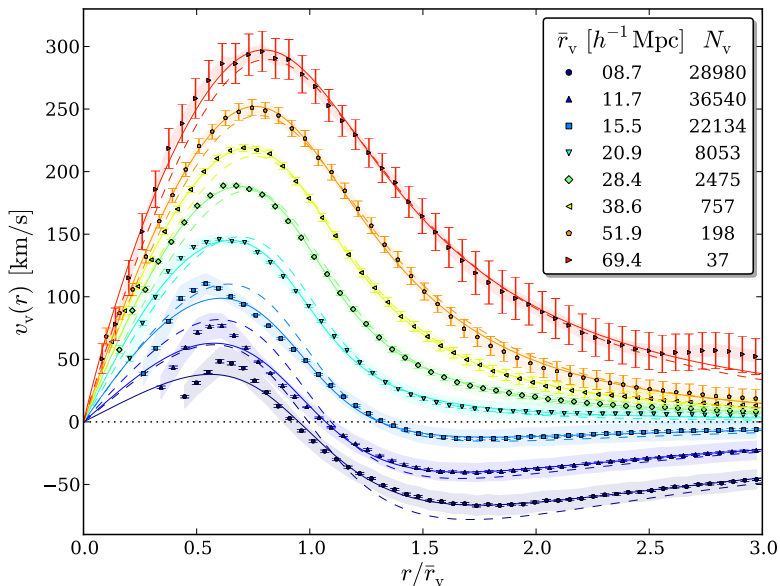
VOID PROFILE: VELOCITY



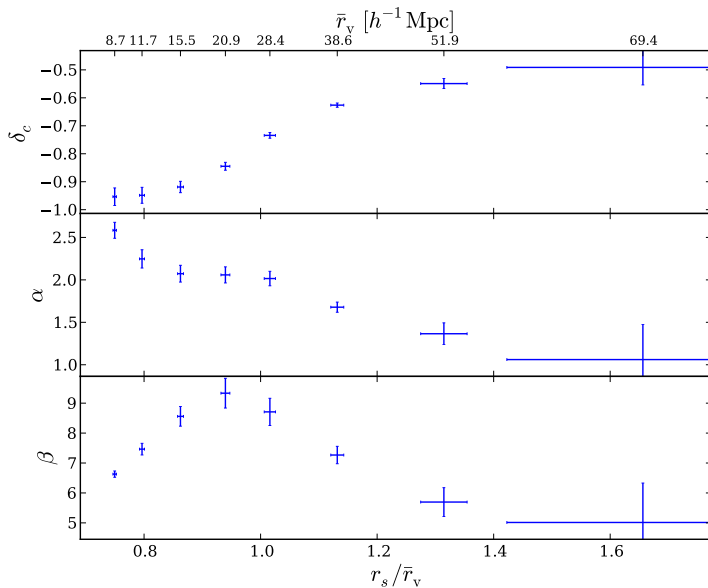
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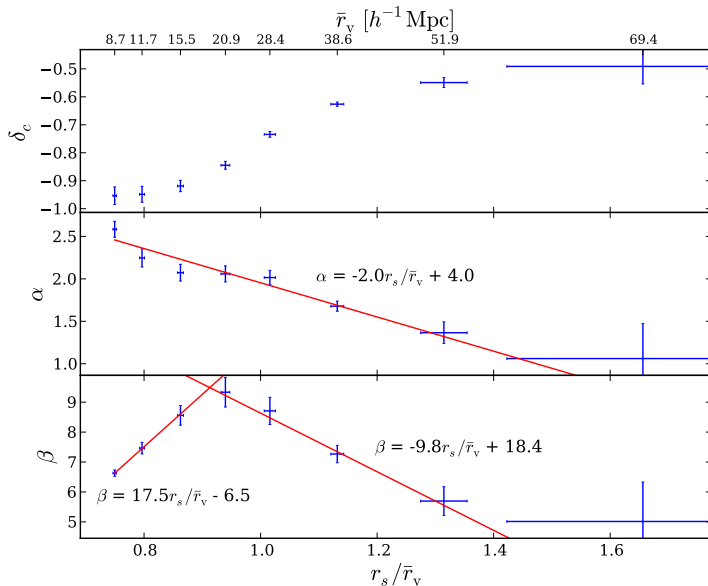
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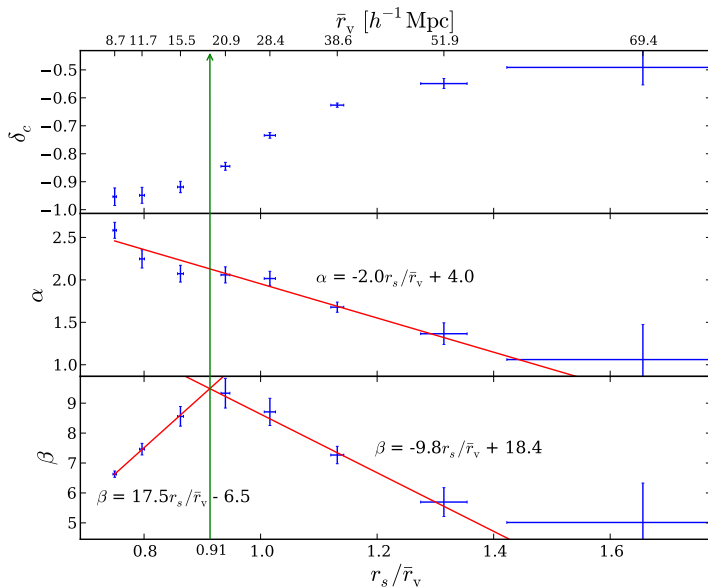
VOID PROFILE: PARAMETERS



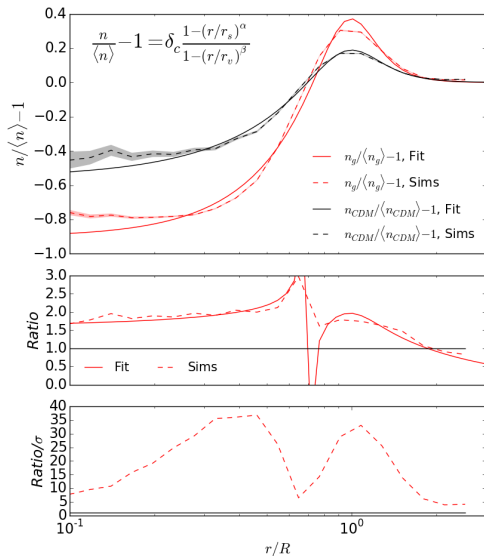
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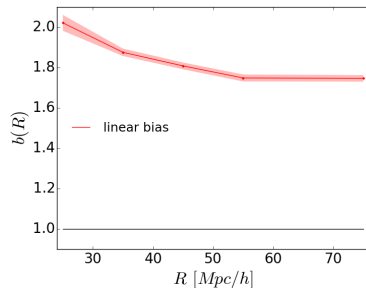
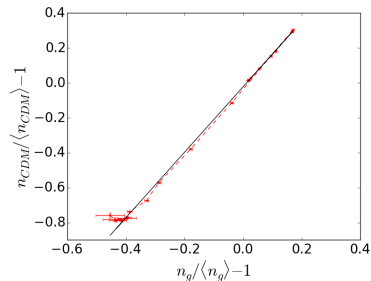
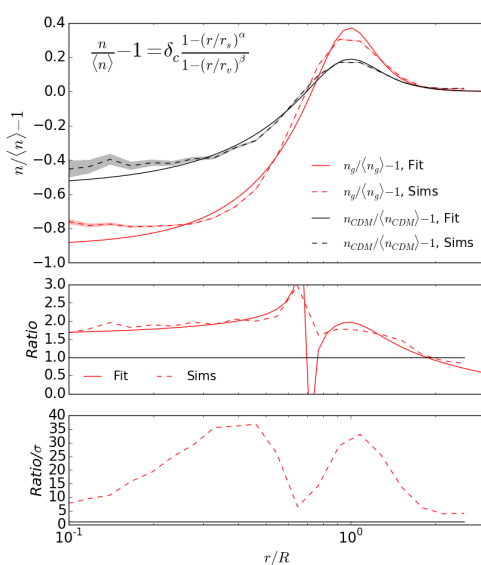
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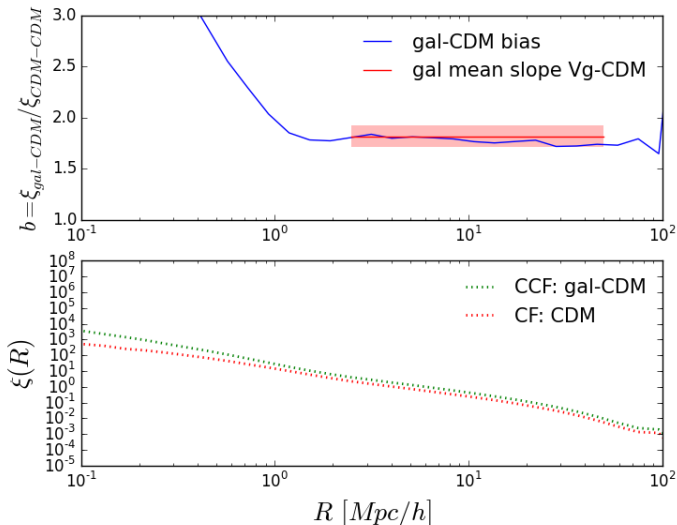
VOID PROFILE: GALAXIES VS. DARK MATTER



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VOIDS IN REDSHIFT SPACE

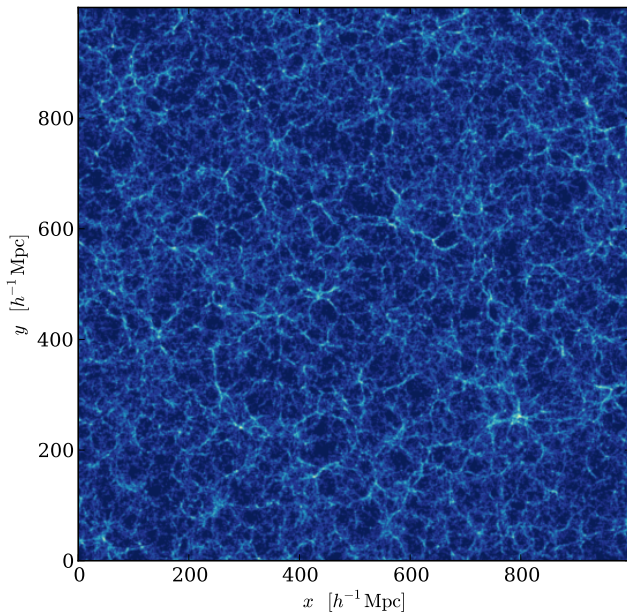
Peculiar motions of galaxies cause **redshift-space distortions**:

$$\tilde{\mathbf{r}} = \mathbf{r} + \mathbf{v}_{\parallel} H^{-1}(z)$$

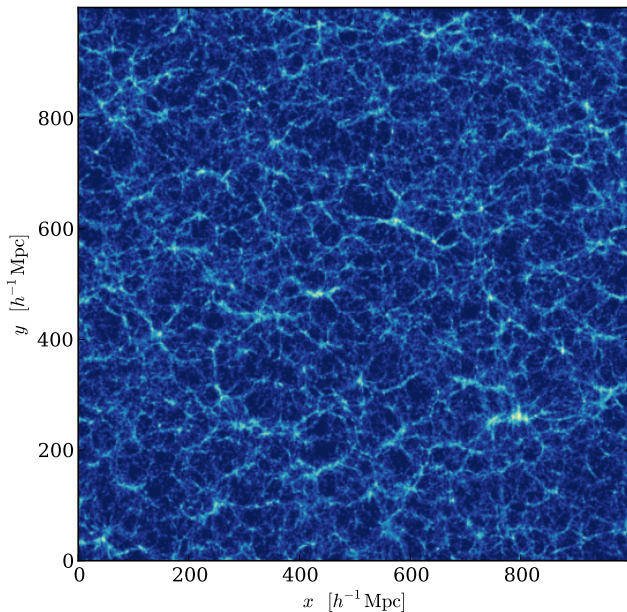
- ➡ $\perp$ to line of sight:
Pancakes of God from linear growth
- ➡ $\parallel$ to line of sight:
Fingers of God from nonlinear collapse
- ➡ Galaxy correlation function no longer isotropic, what about voids?

Melott et al. (1998)

VOIDS IN REDSHIFT SPACE



VOIDS IN REDSHIFT SPACE



MODEL

Void-galaxy cross-correlation function in redshift space:

$$1 + \tilde{\xi}_{\text{vg}}(\tilde{\mathbf{r}}) = \int \mathcal{P}(\mathbf{v}, \mathbf{r}) [1 + \xi_{\text{vg}}(\mathbf{r})] d^3v = \int_{-\infty}^{\infty} \mathcal{P}(v_{\parallel}, \mathbf{r}) \frac{\rho_v(r)}{\bar{\rho}} dv_{\parallel}$$

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Assume a **Gaussian** pairwise velocity distribution with mean $v_v(r) \frac{r_{\parallel}}{r}$

$$\mathcal{P}(v_{\parallel}, \mathbf{r}) = \frac{1}{\sqrt{2\pi}\sigma_v(\mathbf{r})} \exp \left[-\frac{\left(v_{\parallel} - v_v(r) \frac{r_{\parallel}}{r} \right)^2}{2\sigma_v^2(\mathbf{r})} \right]$$

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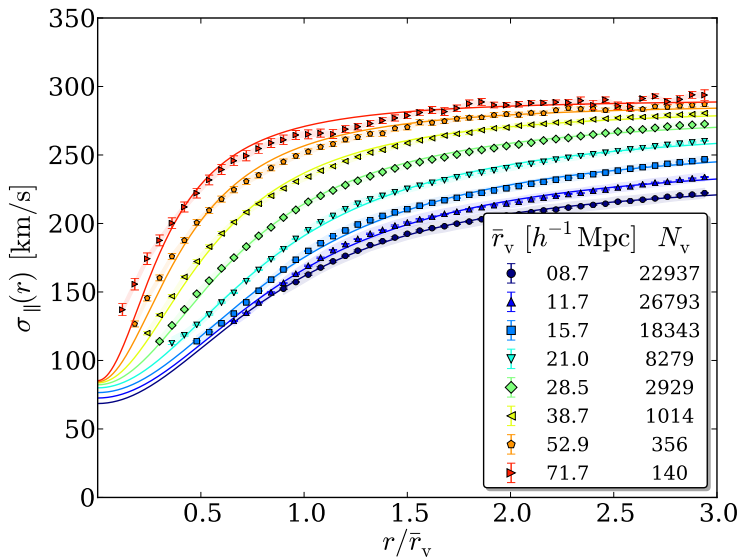
and with velocity dispersion

$$\sigma_v^2(\mathbf{r}) = \sigma_{\parallel}^2(r) \frac{r_{\parallel}^2}{r^2} + \sigma_{\perp}^2(r) \left(1 - \frac{r_{\parallel}^2}{r^2} \right)$$

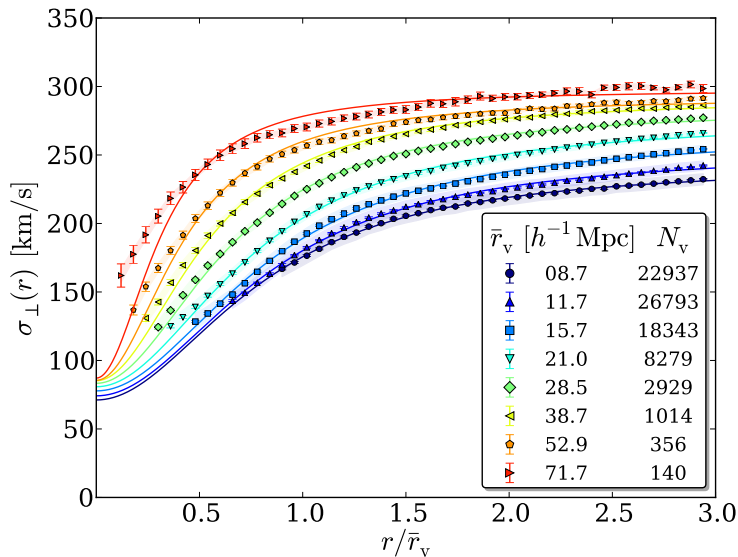
Assume:

$$\sigma_{\parallel, \perp}(r) \equiv \sigma_v = \text{const.}$$

VELOCITY DISPERSION



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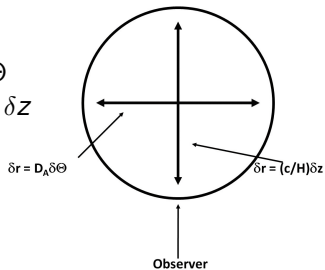
ALCOCK-PACZYNSKI TEST

Perform *Alcock-Paczynski test* to constrain cosmological parameters:

- Angular separation
- Radial separation

$$\delta r_{\perp} = D_A(z) \delta \Theta$$

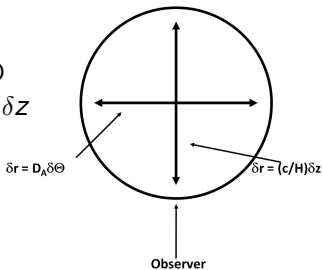
$$\delta r_{\parallel} = c H^{-1}(z) \delta z$$



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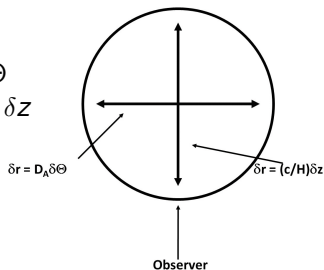
ANGULAR DIAMETER DISTANCE & HUBBLE RATE

$$D_A(z) = c \int_0^z H^{-1}(z') dz' \quad , \quad H(z) = H_0 \sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}$$

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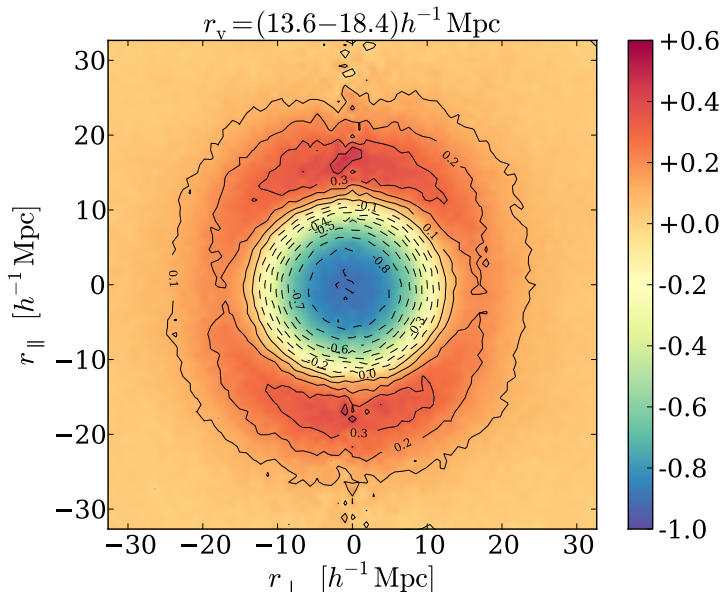
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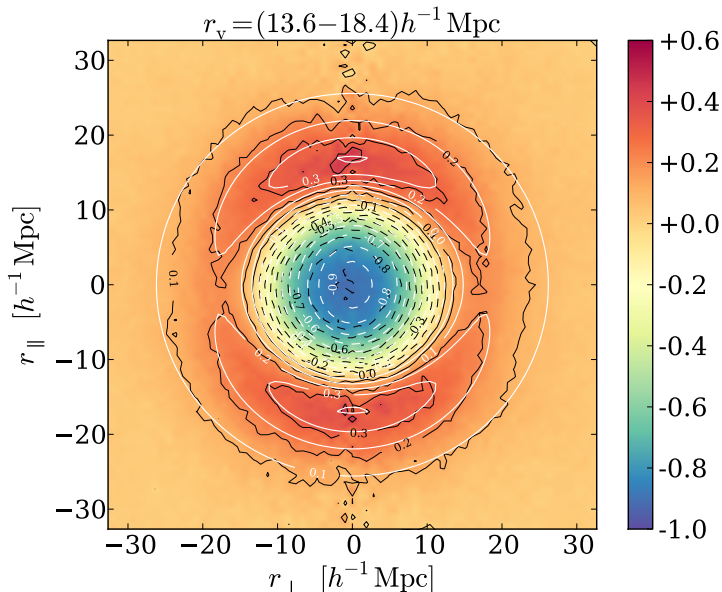
Any deviation from the fiducial cosmology causes geometric distortions. $\Rightarrow$ Determine **ellipticity** ε via

$$\varepsilon = \frac{\delta r_{\parallel}}{\delta r_{\perp}} = \frac{D_A^{\text{true}}(z) H^{\text{true}}(z)}{D_A^{\text{fid}}(z) H^{\text{fid}}(z)}$$

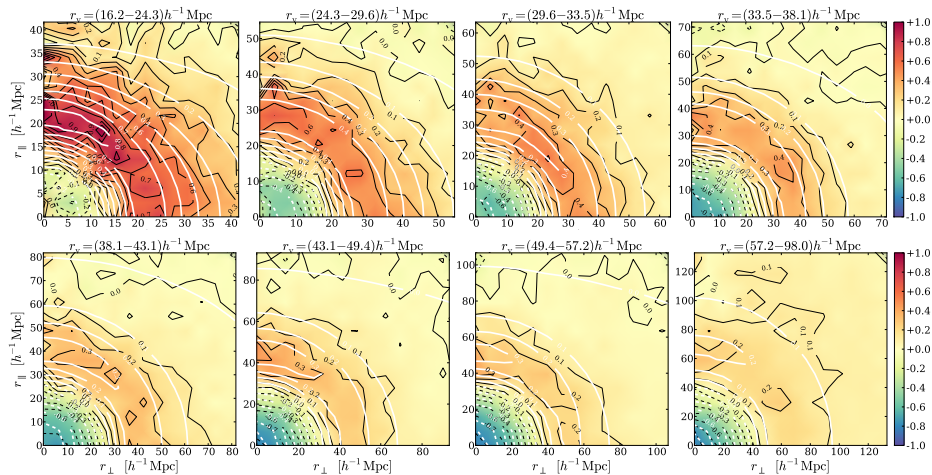
RSD ANALYSIS: DENSE MOCK GALAXIES



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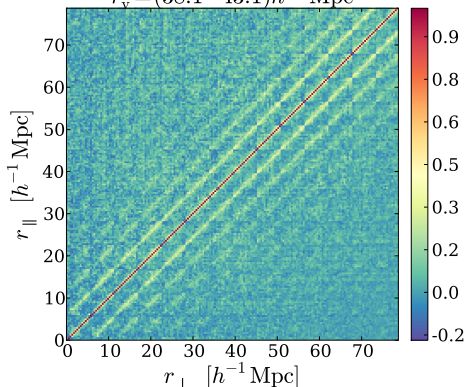
RSD ANALYSIS: SDSS CMASS DR11 GALAXIES



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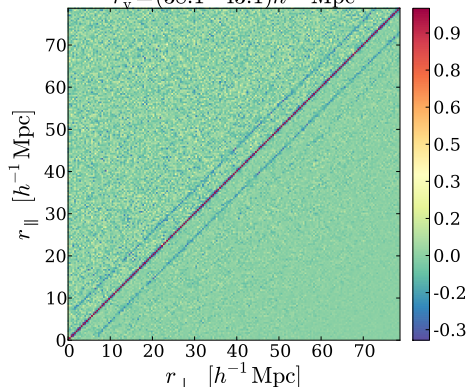
Covariance matrix

$$r_v = (38.1 - 43.1) h^{-1} \text{ Mpc}$$



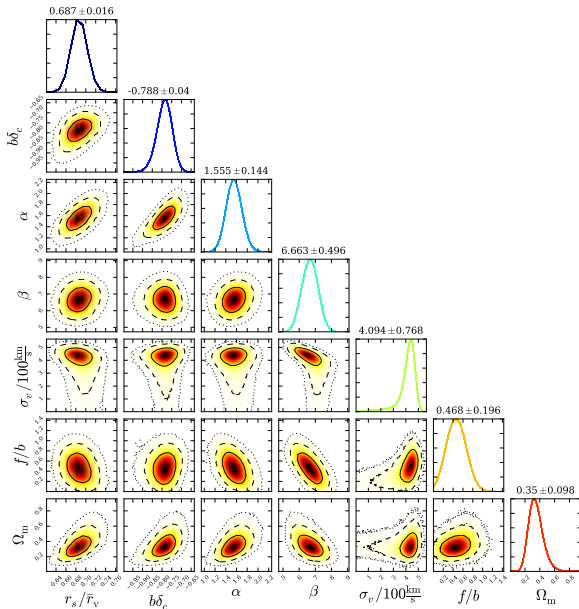
Precision matrix

$$r_v = (38.1 - 43.1) h^{-1} \text{ Mpc}$$

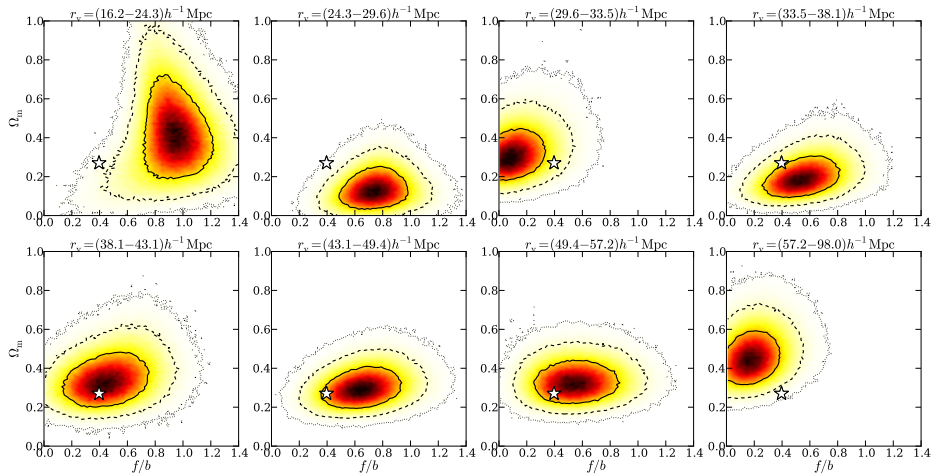


$$\mathcal{L}(\hat{\xi}_{\text{vg}}|\theta) \propto \exp \left[-\frac{1}{2} (\hat{\xi}_{\text{vg}} - \xi_{\text{vg}})^{\top} \mathbf{C}^{-1} (\hat{\xi}_{\text{vg}} - \xi_{\text{vg}}) \right]$$

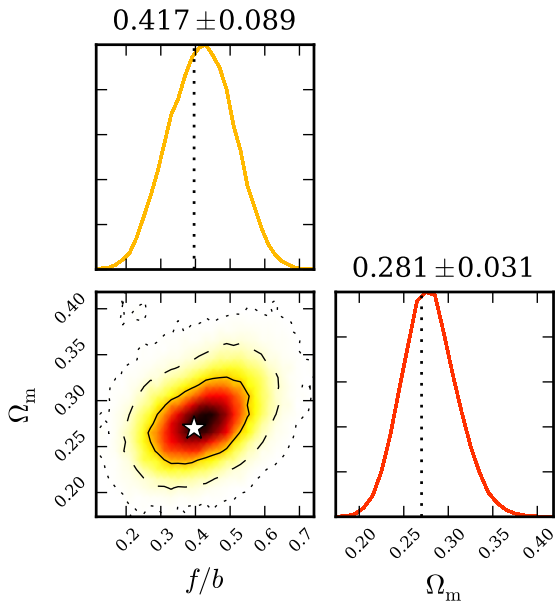
RSD ANALYSIS: SDSS CMASS DR11 GALAXIES



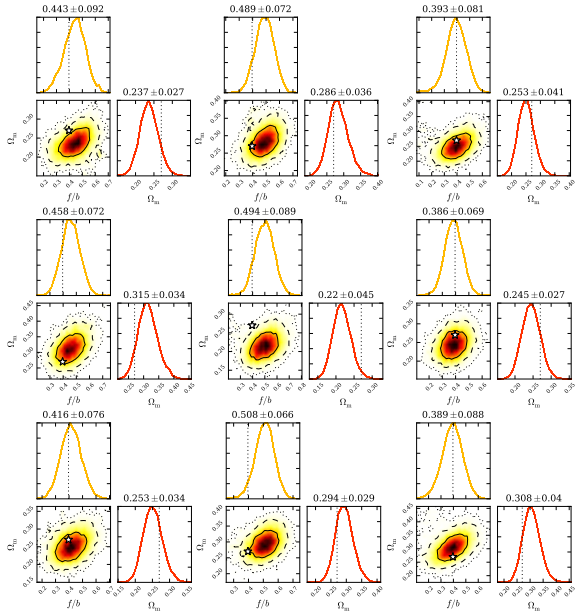
RSD ANALYSIS: SDSS CMASS DR11 GALAXIES



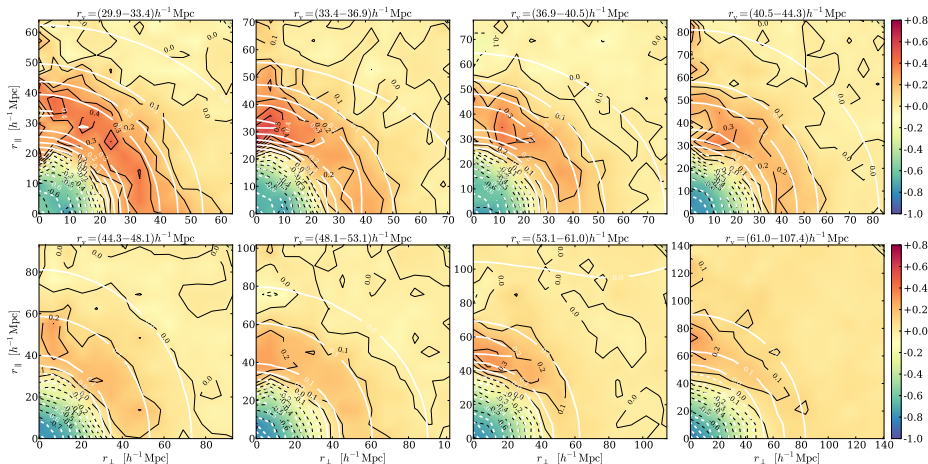
RSD ANALYSIS: SDSS CMASS DR11 GALAXIES



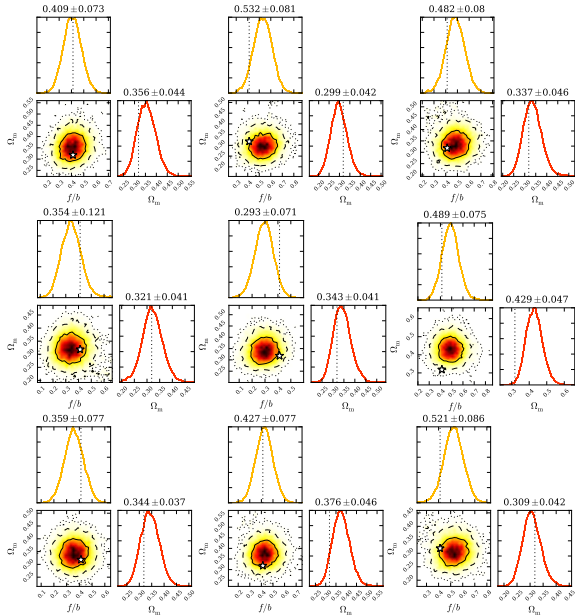
RSD ANALYSIS: SDSS CMASS DR11 BOOTSTRAPS



RSD ANALYSIS: SDSS CMASS DR11 MOCKS



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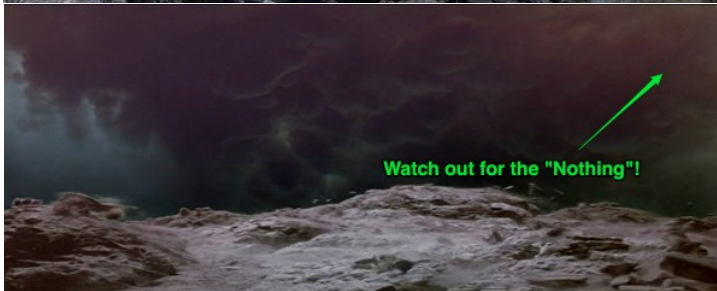
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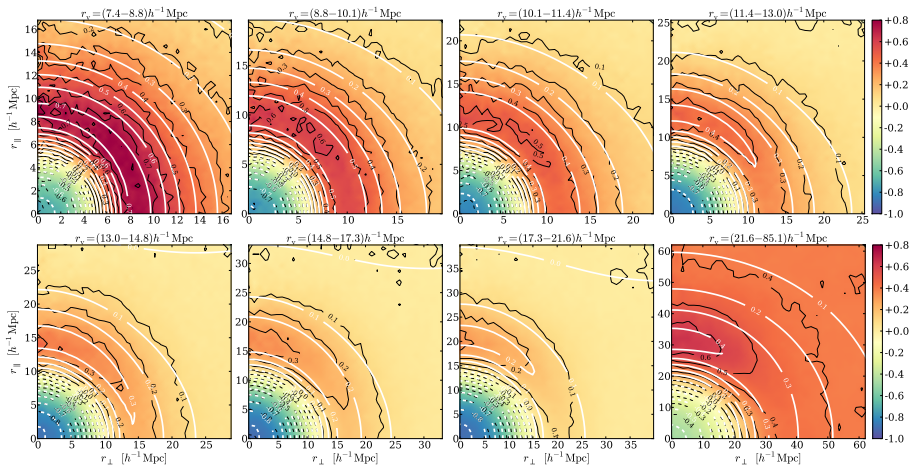
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- Possibility to combine with void lensing (e.g. DES, see arXiv:1605.03982) and void BAO (arXiv:1511.04405).

QUESTIONS ?

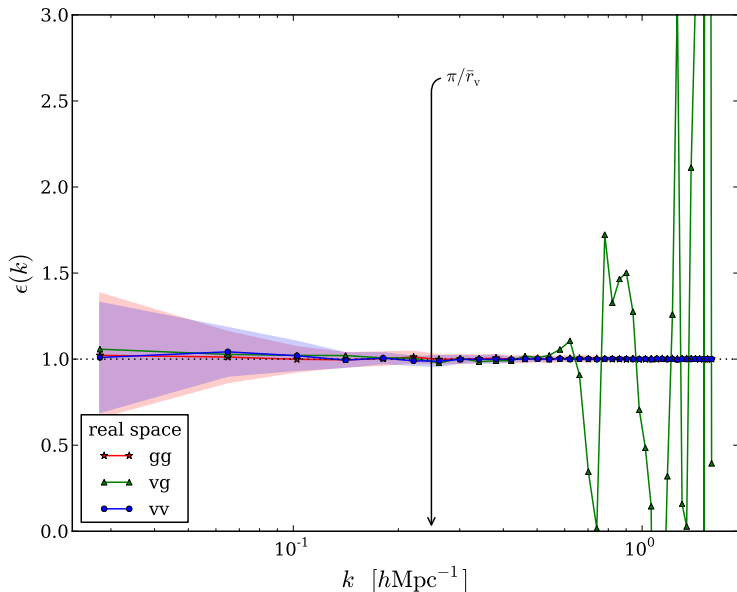
THANK YOU !



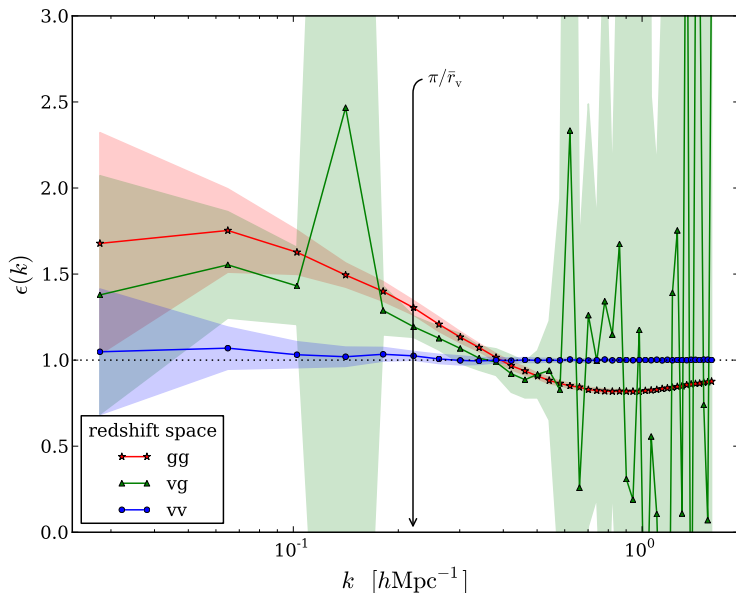
RSD ANALYSIS: SDSS MAIN MOCKS



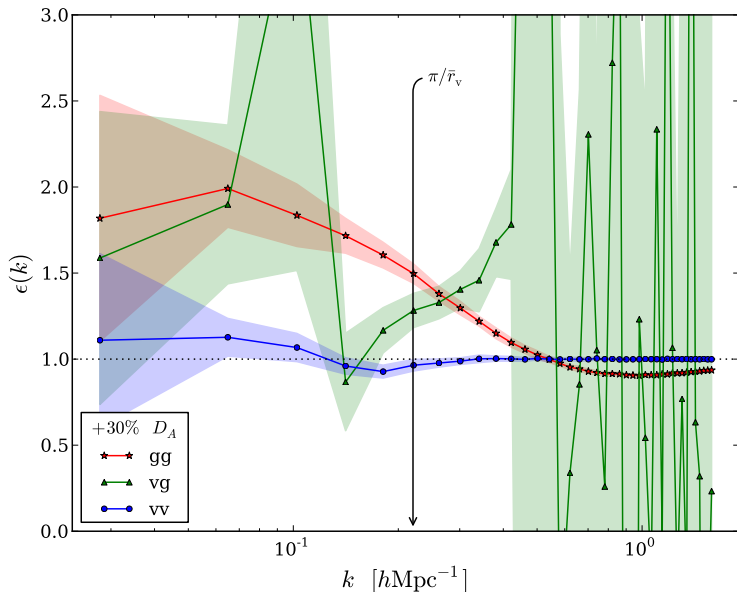
ALCOCK-PACZYNSKI TEST



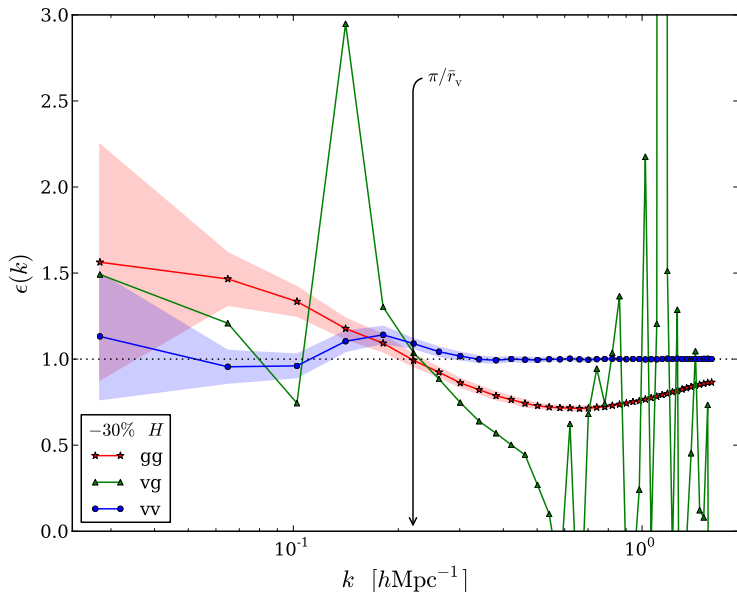
ALCOCK-PACZYNSKI TEST



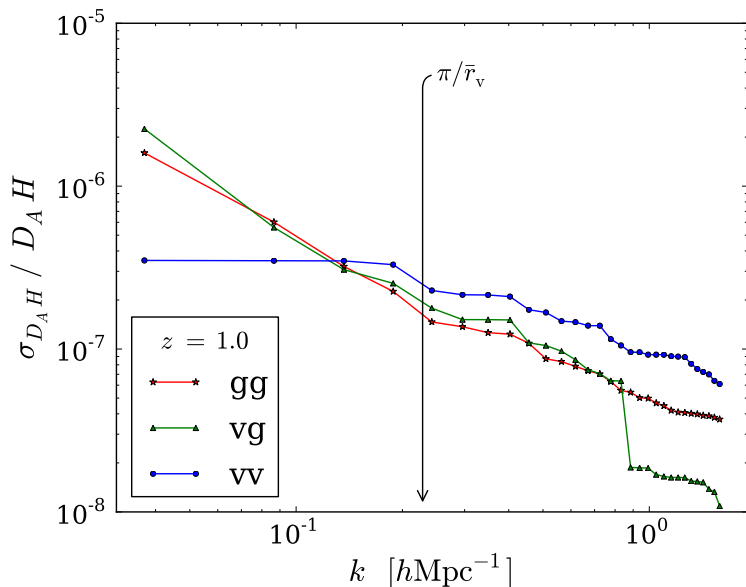
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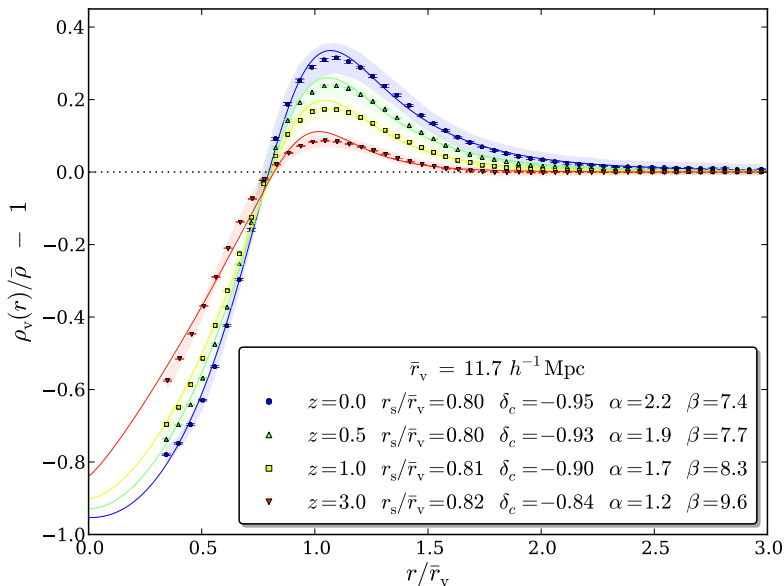
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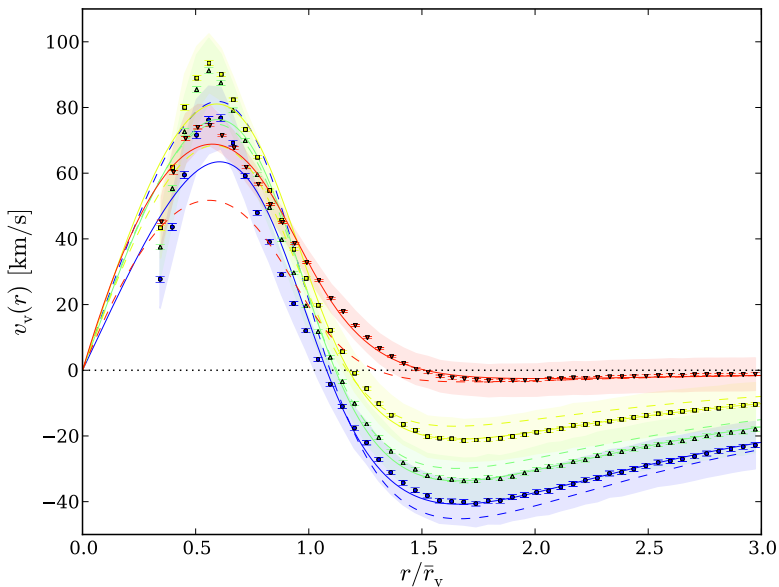
ALCOCK-PACZYNSKI TEST



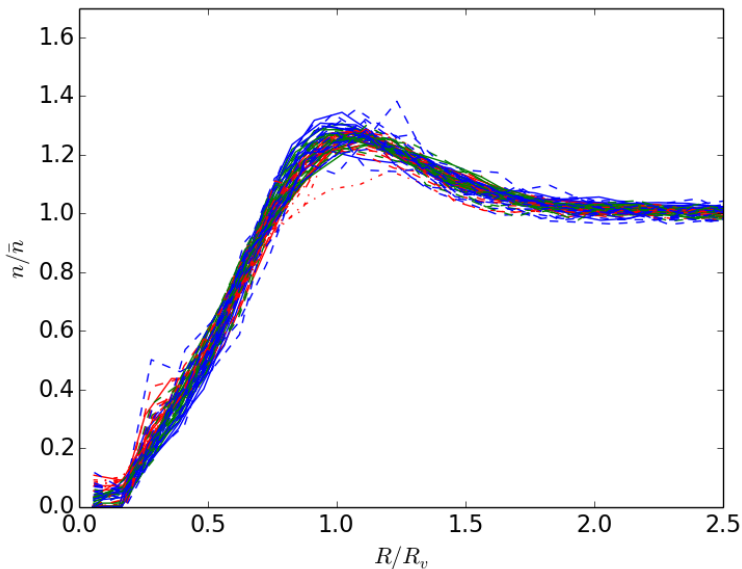
VOID PROFILE: UNIVERSALITY



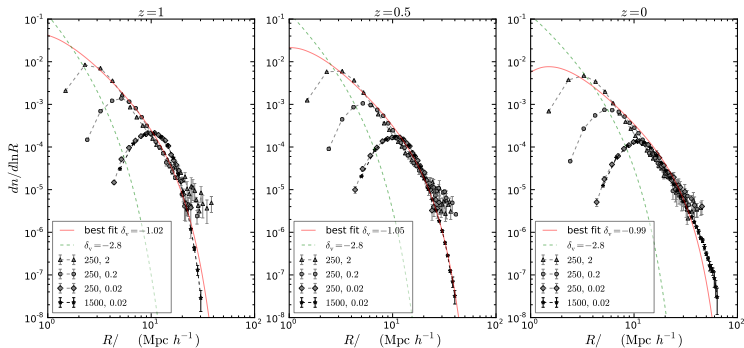
VOID PROFILE: UNIVERSALITY



VOID PROFILE: UNIVERSALITY

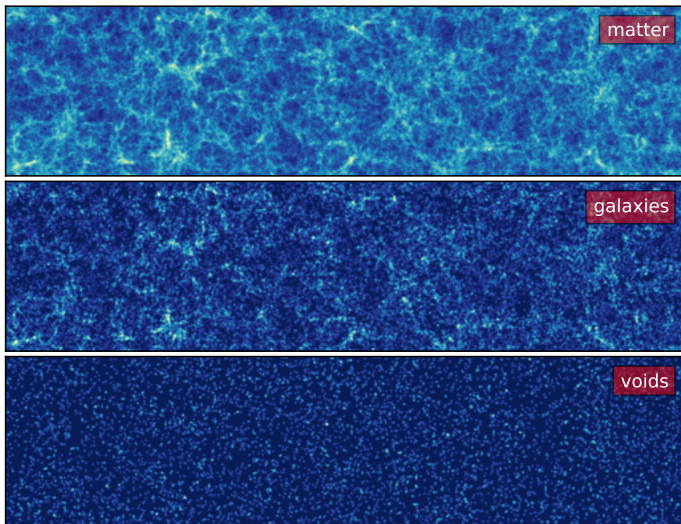


VOID ABUNDANCE

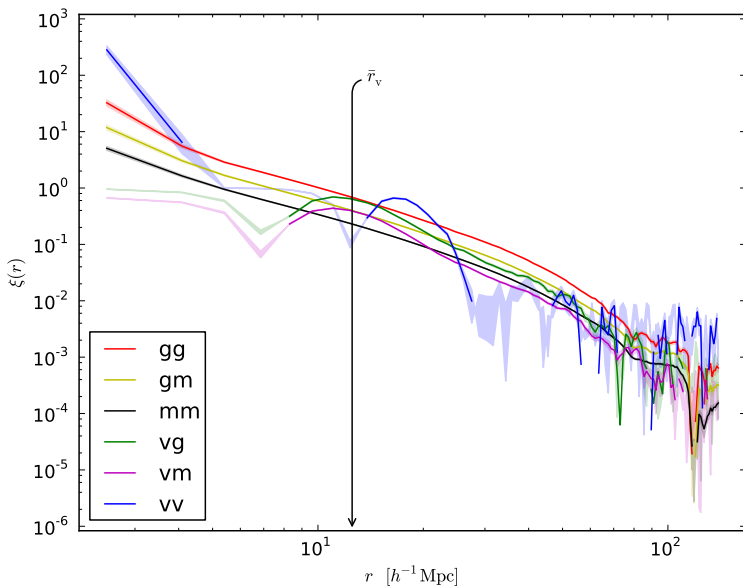


DENSITY FIELDS

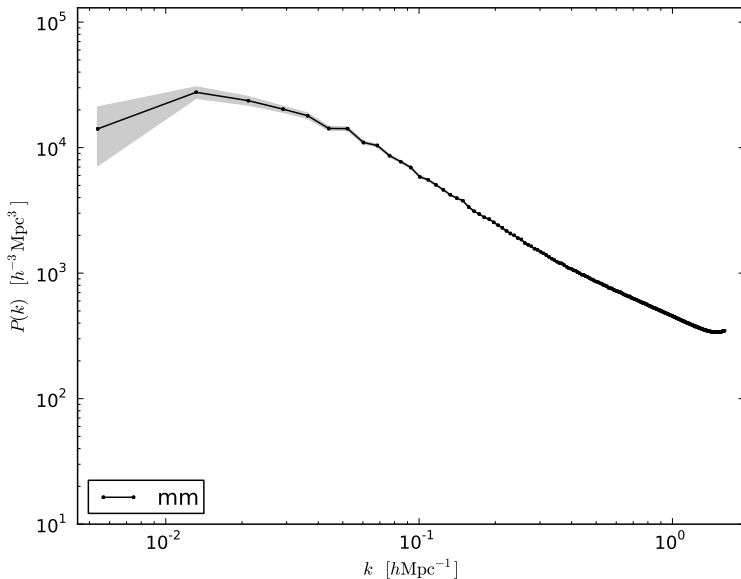
Voids are less clustered and more sparse than galaxies:



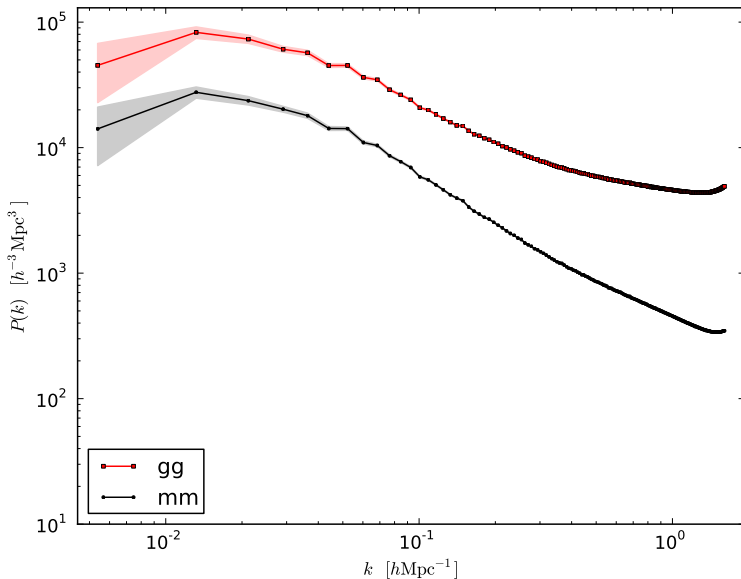
CORRELATION FUNCTION



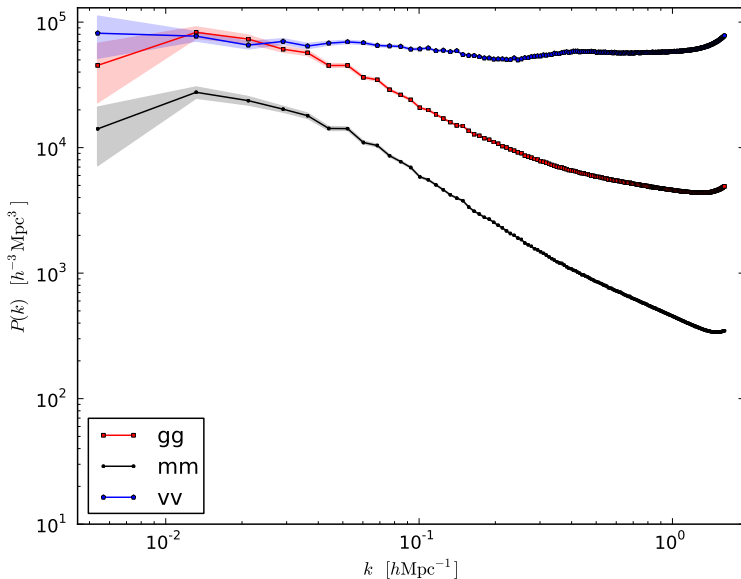
POWER SPECTRUM



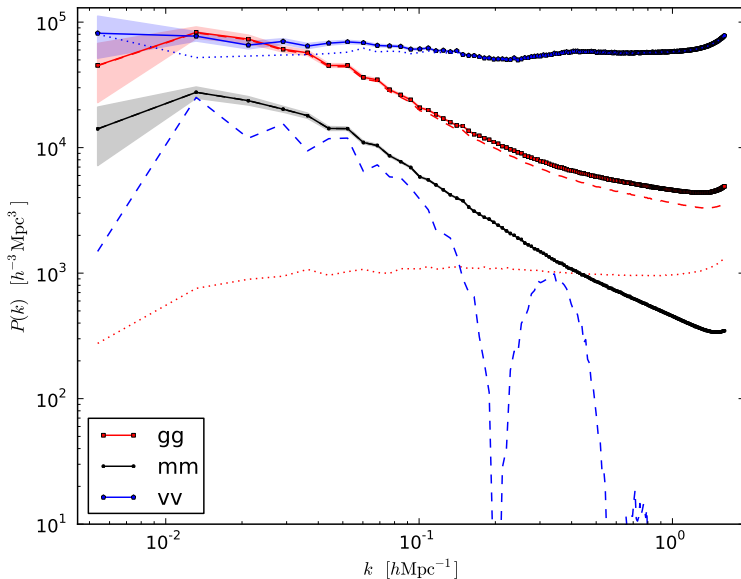
POWER SPECTRUM



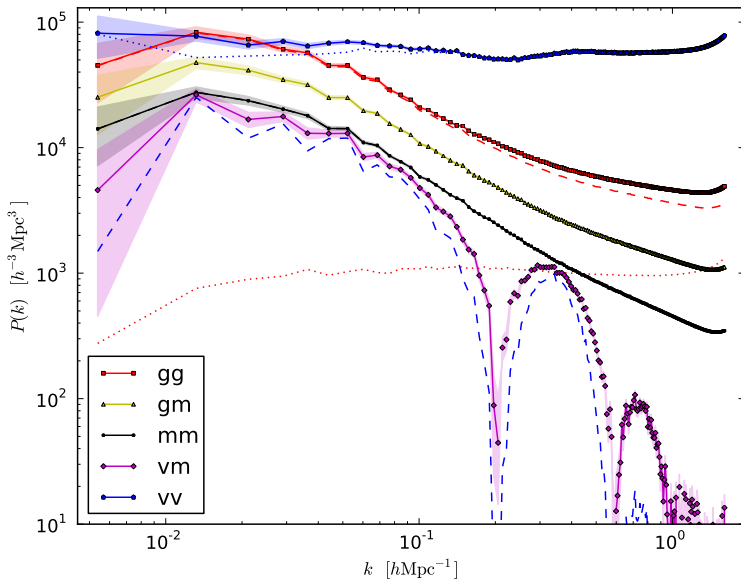
POWER SPECTRUM



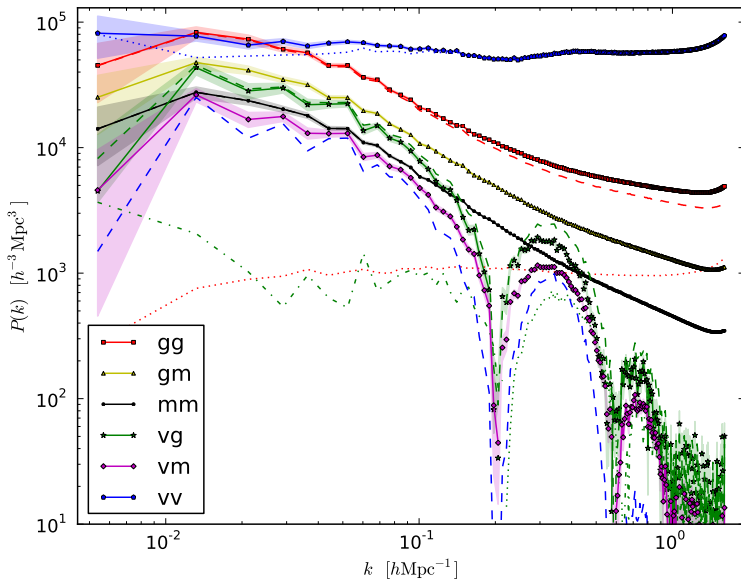
POWER SPECTRUM



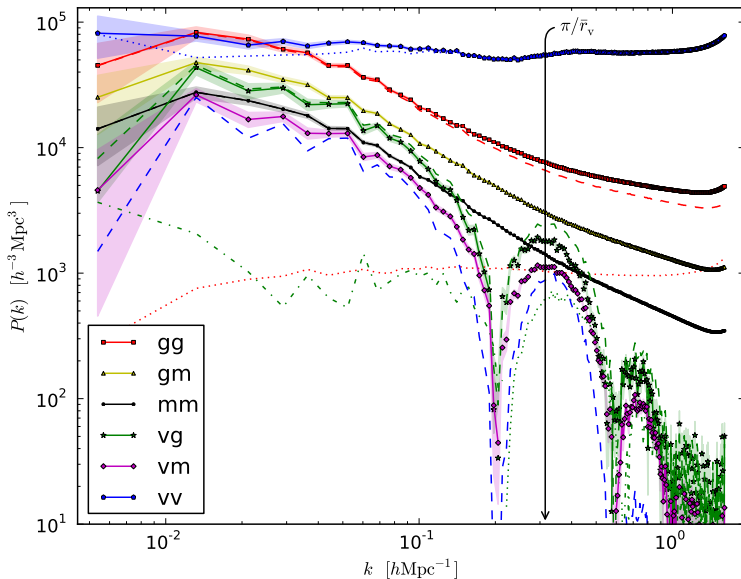
POWER SPECTRUM



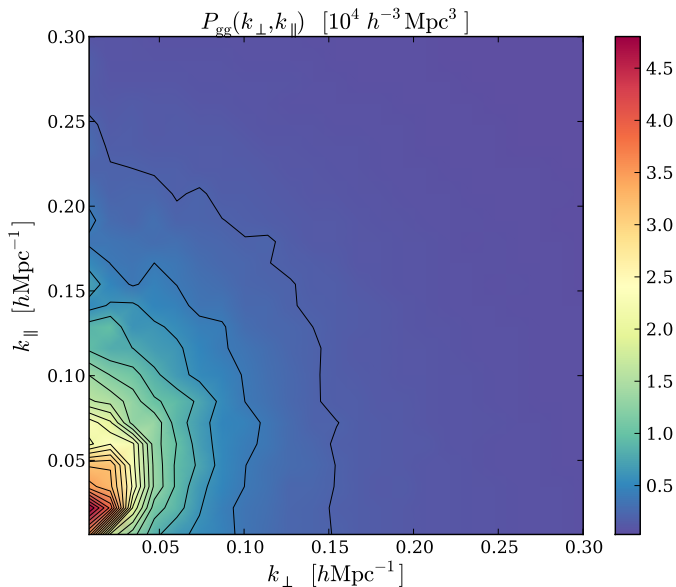
POWER SPECTRUM



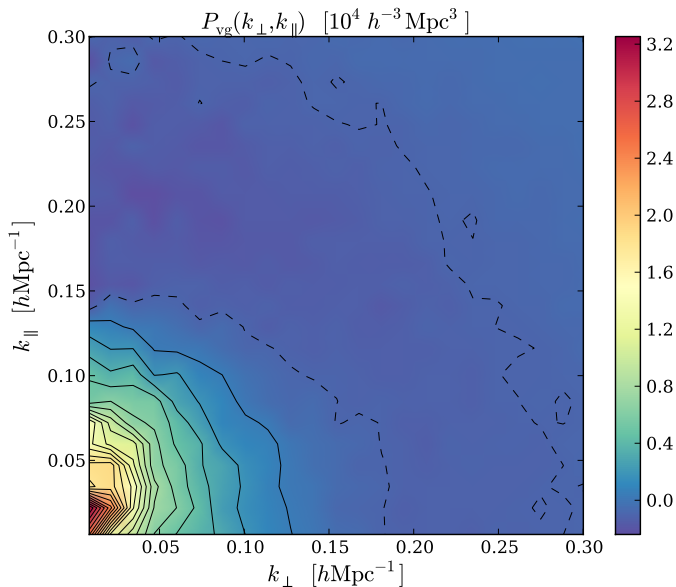
POWER SPECTRUM



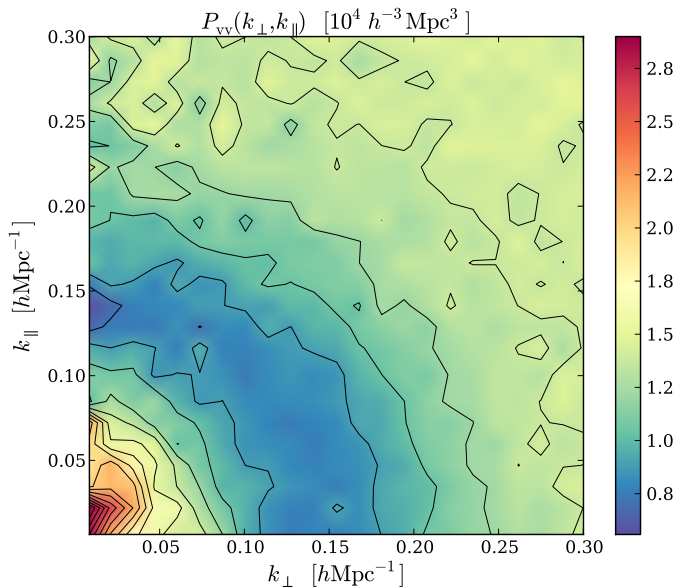
2D POWER SPECTRUM



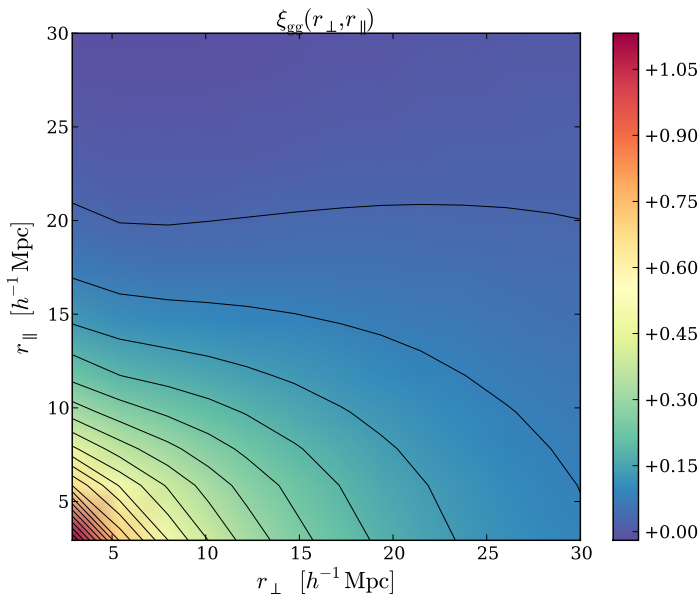
2D POWER SPECTRUM



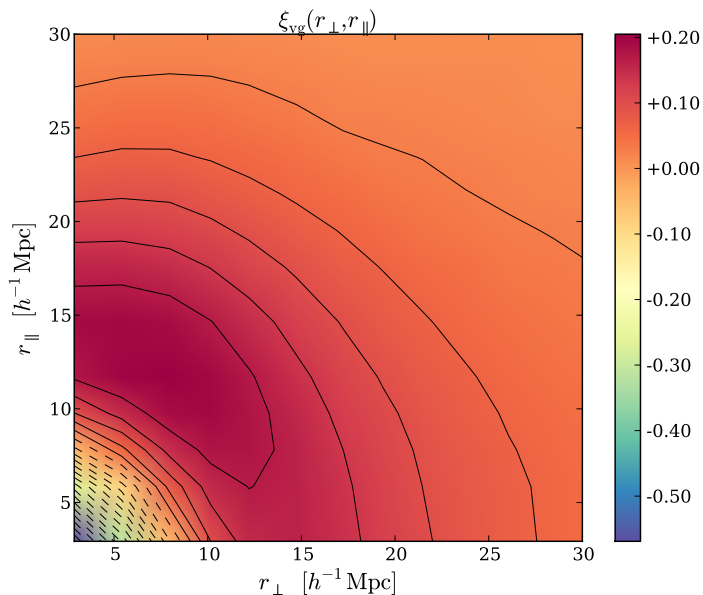
2D POWER SPECTRUM



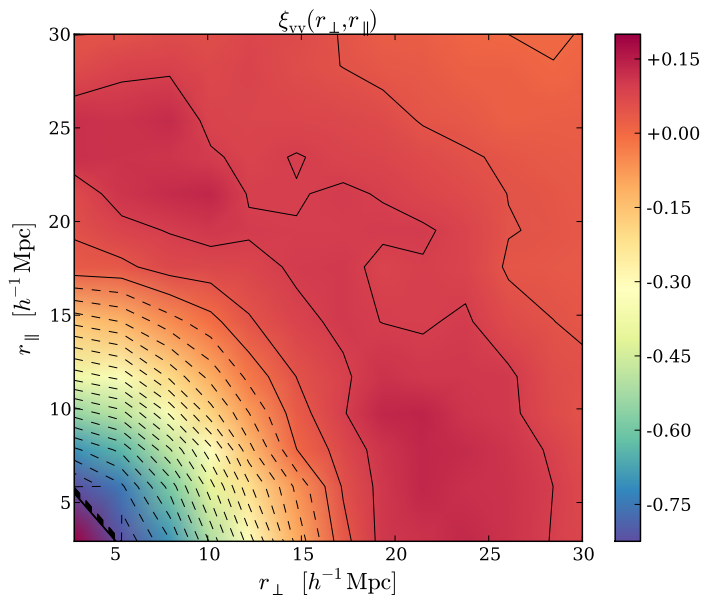
2D CORRELATION FUNCTION



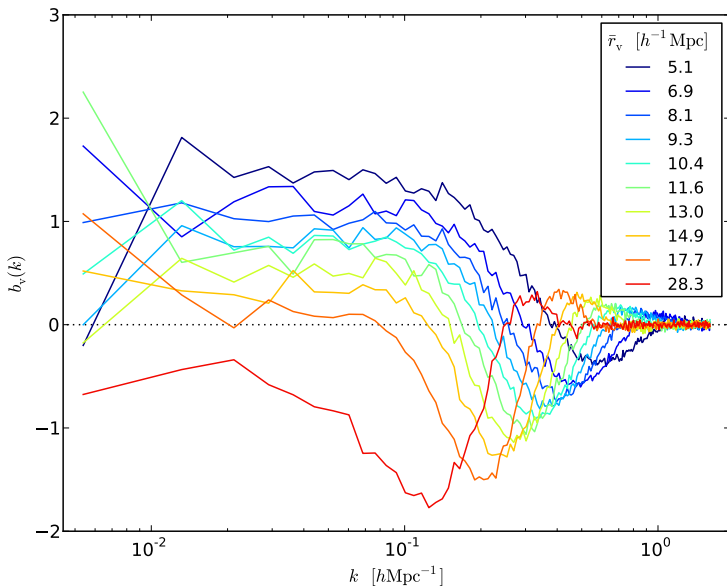
2D CORRELATION FUNCTION



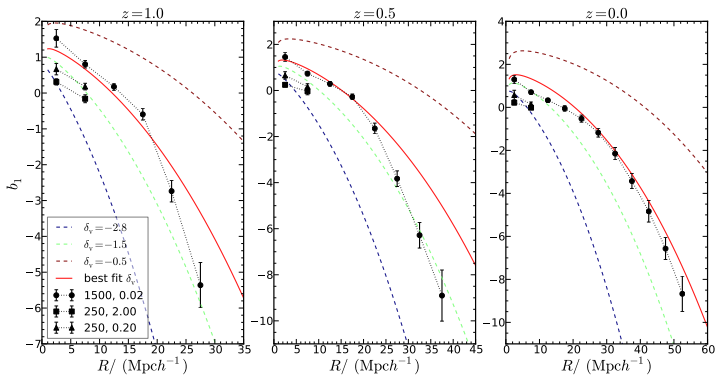
2D CORRELATION FUNCTION



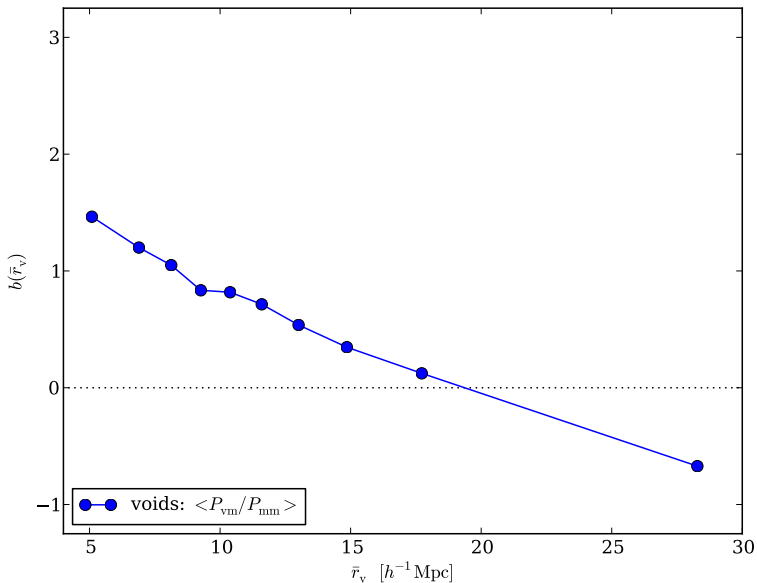
VOID BIAS



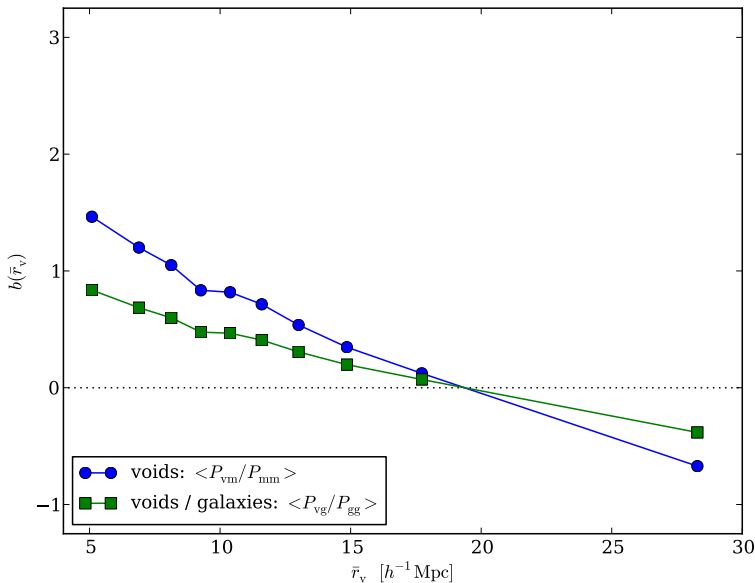
LINEAR VOID BIAS



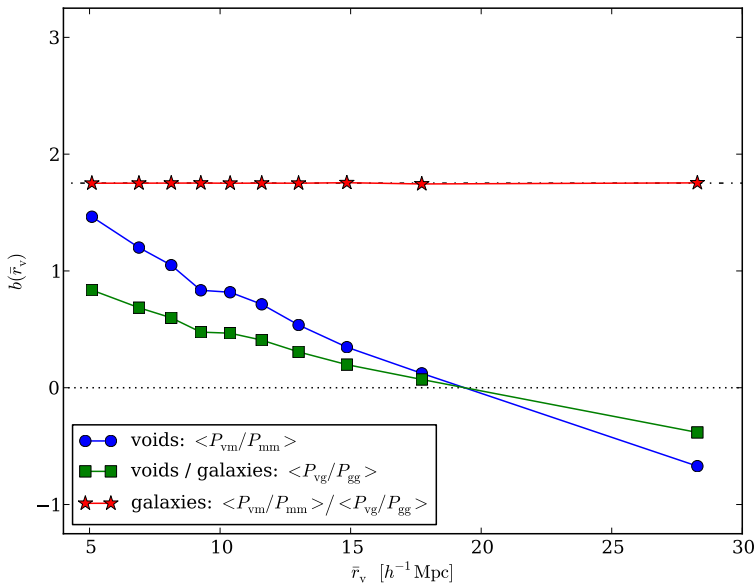
LINEAR VOID BIAS



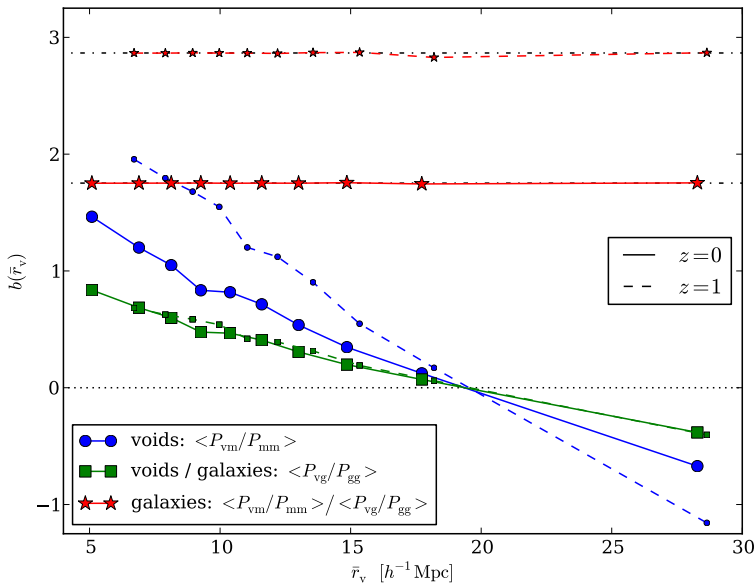
LINEAR VOID BIAS



LINEAR VOID BIAS



LINEAR VOID BIAS



LINEAR VOID BIAS

