

Peculiar velocities in Cosmology

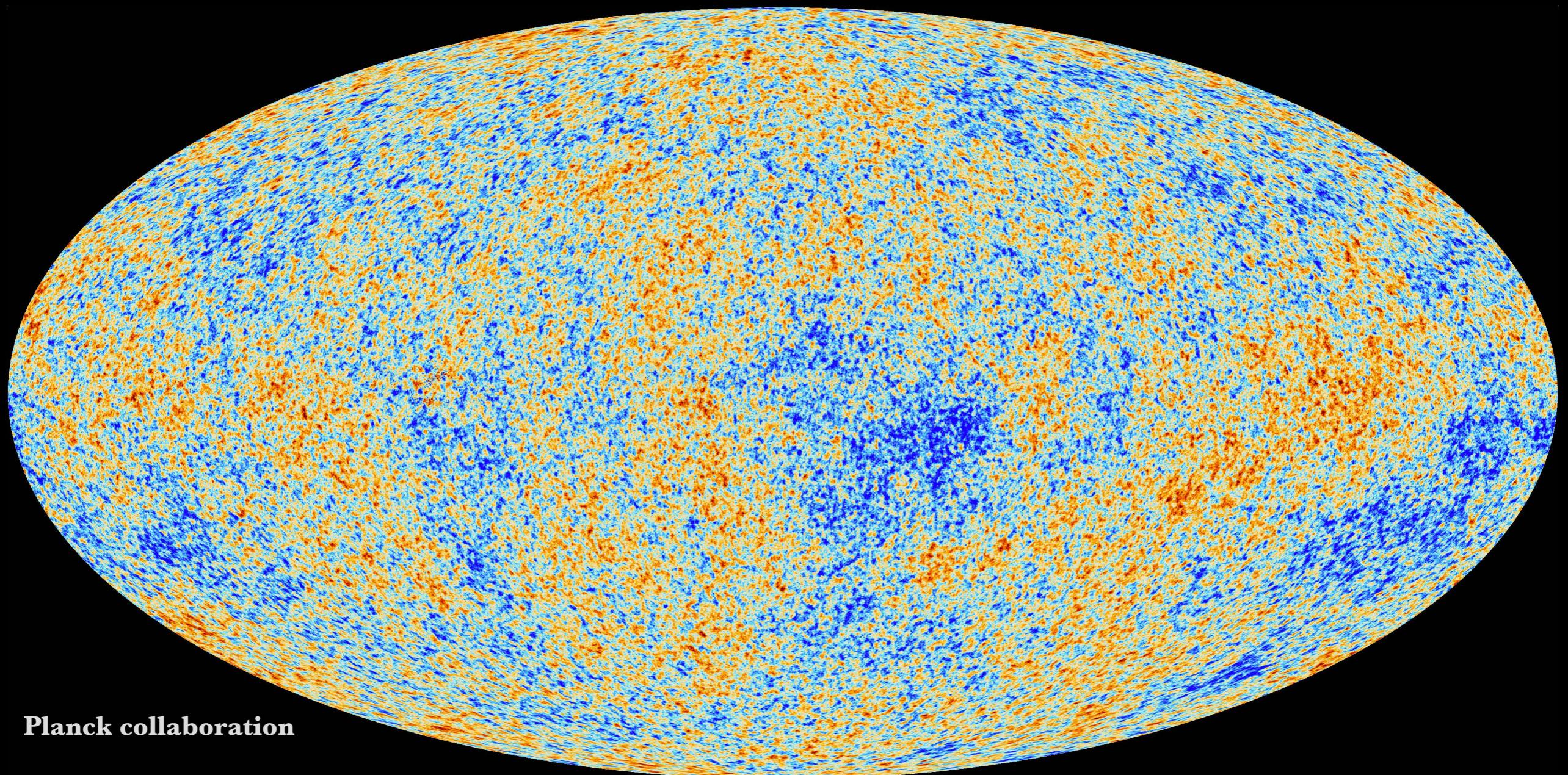
ROMAIN GRAZIANI

September 27th - LBNL



La Région 
Auvergne-Rhône-Alpes

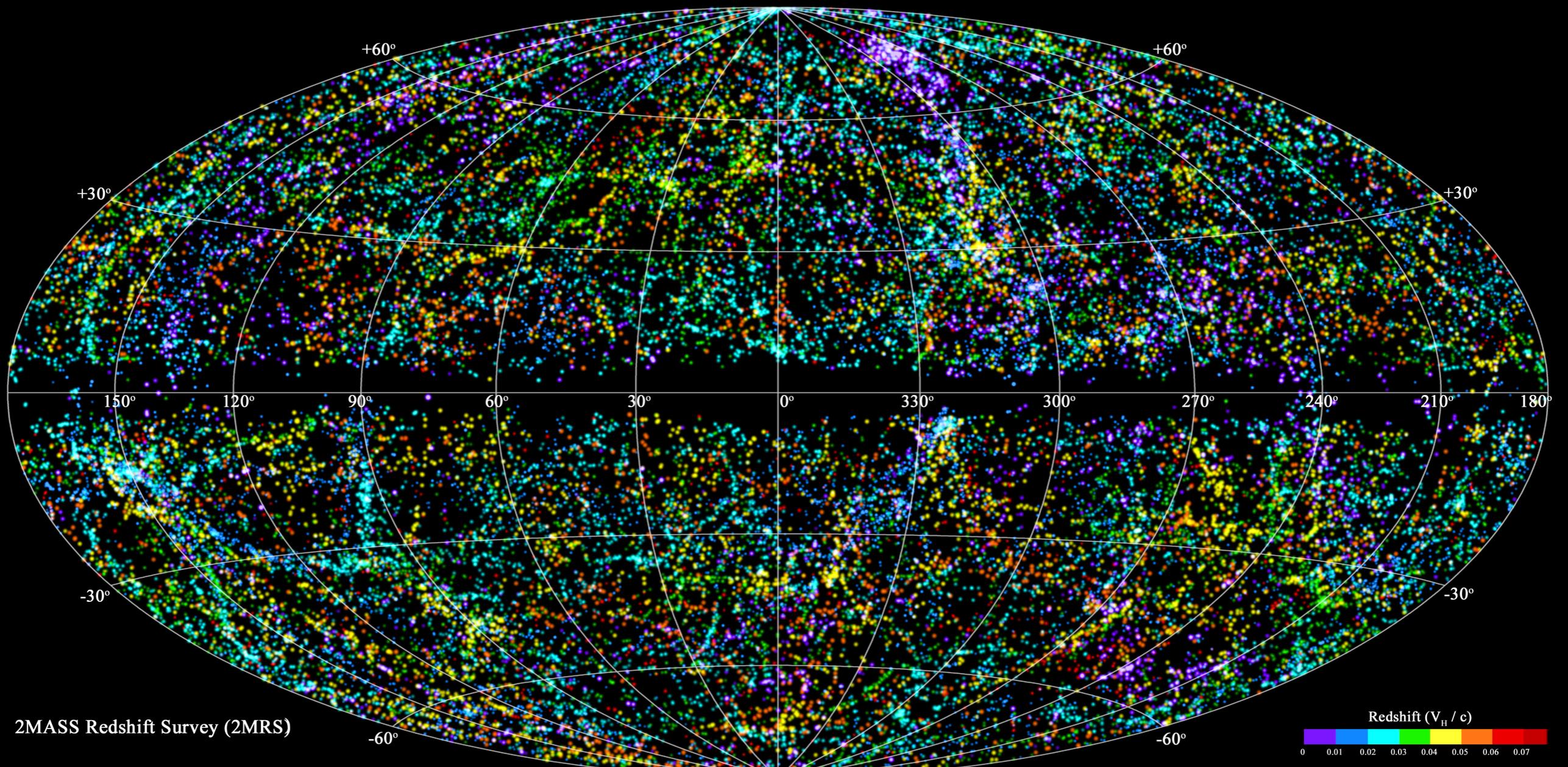




Planck collaboration

$z \sim 1100$

$t \sim 400\,000 \text{ yr}$

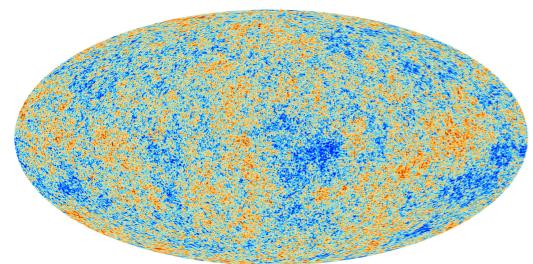


$z \sim 0$

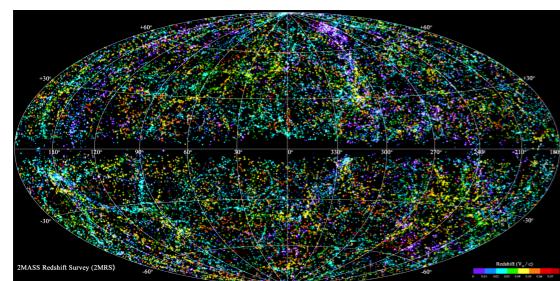
$t \sim 14 \times 10^9 \text{ yr}$

Probing our cosmological model

Universe

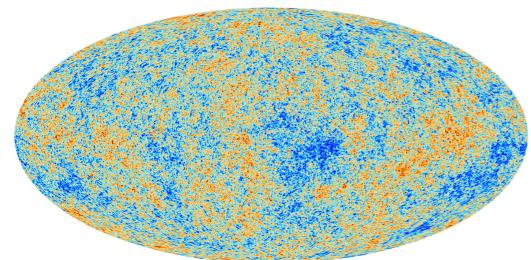


Cosmology

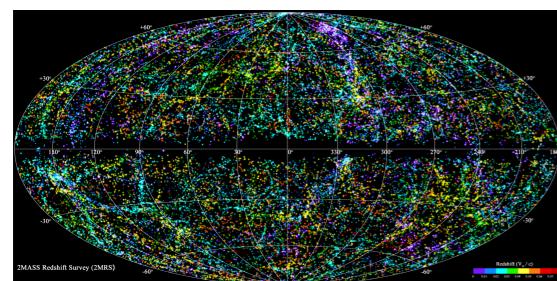


Probing our cosmological model

Universe



Cosmology



Expansion : H_0

Acoustic scale

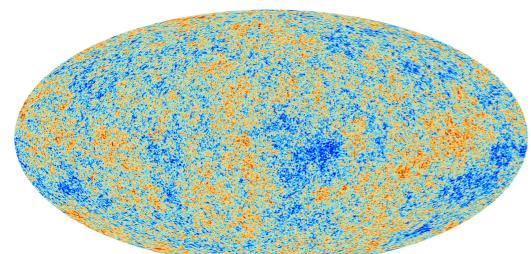
LCDM model

$$67.4 \pm 0.4 \text{ km.s}^{-1}.\text{Mpc}^{-1}$$

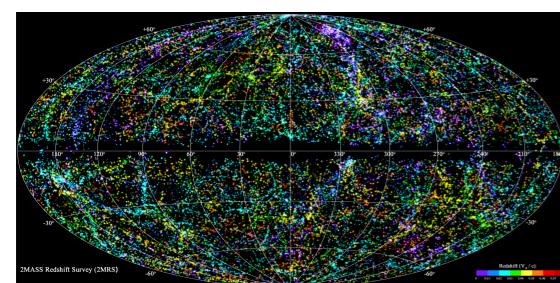
Planck VI. 2018

The Hubble constant tension

Universe



Cosmology



Direct measurement

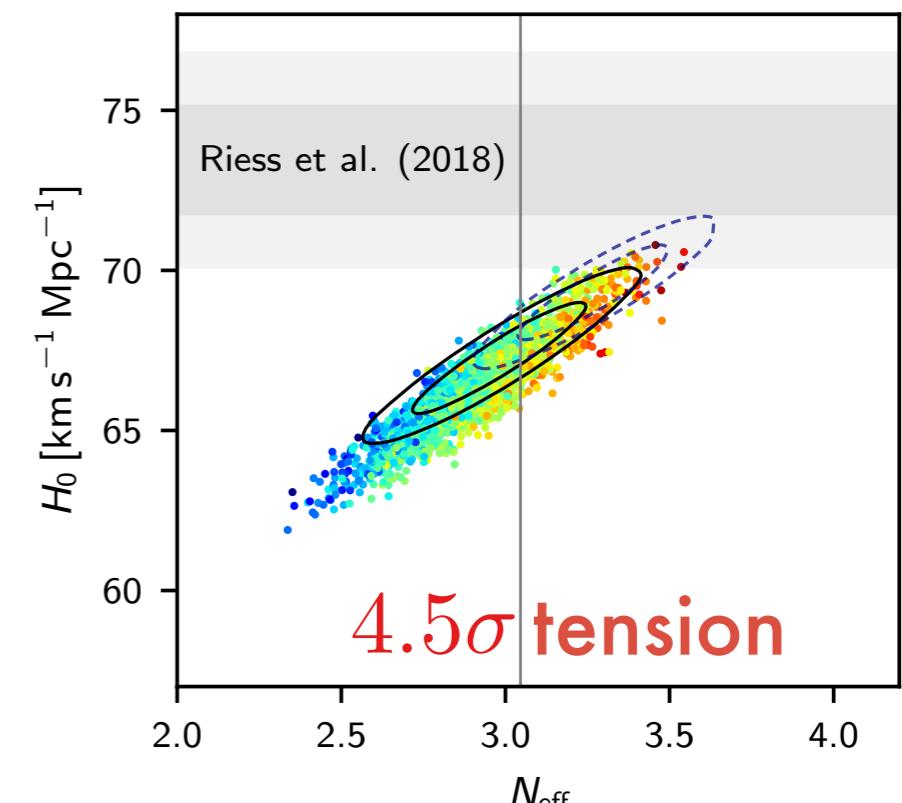
Expansion : H_0

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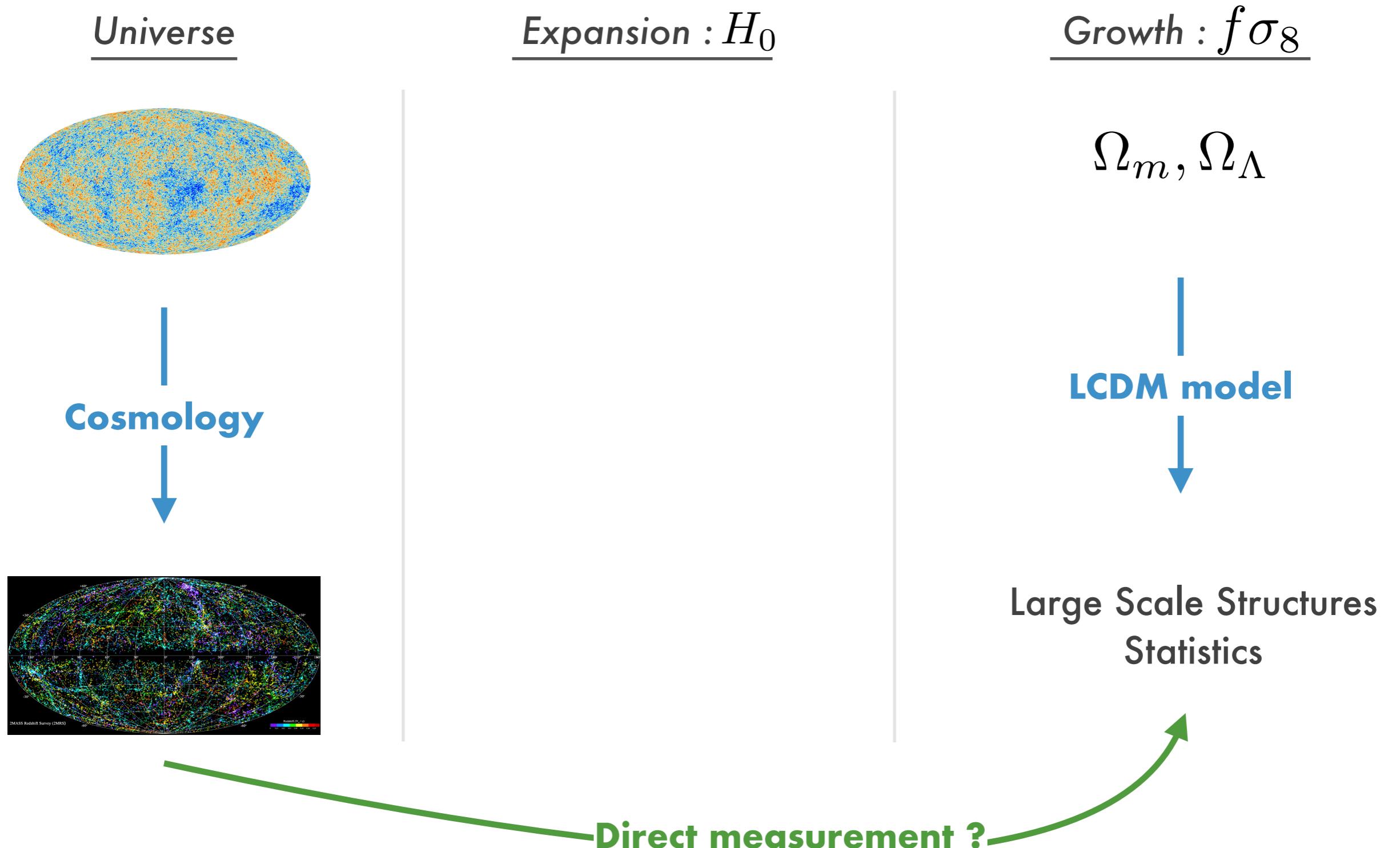
$$67.4 \pm 0.4 \text{ km.s}^{-1}.\text{Mpc}^{-1}$$

$$74.1 \pm 1.4 \text{ km.s}^{-1}.\text{Mpc}^{-1}$$



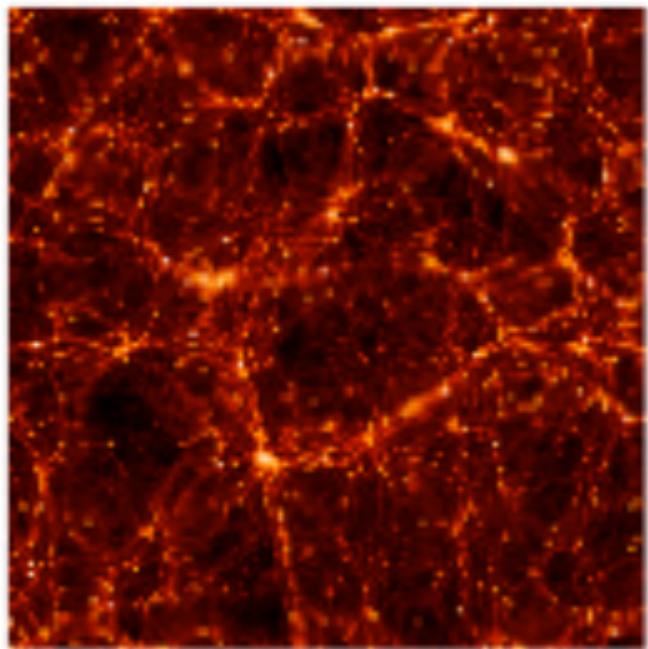
Planck VI. 2018, Riess et al. 2019

Growth rate

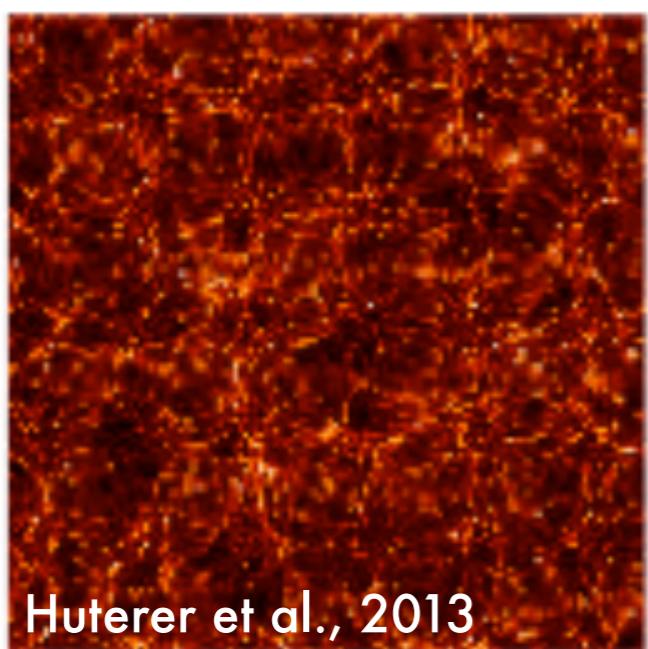


The Local Universe

Simulated Local Universe



$\Omega_m = 0.3$
LCDM



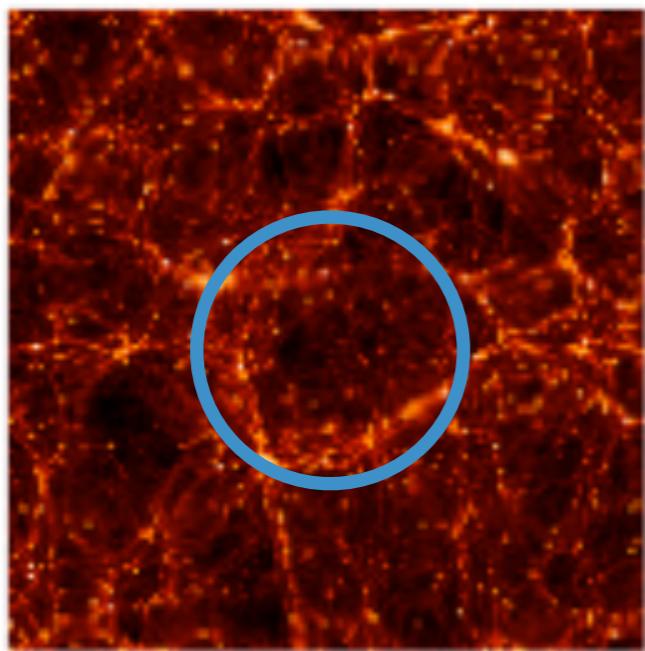
$\Omega_m = 1$
CDM

Huterer et al., 2013

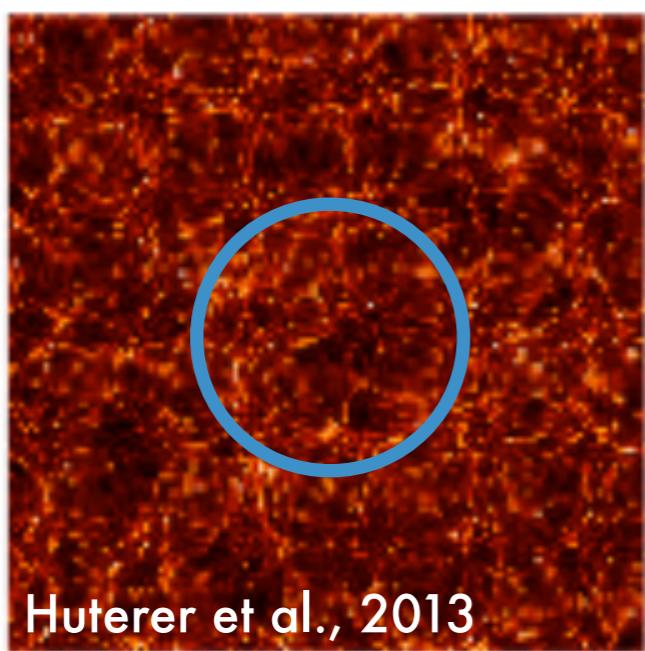
Density fluctuations

Simulated Local Universe

$\Omega_m = 0.3$
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$\Omega_m = 1$
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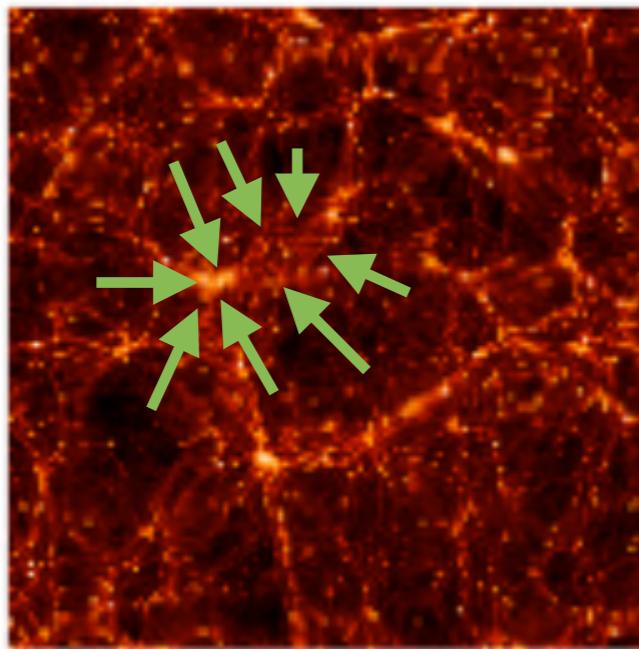
Matter density fluctuations :

$$\sigma_8^2 = \langle \delta^2 \rangle$$

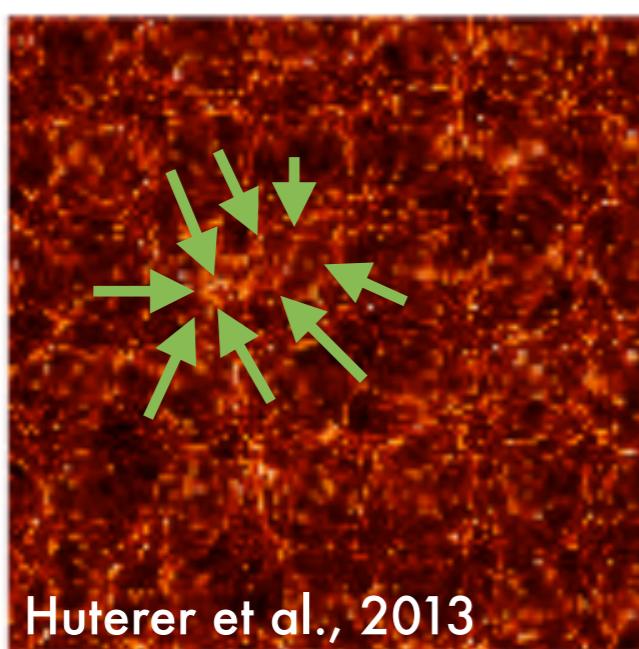
But we don't see dark matter...

Growth rate of structures

Simulated Local Universe



$\Omega_m = 0.3$
LCDM



$\Omega_m = 1$
CDM

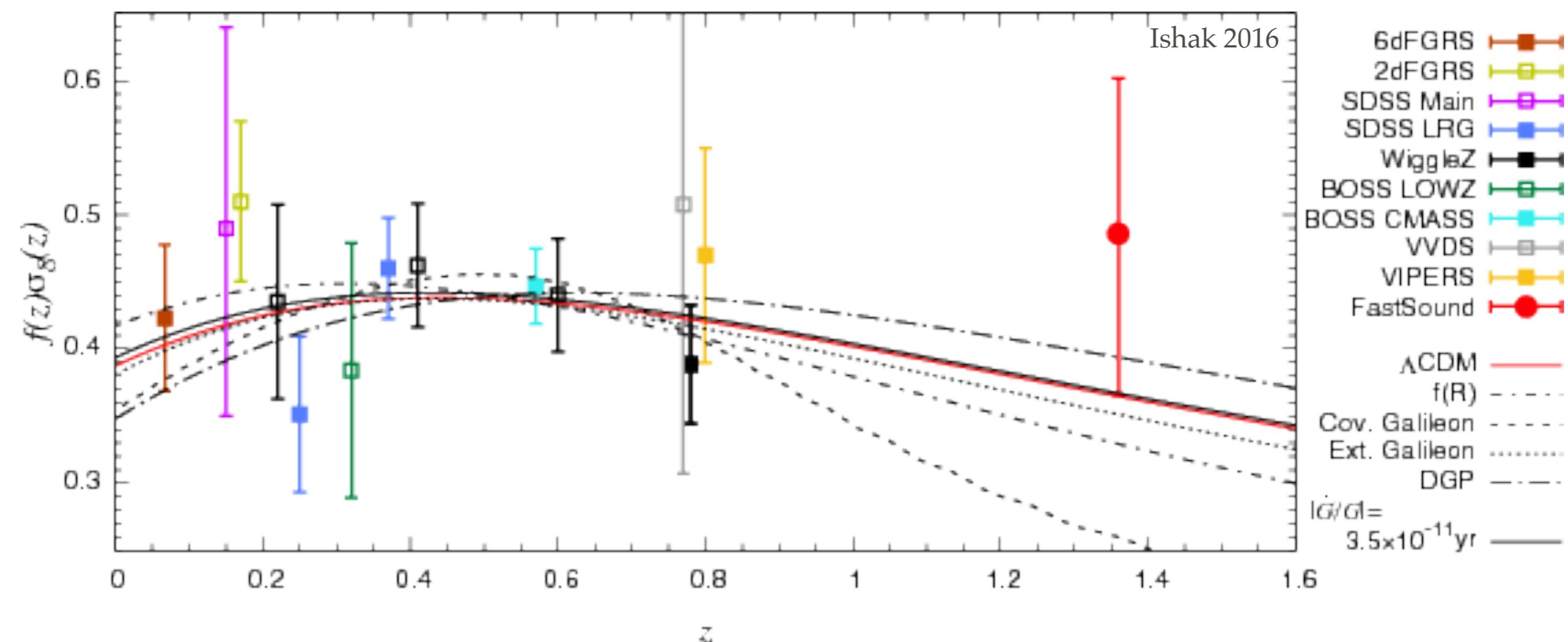
Huterer et al., 2013

Matter density fluctuations
+
Growth factor

$$(f\sigma_8)^2 = \langle v^2 \rangle$$

Depends on the expansion model and gravity

Goal



State of the art: >15% measurement with peculiar velocities

Measuring peculiar velocities

Peculiar velocity measurement

$$1 + z = (1 + \bar{z}) \left(1 + \frac{v^r}{c} \right)$$

Peculiar velocity measurement

$$1 + z = (1 + \bar{z}) \left(1 + \frac{v^r}{c} \right)$$

Apparent redshift

Cosmological (expansion) redshift

Peculiar velocity

The diagram illustrates the decomposition of the apparent redshift z into its cosmological and peculiar velocity components. It starts with the equation $1 + z = (1 + \bar{z}) \left(1 + \frac{v^r}{c} \right)$. A blue arrow points from the term $1 + z$ to the term $1 + \bar{z}$, indicating that the apparent redshift z is composed of the cosmological redshift \bar{z} and the peculiar velocity component v^r/c . A green arrow points from the term $1 + \bar{z}$ to the term $1 + \frac{v^r}{c}$, indicating that the cosmological redshift \bar{z} is composed of the cosmological expansion and the peculiar velocity component v^r/c . The term v^r/c is highlighted with a red circle and labeled "Peculiar velocity".

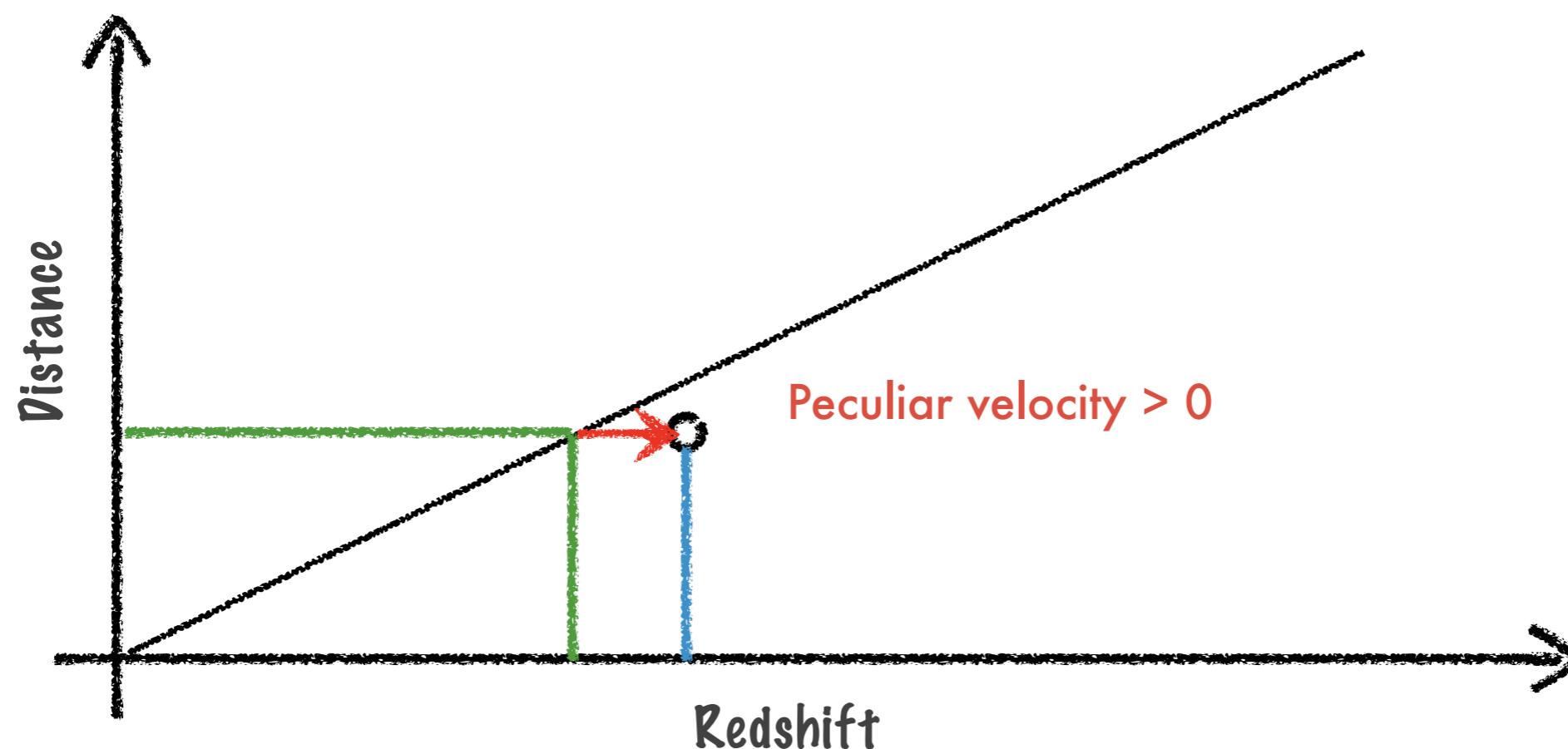
Peculiar velocity measurement

$$1 + z = (1 + \bar{z}) \left(1 + \frac{v^r}{c} \right)$$

Apparent redshift

Cosmological (expansion) redshift

Peculiar velocity



The roadmap to peculiar velocities

$$1 + z = (1 + \frac{\dot{z}}{\bar{z}}) \left(1 + \frac{v^r}{c} \right)$$

The roadmap to peculiar velocities

$$1 + z = (1 + \bar{z}) \left(1 + \frac{v^r}{c} \right)$$

$$\rightarrow \mu = 5 \log_{10} \frac{d}{10 \text{ pc}} = m - M$$

?

The roadmap to peculiar velocities

$$1 + z = (1 + \bar{z}) \left(1 + \frac{v^r}{c} \right)$$

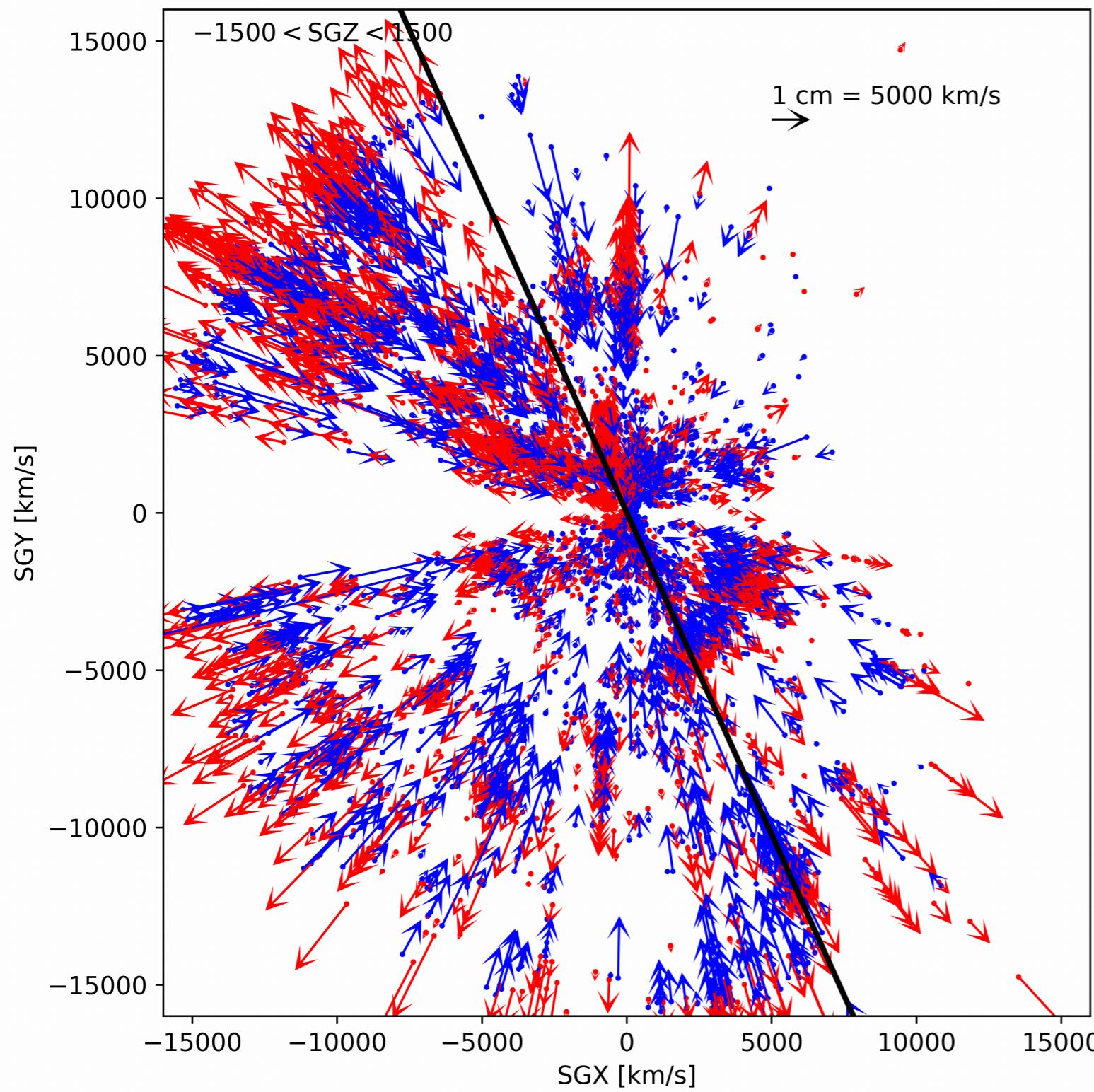
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?

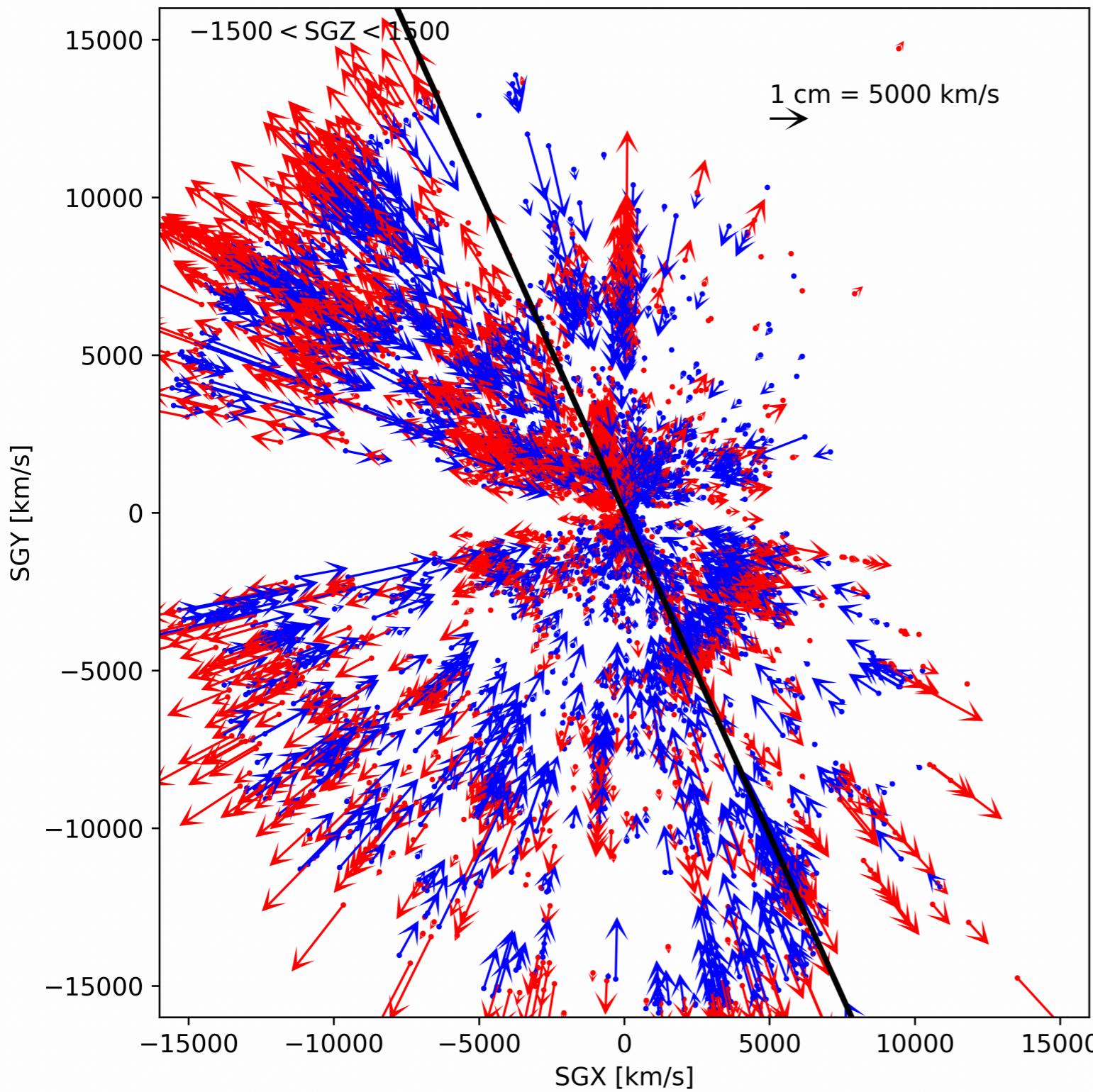
Tully-Fisher Relation	$L \sim V^4$	$\sigma_\mu \sim 0.4$
		$z \sim 0.1$

SNels	$L \sim \text{constant}$	$\sigma_\mu \sim 0.14$
		$z \sim 1$

Radial peculiar velocity measurement : an exemple



Radial peculiar velocity measurement : an exemple

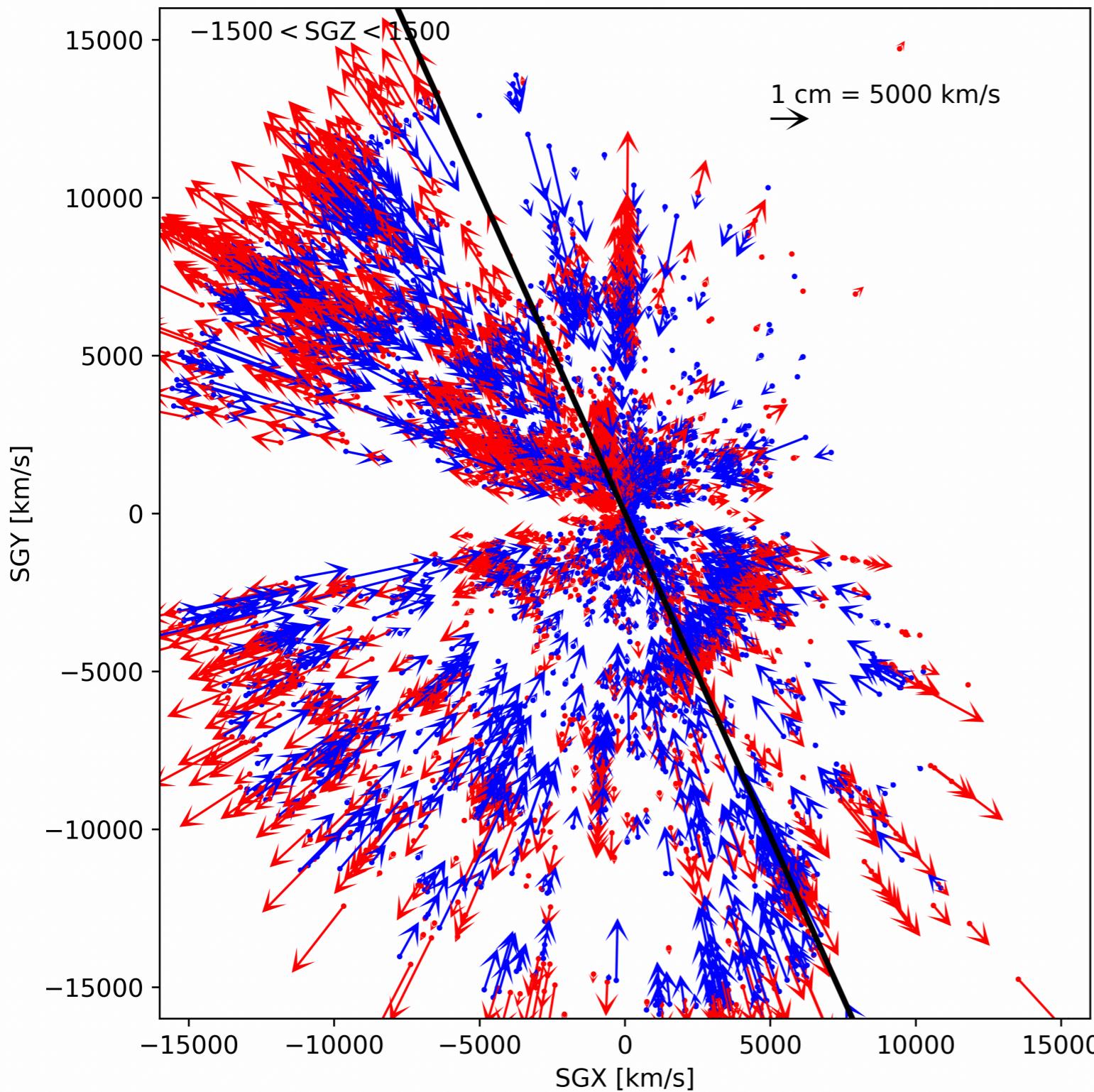


$$d = 100 \pm 20 \text{ Mpc}$$

$$cz = 6500 \text{ km/s}$$

$$v^r = -500 \pm 1400 \text{ km/s}$$

Radial peculiar velocity measurement : an exemple



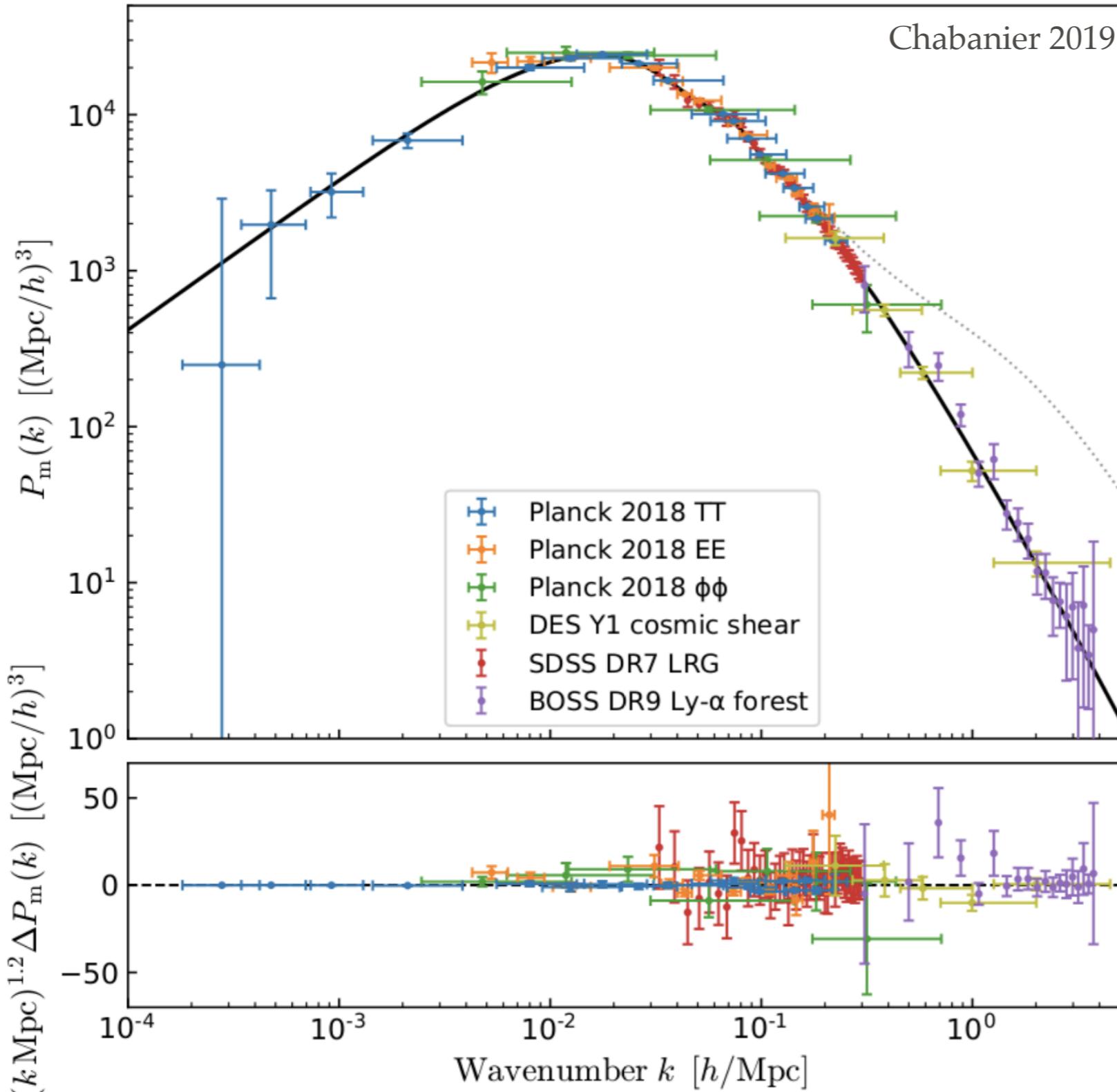
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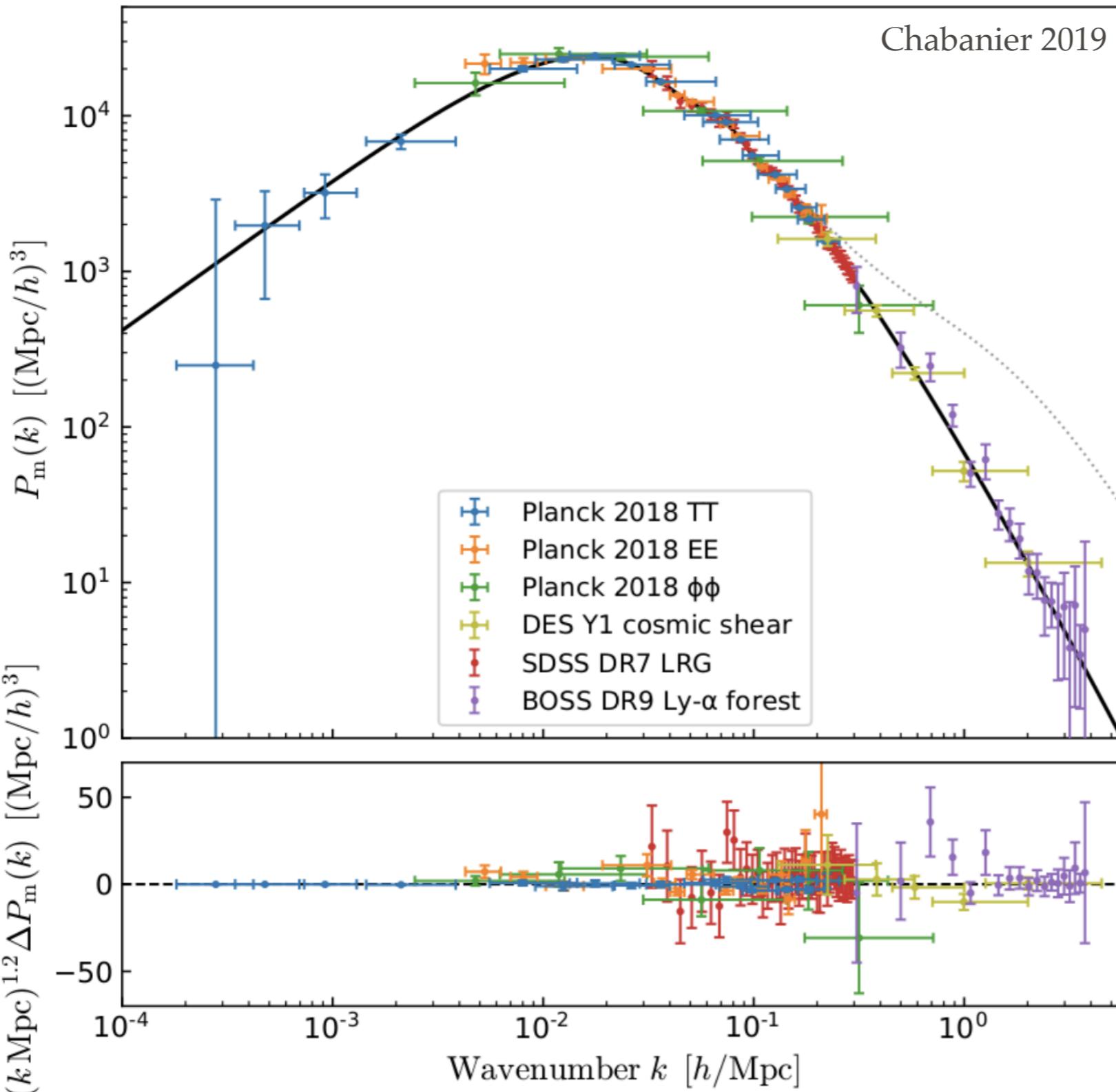
Not enough information?
Be Bayesian!

Power spectrum



$$\langle \delta^2 \rangle = \sigma_8^2 P_0(k)$$

Power spectrum

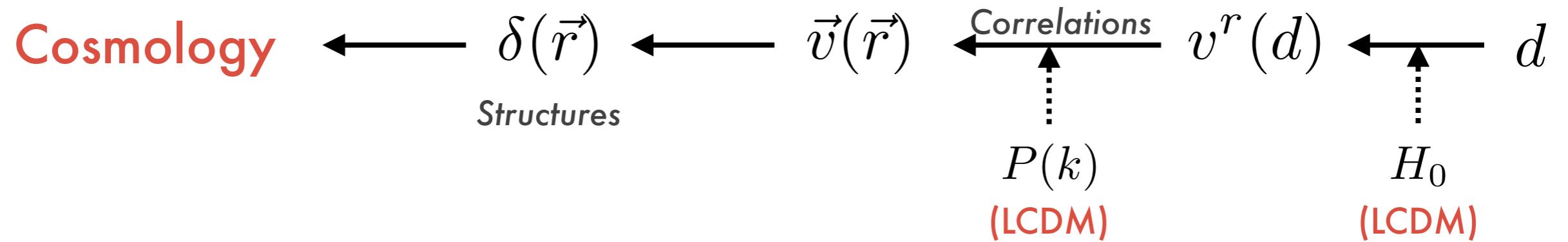


$$\langle \delta^2 \rangle = \sigma_8^2 P_0(k)$$

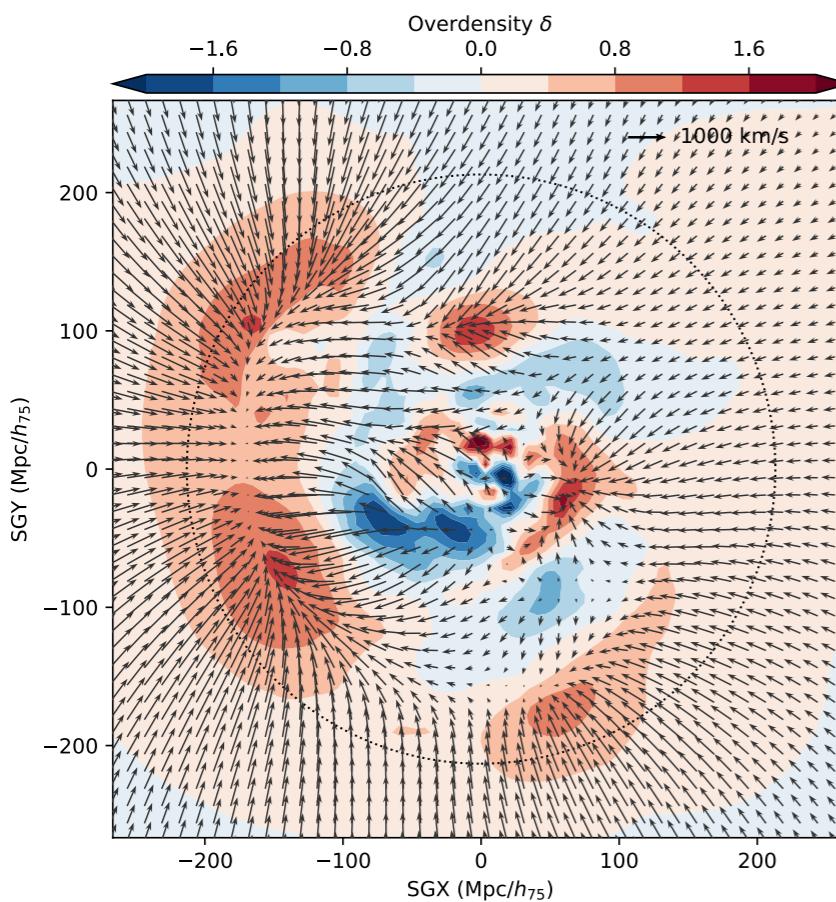
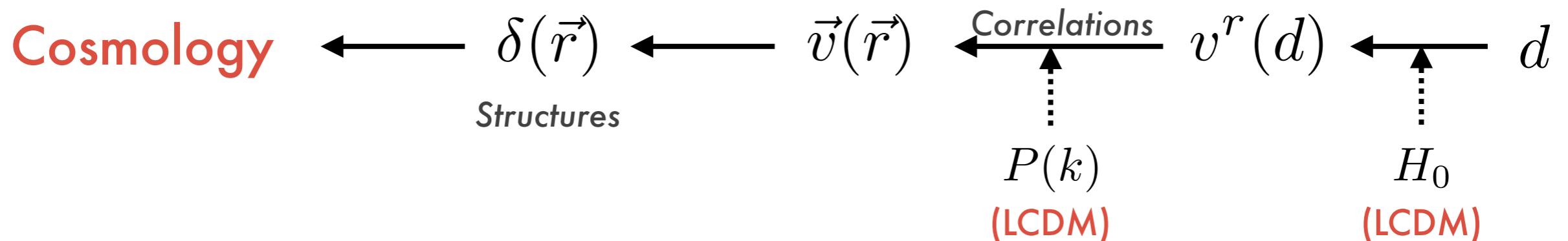
$$\vec{\nabla} \vec{v} = -H_0 f \delta$$

$$\langle v_\alpha^2 \rangle = (f \sigma_8)^2 \frac{k_\alpha^2}{k^4} P_0(k)$$

Inverse analysis



Inverse analysis



Systematic
Errors →

Graziani et al., 2019

- Malmquist bias
- Selection effects
- Error bias
- Density bias
- Covariance bias

Forward modeling

Backward modeling



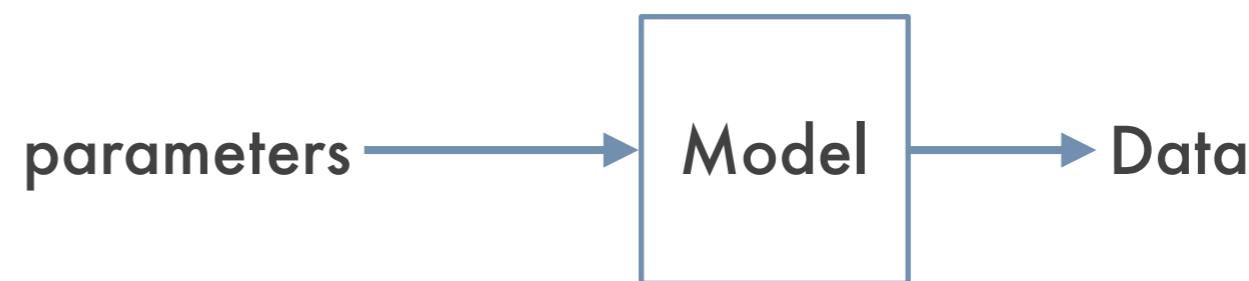
- Information loss
- Systematics ?
- Hard to estimate covariances

Forward modeling

Backward modeling



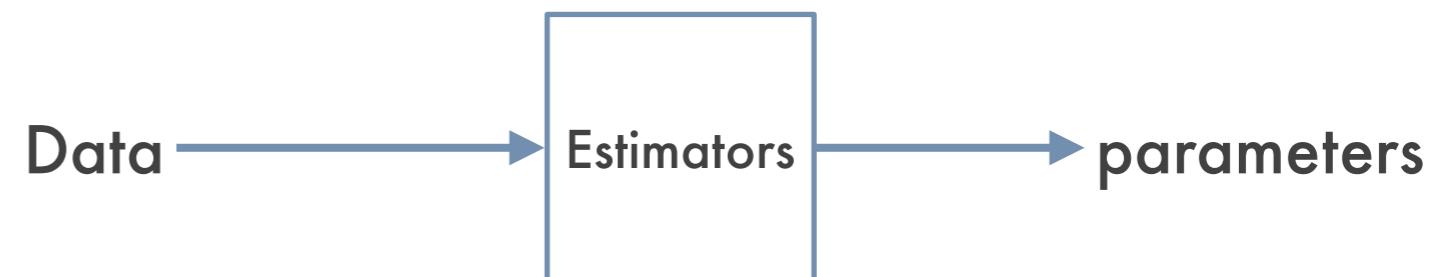
Forward modeling



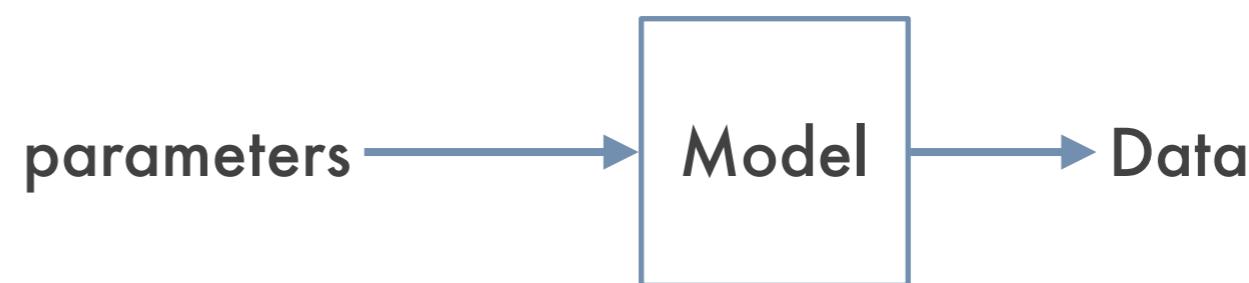
- No convolution of the data
- No need to copy the data
- Numerically expensive

Forward modeling

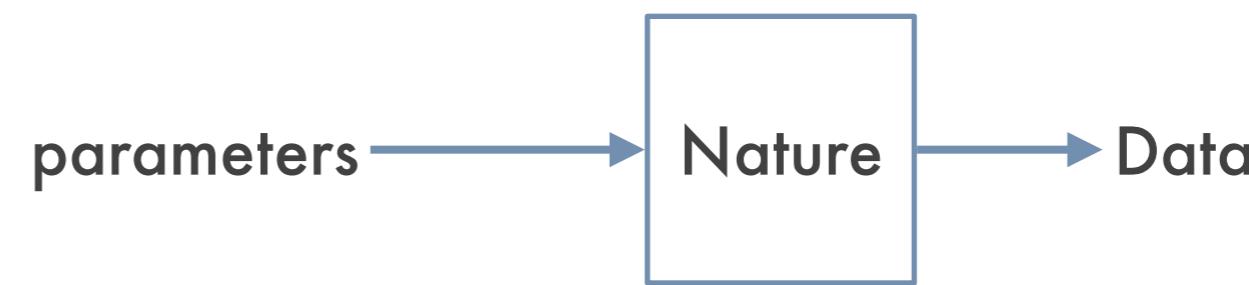
Backward modeling



Forward modeling



What happens

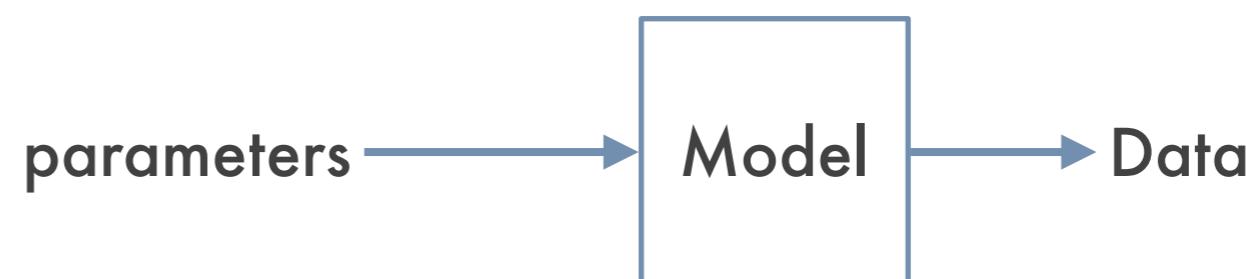


Forward modeling

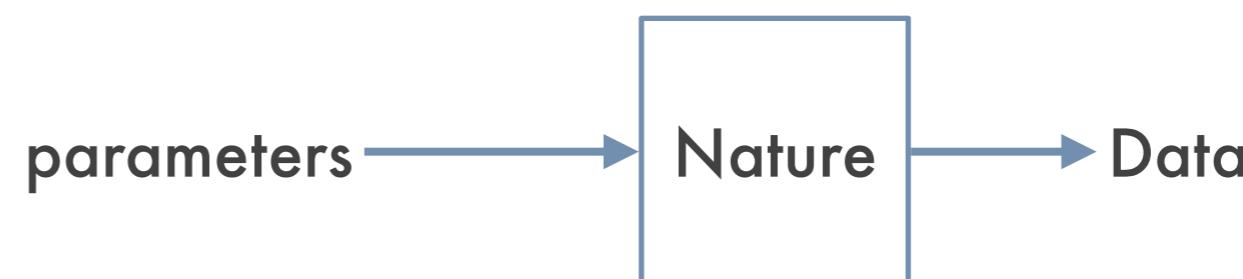
Backward modeling



Forward modeling



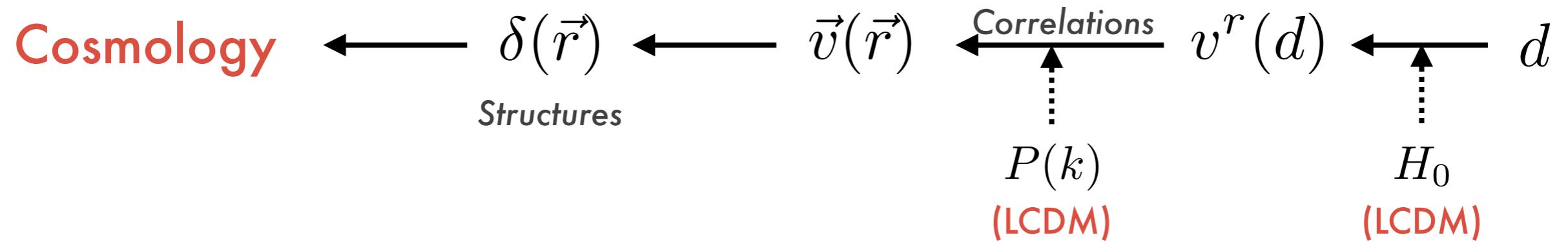
What happens



Machine learning



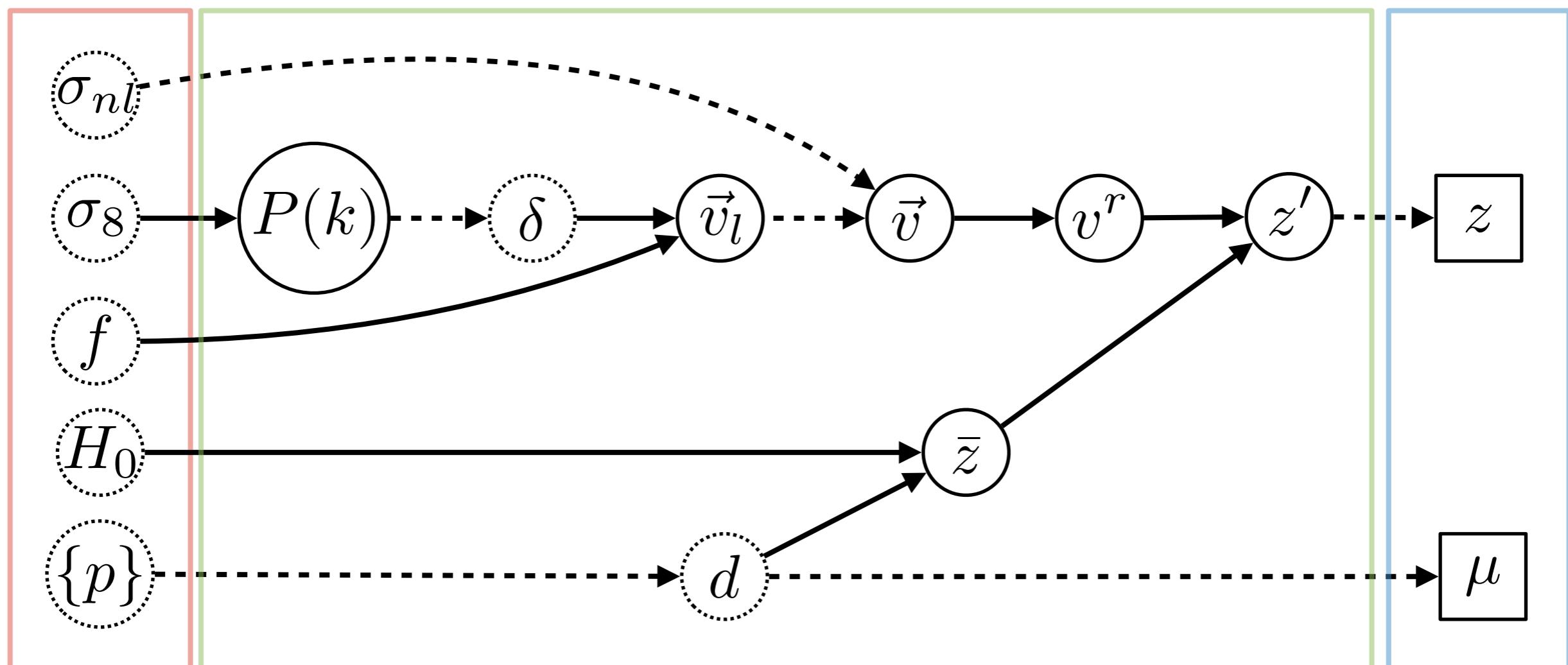
Inverse analysis



A forward model

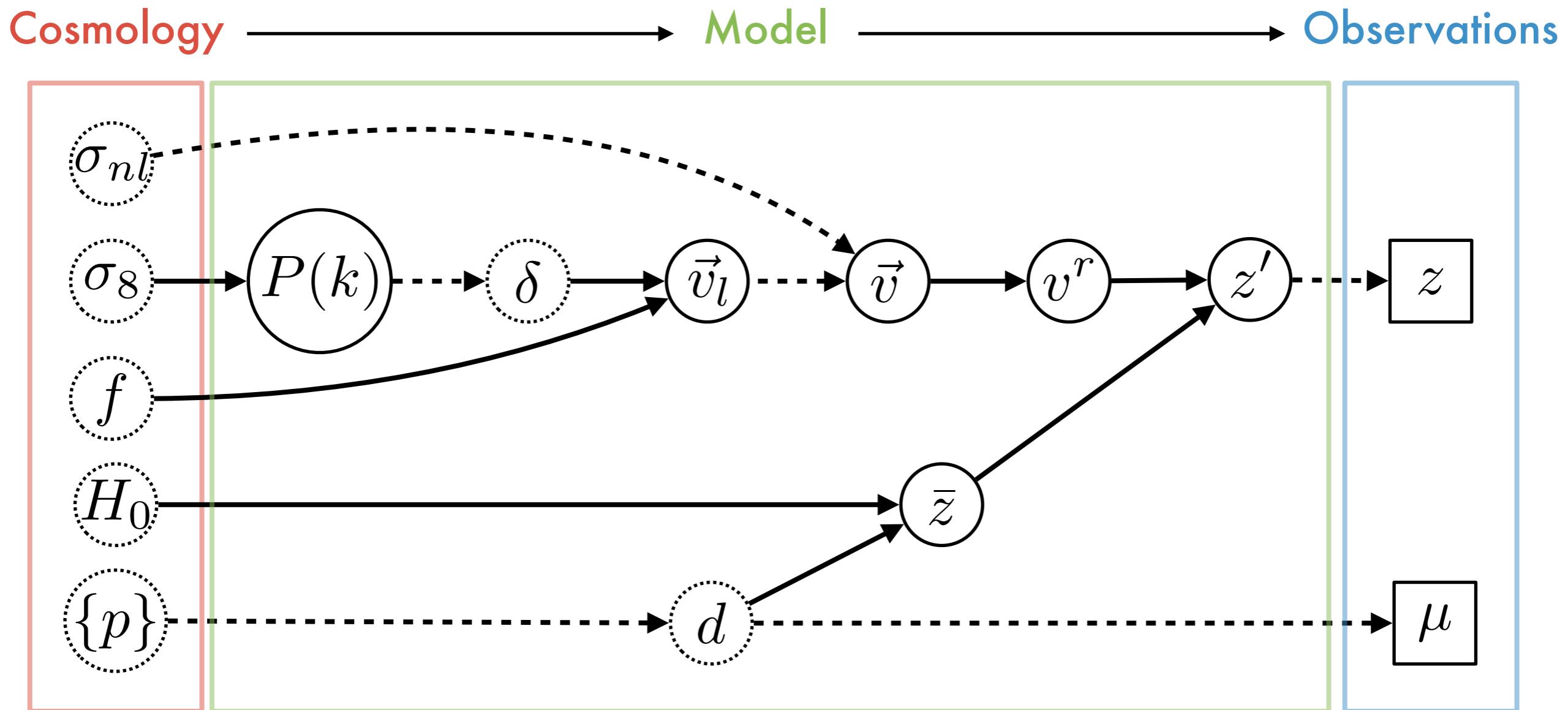
Graziani et al., 2019

Cosmology → Model → Observations



A forward model

Graziani et al., 2019



- Hierarchical Bayesian model
- Highly modular
- Room for systematics modeling

A forward model

$$\begin{aligned}\mathcal{L} &= \int \mathcal{N} \left(m - M_{SN} - 5 \log_{10} \frac{r}{10 \text{ pc}}, \sigma_m \right) \\ &\times \mathcal{N} (v^r(z, r) - \mathbf{v}_\delta(\mathbf{r}), \sigma_{nl}) \\ &\times \mathcal{N} \left(\hat{\delta}(\mathbf{k}), P(k) \right) \text{d}\hat{\delta}\end{aligned}$$

Metropolis Sampling

- Randomly draw a set of parameters
- If the posterior probability is approximately higher than previously, keep this set
- Else, retry

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- Randomly draw a set of parameters
- If the posterior probability is approximately higher than previously, keep this set
- Else, retry

Pros	Cons
Converges* to the solution <small>*sometimes</small>	Inefficient in high dimensions
Easy to implement	Inefficient when parameters are correlated
	Inefficient for multi-modal or multi-scale distribution
	Samples are highly correlated

Gibbs Sampling

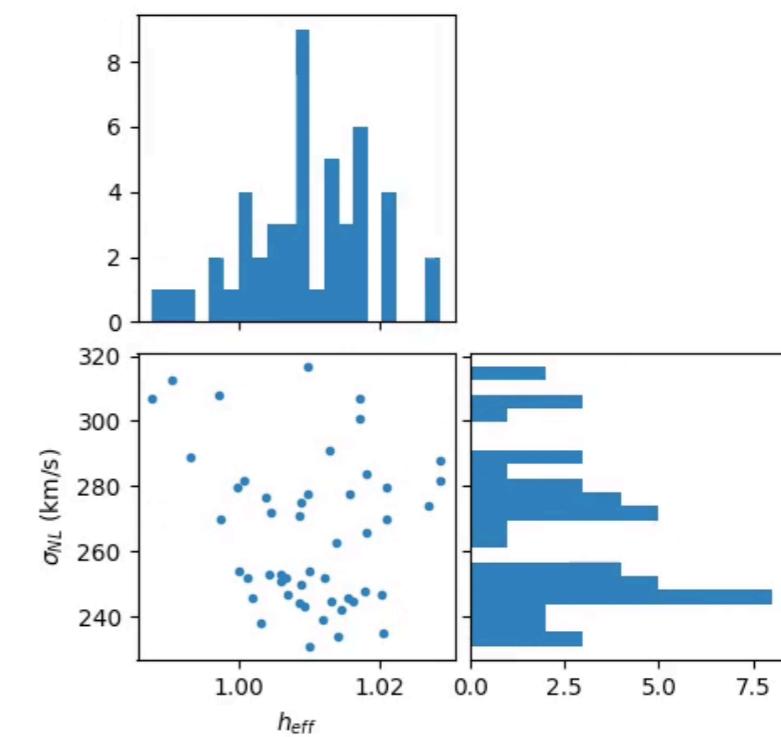
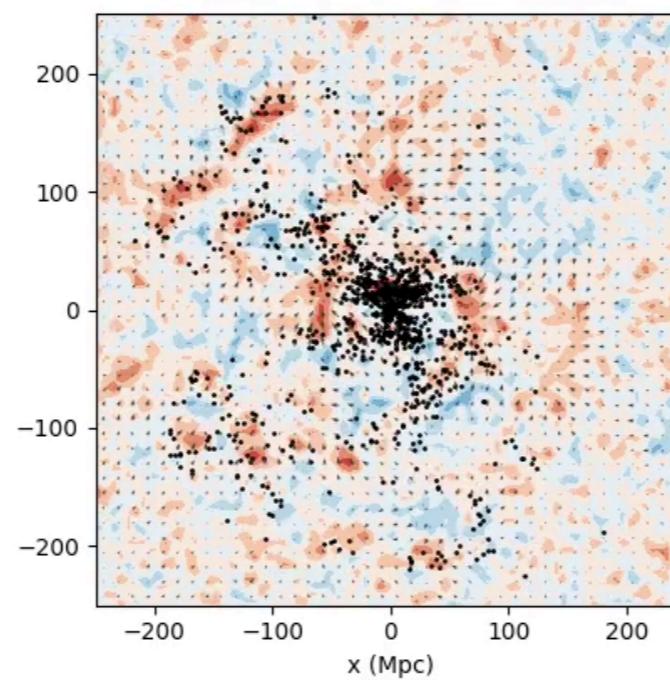
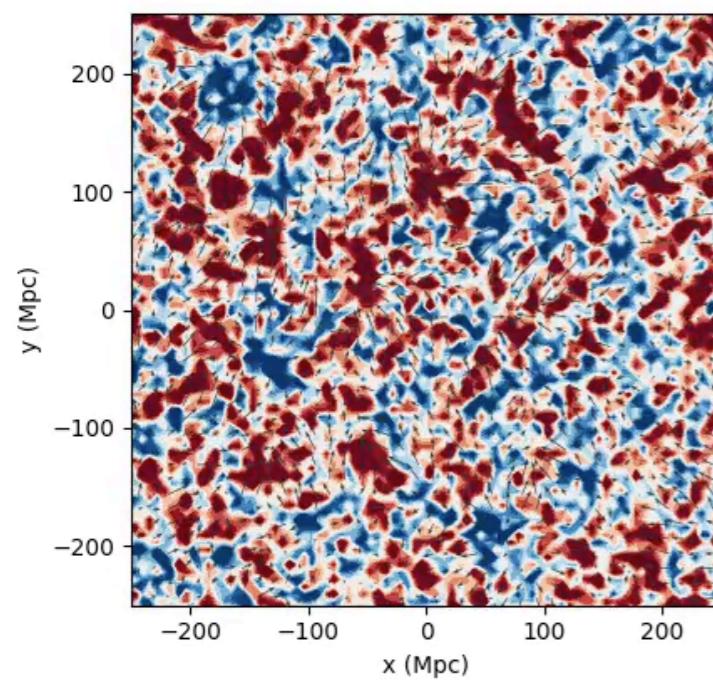
- Draw each parameter from its conditional probability
- Accept all the samples

Gibbs Sampling

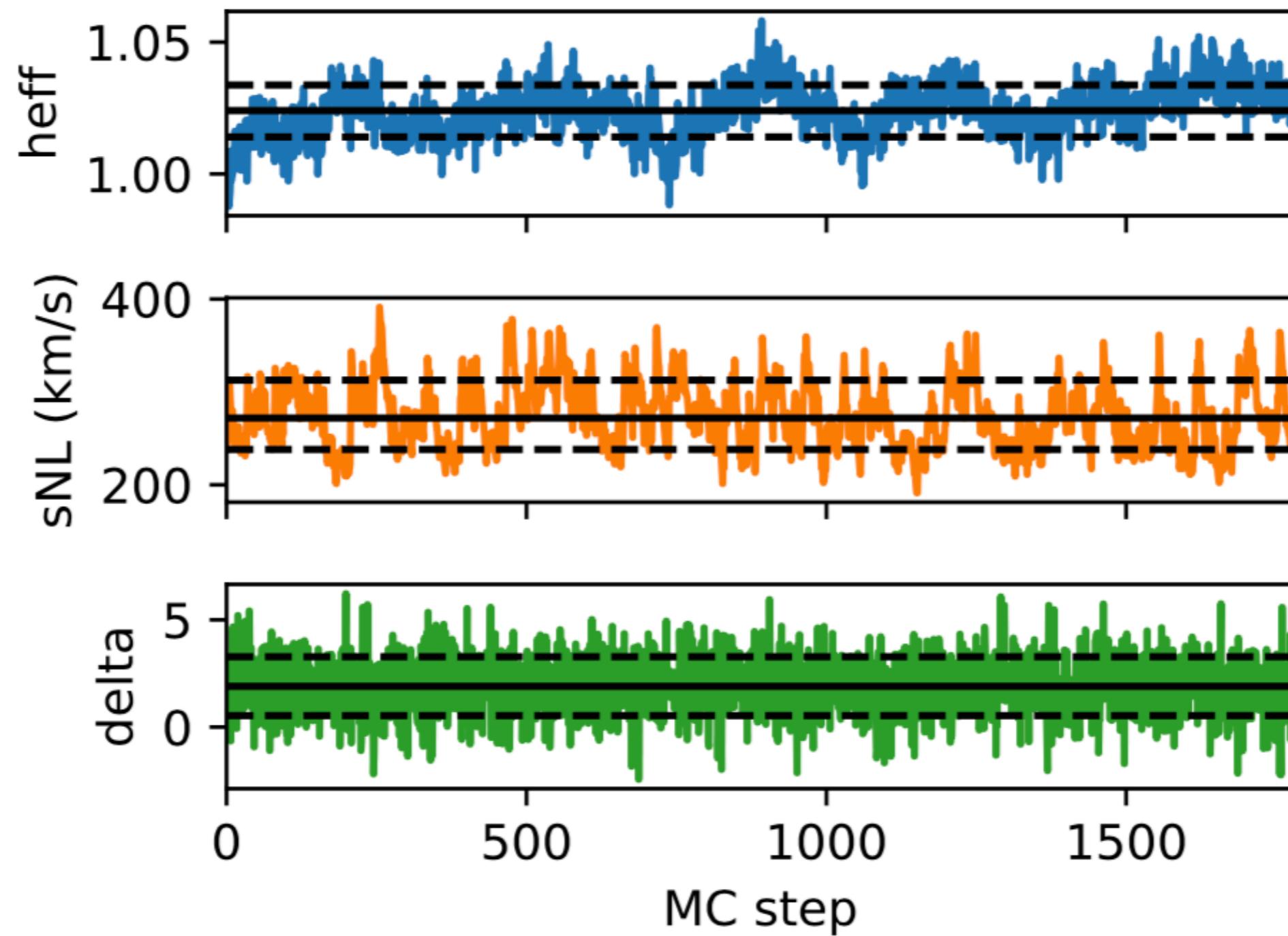
- Draw each parameter from its conditional probability
- Accept all the samples

Pros	Cons
Converges* to the solution *always	Need the conditional probability (rare)
Easy to implement	Samples highly correlated
Acceptance rate of 100%	Model dependent

MCMC

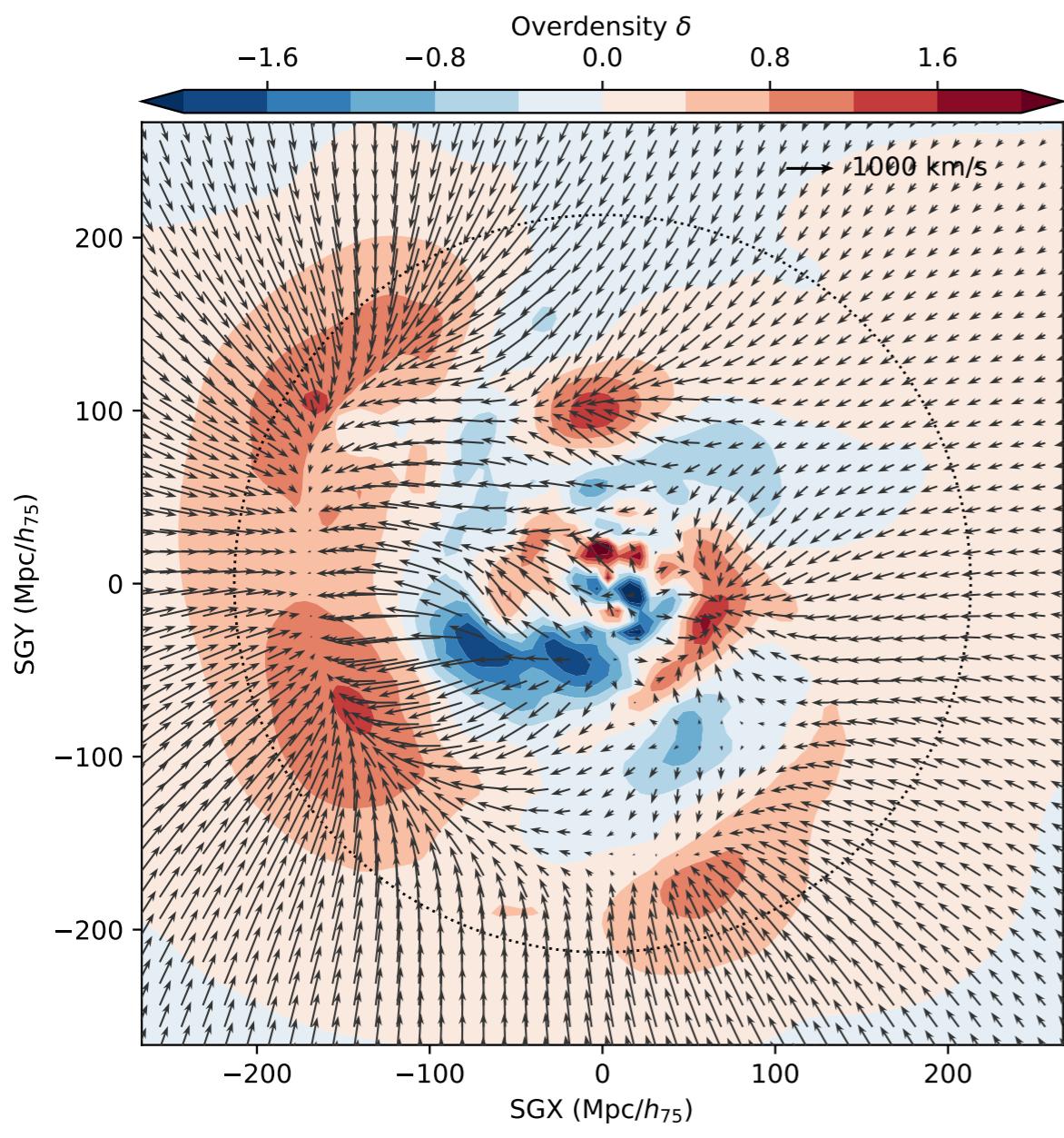


MCMC

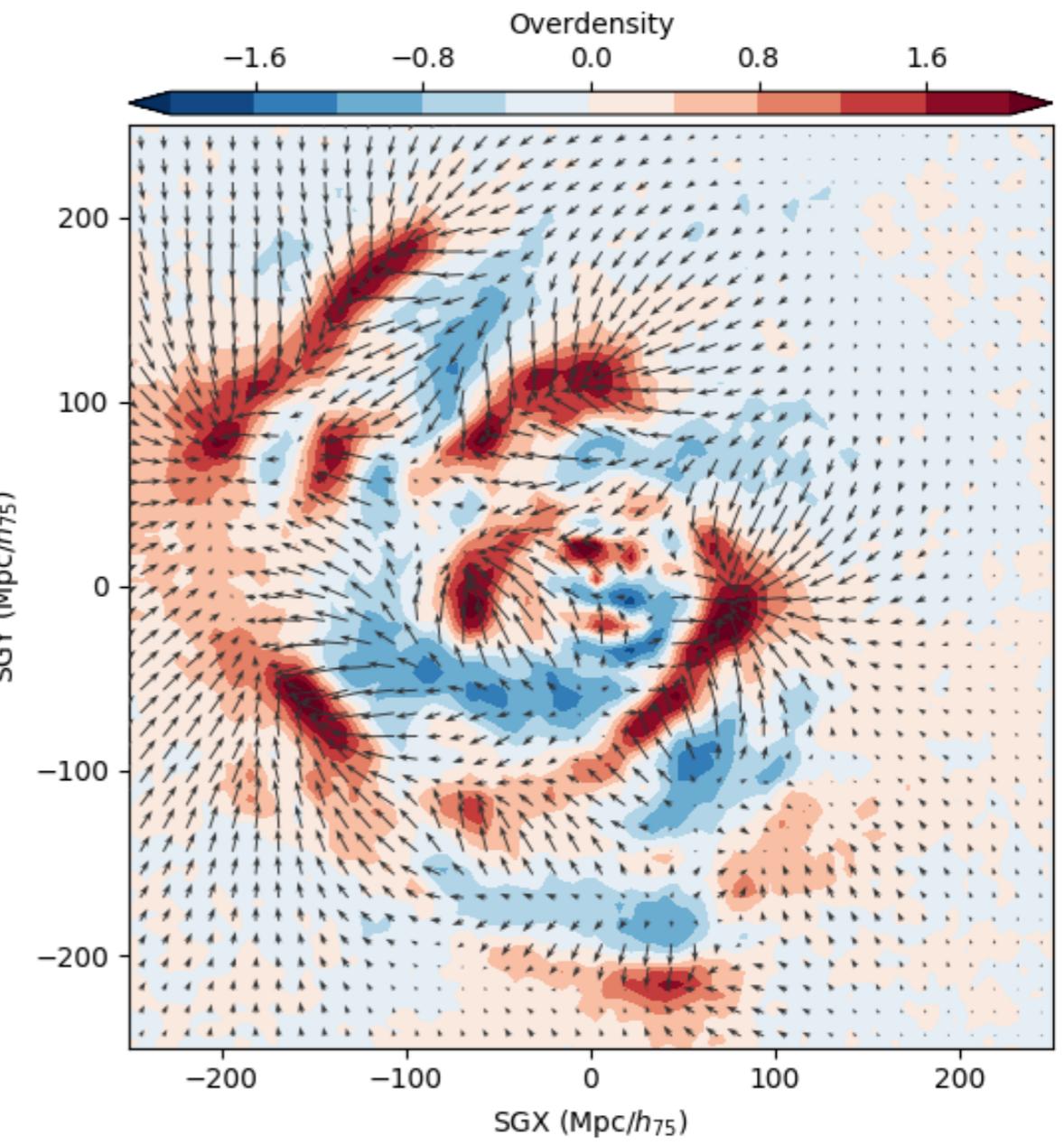


The model applied on galaxy data

Inverse method

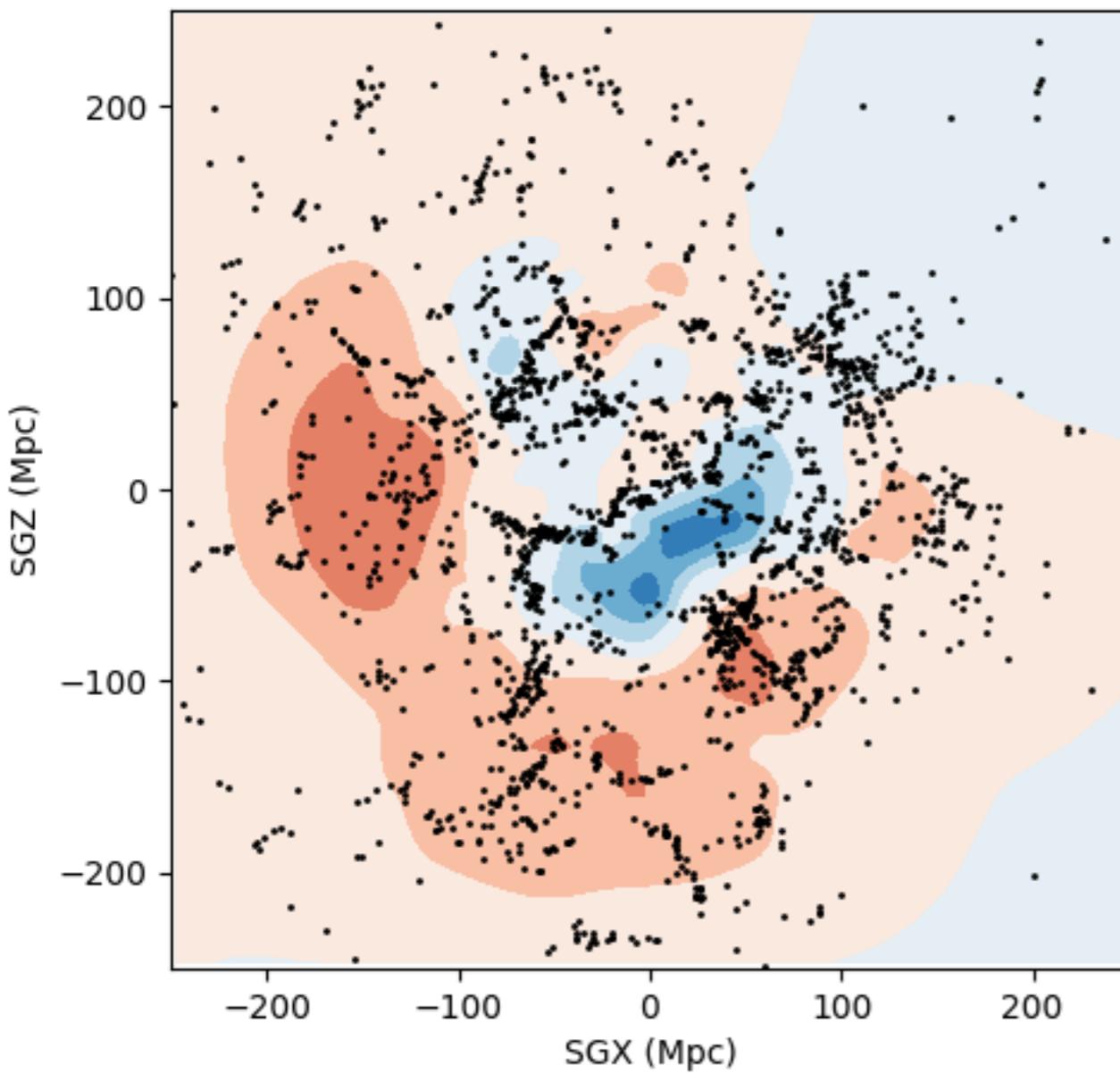


Graziani et al., 2019

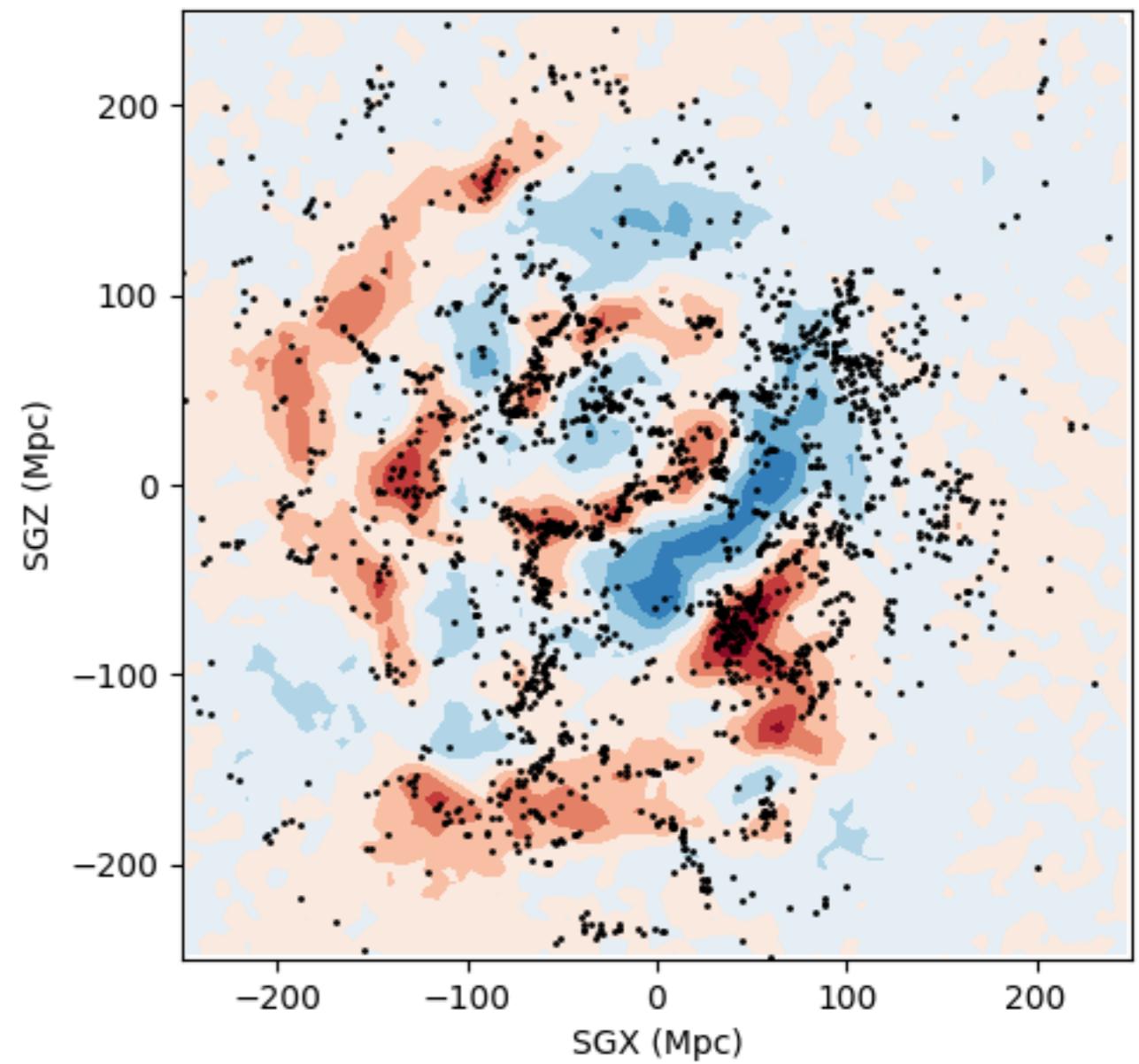


Peculiar velocity field vs galaxy distribution

Inverse method

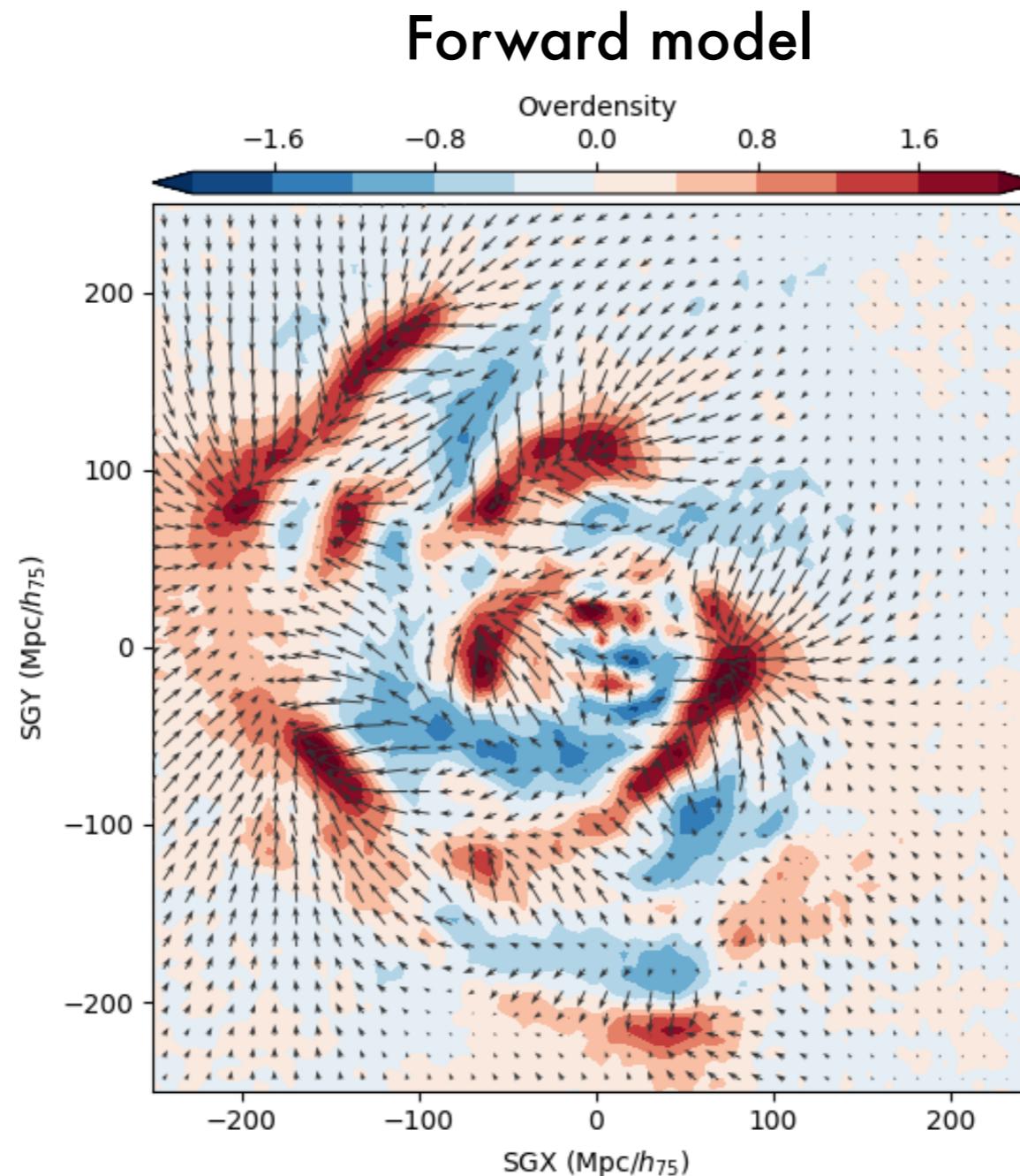


Graziani et al., 2019



The model applied on galaxies

Graziani et al. 2019, 1901.01818



No cosmological parameter fitting because galaxy data are prone to **systematics**

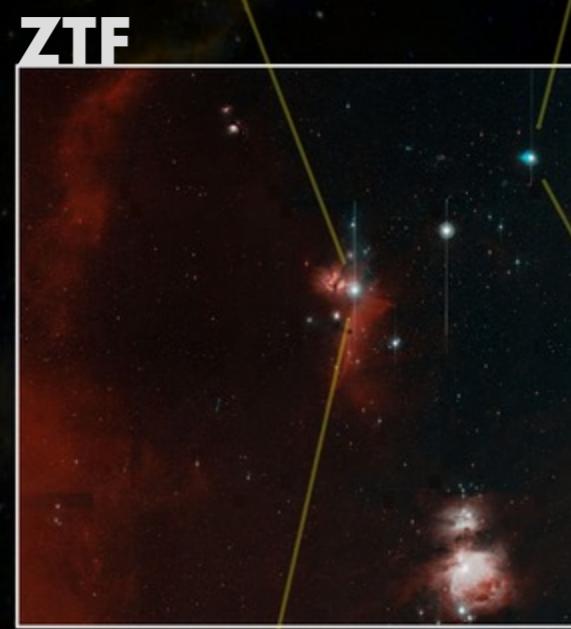
Cosmology

Why SNela ?

- Brightness
- Precision : 1 SNela = 15 galaxies
- Systematics studied for cosmology
- Number ?

Graziani et al., *in prep.*

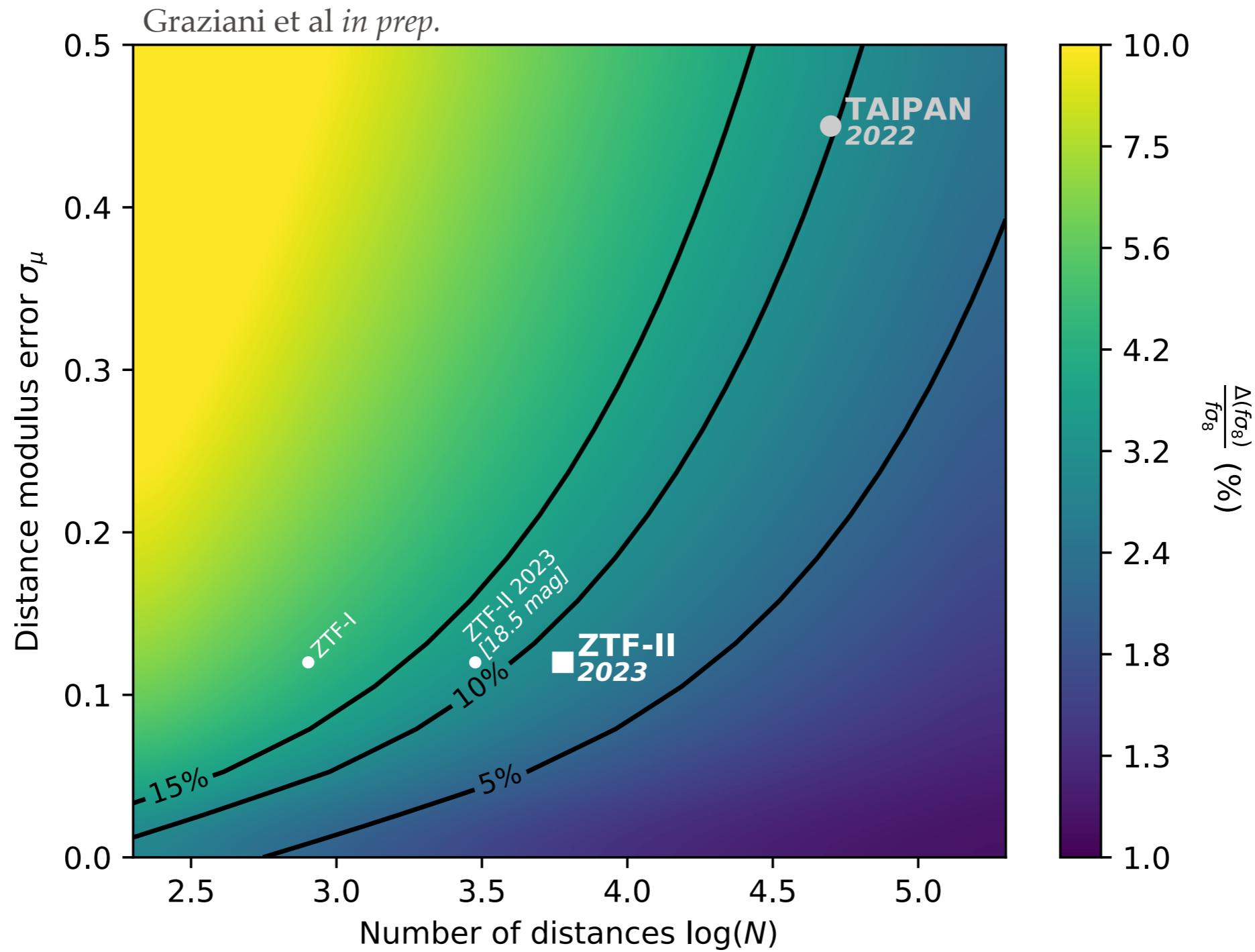
Kim, ..., Graziani,... et al. 2019



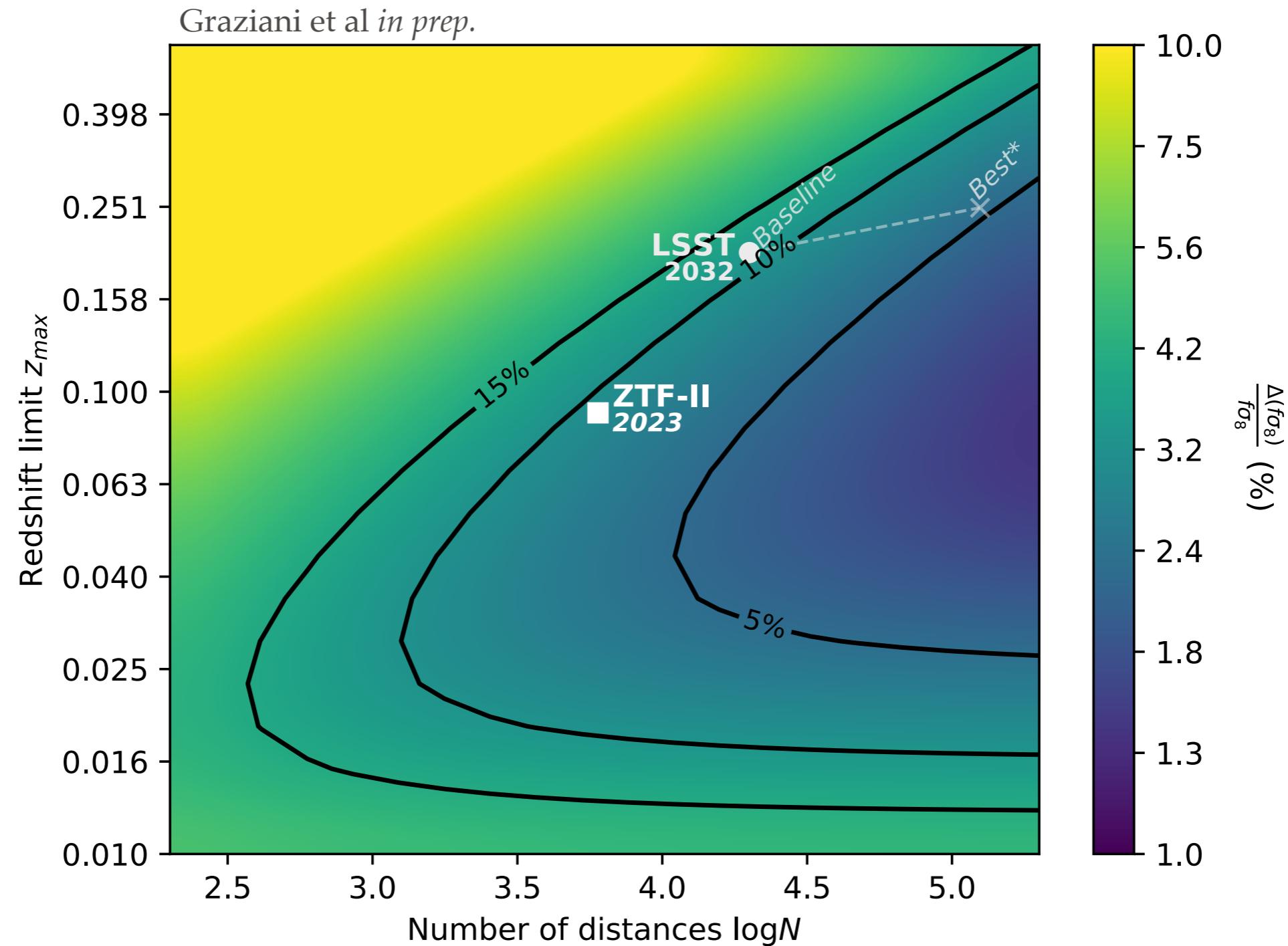
ZTF: 600 SNeIa/yr, z<0.1

LSST: 4000 SNeIa/yr z<0.2

Forecasts



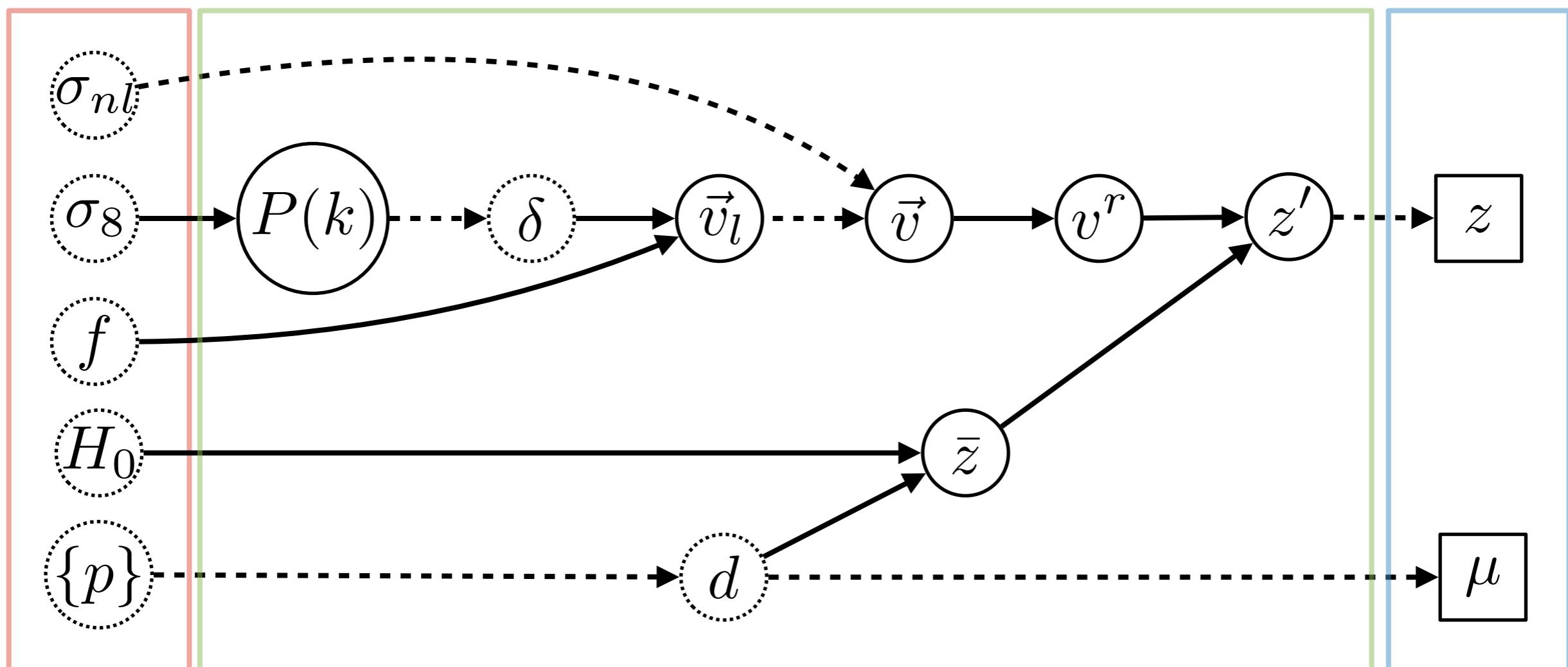
Forecasts



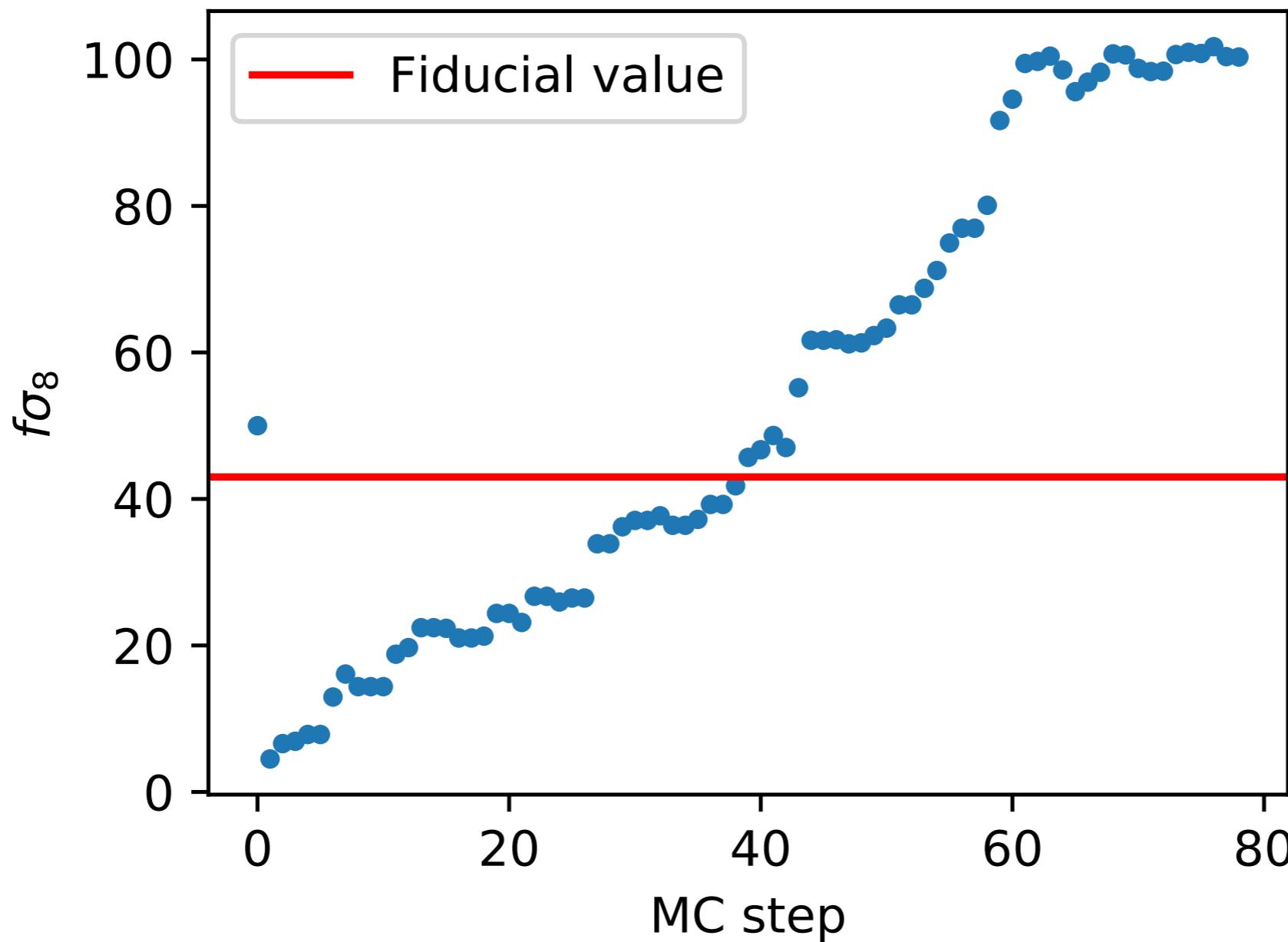
A forward model

Graziani et al., 2019

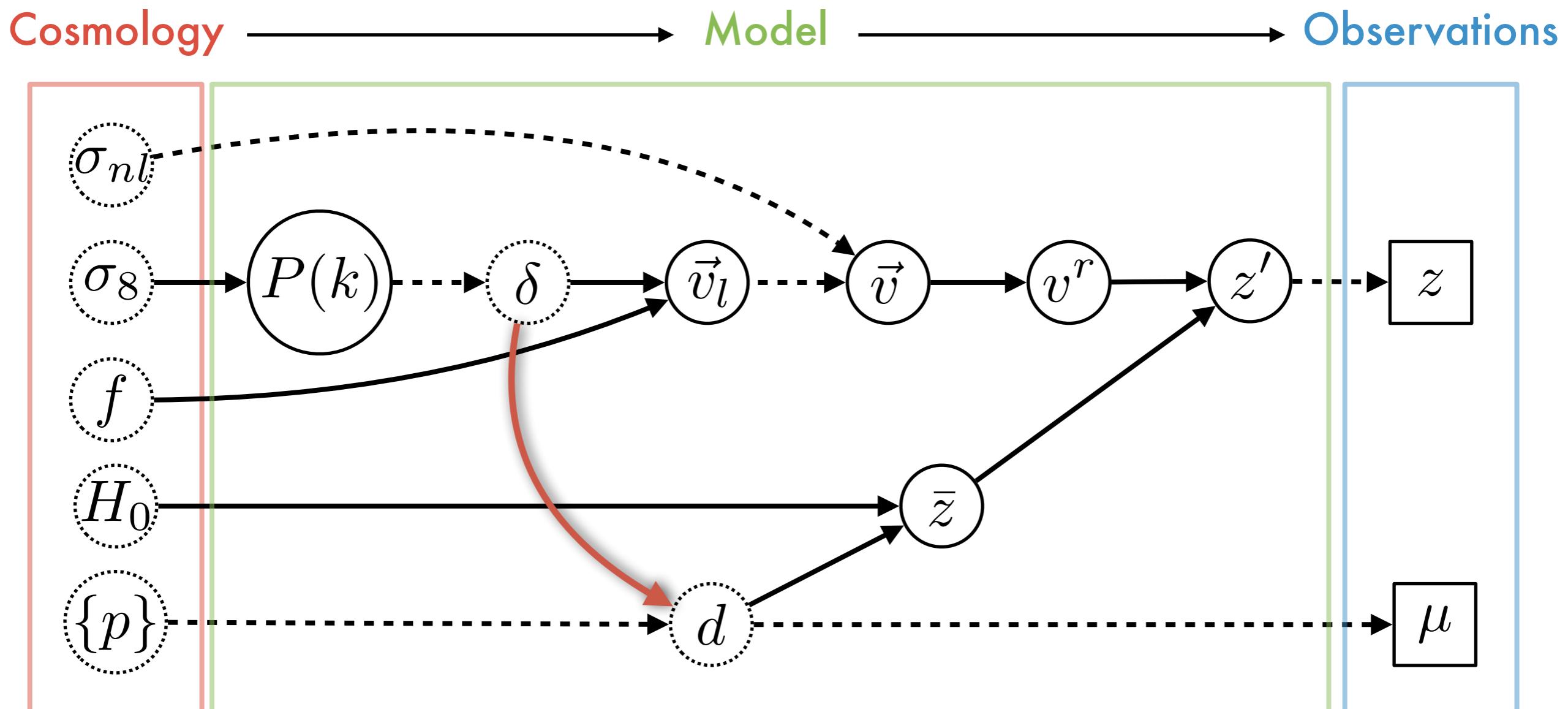
Cosmology → Model → Observations



Results on mock



Including density correlations



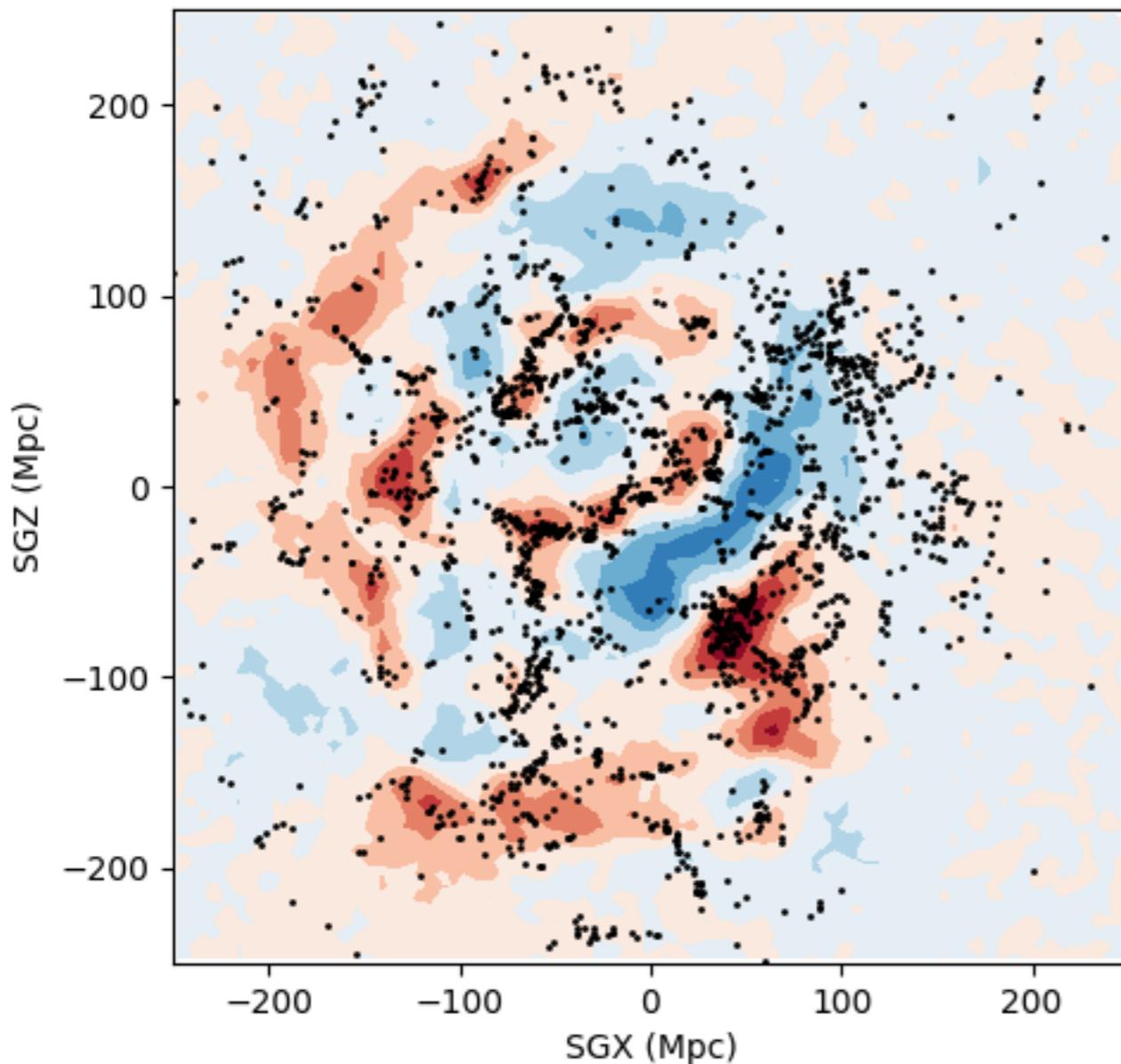
$\mathcal{P}(\mathcal{O}|\delta)?$

Density model

$$\mathcal{P}\text{oisson}(\mathcal{O}|\mathbf{r}) \propto n_g(\mathbf{r}) \times e^{-\int n_g(\mathbf{x}) d\mathbf{x}}$$

Density model: Linear bias

$$\text{Poisson } (\mathcal{O}|\mathbf{r}) \propto n_g(\mathbf{r}) \times e^{-\int n_g(\mathbf{x}) \, d\mathbf{x}}$$

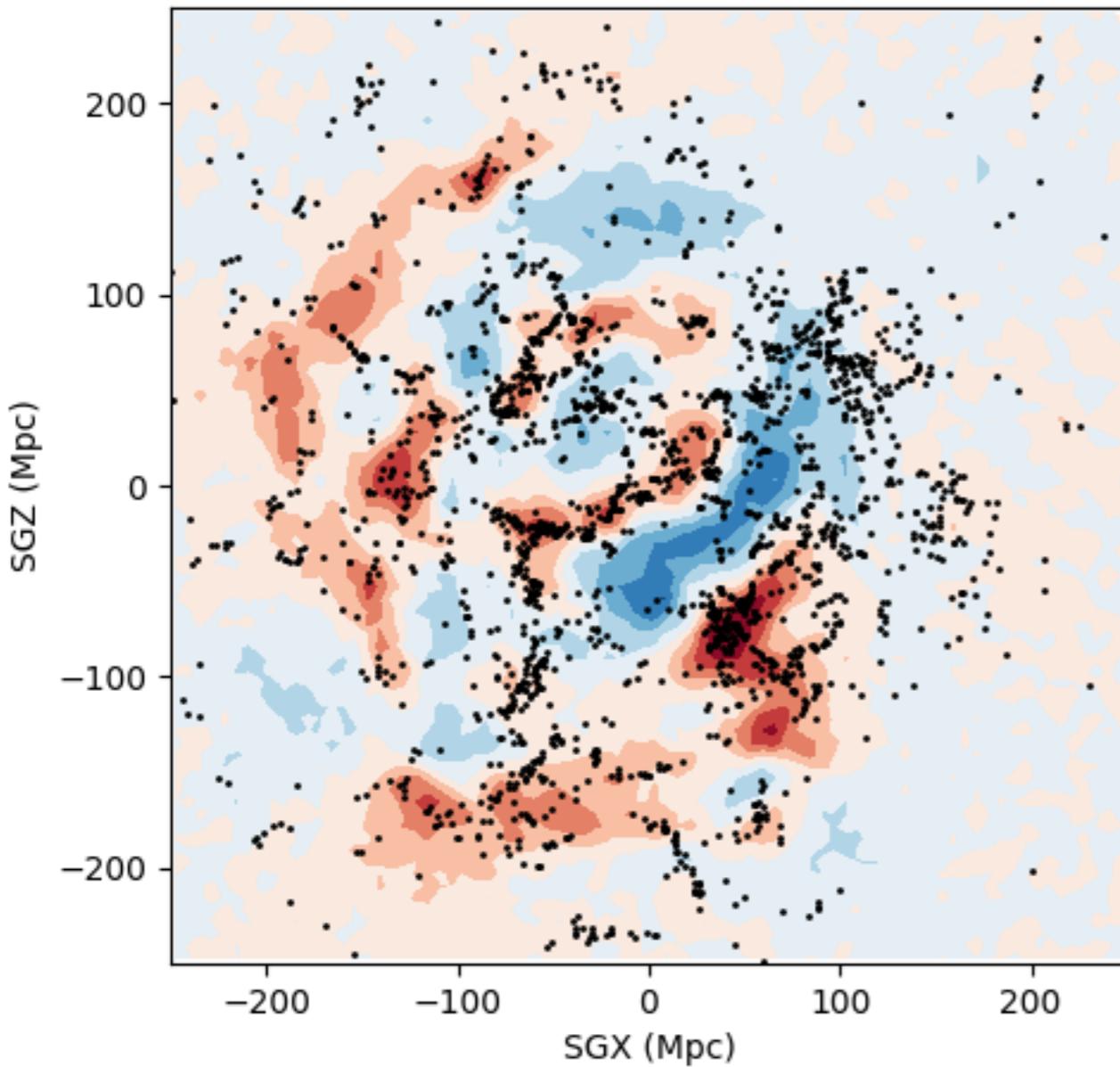


$$n_g = 1 + \delta_g = 1 + b\delta$$

Linear bias

Density model: Non-linear model

$$\text{Poisson } (\mathcal{O}|\mathbf{r}) \propto n_g(\mathbf{r}) \times e^{-\int n_g(\mathbf{x}) \, d\mathbf{x}}$$



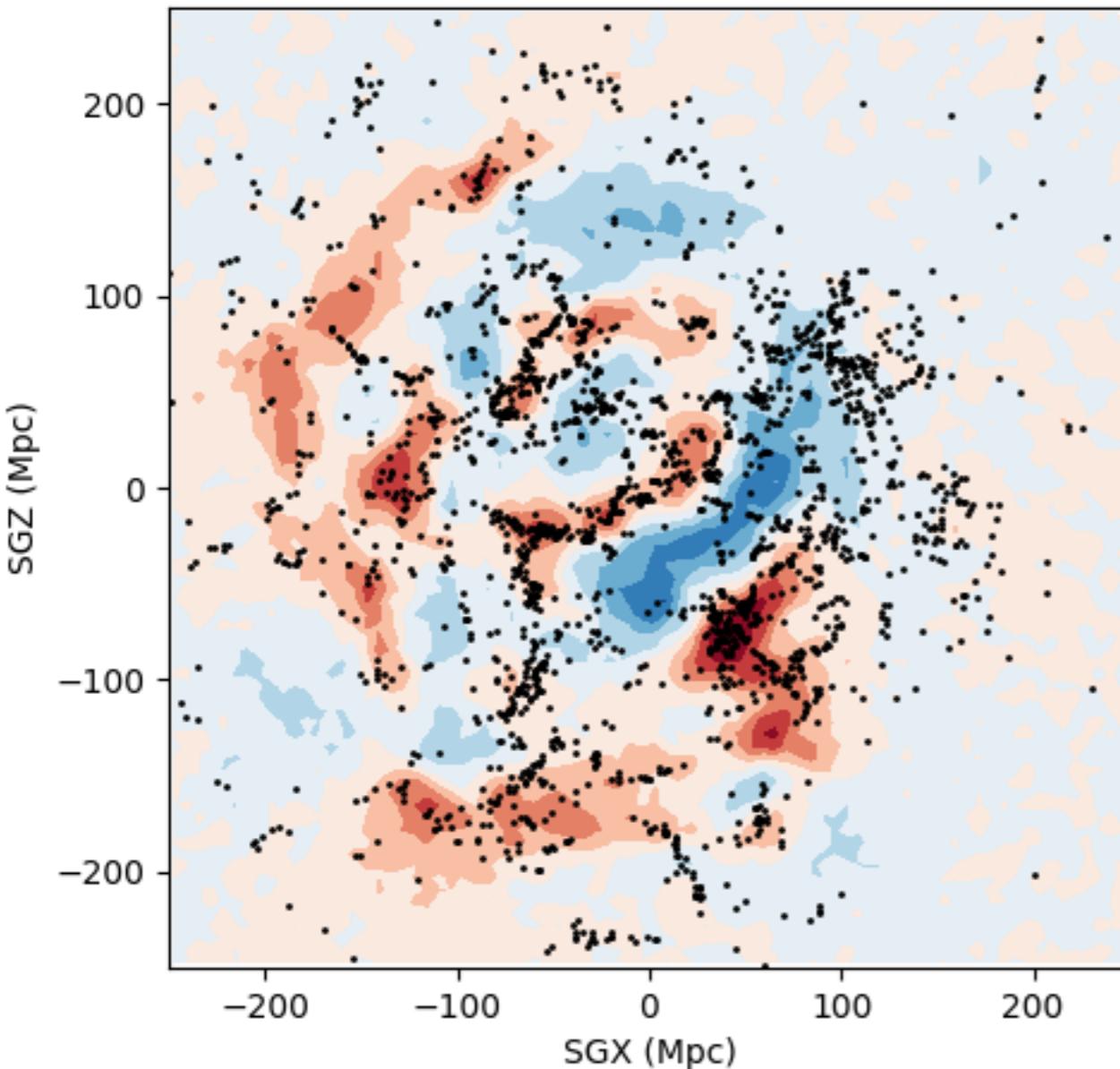
$$n_g = 1 + \delta_g = 1 + b\delta$$

Linear bias

$$\delta = f(\delta^L)?$$

Density model: Non-linear model

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$$n_g = 1 + \delta_g = 1 + b\delta$$

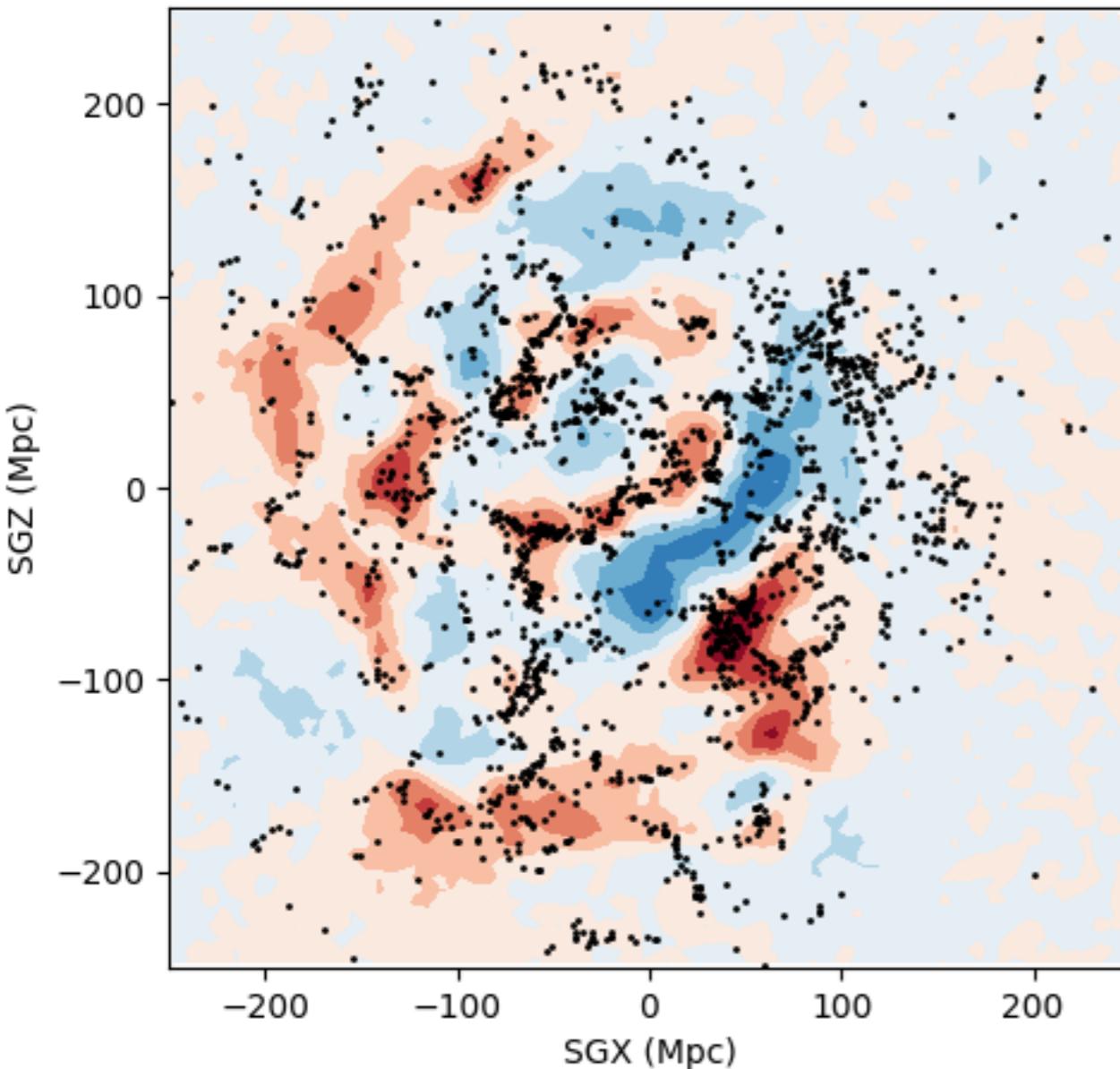
Linear bias

$$\delta = f(\delta^L)?$$

- Eulerian perturbation theory
- Lagrangian perturbation theory
- Effective perturbation theory

Density model: Non-linear model

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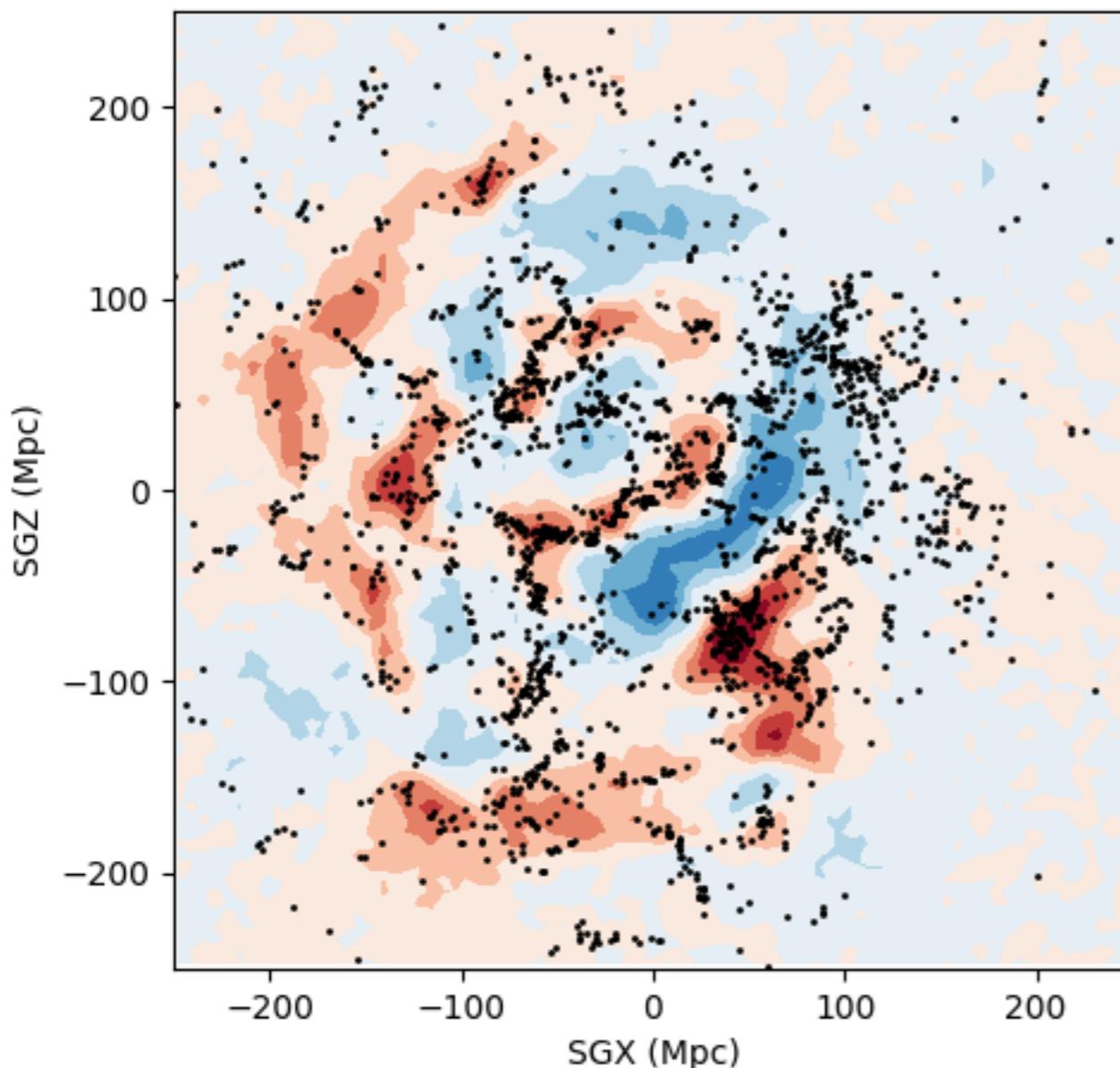
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Density model: Non-linear model

$$\text{Poisson } (\mathcal{O}|\mathbf{r}) \propto n_g(\mathbf{r}) \times e^{-\int n_g(\mathbf{x}) d\mathbf{x}}$$



$$n_g = 1 + \delta_g = 1 + b\delta$$

Linear bias

$$n_g = \exp(b\delta^L)$$

(it is positive)

Hamiltonian sampling

- Draw a momentum for each parameter
- Integrate Hamiltonian equation for the parameters and their momenta
- Accept the state

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Potential : $\psi = -\ln \mathcal{L}$

Hamiltonian : $H = \sum_i \sum_j \frac{1}{2} p_i \mathbf{M}_{ij}^{-1} p_j + \psi$

$$\frac{dx_i}{dt} = \frac{\partial H}{\partial p_i}$$

Hamilton's equation of motion :

$$\frac{dp_i}{dt} = -\frac{\partial \psi}{\partial x_i}$$

Hamiltonian sampling

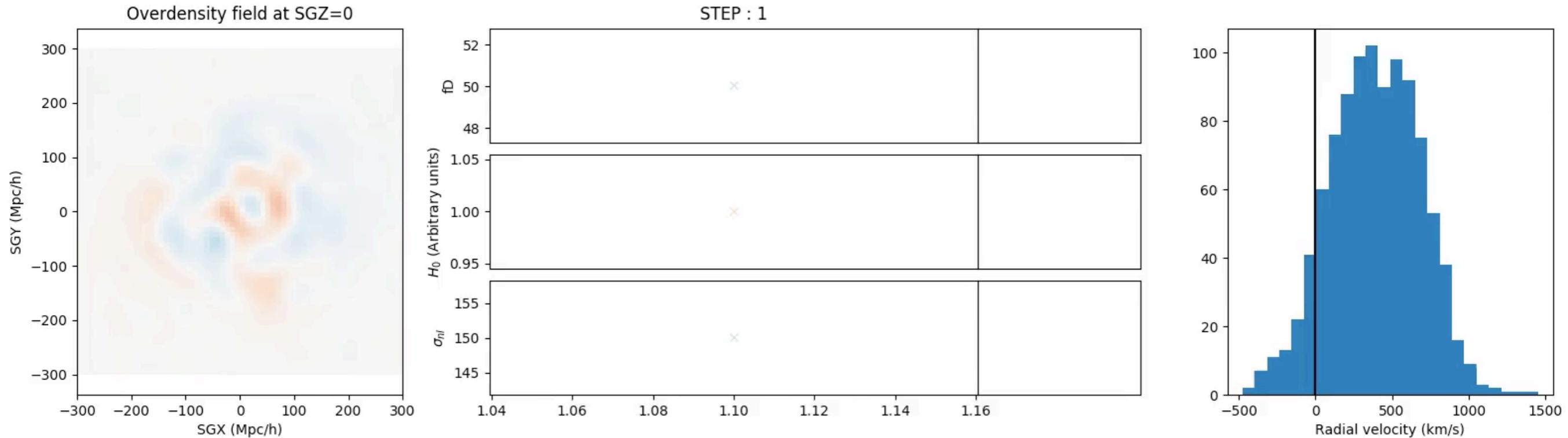
- Draw a momentum for each parameter
- Integrate Hamiltonian equation for the parameters and their momenta
- Accept the state

Pros	Cons
Converges to the solution	Hard to implement
Theoretical acceptance rate of 100%	Need to do math
Efficient for high dimensions and correlated models	

[Link](#)

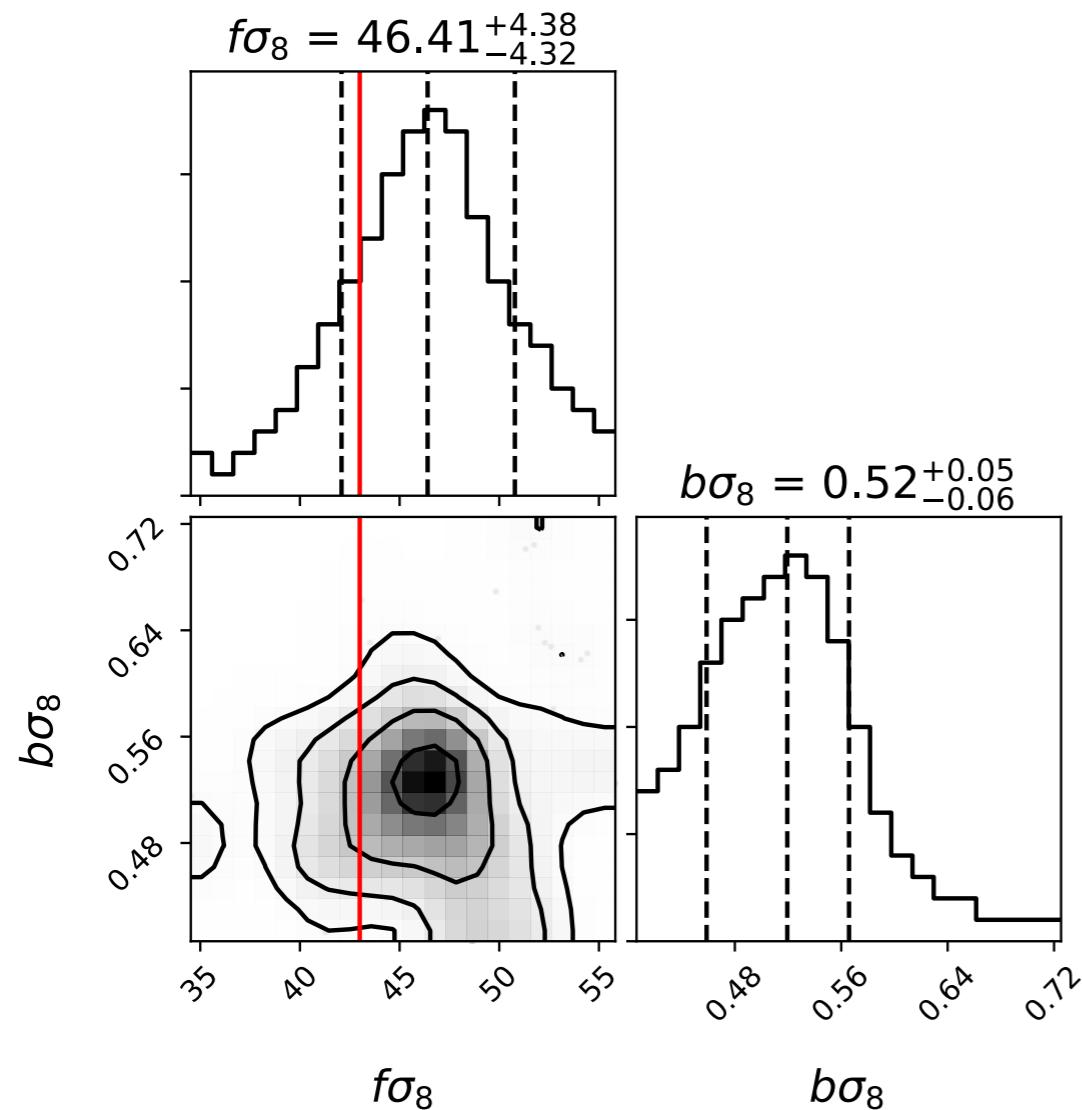
Results on mocks

- Mocks based on DM-only simulation
- 1000 SNe at $z < 0.05$
- Observational uncertainty of 0.1 mag
- Includes LSST angular mask



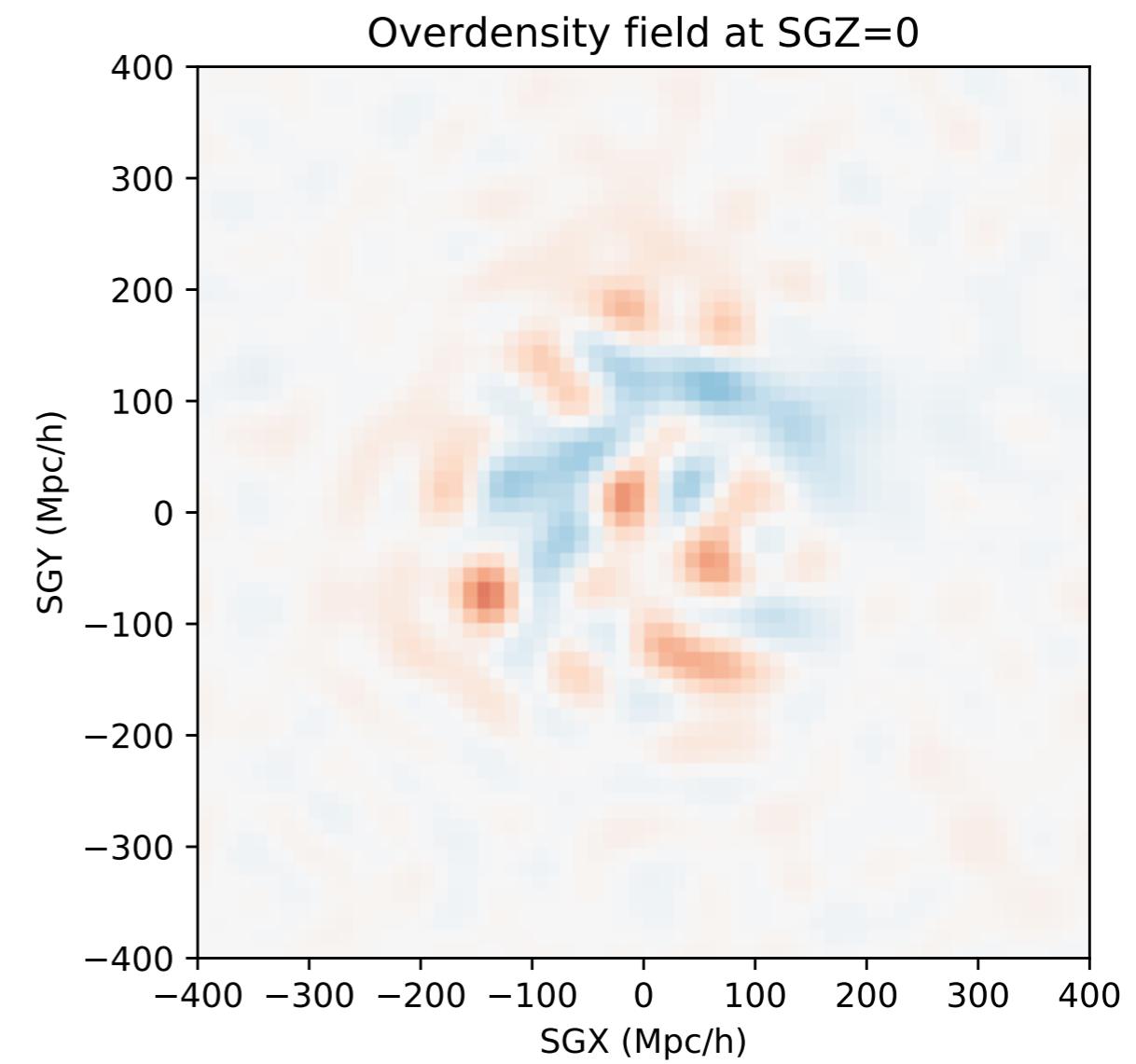
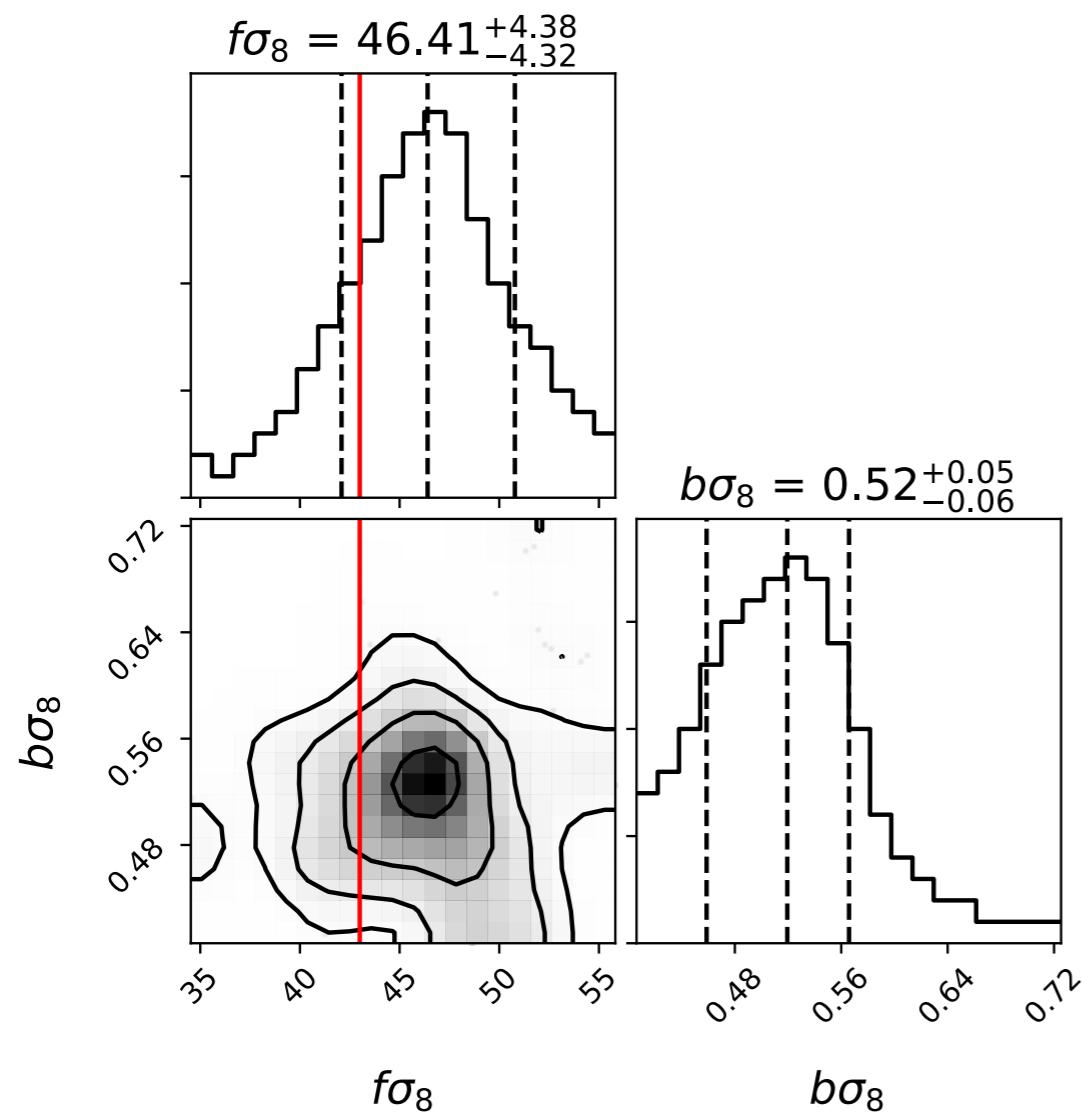
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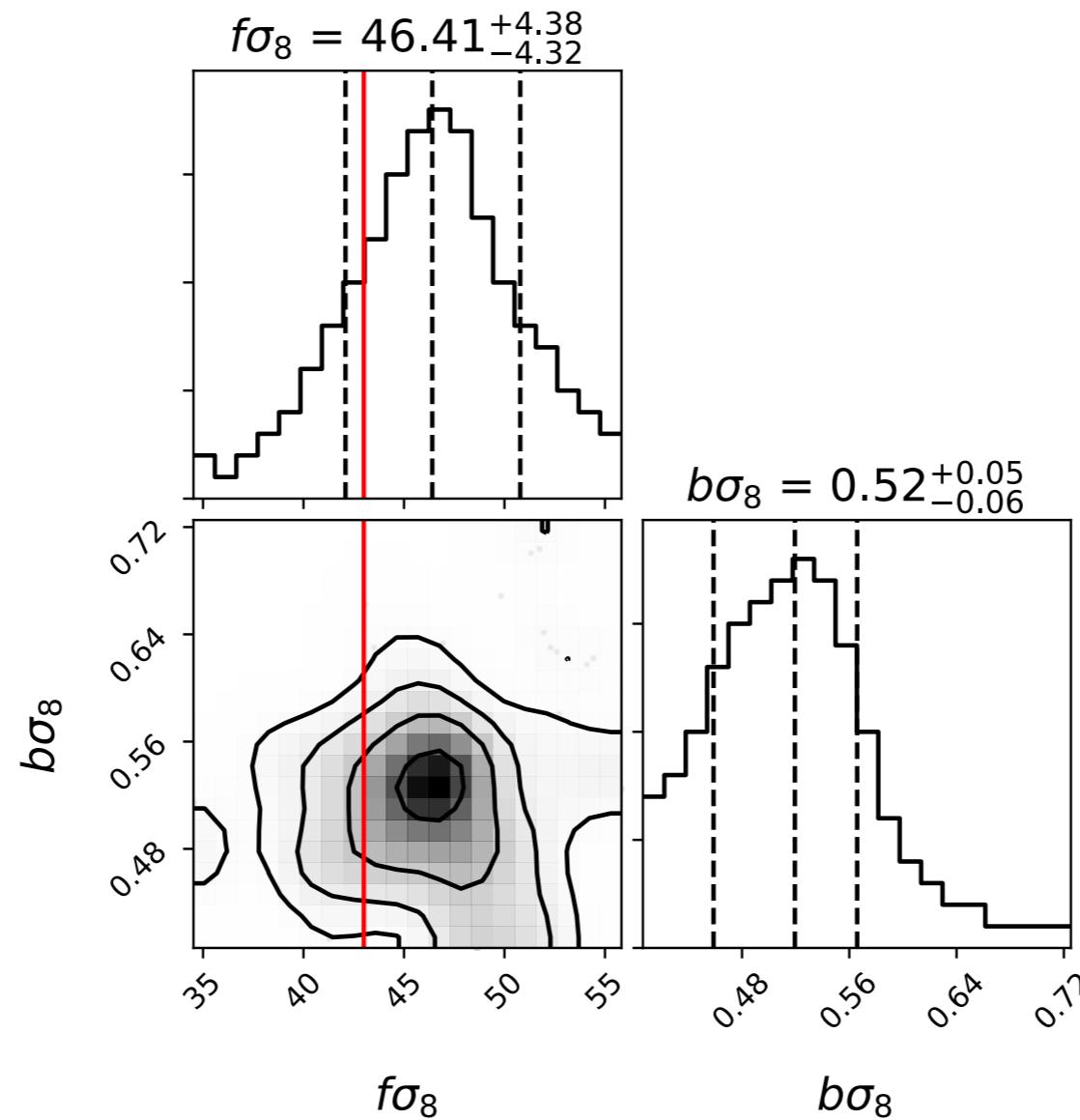
Results on mocks

- Mocks based on DM-only simulation
- 1000 SNe at $z < 0.05$
- Observational uncertainty of 0.1 mag
- Includes LSST angular mask

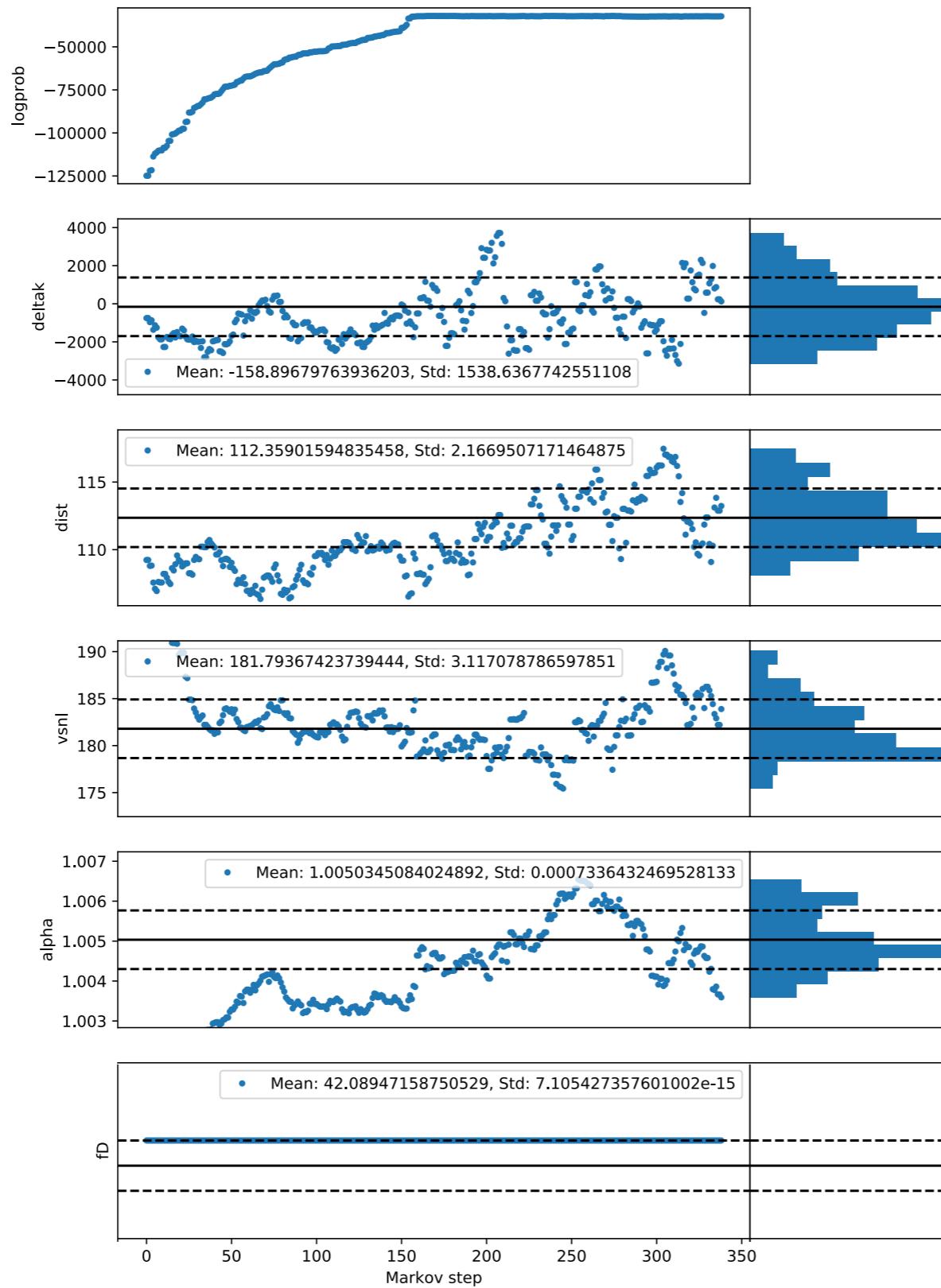


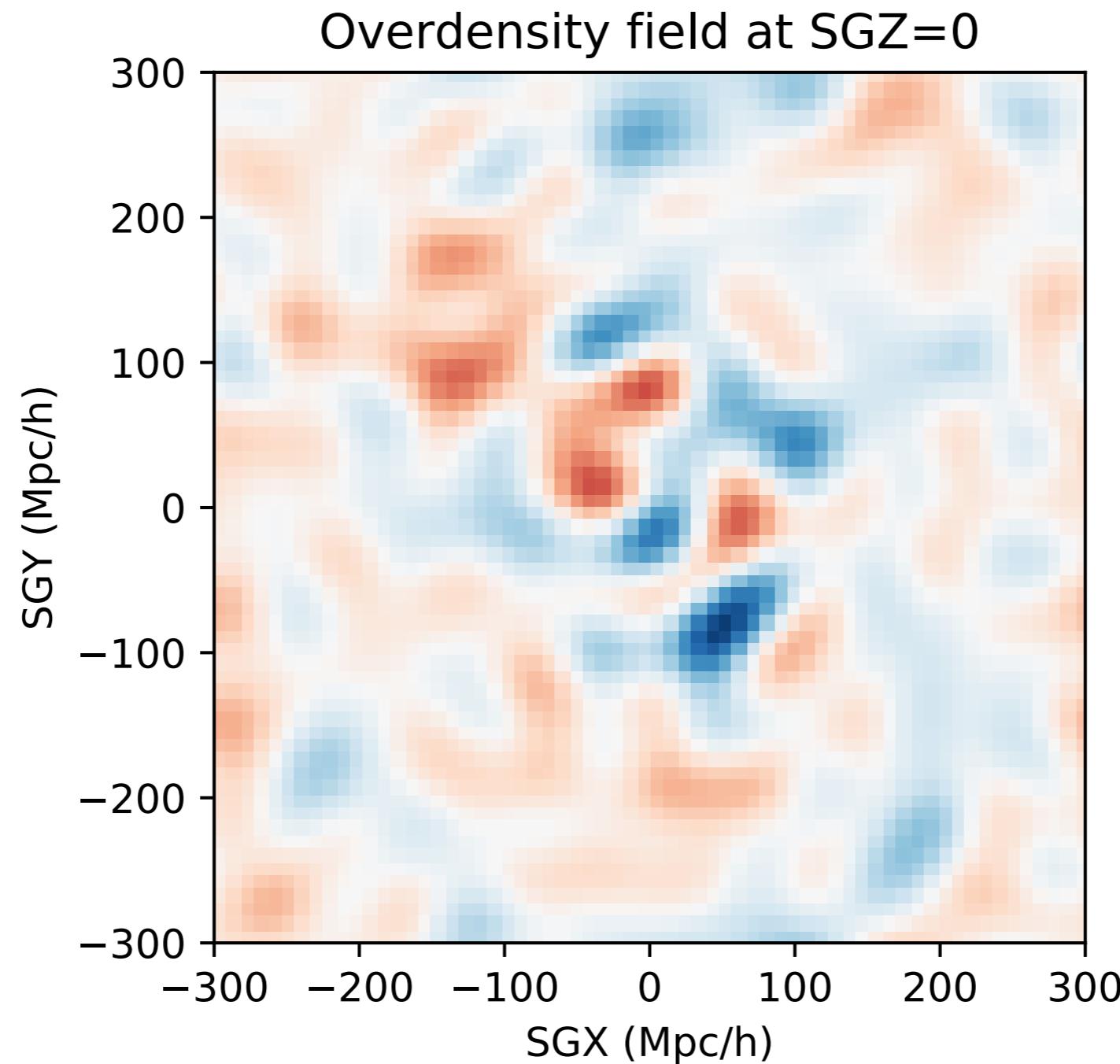
Comments

- Peculiar-velocity only Fisher-Matrix error: 6.3 (15%)
- Algorithm converges in approx. few hours
- Need to know the selection function



CF2





Take home messages

- We can do maps from peculiar velocities
- We can do cosmology from peculiar velocities
- Know your selection effects