

# Gravitational lensing of line intensity maps

*(and a few related topics)*

Simon Foreman

Canadian Institute for Theoretical Astrophysics

*with*

*Alex van Engelen, Daan Meerburg, Joel Meyers*

*based on 1803.04975, 1811.00529*



**CITA**  
**ICAT**

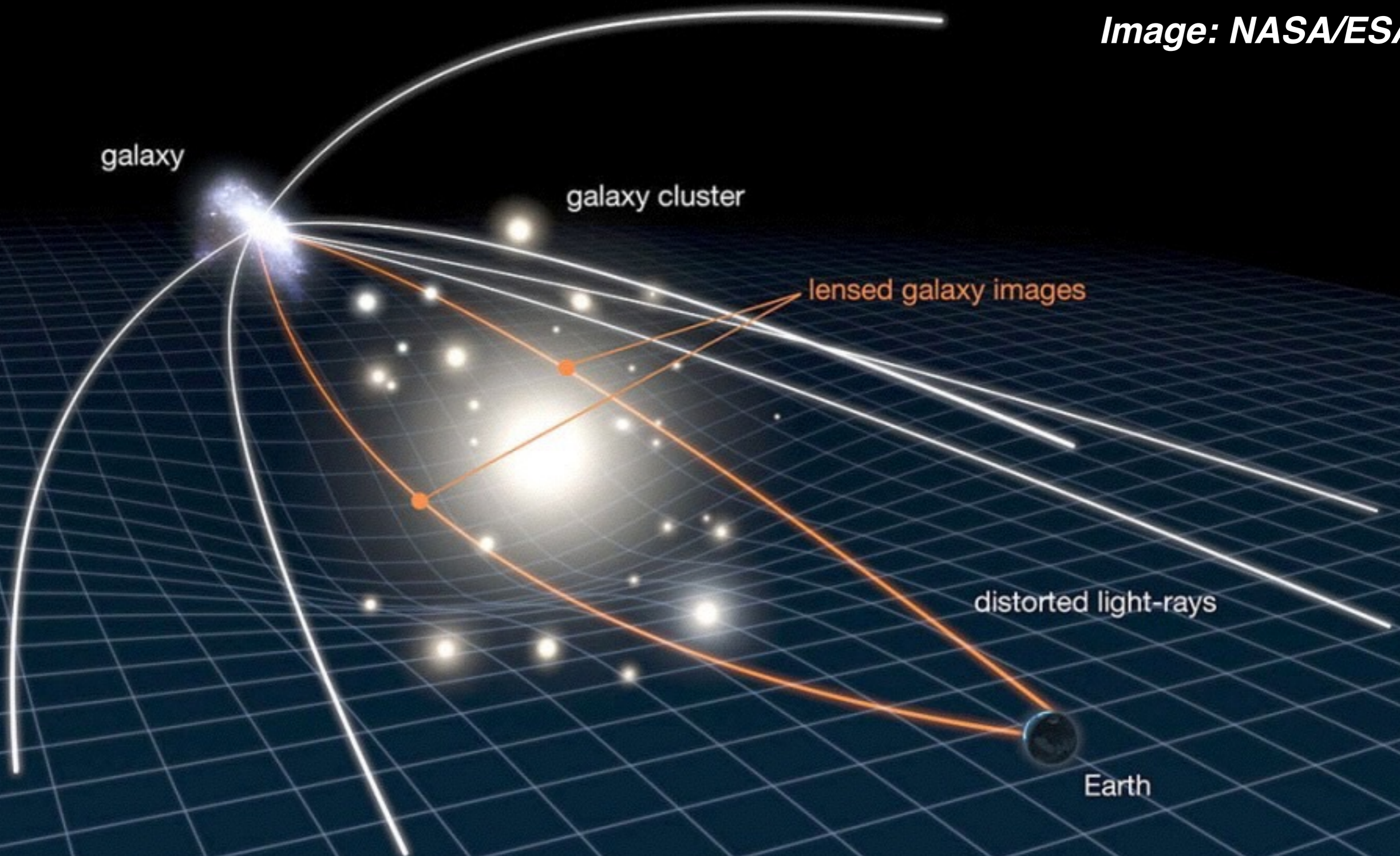
Canadian Institute for  
Theoretical Astrophysics

L'institut Canadien  
d'astrophysique théorique

LBL INPA Seminar  
November 30, 2018

# A cartoon of gravitational lensing

*Image: NASA/ESA*

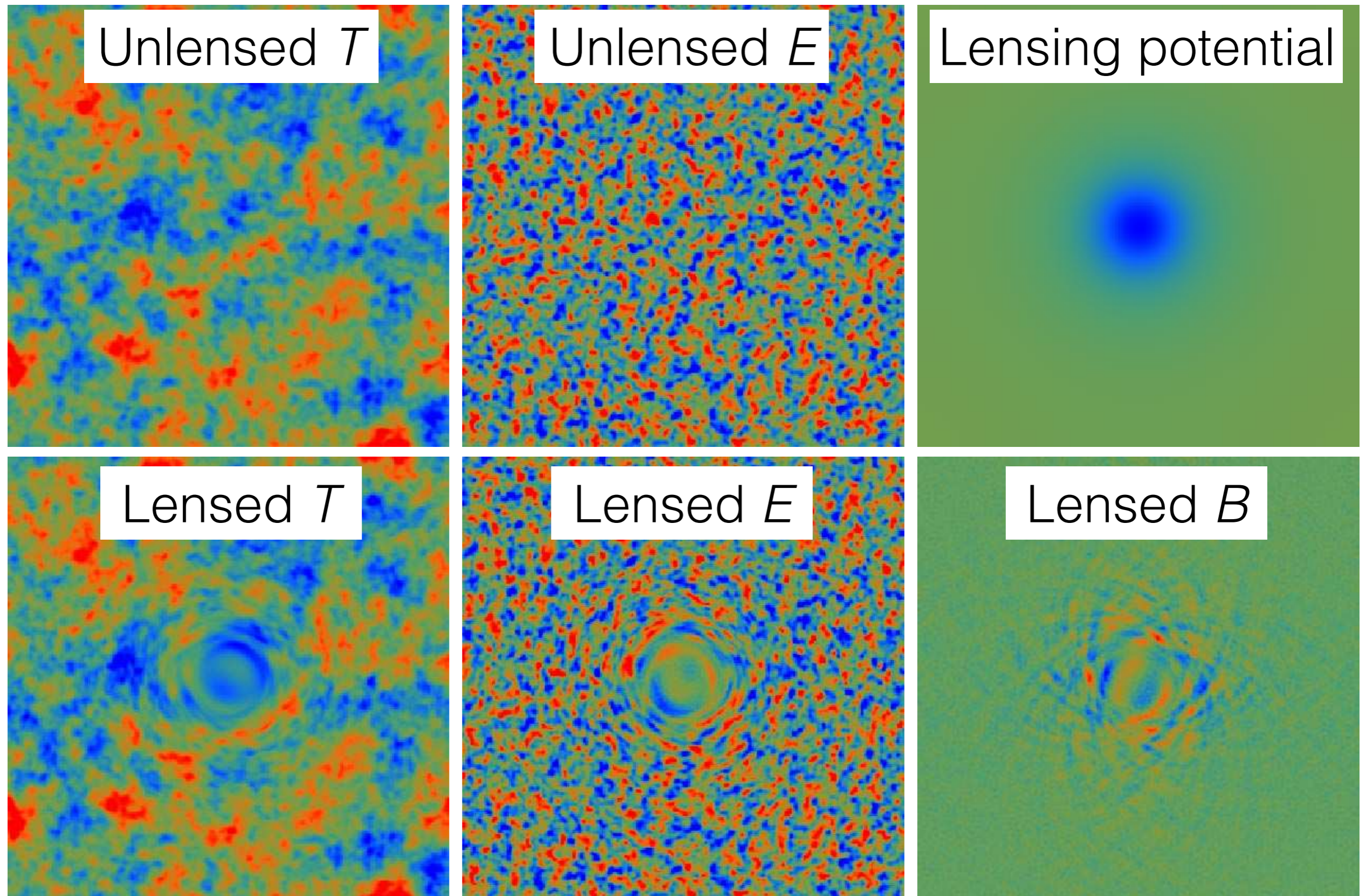


Directly traces low-redshift structure (via Weyl potential)

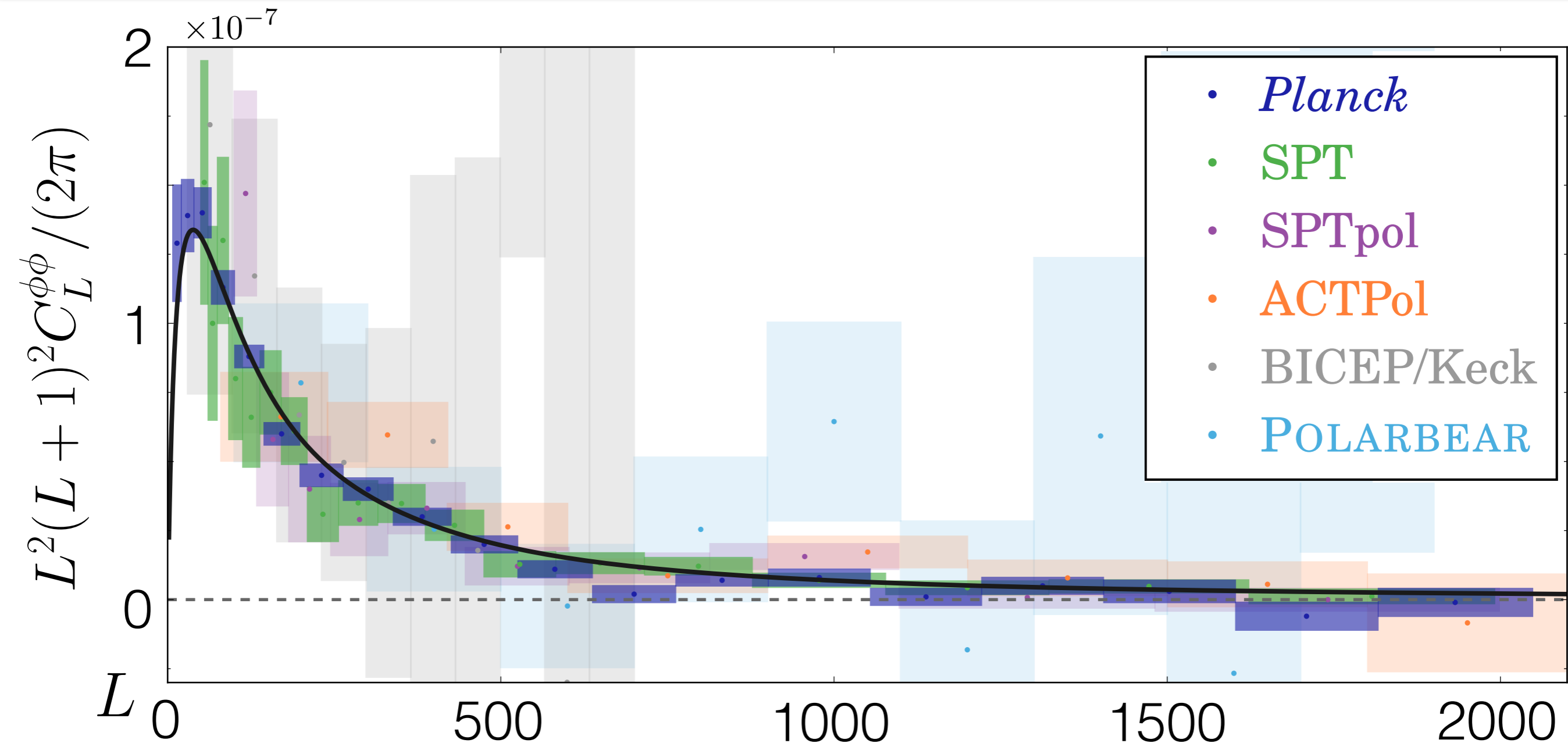


Neutrino masses, structure growth, cross-correlations

## Low angular resolution lensing: CMB



## Low angular resolution lensing: CMB



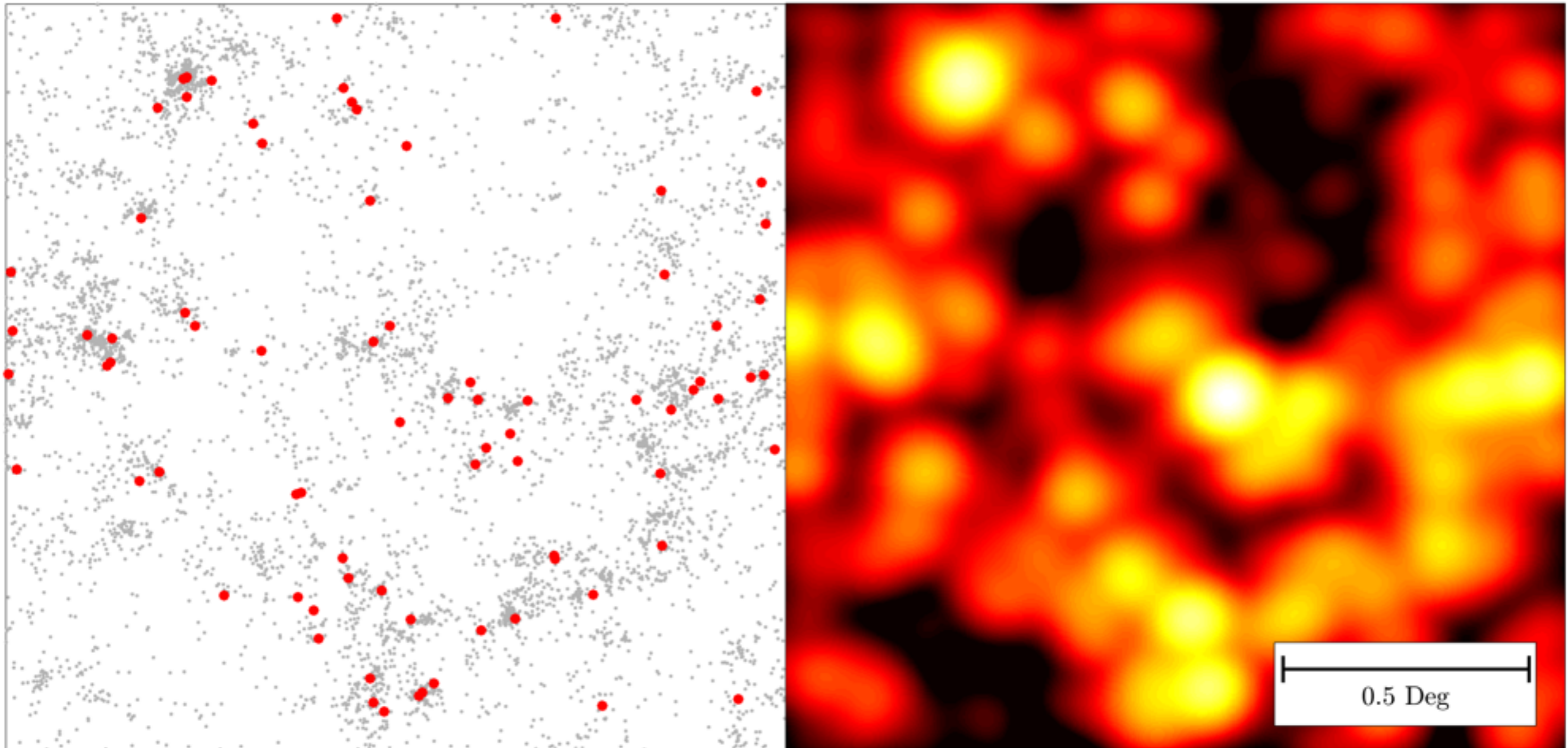
State of the art in CMB lensing:

40 $\sigma$  detection in Planck, 15 $\sigma$  in SPT+Planck, 7.1 $\sigma$  in ACTpol

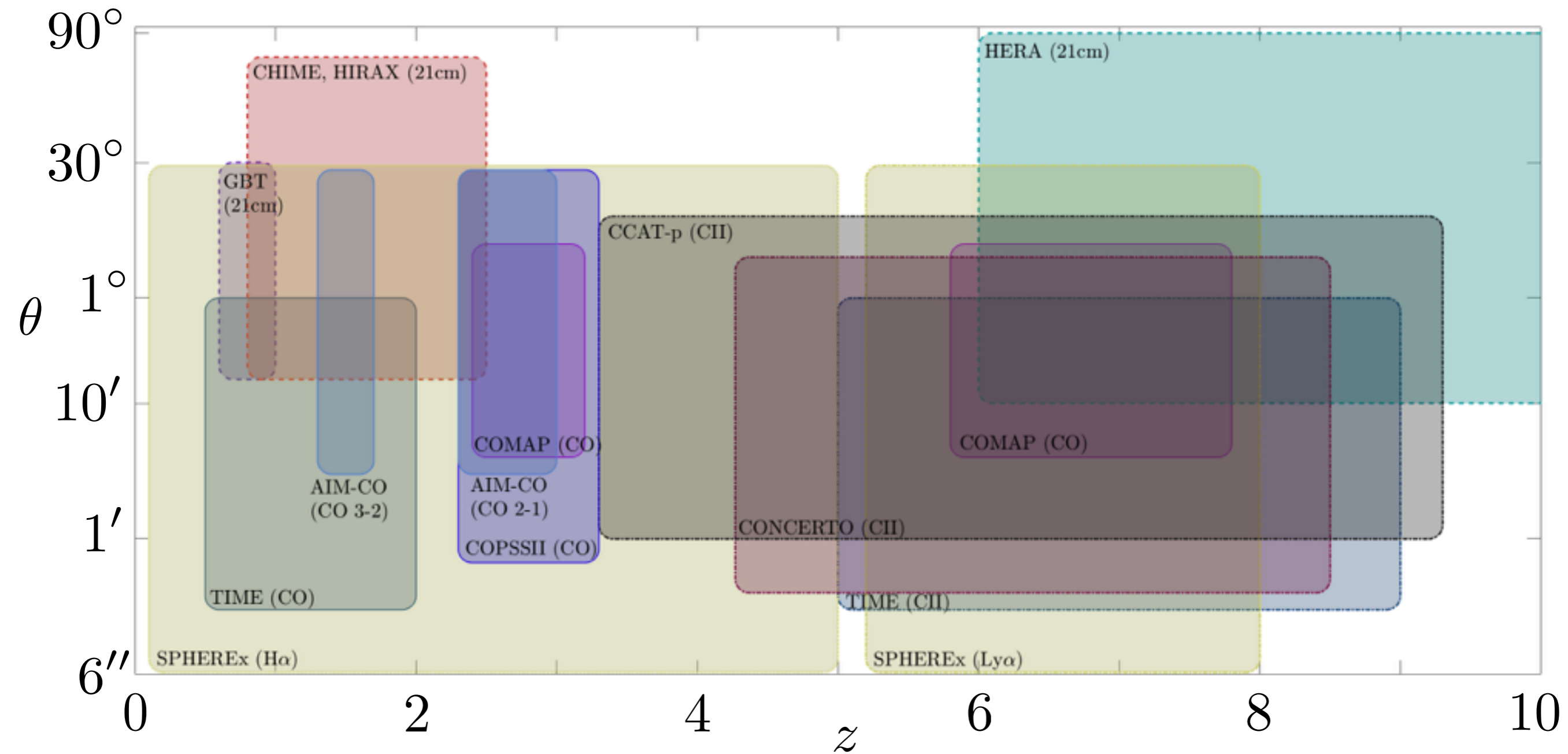
CMB-S4: projected  $\sim 500\sigma$  detection

# Low angular resolution lensing: the future?

Low angular resolution maps can also be made at other wavelengths: “(line) intensity mapping”



## The landscape of line intensity mapping experiments



Observations planned for 21cm, CO, CII, ...

# The promise of lensing reconstruction from intensity maps

Line intensity maps provide many 2d screens for lensing reconstruction

Closely-spaced screens

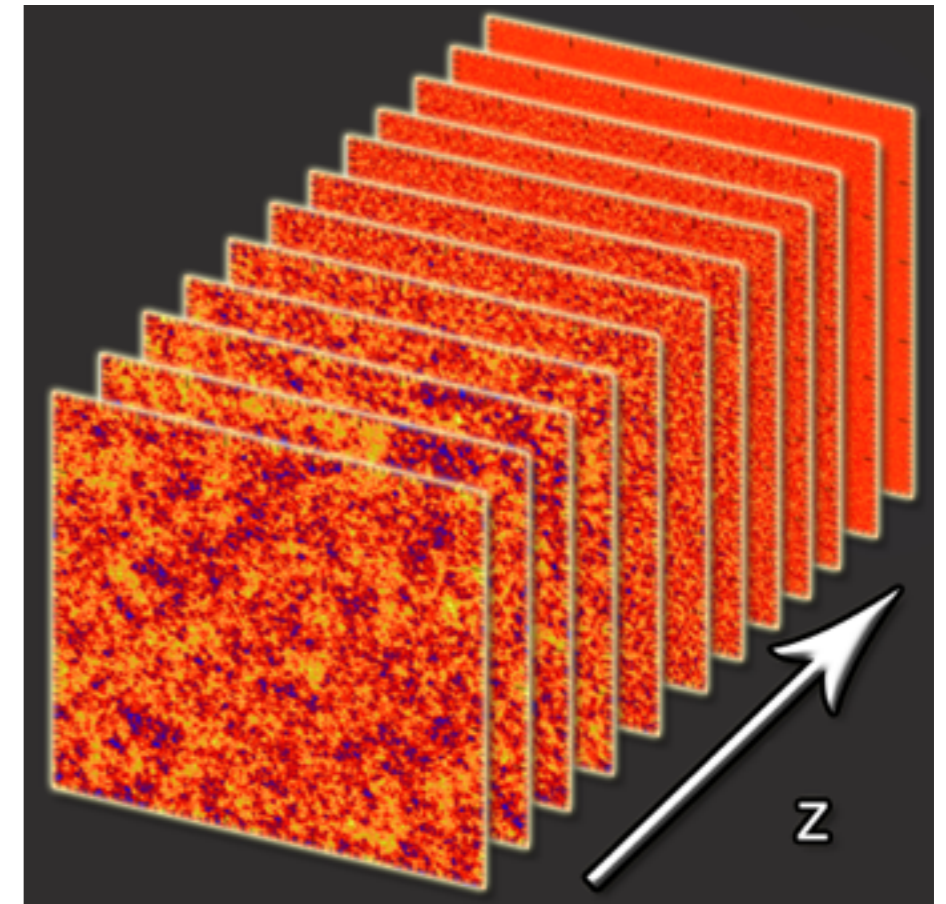
→ potentially high S/N on lensing

Widely-spaced sets of screens

→ different lensing kernels for tomography

Different systematics than CMB or galaxy lensing

Understanding a contaminant for e.g. nG constraints



*figure: Romeo et al. 2017*

# Outline

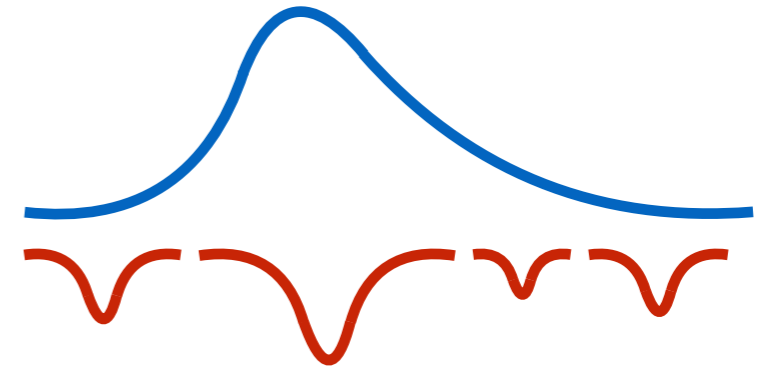
1. How CMB lensing is measured
2. Extension of method to 3d
  - *impact of gravitational nonlinearities*
3. Reducing gravitational effects in variance:  
“bias-hardening”
4. Forecasts
5. \*\* Recent work: CMB temperature reconstruction



## Review of CMB lensing

*Lensing potential*: projection of gravitational potentials

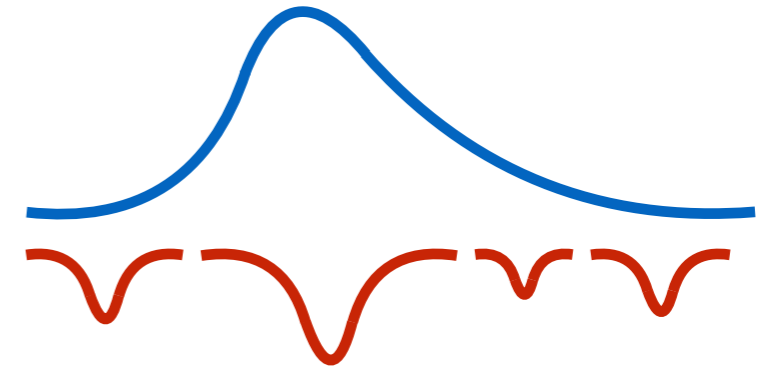
$$\phi \sim \int_0^{\chi_s} d\chi W(\chi) \Phi(\chi \hat{n}, z[\chi])$$



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$$\phi \sim \int_0^{\chi_s} d\chi W(\chi) \Phi(\chi \hat{n}, z[\chi])$$



Unlensed CMB: different Fourier modes are uncorrelated

$$\langle T(\vec{\ell}_1) T^*(\vec{\ell}_2) \rangle = (2\pi)^2 \delta_D(\vec{\ell}_1 - \vec{\ell}_2) C_{\ell_1}^{(\text{unlensed})}$$

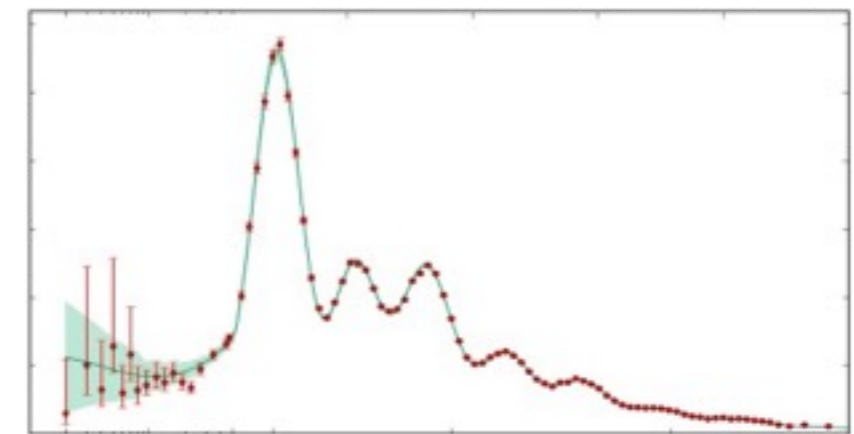
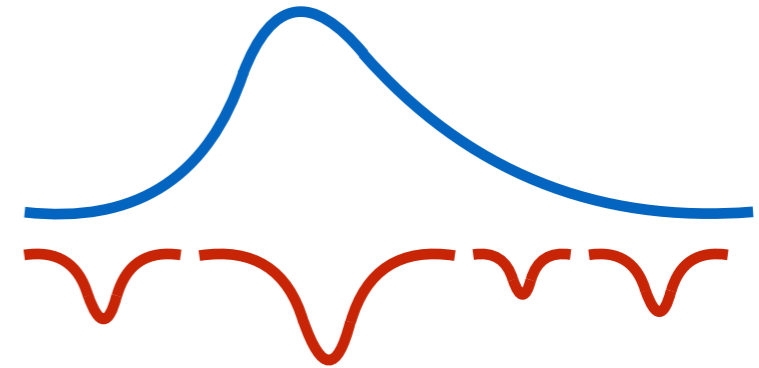


figure: ESA

## Review of CMB lensing

*Lensing potential*: projection of gravitational potentials

$$\phi \sim \int_0^{\chi_s} d\chi W(\chi) \Phi(\chi \hat{n}, z[\chi])$$



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$$\begin{aligned} \langle T(\vec{\ell}_1) T^*(\vec{\ell}_2) \rangle &= (2\pi)^2 \delta_{\text{D}}(\vec{\ell}_1 - \vec{\ell}_2) C_{\ell_1}^{(\text{unlensed})} \\ &+ f(\vec{\ell}_1, \vec{\ell}_2) \phi(\vec{\ell}_1 - \vec{\ell}_2) \end{aligned}$$

Lensed CMB: different Fourier modes become correlated

## Review of CMB lensing

Can use this correlation to construct an *estimator* for  $\phi$ :

$$\hat{\phi}_{\vec{\ell}}(\vec{L}) = \frac{T(\vec{\ell})T^*(\vec{\ell} - \vec{L})}{f(\vec{\ell}, \vec{\ell} - \vec{L})}$$

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Can do better by inverse-variance weighting:

$$\hat{\phi}(\vec{L}) = N_L \sum_{\vec{\ell}} \frac{\hat{\phi}_{\vec{\ell}}(\vec{L})}{\text{Var} [\hat{\phi}_{\vec{\ell}}(\vec{L})]}$$

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Power spectrum of reconstructed  $\phi$  map:

$$\langle \hat{\phi}(\vec{L}) \hat{\phi}^*(\vec{L}) \rangle = C_L^{\phi\phi} + N_L + \dots$$

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Power spectrum of reconstructed  $\phi$  map:

$$\langle \hat{\phi}(\vec{L})\hat{\phi}^*(\vec{L}) \rangle = \underbrace{C_L^{\phi\phi}}_{\text{Gaussian}} + \underbrace{N_L}_{\text{non-Gaussian}} + \dots$$

$$\left( \langle \hat{\phi}\hat{\phi} \rangle \sim \langle TTTT \rangle \sim \underbrace{\langle TT \rangle^2}_{\text{Gaussian}} + \underbrace{\langle TTTT \rangle_c}_{\text{non-Gaussian}} \right)$$

# Outline

1. How CMB lensing is measured
  - *exploits mode-couplings induced by lensing*
  - *connected 4-pt function  $\rightarrow$  lensing potential power spectrum*
- 2. Extension of method to 3d**
3. Reducing gravitational effects in variance:  
“bias-hardening”
4. Forecasts



## Observations in 3d

3d intensity field, observed within comoving thickness  $\mathcal{L}$ :

$$I(\vec{x}_\perp, x_\parallel) \longrightarrow I(\vec{\ell}, k_\parallel), \quad k_\parallel = \frac{2\pi}{\mathcal{L}} j, \quad j = 0, 1, 2, \dots$$

Angular power spectrum  
for given  $j$ :

$$C_\ell(k_\parallel) \propto P_I \left( \sqrt{\ell^2 / \chi^2 + k_\parallel^2} \right)$$

(Easier to account for  
correlations this way)

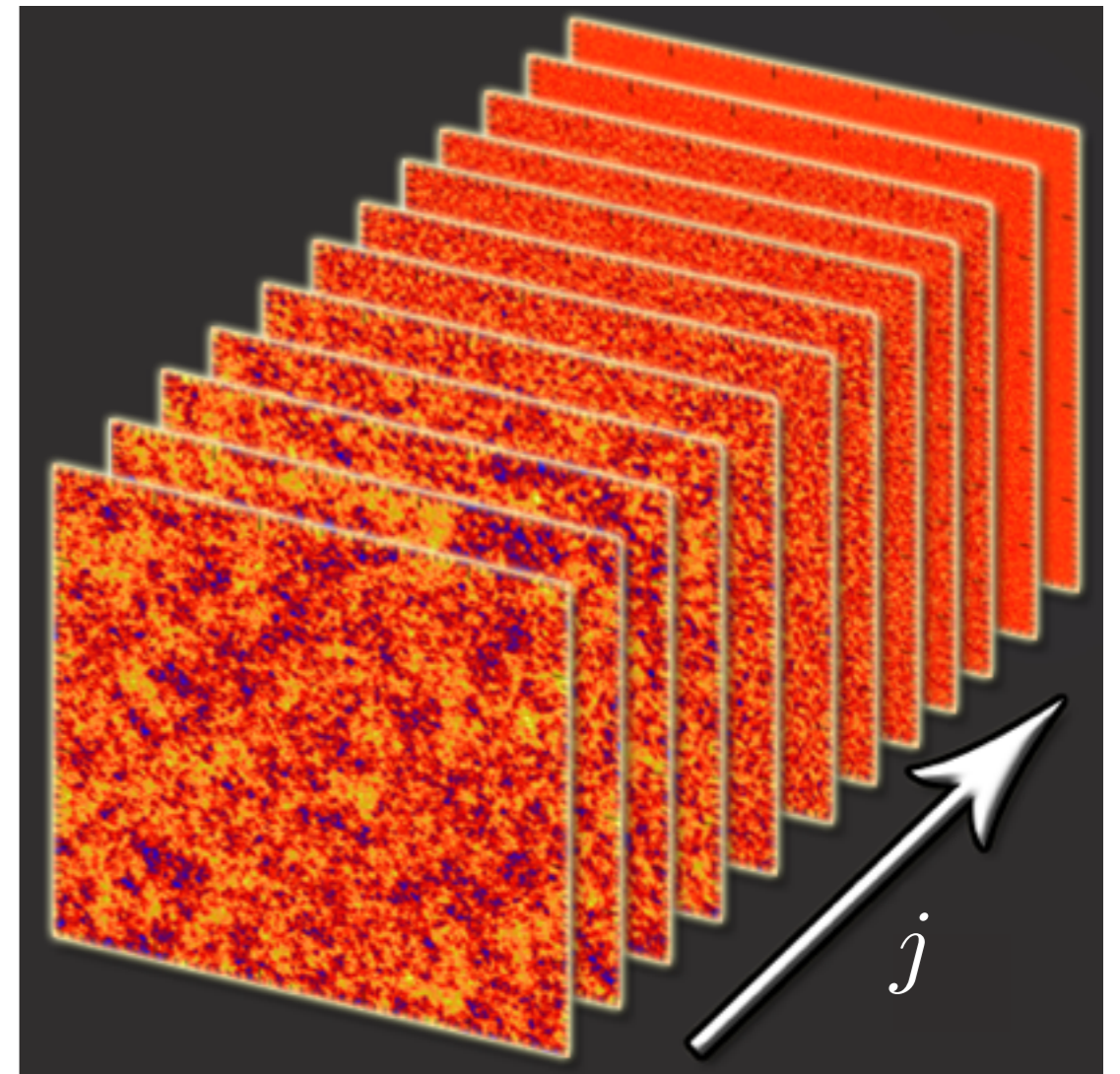
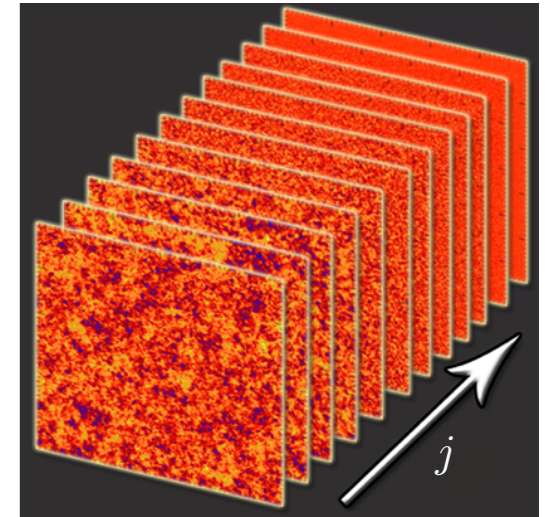


figure: Romeo et al. 2017

## 3d lensing estimator

Can construct estimator for each  $j$ :

$$\hat{\phi}(\vec{L}, k_{\parallel}) = N_{\phi\phi}(L, k_{\parallel}) \times \int_{\vec{\ell}} g(\vec{\ell}, \vec{L} - \vec{\ell}) I(\vec{\ell}, k_{\parallel}) I(\vec{L} - \vec{\ell}, -k_{\parallel})$$



Power spectra of reconstructed  $\phi$  maps:

$$\langle \hat{\phi}(\vec{L}, k_{\parallel}) \hat{\phi}^*(\vec{L}, k_{\parallel}) \rangle = C_L^{\phi\phi} + N_{\phi\phi}(\vec{L}, k_{\parallel}) + \dots$$

Can coadd  $j$ 's to reduce noise in maps:

$$\longrightarrow \text{Var}[\hat{\phi}(\vec{L})] = \frac{1}{\sum_j N_{\phi\phi}^{-1}(L, k_{\parallel})} \sim \frac{1}{j_{\max}} N_{\phi\phi}$$

However, we missed an important contribution!

$$\left\langle \hat{\phi}(\vec{L}, k_{||1}) \hat{\phi}^*(\vec{L}, k_{||2}) \right\rangle$$

**2-pt function of  $\hat{\phi}$**

$$\sim \int_{\vec{\ell}_1} \int_{\vec{\ell}_2} (\dots)(\dots) \langle IIII^* I^* \rangle$$

**4-pt function of  $I$**

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**4-pt function of  $I$**

$$\sim \delta_{k_{\parallel 1}, k_{\parallel 2}} N_{\phi\phi}(L, k_{\parallel 1})$$

**disconnected 4-pt**

$$+ C_L^{\phi\phi}$$

**connected 4-pt from lensing**

However, we missed an important contribution!

$$\left\langle \hat{\phi}(\vec{L}, k_{\parallel 1}) \hat{\phi}^*(\vec{L}, k_{\parallel 2}) \right\rangle$$

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**disconnected 4-pt**

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**connected 4-pt from lensing**

$$+ \int_{\vec{\ell}_1} \int_{\vec{\ell}_2} (\dots)(\dots) \left\langle \tilde{I}\tilde{I}\tilde{I}^* \tilde{I}^* \right\rangle_c$$

**connected 4-pt of unlensed field**

---

If  $I$  traces  $\delta_{\text{matter}}$ ,  $\left\langle \tilde{I}\tilde{I}\tilde{I}^* \tilde{I}^* \right\rangle_c \sim \langle \delta\delta\delta\delta \rangle_{c, \text{gravity}}$

# Quantifying the gravitational contribution

**Main goal:** quantify impact of gravitational contributions  
 (  $\langle \delta\delta\delta\delta \rangle_{c,gravity}$  ) on lensing estimator

## Assumptions (21cm):

$\tilde{I} \sim b \delta_{\text{matter}}$  (linearly biased tracer)

tree-level perturbation theory for grav. 4-pt. function

instrumental noise = thermal noise, set by  $T_{\text{sys}}$ ,  $n_{\text{base}}$ , ...

foregrounds kill modes with low  $k_{\parallel}$

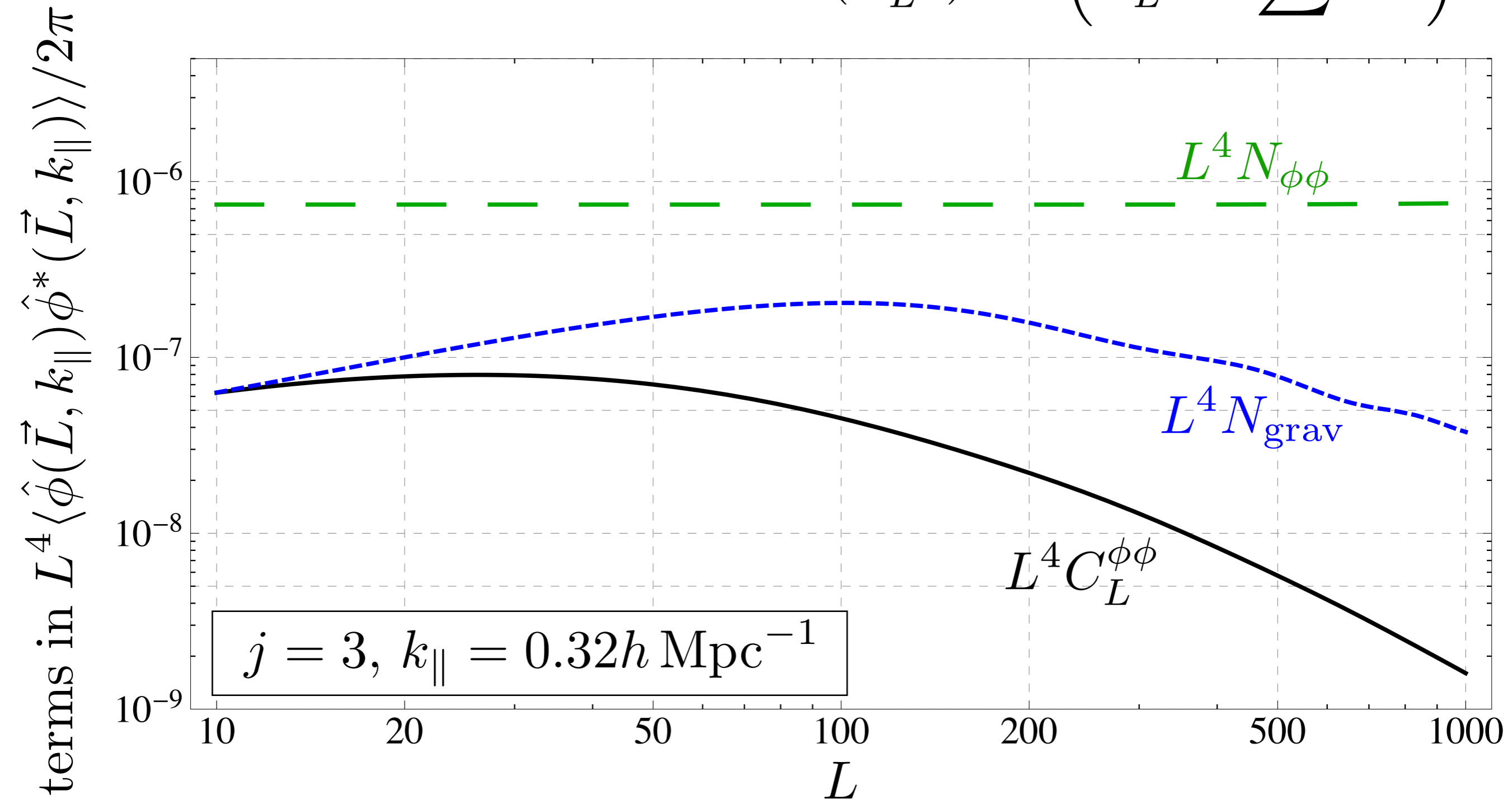
can cross-correlate with  $\sim$ LSST

Lensing estimator for single  $k_{\parallel}$ 

$N...$  terms add both  
*bias* and *noise* to  $C_L^{\phi\phi}$

$$\langle \hat{\phi} \hat{\phi}^* \rangle \propto C_L^{\phi\phi} + \sum N...$$

$$\sigma(\hat{C}_L^{\phi\phi})^2 \propto \left( C_L^{\phi\phi} + \sum N... \right)$$

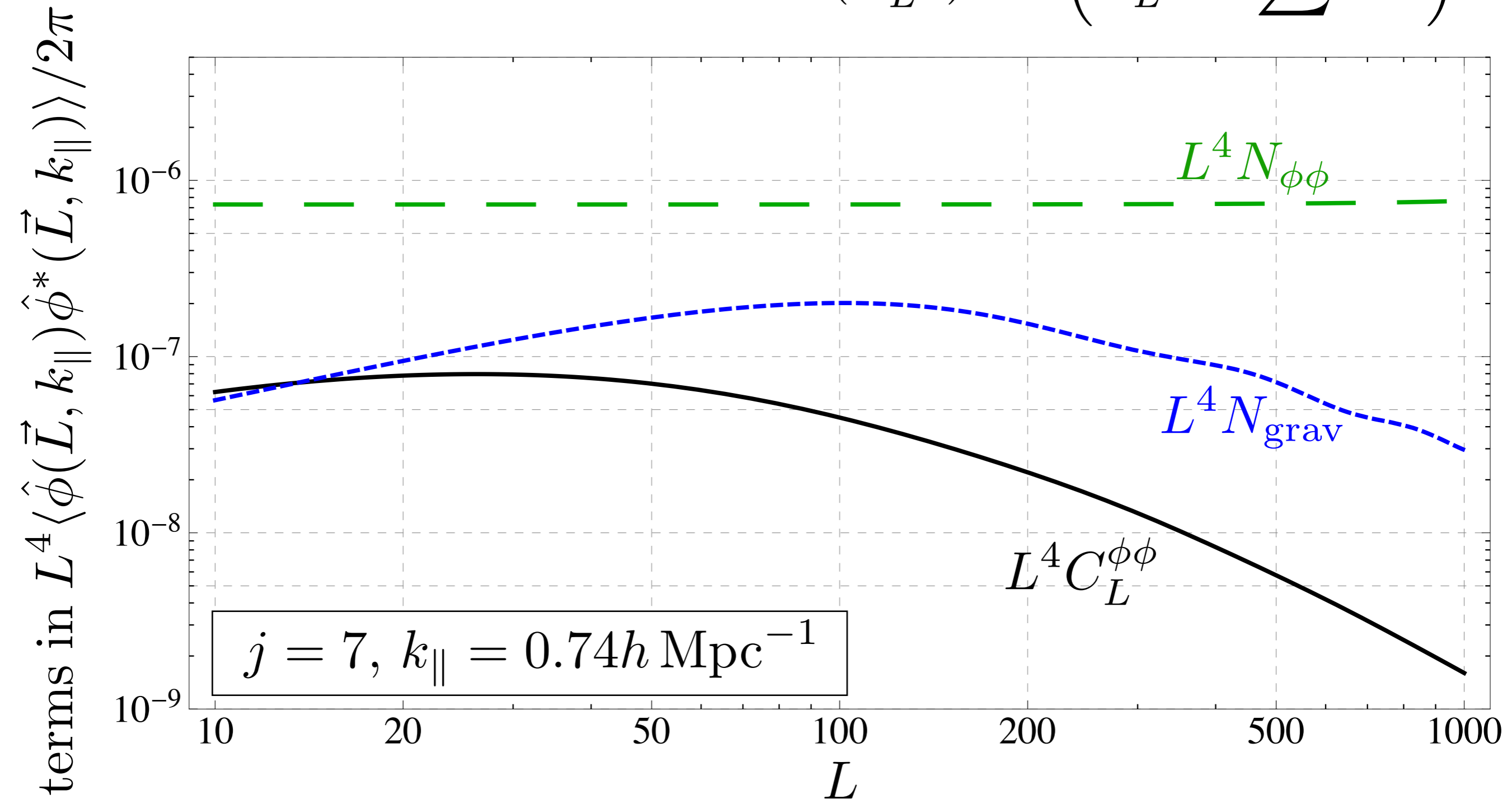


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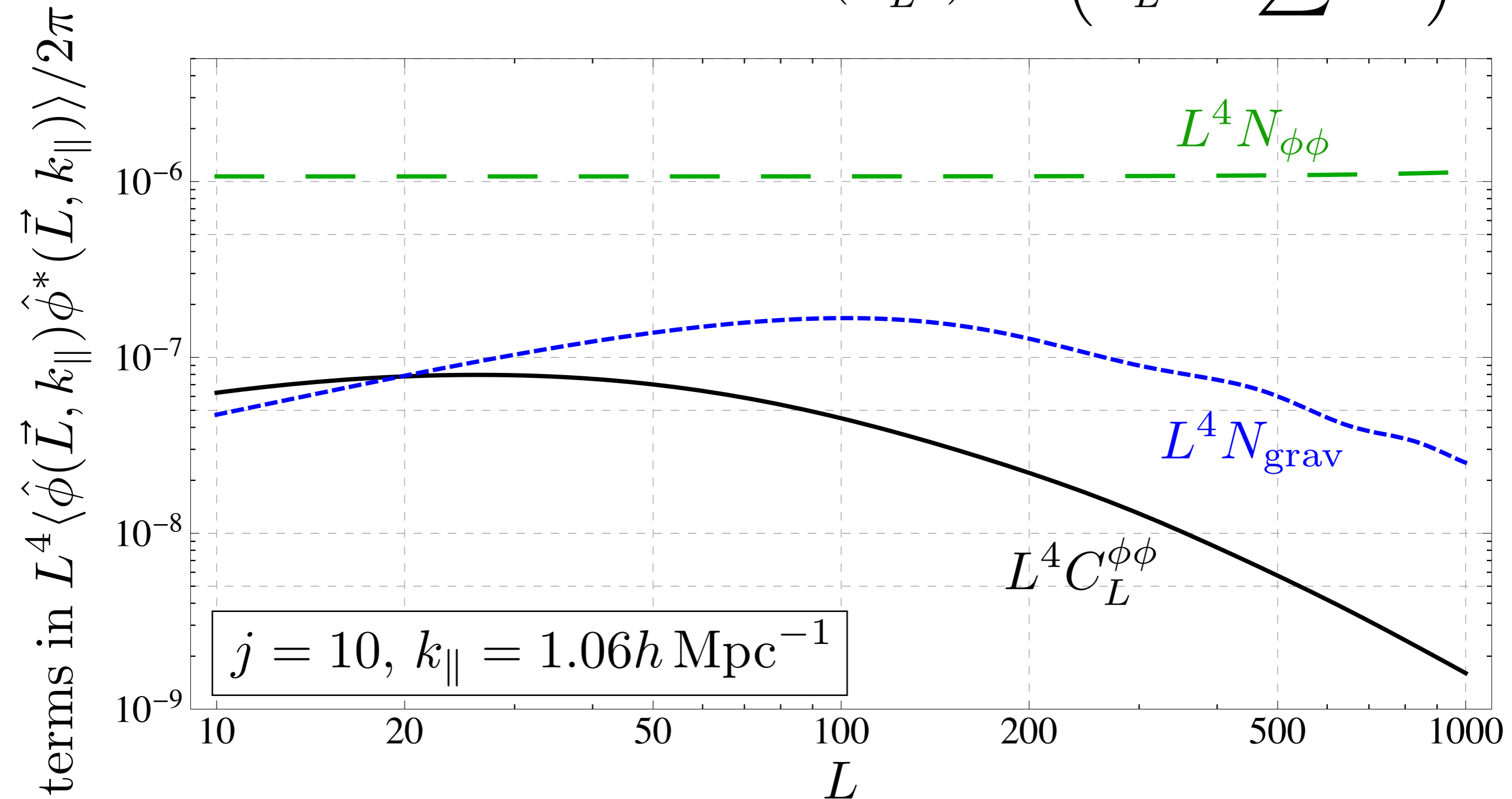


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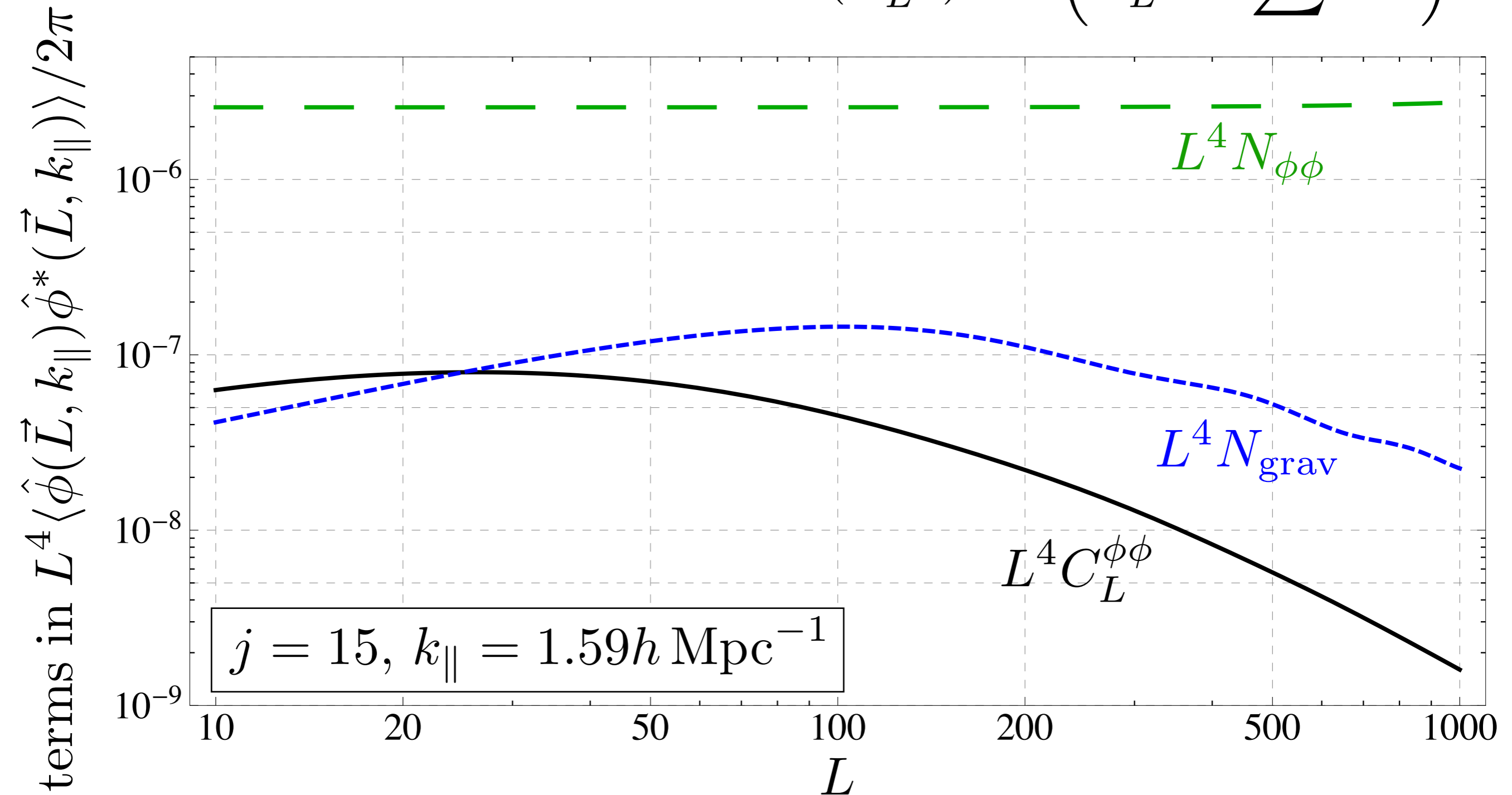


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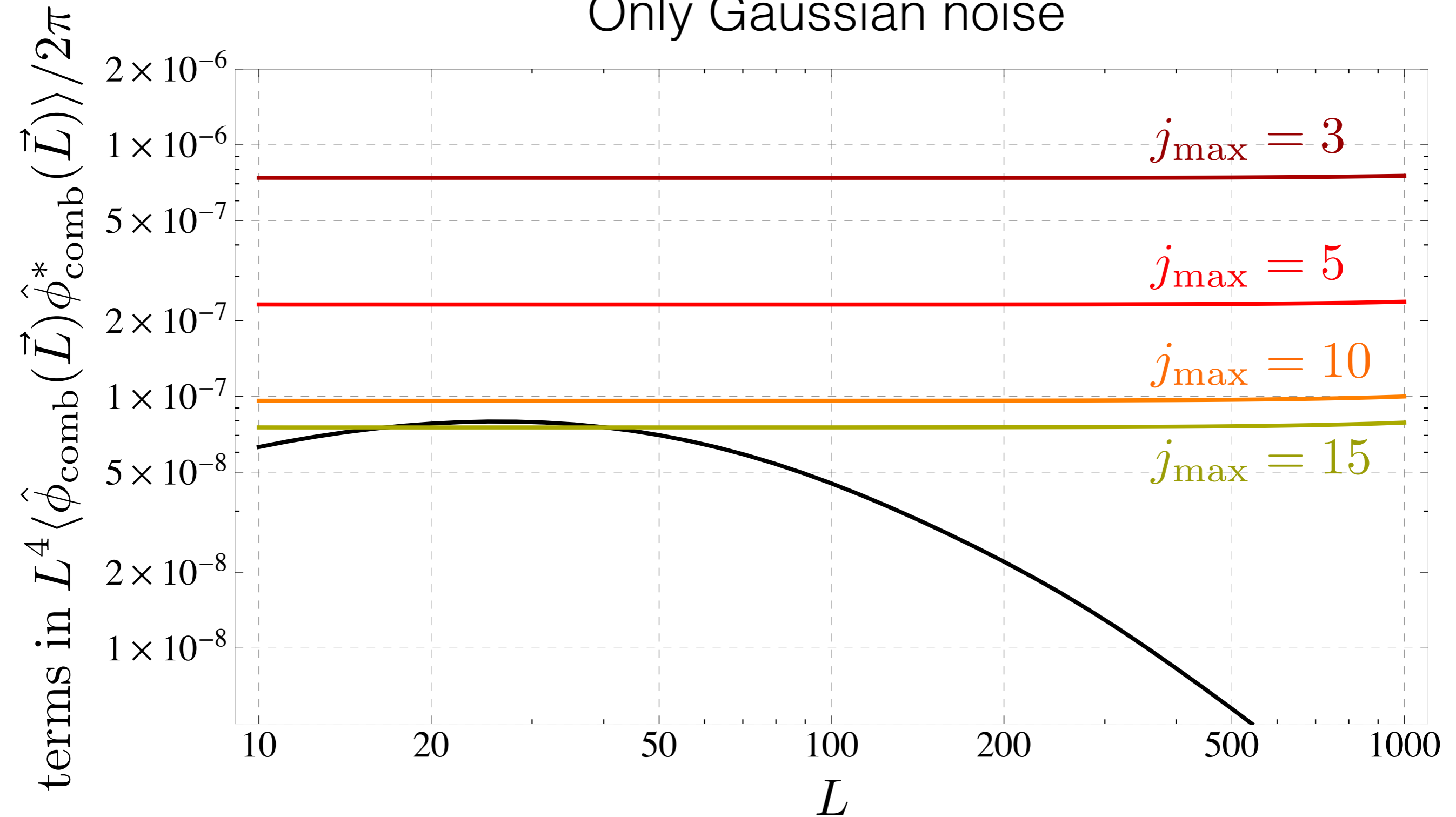
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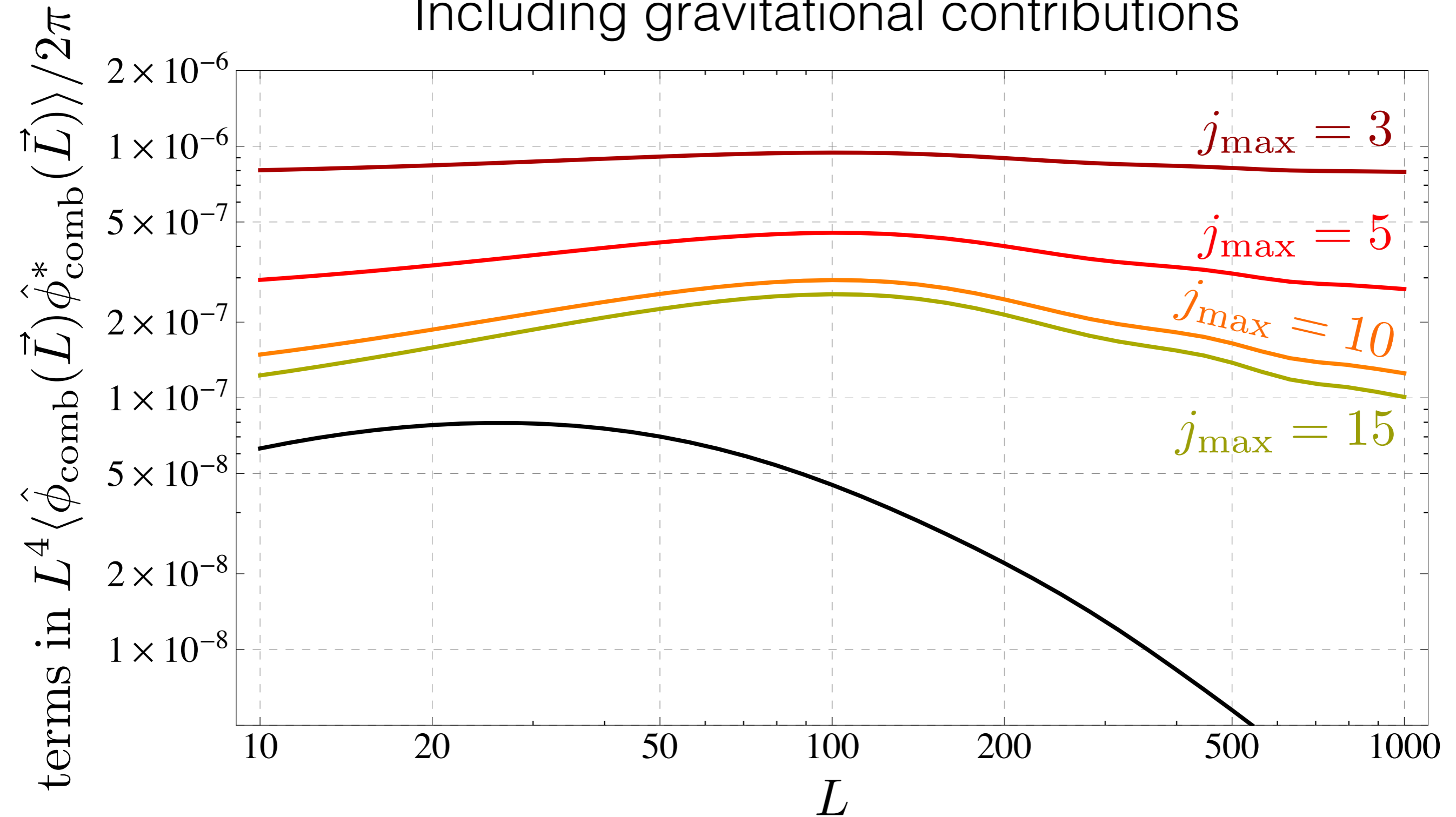
Lensing estimator, combining signal from several  $j$ 's

Only Gaussian noise



Lensing estimator, combining signal from several  $j$ 's

Including gravitational contributions



# Outline

1. How CMB lensing is measured
  - *exploits mode-couplings induced by lensing*
  - *connected 4-pt function  $\rightarrow$  lensing potential power spectrum*
2. Extension of method to 3d
  - *apply 2d estimator to maps with different  $k_{\parallel}$  values*
  - *gravity adds noise, that is correlated between  $k_{\parallel}$ s*
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## Lensing and gravity both induce mode-coupling

Unlensed intensity: different Fourier modes are uncorrelated

$$\left\langle I(\vec{\ell}_1, k_{\parallel}) I^*(\vec{\ell}_2, -k_{\parallel}) \right\rangle = (2\pi)^2 \delta_{\text{D}}(\vec{\ell}_1 - \vec{\ell}_2) C_{\ell}^{(\text{unlensed})}(k_{\parallel})$$

$$+ \underline{f_{\phi}(\vec{\ell}_1, \vec{\ell}_2) \phi(\vec{\ell}_1 - \vec{\ell}_2)}$$

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Lensed, nonlinear intensity: different Fourier modes become correlated

*(can obtain  $f_{\delta}(\vec{\ell}_1, \vec{\ell}_2)$  from perturbation theory)*

# Bias-hardened estimators

Define  $\phi$  and  $\delta$  estimators like so:

$$\hat{X}(\vec{L}) \sim \int_{\vec{\ell}} g_X(\vec{\ell}, \vec{L} - \vec{\ell}) I(\vec{\ell}) I(\vec{L} - \vec{\ell})$$

Each estimator is biased by the other field:

$$\begin{cases} \langle \hat{\phi} \rangle \sim \phi + (\dots) \delta_1(\vec{L}/\chi) \\ \langle \hat{\delta} \rangle \sim (\dots) \phi + \delta_1(\vec{L}/\chi) \end{cases}$$



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Define new estimators as solutions of linear system!

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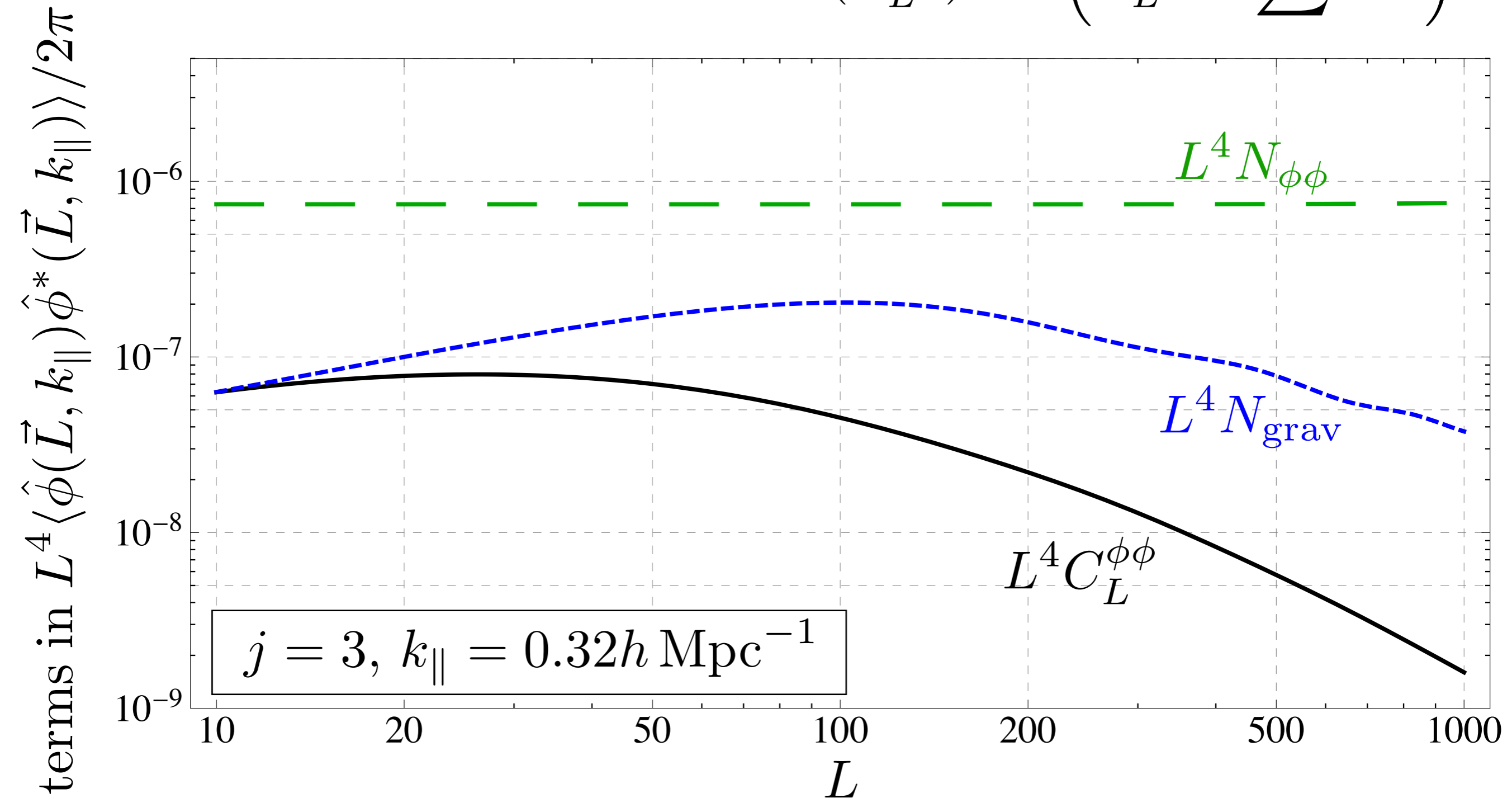
*Caveat:*  
*increased variance*

$$\text{Var} \left[ \hat{\phi}^{\text{H}} \right] = \frac{N_{\phi\phi}}{1 - \rho(\hat{\phi}, \hat{\delta})^2} + \dots$$

Previous lensing estimator for single  $k_{\parallel}$ 

$N...$  terms add both  
*bias* and *noise* to  $C_L^{\phi\phi}$

$$\langle \hat{\phi} \hat{\phi}^* \rangle \propto C_L^{\phi\phi} + \sum N...$$

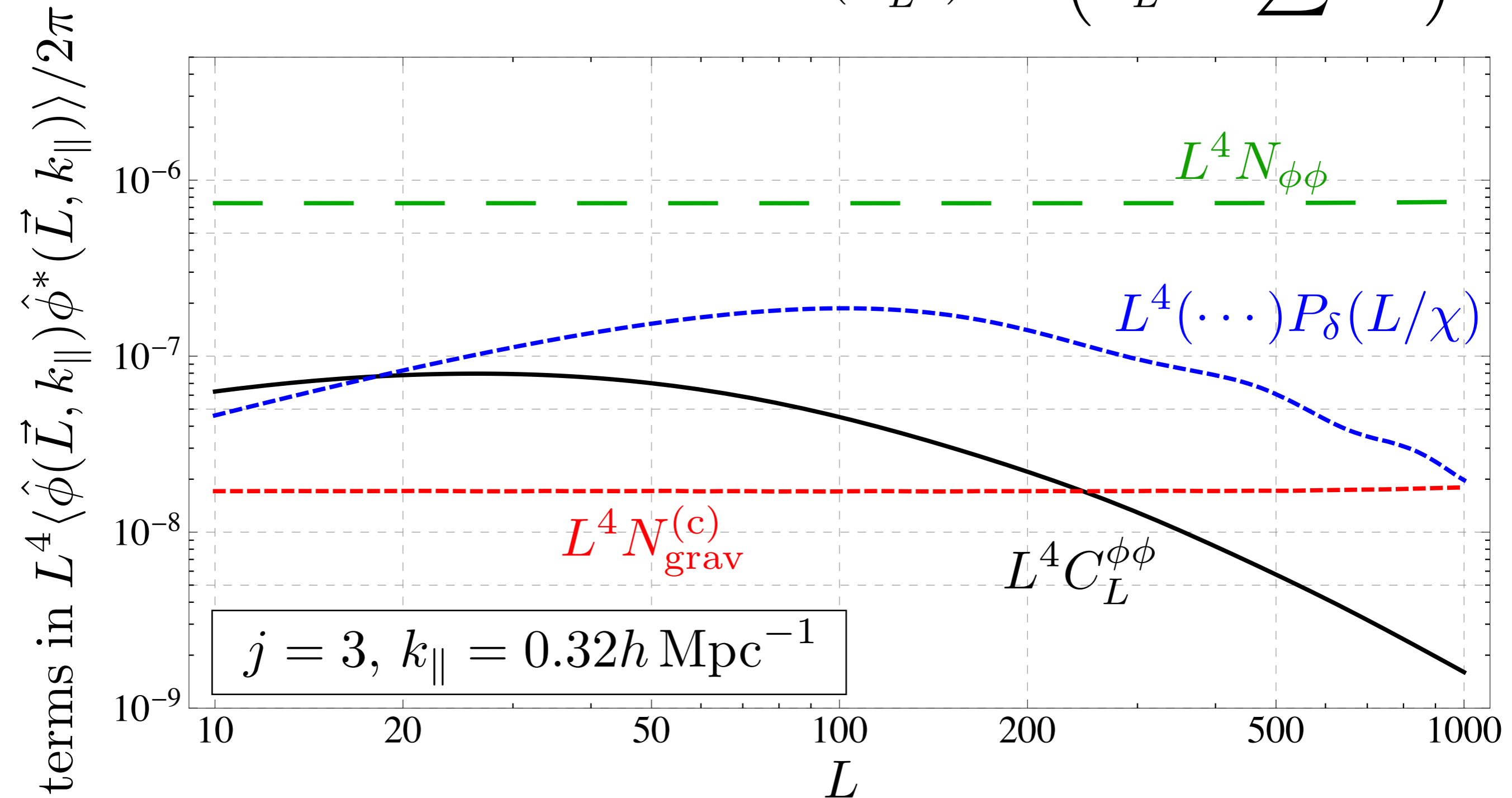
$$\sigma(\hat{C}_L^{\phi\phi})^2 \propto \left( C_L^{\phi\phi} + \sum N... \right)$$


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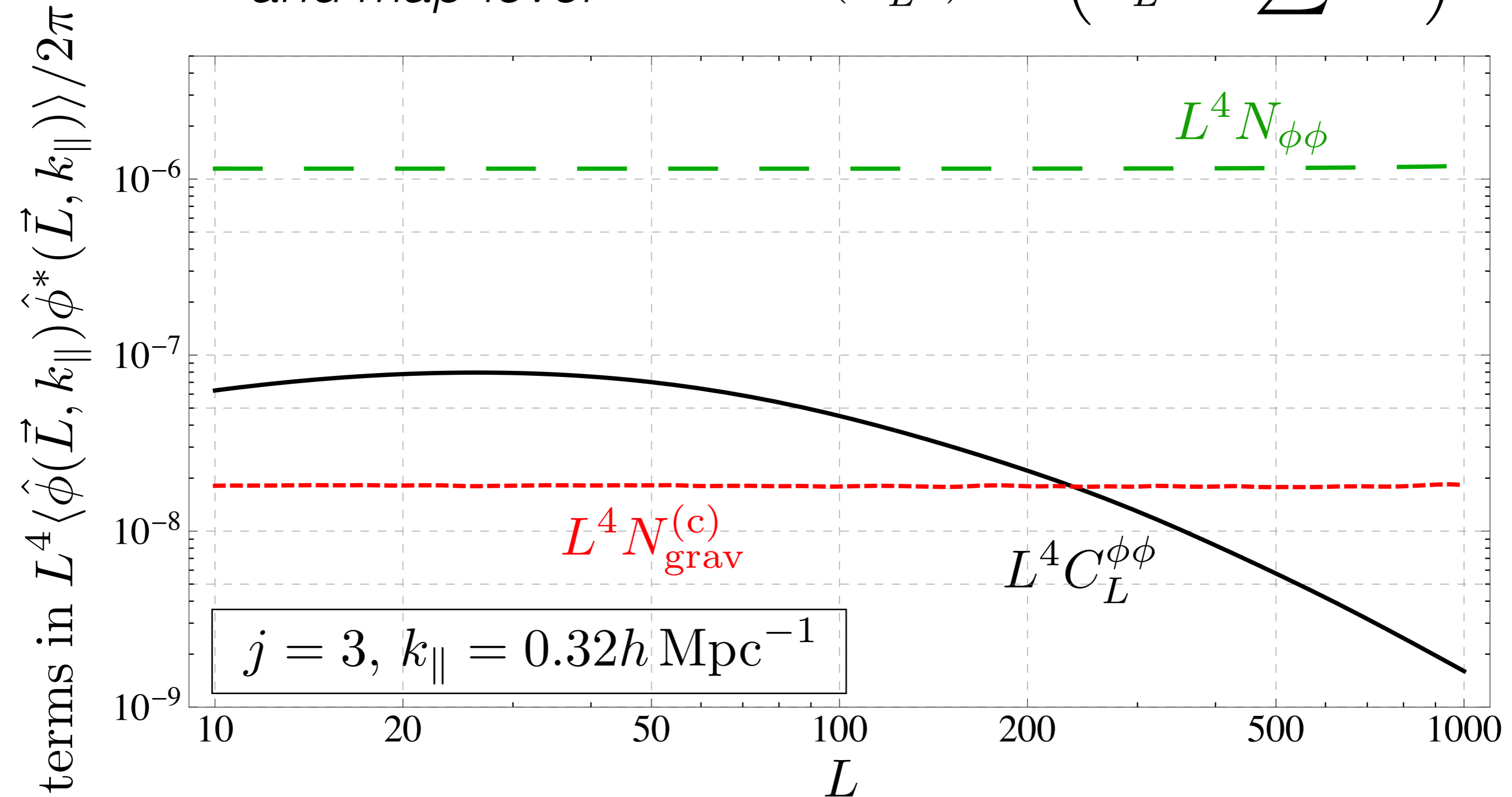


Bias-hardened lensing estimator for single  $k_{\parallel}$ 

BH removes dominant bias at  
power-spectrum-level  
*and map-level*

$$\langle \hat{\phi} \hat{\phi}^* \rangle \propto C_L^{\phi\phi} + \sum N...$$

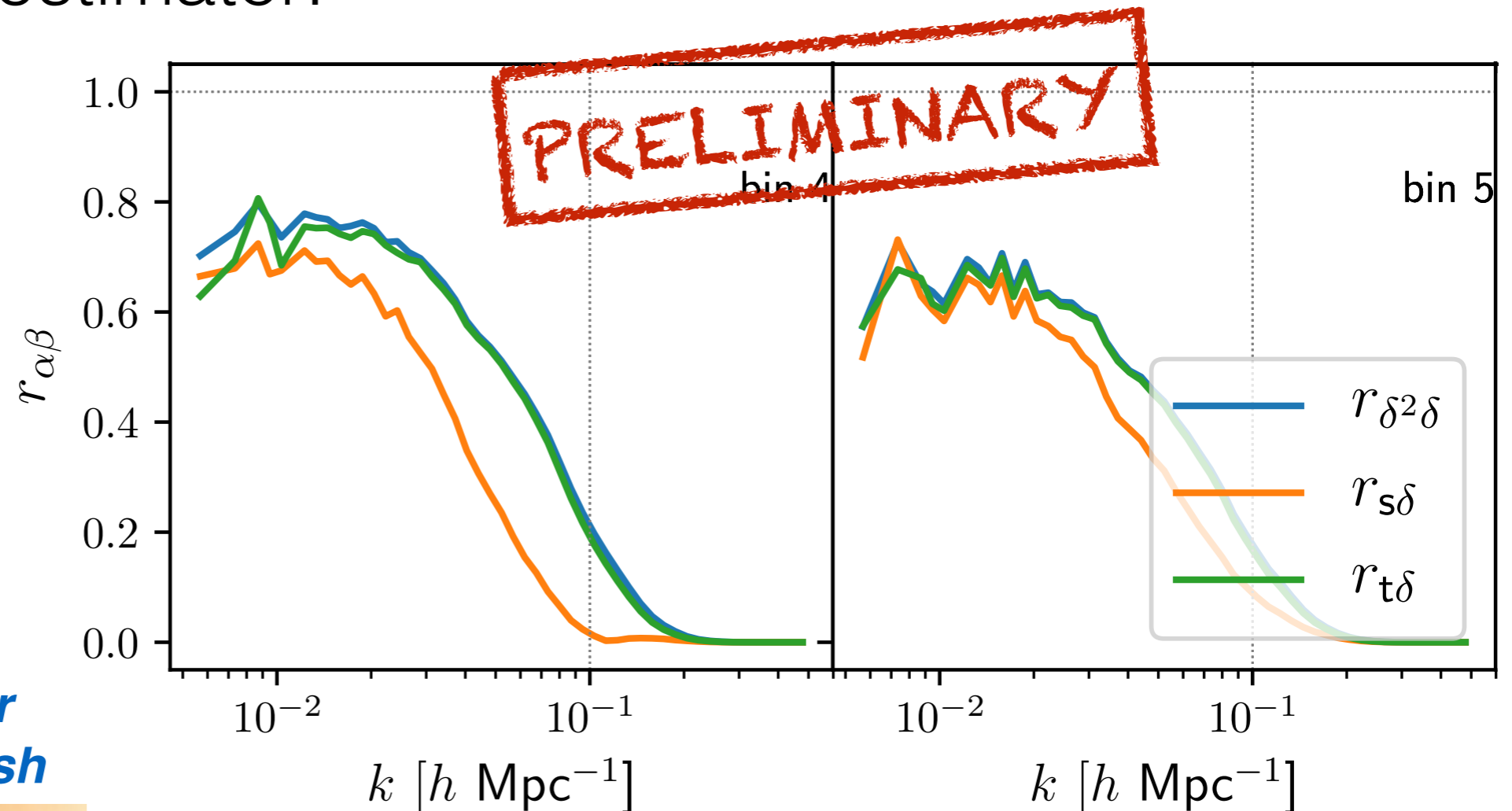
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## Removable mode-coupling from gravity - also interesting signal!

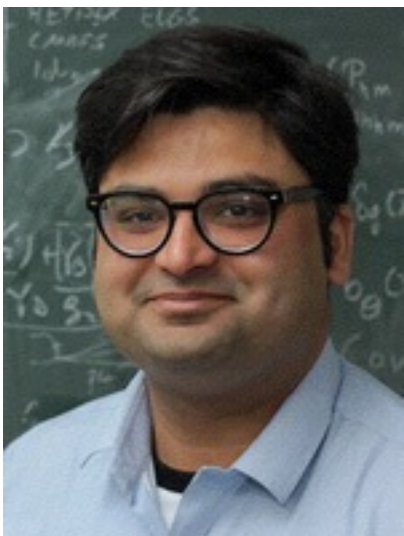
Can also reconstruct long density modes using quadratic estimator:

Cross-correlation between reconstruction and true modes



**Muntazir M.  
Abidi**

**Omar  
Darwish**



+ **T. Baldauf, SF, D. Meerburg, B. Sherwin**  
(work in progress)

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  - *connected 4-pt function  $\rightarrow$  lensing potential power spectrum*
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  - *apply 2d estimator to maps with different  $k_{\parallel}$  values*
  - *gravity adds noise, that is correlated between  $k_{\parallel}$ s*
3. Reducing gravitational effects in variance:  
“bias-hardening”
  - *can remove dominant effect with modified lensing estimator*
  - *can increase noise, depending on observational setup*
- 4. Forecasts**

# Examples of 21cm interferometers



## **SKA:** $3 < z < 27$ (SKA1-Low)

- large dish array w/ dense core
- facility, targeting cosmology + other astro



## **CHIME:** $0.8 < z < 2.5$

- 4 20m x 100m cylinders
- dedicated instrument, targeting BAO + FRBs



## **HIRAX:** $0.8 < z < 2.5$

- 32x32 close-packed 6m dishes
- dedicated instrument, targeting BAO + FRBs



## Forecasts for 21cm surveys

S/N on lensing power spectra for 21cm surveys					
	$z$	$f_{\text{sky}}$	$\langle \kappa \kappa \rangle$	$\langle \kappa g_{\text{LSST}} \rangle$	$\langle \kappa \gamma_{\text{LSST}} \rangle$
SKA1-Low	$6 < z < 14$	$6.5 \times 10^{-4}$	3.7	27	14
CHIME	$1.1 < z < 2.5$	0.5	0.26	35	28
HIRAX	$1.35 < z < 2.5$	0.5	0.98	46	36

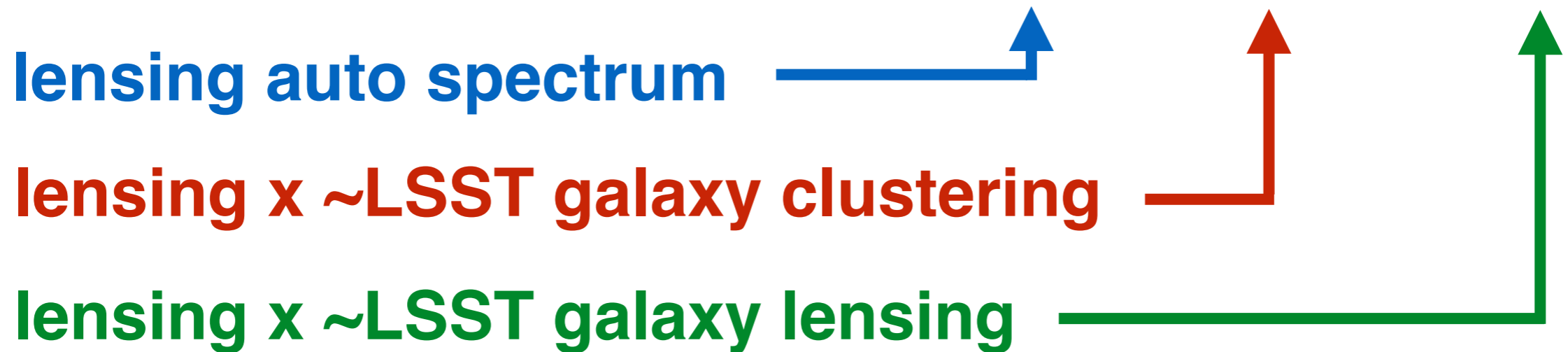


Conclusion: cross-correlations might be worth a try!

Key factor: angular resolution

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**Next-gen 21cm can do much better:  
see Cosmic Visions white paper!**

*Ansari et al (incl. SF), 1810.09572*



*Monty Python  
1971*

## Another application of small-scale mode-couplings

**Lensing estimator** based on 3-pt correlation:

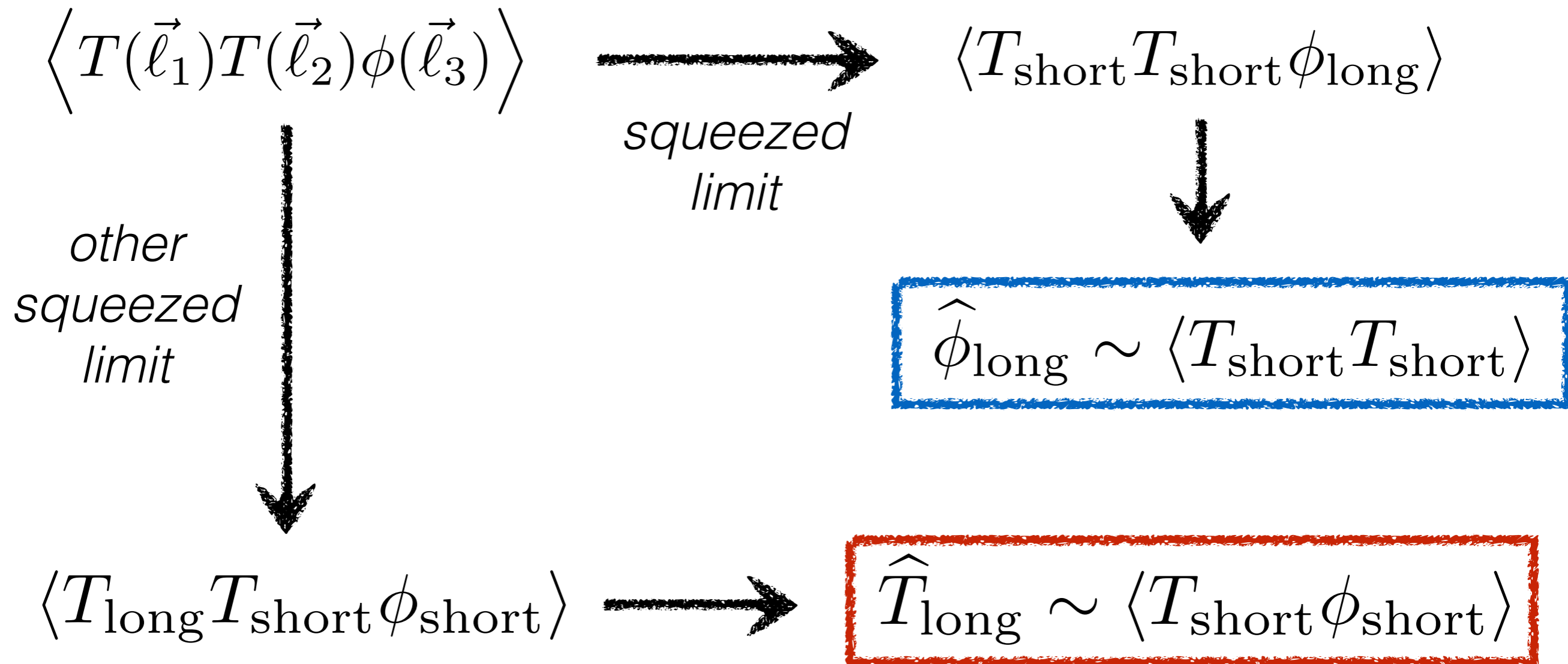
$$\left\langle T(\vec{\ell}_1) T(\vec{\ell}_2) \phi(\vec{\ell}_3) \right\rangle \xrightarrow{\substack{\text{---} \\ \text{squeezed} \\ \text{limit}}} \left\langle T_{\text{short}} T_{\text{short}} \phi_{\text{long}} \right\rangle$$

$$\downarrow$$

$$\hat{\phi}_{\text{long}} \sim \left\langle T_{\text{short}} T_{\text{short}} \right\rangle$$

## Another application of small-scale mode-couplings

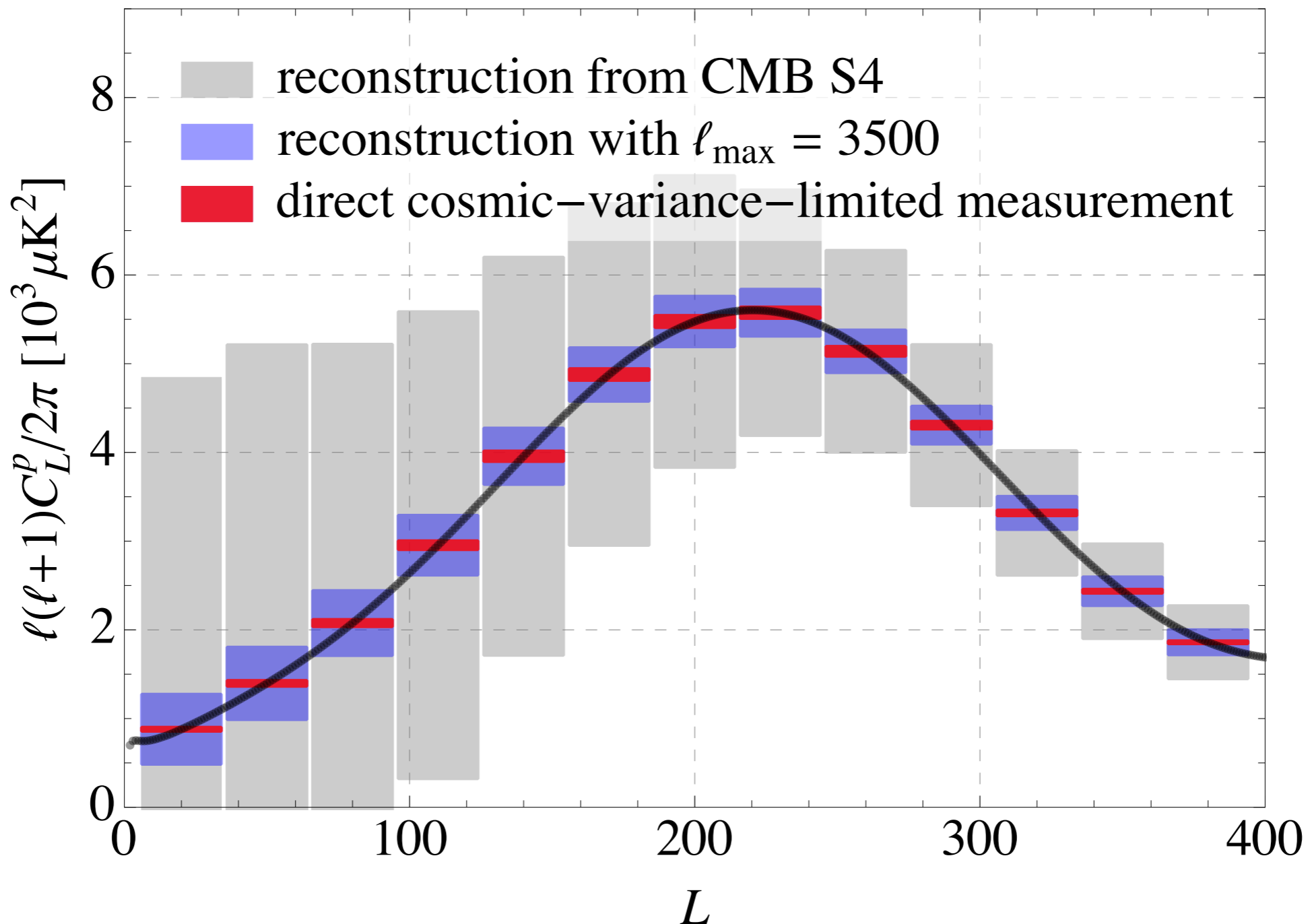
**Lensing estimator** based on 3-pt correlation:

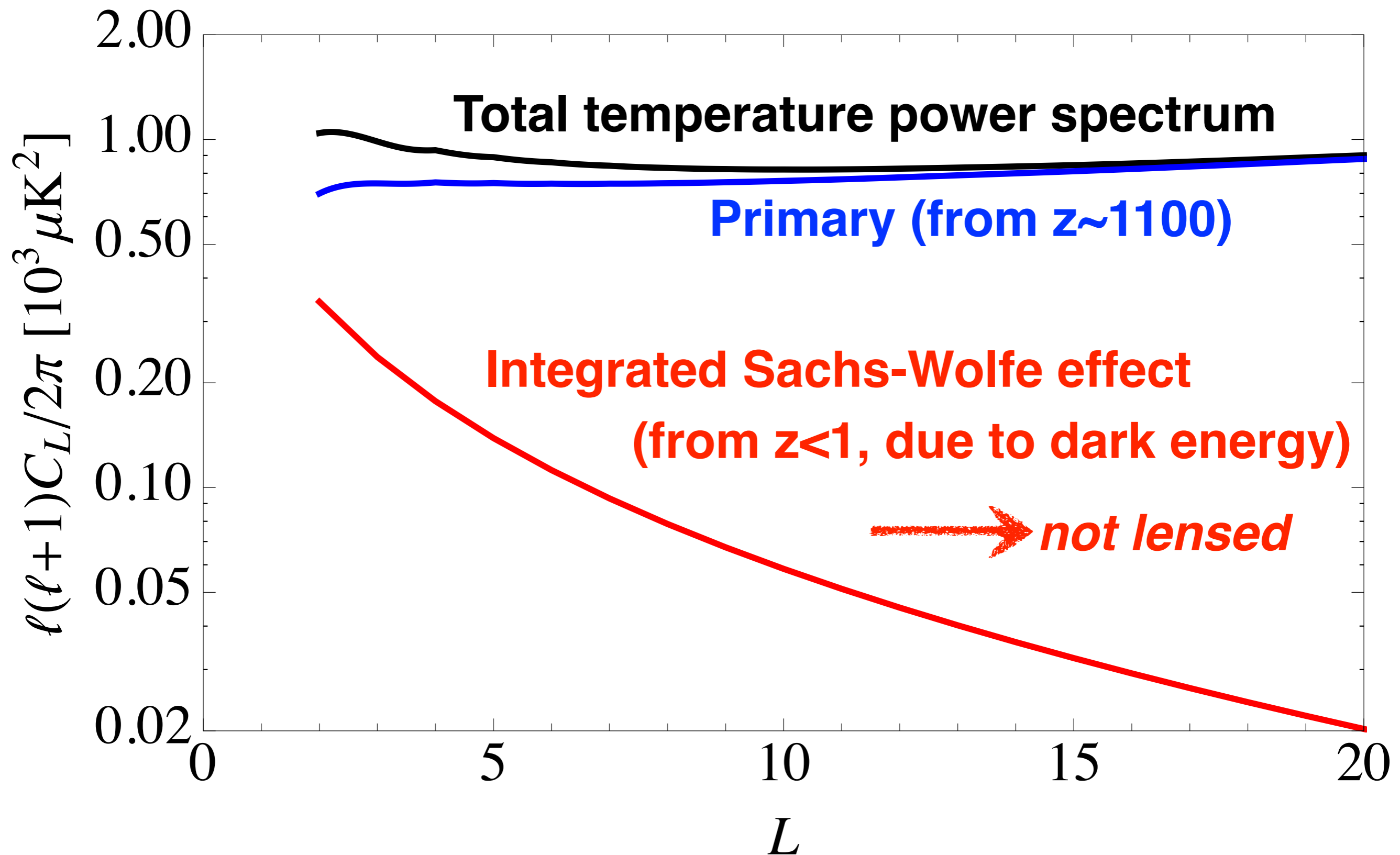


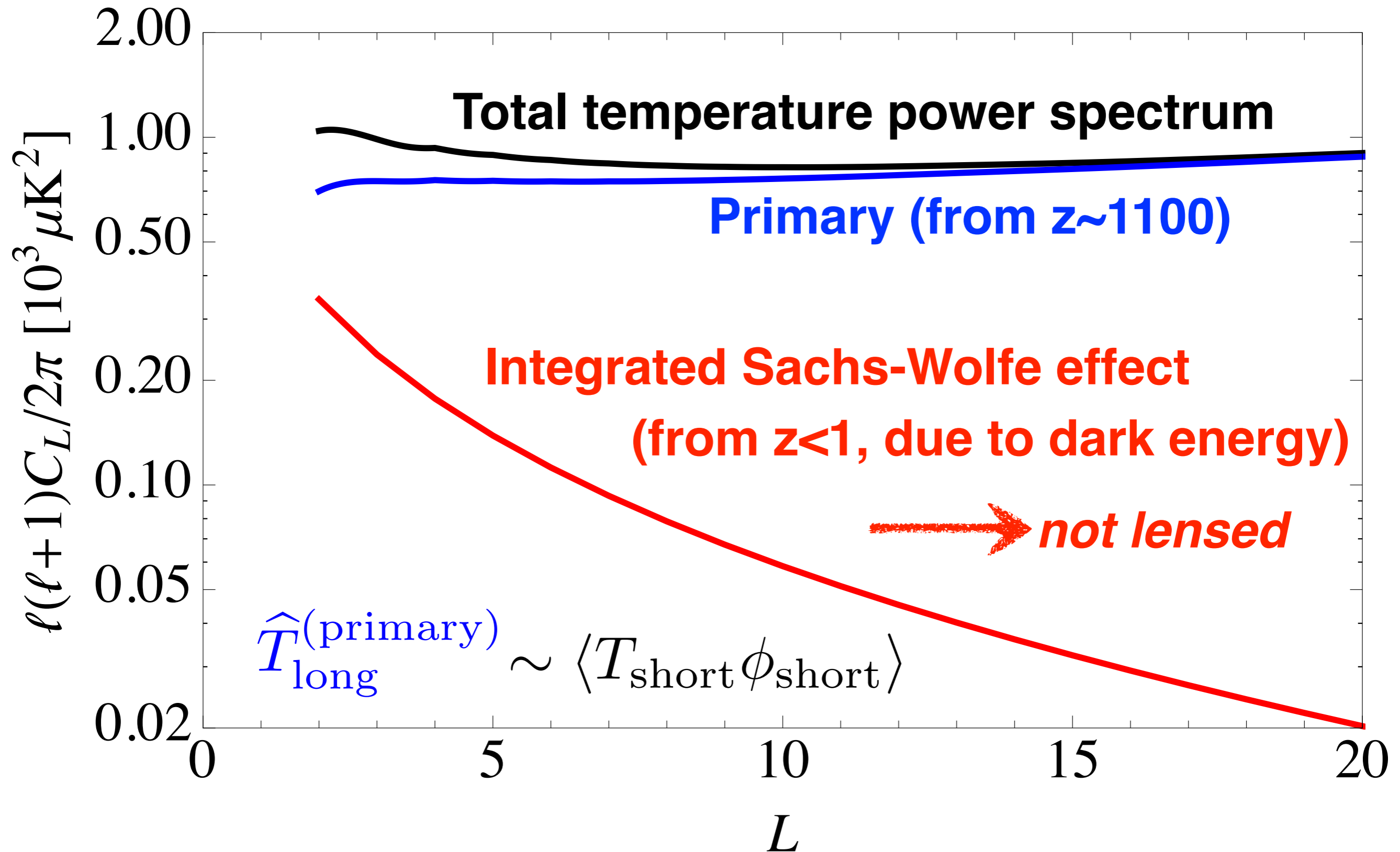
Same logic leads to **estimator for long T modes**

## Reconstructing long modes of CMB temperature

Cross-correlate high-res. temperature + lensing maps  
 → Recover large-angle temperature information



CMB temperature power spectrum: low- $z$  contribution

CMB temperature power spectrum: low- $z$  contribution



# Reconstruction improves measurements of ISW effect

Subtract reconstructed  $T$  from directly measured  $T$

→ Isolate ISW contribution (with lower noise)

Our (simplistic) forecasts:

*Consider CV-limited measurements of  $T$ ,  $\phi$  up to  $\ell_{\max}$*

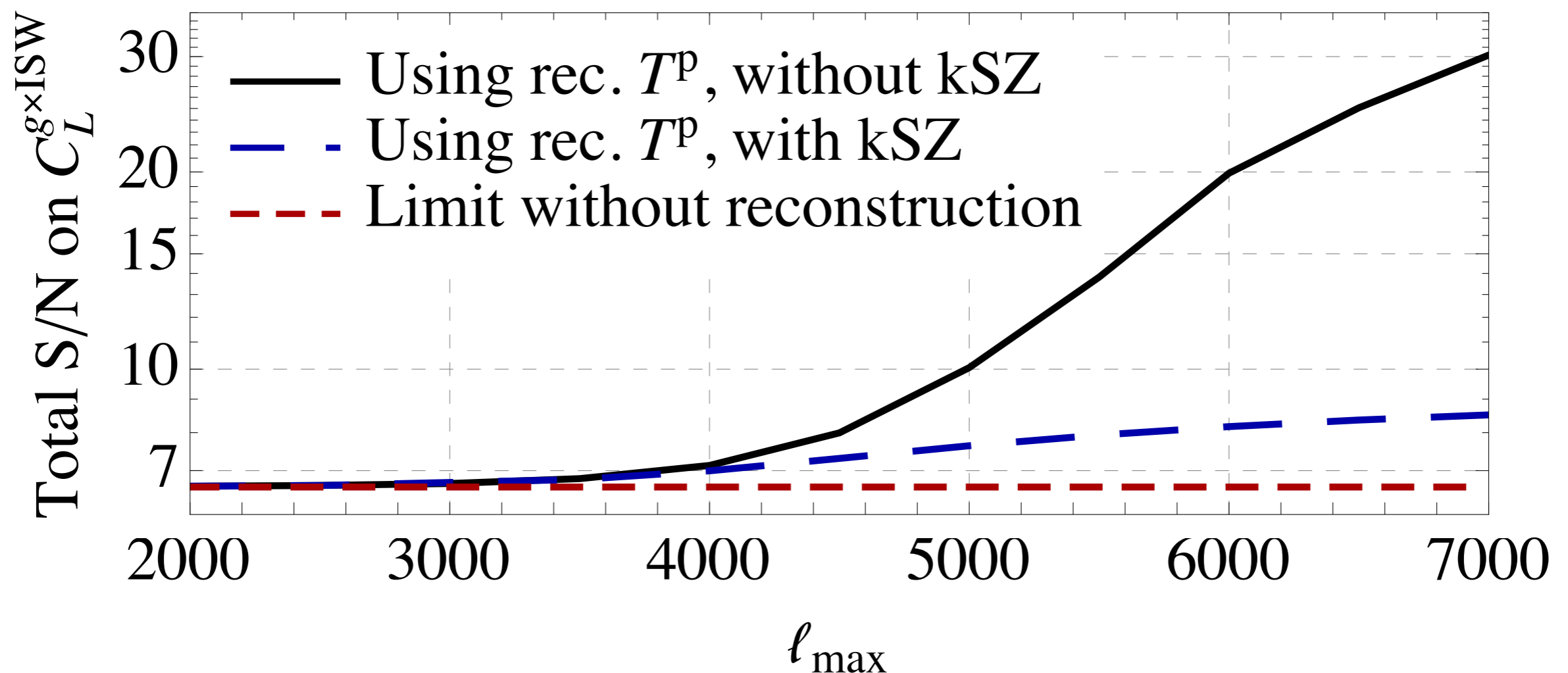
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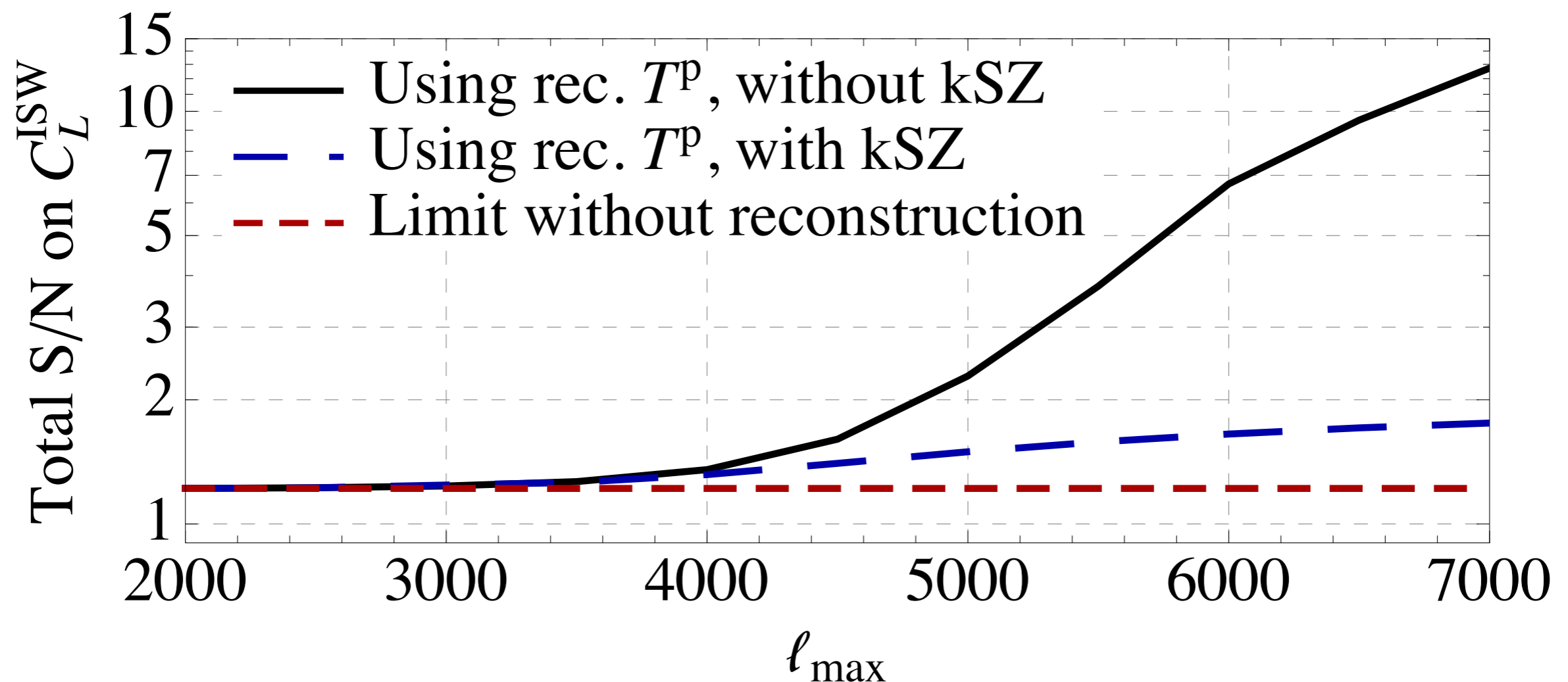
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- Need to clean kSZ + other  $T$  secondaries at small scales

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Dec

12

## The CMB in HD: The Low-noise High-resolution Frontier

### Date & Time

December 12 - 14,  
2018

 Add to Calendar

### Location

Flatiron Institute,  
162 Fifth Avenue

The CMB still contains a wealth of information about the cosmology and fundamental physics of our Universe. Unlocking all the information likely necessitates opening up a new window of CMB observations over a significant portion of the sky ( $\sim 10\%$ ) that is of much lower noise (0.1  $\mu\text{K-arcmin}$ ) and higher resolution (10 to 20 arcsec) than previous CMB surveys. Such ultra-deep, high-resolution CMB measurements could potentially provide a novel way to map small scale dark matter, allowing, for example, a new probe of dark matter's particle properties. They would also open a new window on galaxy cluster physics through the thermal and kinetic SZ effects and high- $z$  cluster detection, and on extragalactic mm/submm source populations. In addition, such observations would push the boundaries of our knowledge about the early Universe, dark energy, reionization, and galaxy evolution.

# Conclusions

1. How CMB lensing is measured
  - *exploits mode-couplings induced by lensing*
  - *connected 4-pt function  $\rightarrow$  lensing potential power spectrum*
2. Extension of method to 3d
  - *apply 2d estimator to maps with different  $k_{\parallel}$  values*
  - *gravity adds noise, that is correlated between  $k_{\parallel}$ s*
3. Reducing gravitational effects in variance:  
“bias-hardening”
  - *can remove dominant effect with modified lensing estimator*
  - *can increase noise, depending on observational setup*
4. Forecasts
  - *first detections may be possible in the near term!*
  - *future promise: “stage 2” 21cm survey could compete with CMB-S4 in lensing precision*