

The intrinsic alignment as a new cosmological probe

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based on arXiv:2007.03670, arXiv:2009.05517, and arXiv:2011.06584

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Outline

- ▶ Intrinsic Alignment (IA)
 - ▶ Linear alignment model
 - ▶ 3D power spectrum of IA
- ▶ Shape assembly bias
- ▶ Dependence of the IA coefficient on the halo concentration
- ▶ Imprint of angular-dependent PNG on IA
- ▶ Scale-dependent bias in the IA power spectrum

Intrinsic alignment : a big picture



Halo/galaxy clusters



Central galaxy shape

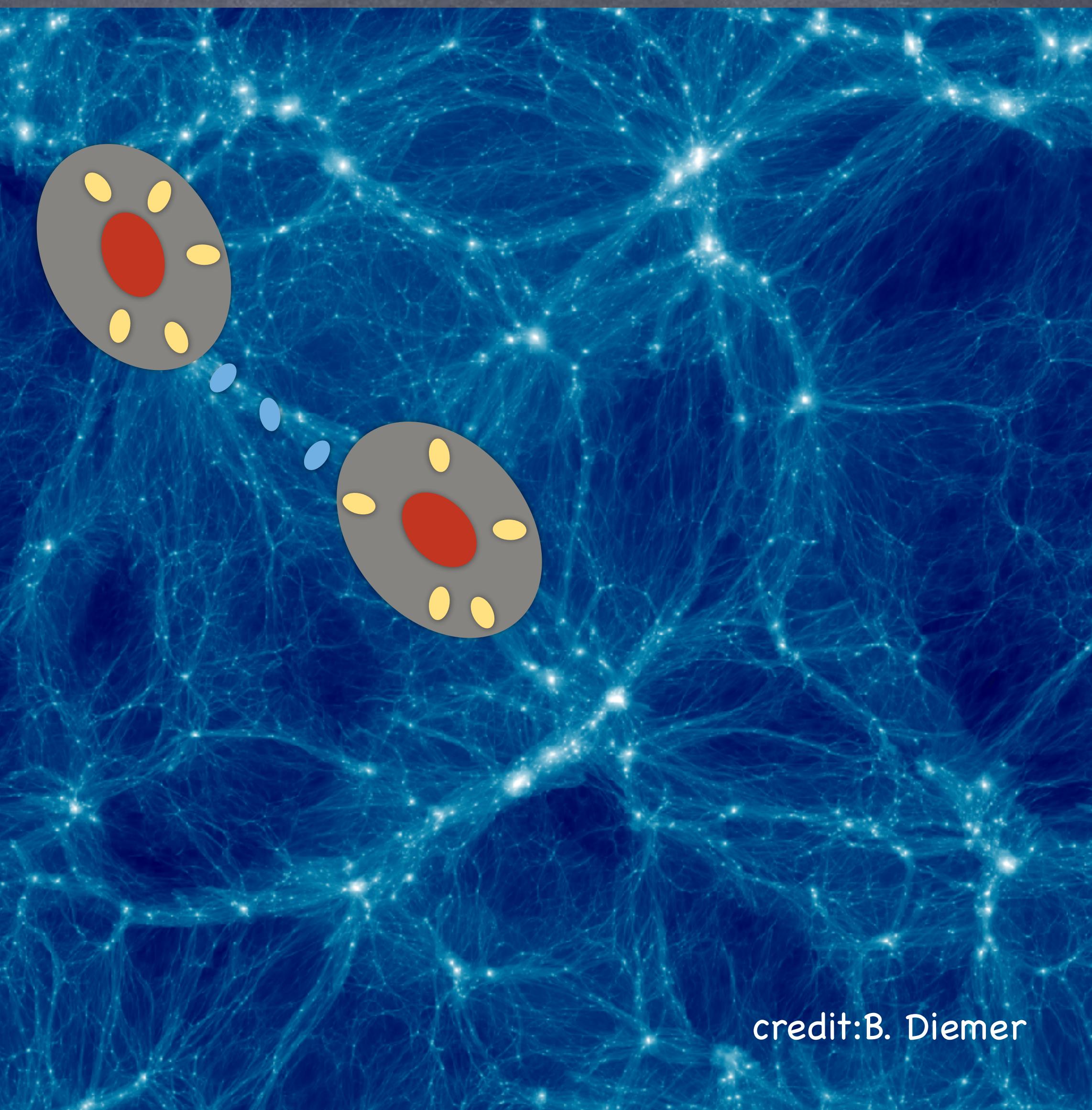
- Red galaxies
- Shape \sim halo shape
- Tidal alignment



Satellite galaxy



Galaxy on filaments



credit:B. Diemer

Intrinsic Alignments (IA)

= Physical correlations between shapes of galaxy or halos though LSS

- ▶ Intrinsic correlation before the weak lensing effect *Catelan+ '00*
- ▶ weak lensing : extrinsic effect
- ▶ Source of systematic errors in weak lensing *Hirata&Seljak '04*
- ▶ $\gamma_{ij}^{\text{obs}} = \underbrace{\gamma_{ij}^G}_{\text{WL}} + \underbrace{\gamma_{ij}^I}_{\text{IA}} \rightarrow C_{\ell}^{\gamma\gamma} = C_{\ell}^{\text{GG}} + \underbrace{C_{\ell}^{\text{GI}} + C_{\ell}^{\text{IG}} + C_{\ell}^{\text{II}}}_{\text{Contaminations}}$
- ▶ New cosmological signal

Tidal alignment (Linear alignment) model

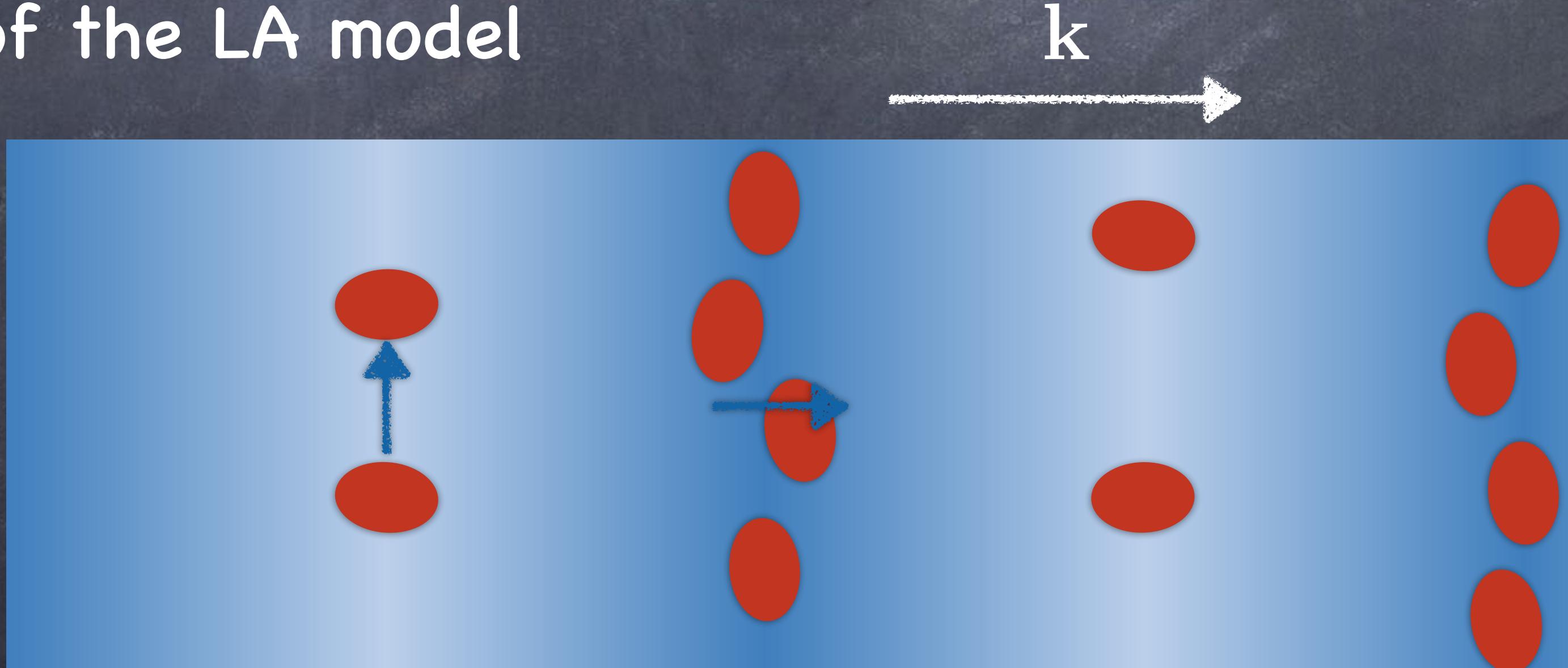
Catelan+ '00, Hirata&Seljak '04

- ▶ Origin of IA : interaction with the gravitational tidal field
 - ▶ similar to the polarization of CMB photon
 - ▶ Quadrupole ~ tidal field



shape as a biased tracer of tidal fields

- ▶ Galaxy shape ~ Halo shape ~ Tidal field of large-scale structure
- ▶ $\gamma_{ij}(\mathbf{x}) = b_K K_{ij}(\mathbf{x})$ w/ $K_{ij}(\mathbf{x}) = \left(\frac{\partial_i \partial_j}{\partial^2} - \frac{1}{3} \delta_{ij}^K \right) \delta_m(\mathbf{x}) \sim \left(\partial_i \partial_j - \frac{1}{3} \delta_{ij}^K \partial^2 \right) \Phi(\mathbf{x})$
- ▶ cf. Galaxy number density ~ matter density field: $\delta_g(\mathbf{x}) = b_1 \delta_m(\mathbf{x})$
- ▶ $b_K < 0$: prediction of the LA model
- ▶ $\gamma_{ij} \perp K_{ij}$



The shape-density correlation as a clean probe of IA

Mandelbaum et al. 2006, Hirata et al. 2007

- ▶ How to extract IA signal from observed shapes?

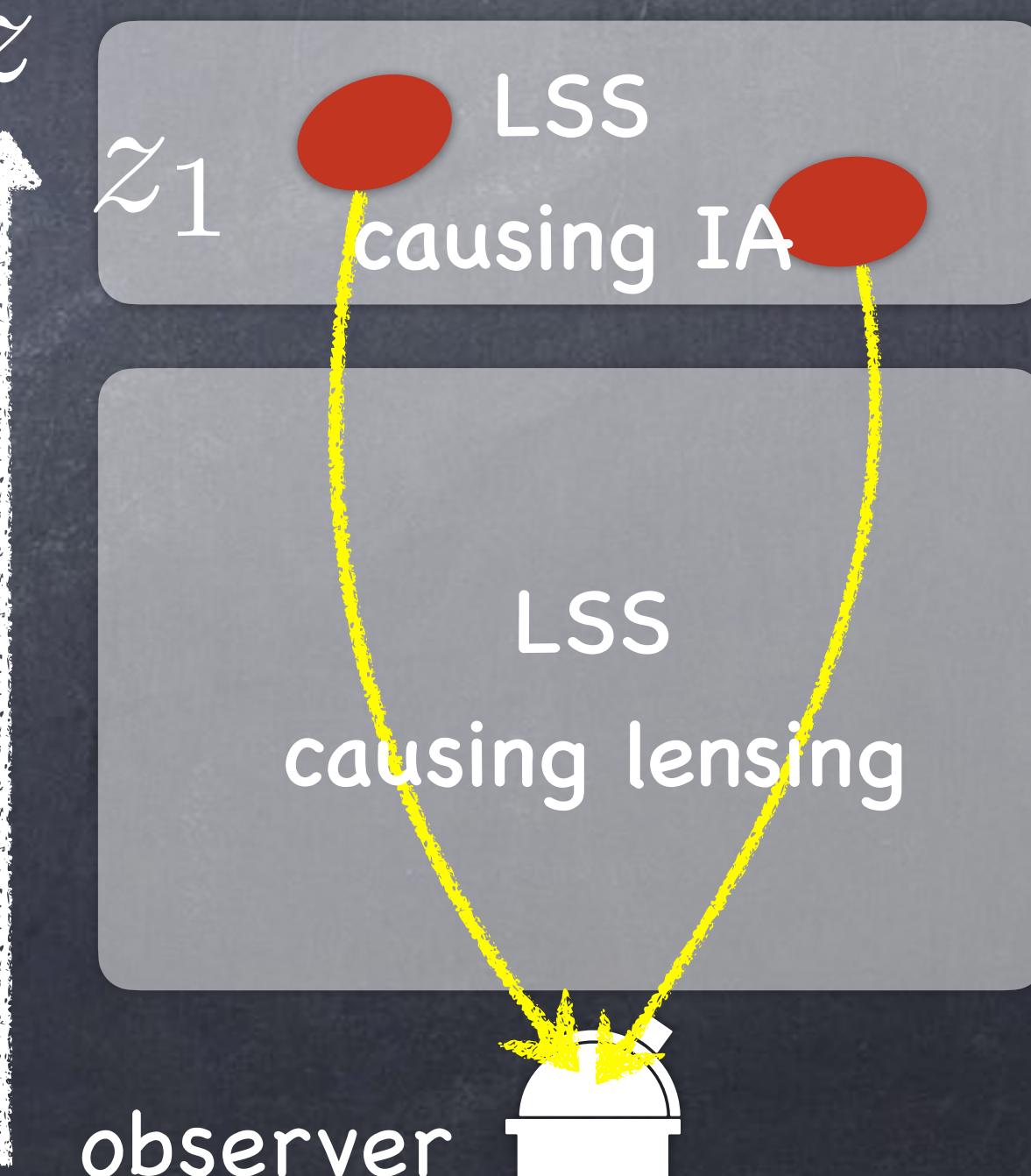
$$\gamma_{ij}^{\text{obs}} = \underbrace{\gamma_{ij}^G}_{\text{WL}} + \underbrace{\gamma_{ij}^I}_{\text{IA}} + \underbrace{\gamma_{ij}^N}_{\text{Noise}}$$

- ▶ lensing : LSS between us and source galaxy
- ▶ IA : Tidal field (LSS) surrounding source galaxy

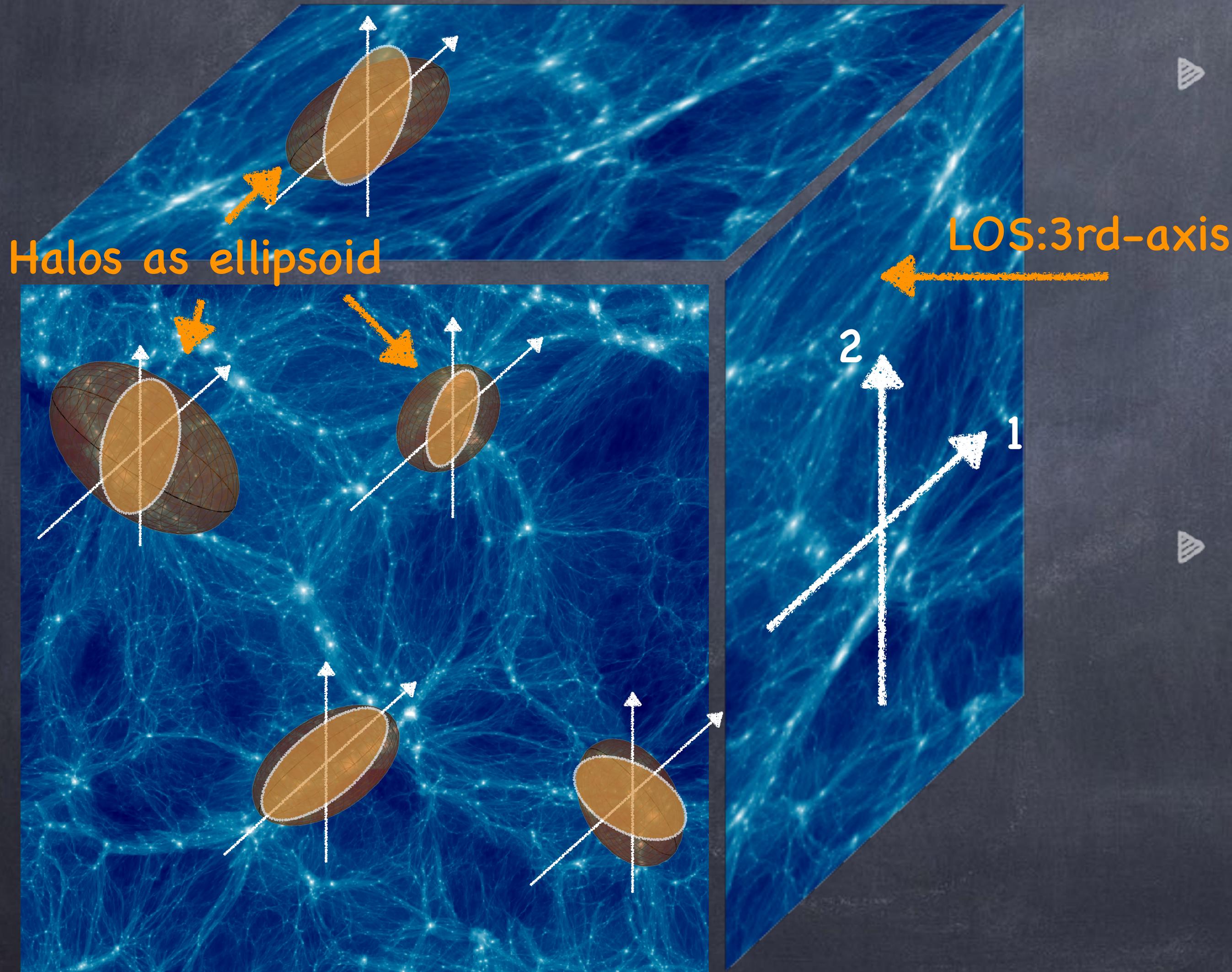
$$\▶ \langle \gamma^{\text{obs}}(z_1) \gamma^{\text{obs}}(z_1) \rangle \supset \langle \gamma^G \gamma^G \rangle, \langle \gamma^I \gamma^I \rangle$$

$$\▶ \langle \gamma^{\text{obs}}(z_1) \delta_g(z_1) \rangle = \langle \gamma^I(z_1) \delta_g(z_1) \rangle \sim b_K b_1 P_m(z_1)$$

- ▶ The shape-density correlation is suite for exploring IA.



Observable = 2D projected shape as a function of 3D position



► Projection: $I_{ij}^{\text{obs}}(\mathbf{x}) = \mathcal{P}_i^\ell(\hat{n})\mathcal{P}_j^m(\hat{n})I_{\ell m}^{\text{3D}}(\mathbf{x})$

3D position $\mathcal{P}_{ij}(\hat{n}) = \delta_{ij}^K - \hat{n}_i \hat{n}_j$

2D shape

$$I_{ij}(\mathbf{x}) = \begin{pmatrix} I_{11}(\mathbf{x}) & I_{12}(\mathbf{x}) & I_{13}(\mathbf{x}) \\ I_{21}(\mathbf{x}) & I_{22}(\mathbf{x}) & I_{23}(\mathbf{x}) \\ I_{31}(\mathbf{x}) & I_{32}(\mathbf{x}) & I_{33}(\mathbf{x}) \end{pmatrix}$$

► Projected ellipticity: spin-2 field

► $\gamma_+ = \frac{I_{11} - I_{22}}{I_{11} + I_{22}}$ $\gamma_\times = \frac{2I_{12}}{I_{11} + I_{22}}$

► $\pm 2\gamma(\mathbf{k}) = \gamma_+(\mathbf{k}) \pm i\gamma_\times(\mathbf{k})$

E/B decomposition of shape fields

Hirata&Seljak '04, Blazak+'11, Blazak+'15

- At each 3D grid, projected 2D shape fields (and density field) are defined.

$$\{\delta_m(\mathbf{k}), \delta_h(\mathbf{k}), \underline{\gamma_+(\mathbf{k})}, \underline{\gamma_\times(\mathbf{k})}\} \xrightarrow{\text{E/B decomposition}} \{\delta_m(\mathbf{k}), \delta_h(\mathbf{k}), \underline{E(\mathbf{k})}, \underline{B(\mathbf{k})}\}$$

$$E(\mathbf{k}) = \gamma_+(\mathbf{k}) \cos 2\phi_k + \gamma_\times(\mathbf{k}) \sin 2\phi_k$$
$$B(\mathbf{k}) = \gamma_+(\mathbf{k}) \sin 2\phi_k - \gamma_\times(\mathbf{k}) \cos 2\phi_k$$

- IA power spectra: 3D power spectra of 2D projected shape field
 - Linear theory prediction (linear alignment(LA) model) : $\gamma_{ij} = b_K K_{ij}$

$$P_{mE}(\mathbf{k}) = b_K(1 - \mu^2)P_m(k) \quad (\mu = \hat{\mathbf{k}} \cdot \hat{\mathbf{n}})$$
$$P_{EE}(\mathbf{k}) = b_K^2(1 - \mu^2)^2 P_m(k)$$

cf. Kaiser's formula:

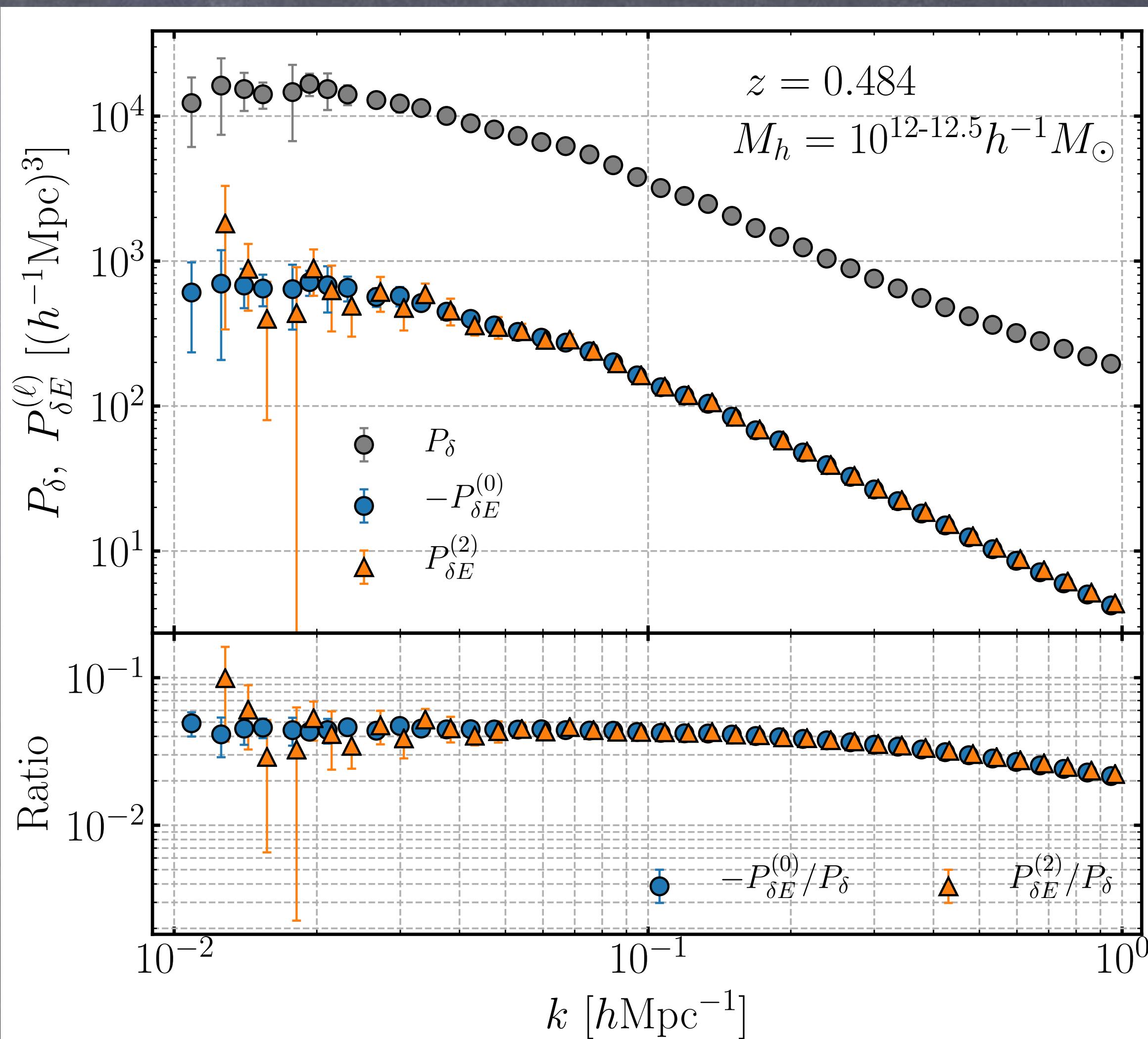
$$P_{mh}(\mathbf{k}) = (b_1 + f\mu^2)P_m(k)$$
$$P_{hh}(\mathbf{k}) = (b_1 + f\mu^2)^2 P_m(k)$$



E-mode power spectra from N-body

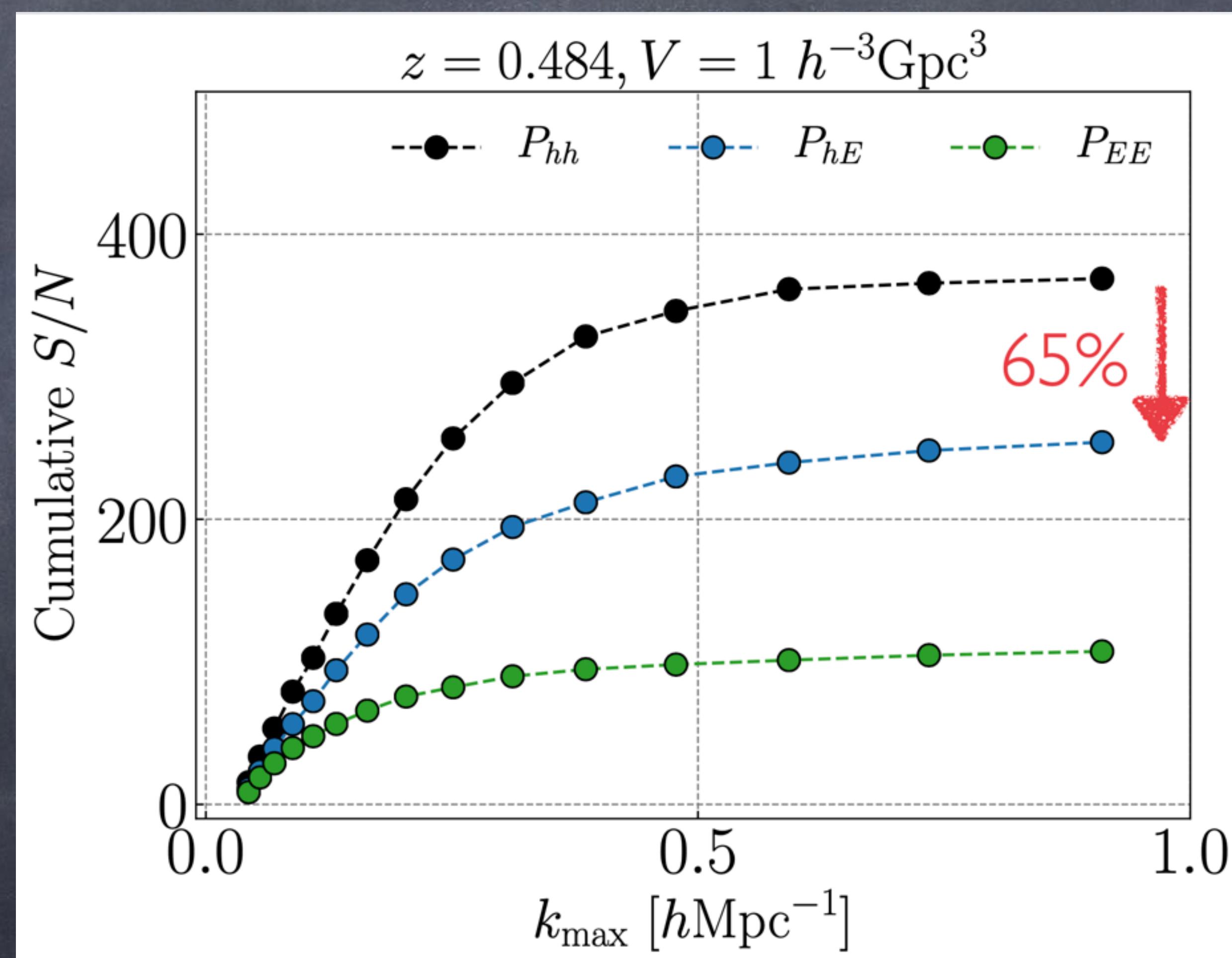
- ▶ LA model works on large scales.
- ▶ Negative correlation $P_{mE}^{(0)} < 0$
 - ▶ $\gamma_{ij} \perp K_{ij}$
- ▶ $P_{mE} \propto P_{mm}$ on large-scales
- ▶ $E(\mathbf{k}) \sim b_K \delta_m(\mathbf{k})$ with $b_K \sim -0.1$
- ▶ The large-scale constant bias when
- ▶ Equivalence principle
- ▶ Adiabatic&Gaussian ICs

What happens with PNG?



S/N of shape power spectrum

- ▶ S/N of P_{hE} is about **65%** compared with halo clustering P_{hh}
- ▶ bias: $b_h \sim \mathcal{O}(1)$, $b_K \sim \mathcal{O}(0.1)$
- ▶ Noise: $1/\bar{n}_h$, σ_γ^2/n_h
 $\sigma_\gamma^2 \sim 0.1$
- ▶ For galaxies S/N can be decreased
- ▶ misalignment Okumura+’09



The importance of 3D power spectrum

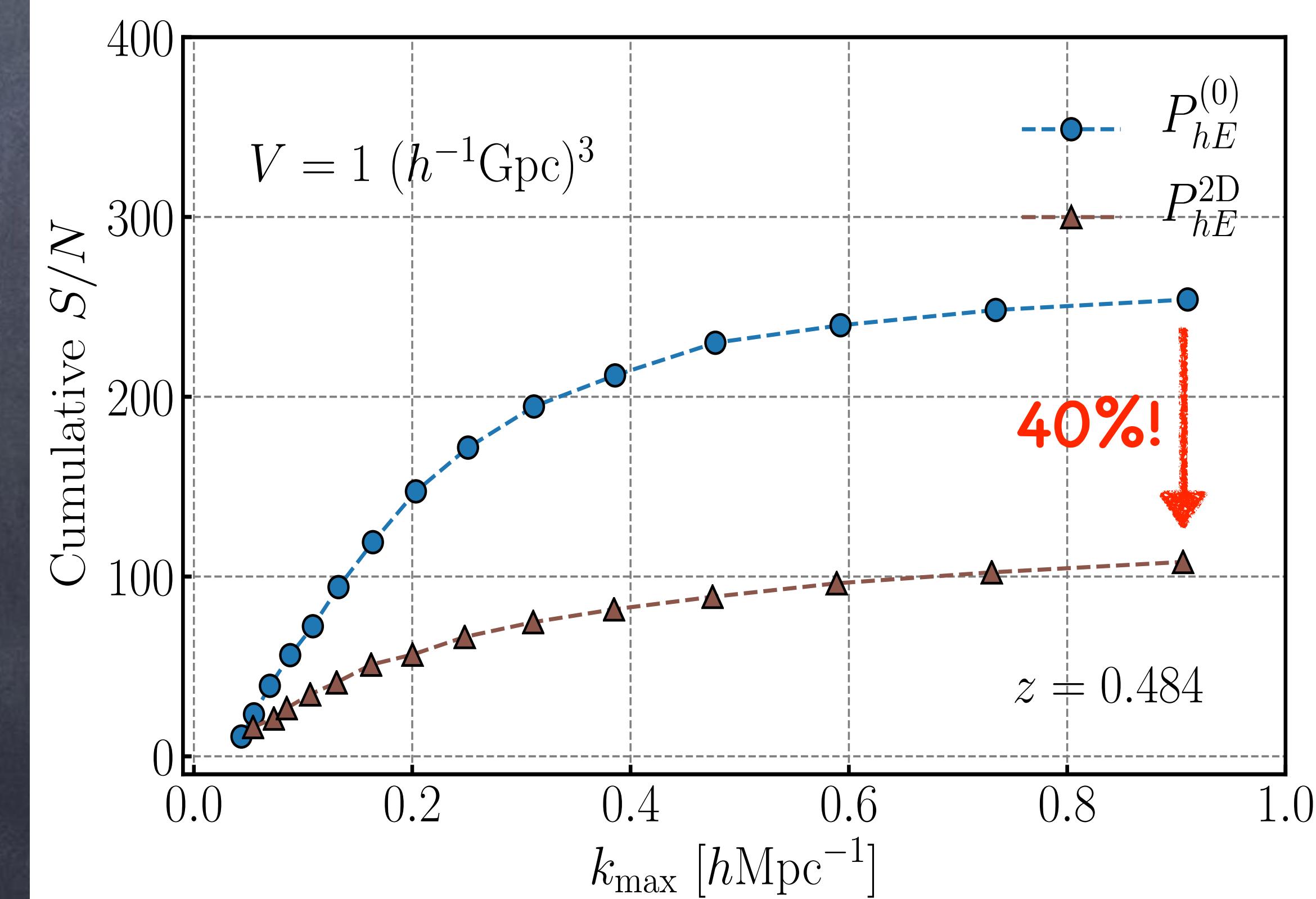
$$\underline{\gamma}_{ij}(\underline{x}) = \begin{pmatrix} \underline{\gamma}_{11}(\underline{x}) & \underline{\gamma}_{12}(\underline{x}) \\ \underline{\gamma}_{21}(\underline{x}) & \underline{\gamma}_{22}(\underline{x}) \end{pmatrix}$$

- ▶ 2D shape components from imaging
- ▶ 3D position from spectroscopy
- ▶ What if only using imaging survey?

$$\underline{\gamma}_{ij}^{2D}(x_{\perp}) = \int_{\bar{x}-\Delta\chi/2}^{\bar{x}+\Delta\chi/2} dx_3 \underline{\gamma}_{ij}(x_{\perp}, x_3)$$

2D position

▶ $\Delta\chi$ corresponds to $\sigma_z \sim 0.04$

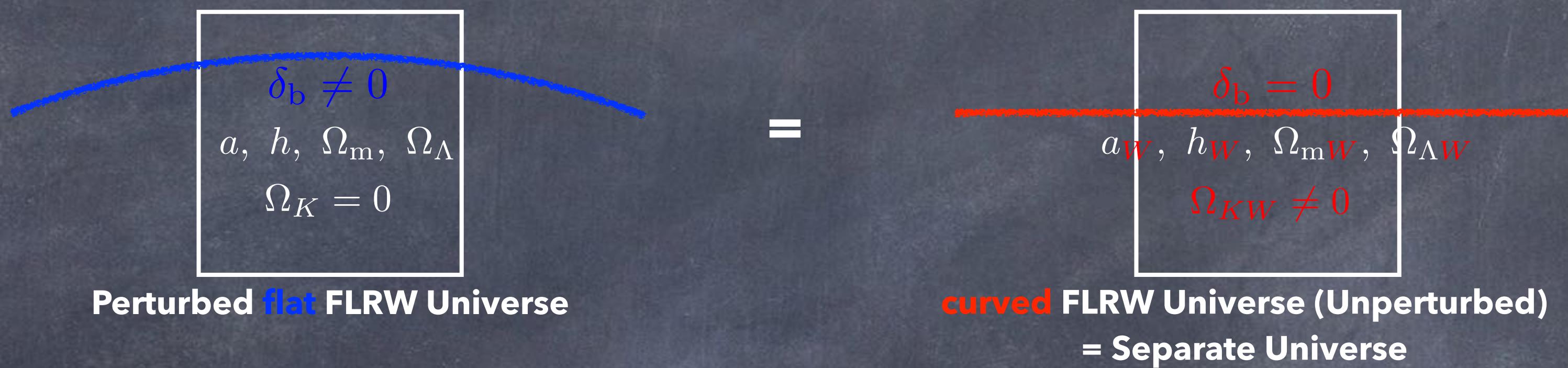


The linear alignment coefficient b_K from
the tidal separate universe simulation

Separate universe simulation

Sirko'05, Baldauf+'11, Li+'14a, Wagner+'14, Baldauf+'16, Lazeyras+'16

- ▶ Long-wavelength perturbation can be absorbed into the local background



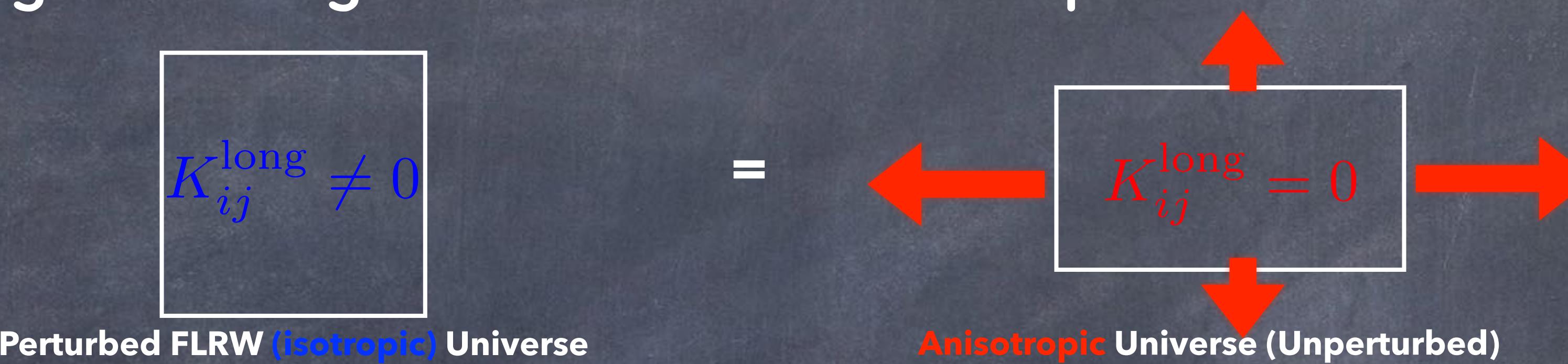
- ▶ Mass conservation: $a^3 \bar{\rho}_m [1 + \delta_b] = a_W^3 \bar{\rho}_{mW} \rightarrow a_W \simeq a \left[1 - \frac{1}{3} \delta_b \right]$
- ▶ From the same initial seeds
- ▶ Halo biases can be well calibrated by using this technique.

$$b_1 = \frac{d \ln \bar{n}_h}{d \ln \bar{\rho}_m} = \frac{d \ln \bar{n}_h}{d \delta_b}$$

Tidal separate universe simulation

KA+’20, see also Stucker+’20 and Masaki+’20

- ▶ Including long-wavelength tidal field: anisotropic scale factor



$$a_x = a_y = a_z = a$$

$$a_x = a[1 - K_x]$$

$$a_y = a[1 - K_y]$$

$$a_z = a[1 - K_z]$$

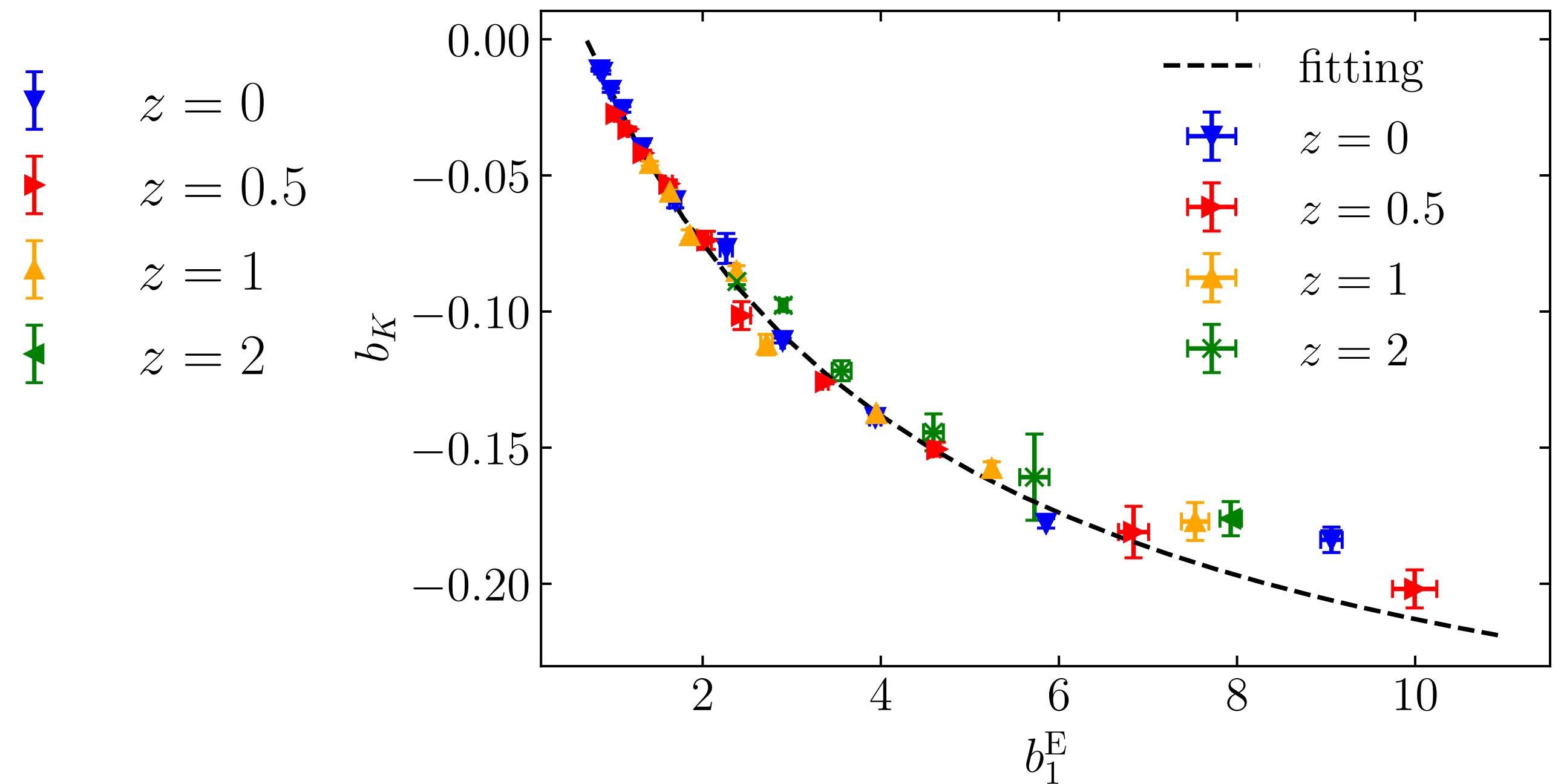
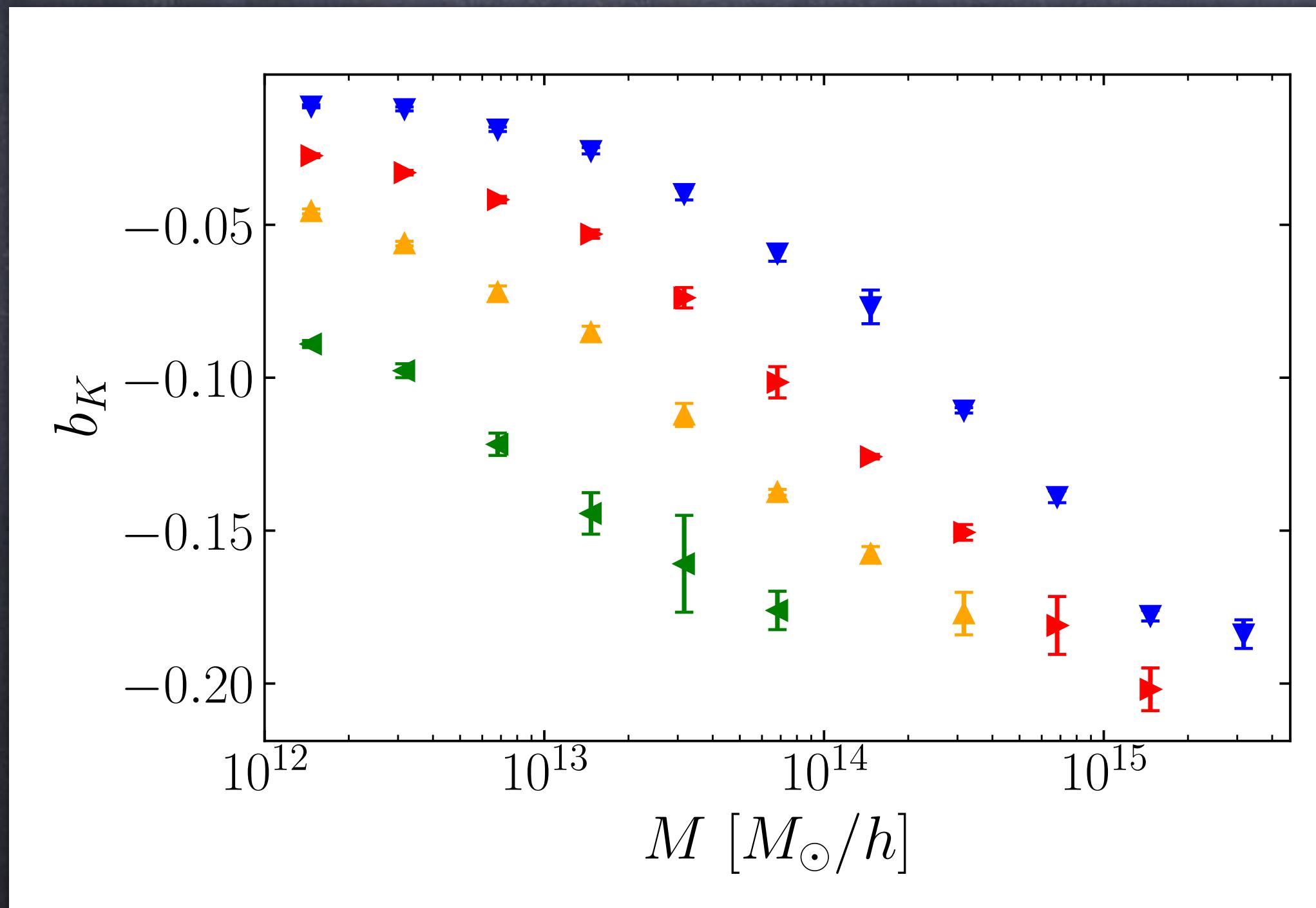
- ▶ The shape bias can be well calibrated by this simulation.

$$b_K = \frac{d \ln \bar{I}_{ij}}{d K_{ij}}$$

Similarity to the linear bias

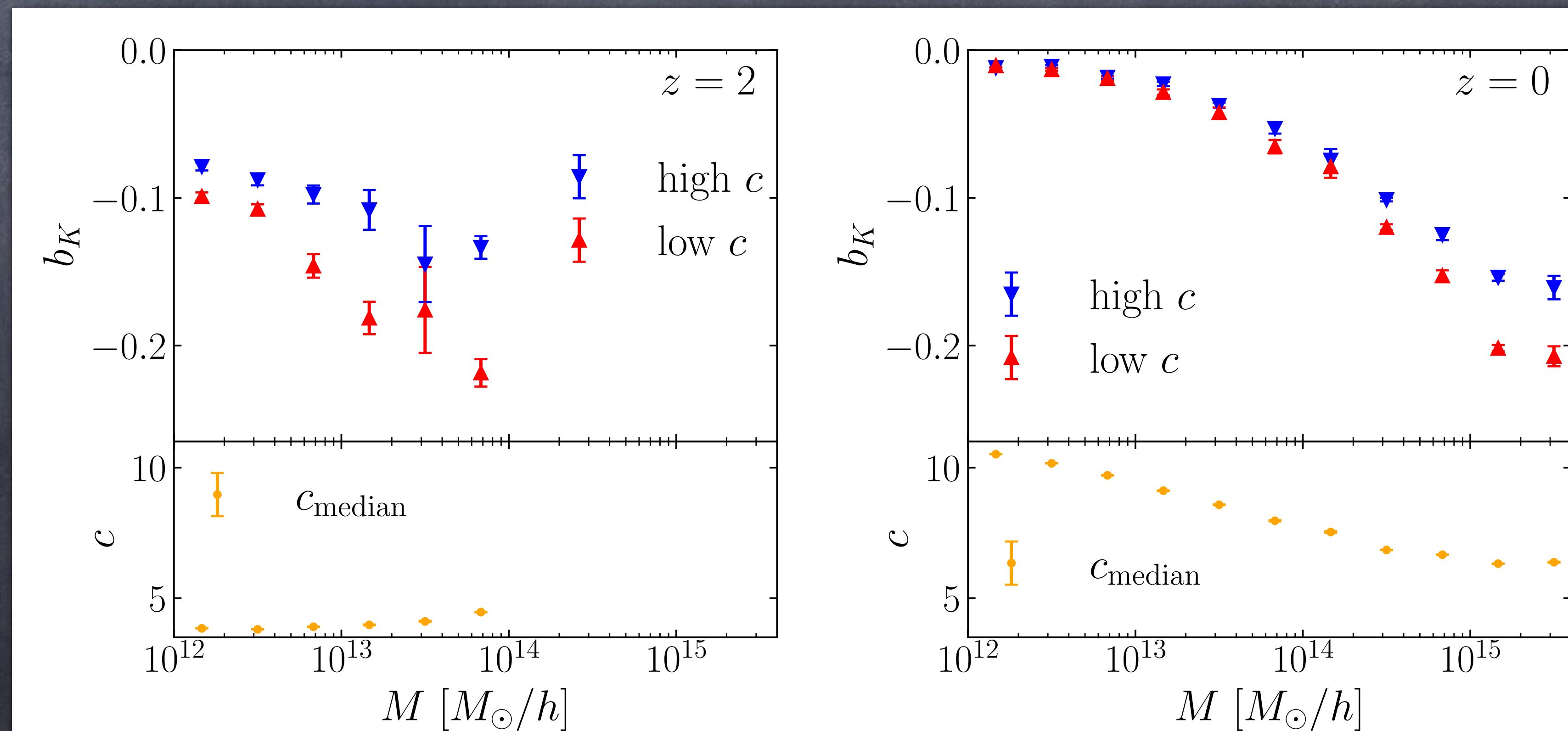
KA+'20

- ▶ Similar dependence on halo mass and redshift to the linear bias
- ▶ Hint for a theory of b_K ?



Shape assembly bias: concentration

- ▶ The shape bias depends on the halo concentration.
- ▶ High peak is less affected by large-scale tides?



The intrinsic alignment as a probe of
the angular-dependent PNG

Primordial non-Gaussianity (PNG)

- ▶ The primordial perturbations obey the Gaussian distribution
 - ▶ predicted by the standard (single field & slow roll) inflation
 - ▶ completely described by the power spectrum (2pt function):

$$\langle \Phi(\mathbf{k}_1)\Phi(\mathbf{k}_2) \rangle = (2\pi)^3 \delta_D^3(\mathbf{k}_1 + \mathbf{k}_2) P_\Phi(\mathbf{k}_1) : \text{No mode-coupling}$$

- ▶ PNG: the deviation from the Gaussianity (i.e. the standard inflation)
 - ▶ its leading order effect is characterized by the bispectrum (3pt function):

$$\langle \Phi(\mathbf{k}_1)\Phi(\mathbf{k}_2)\Phi(\mathbf{k}_3) \rangle = (2\pi)^3 \delta_D^3(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) B_\Phi(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3)$$

- ▶ Local-type: $B_\Phi(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) = 2f_{NL} [P_\Phi(\mathbf{k}_1)P_\Phi(\mathbf{k}_2) + 2 \text{ perms.}]$

Effect of PNG on galaxy number density

Dalal+'08

► What if there is the local-type PNG?

► long-&short-modes are coupled -> the power spectrum is position-dependent.

$$P_m(k_{\text{short}}) \rightarrow P_m(k_{\text{short}} | \mathbf{x}) = P_m(k_{\text{short}}) [1 + \underline{4f_{\text{NL}}\phi^{\text{long}}(\mathbf{x})}] \quad \leftarrow B_\Phi(\mathbf{k}_{\text{short}}, \mathbf{k}_{\text{short}}, \mathbf{k}_{\text{long}}) \simeq 4f_{\text{NL}} P_\Phi(\mathbf{k}_{\text{short}}) P_\Phi(\mathbf{k}_{\text{long}})$$

► Amplitudes of small-scale fluctuations at distant points are now correlated.

$$\begin{aligned} \delta_g(\mathbf{k}_{\text{long}}) &= b_1 \delta_m(\mathbf{k}_{\text{long}}) + \underline{4b_\phi f_{\text{NL}} \phi(\mathbf{k}_{\text{long}})} \\ &= [b_1 + 4b_\phi f_{\text{NL}} \mathcal{M}^{-1}(k_{\text{long}})] \delta_m(\mathbf{k}_{\text{long}}) \quad \bar{\rho}_m \rightarrow \bar{\rho}_m [1 + \delta_m^{\text{long}}(\mathbf{x}_1)] \quad \bar{\rho}_m \rightarrow \bar{\rho}_m [1 + \delta_m^{\text{long}}(\mathbf{x}_2)] \end{aligned}$$

with $\delta_m(\mathbf{k}) = \mathcal{M}(k)\phi(\mathbf{k})$

$$b_\phi = \frac{d \ln n_g}{d \ln A_s} = \frac{d \ln n_g}{d \ln \sigma_8} = \frac{d \ln n_g}{d(4f_{\text{NL}}\phi^{\text{long}})}$$



$$P_m(\mathbf{k}_{\text{short}} | \mathbf{x}_1) = P_m(k_{\text{short}}) [1 + 4f_{\text{NL}}\phi^{\text{long}}(\mathbf{x}_1)]$$

$$P_m(\mathbf{k}_{\text{short}} | \mathbf{x}_2) = P_m(k_{\text{short}}) [1 + 4f_{\text{NL}}\phi^{\text{long}}(\mathbf{x}_2)]$$

Scale-dependent bias from the local-type PNG

- ▶ There appears $1/k^2$ enhancement in galaxy/halo density field on large-scales.

$$\triangleright \delta_g(\mathbf{k}) = [b_1 + 4b_\phi f_{\text{NL}} \mathcal{M}^{-1}(k)] \delta_m(\mathbf{k})$$

$$\rightarrow P_{mg}(k) = [b_1 + 4b_\phi f_{\text{NL}} \mathcal{M}^{-1}(k)] P_m(k)$$

- ▶ $\mathcal{M}^{-1}(k) \propto 1/k^2$ on large-scales

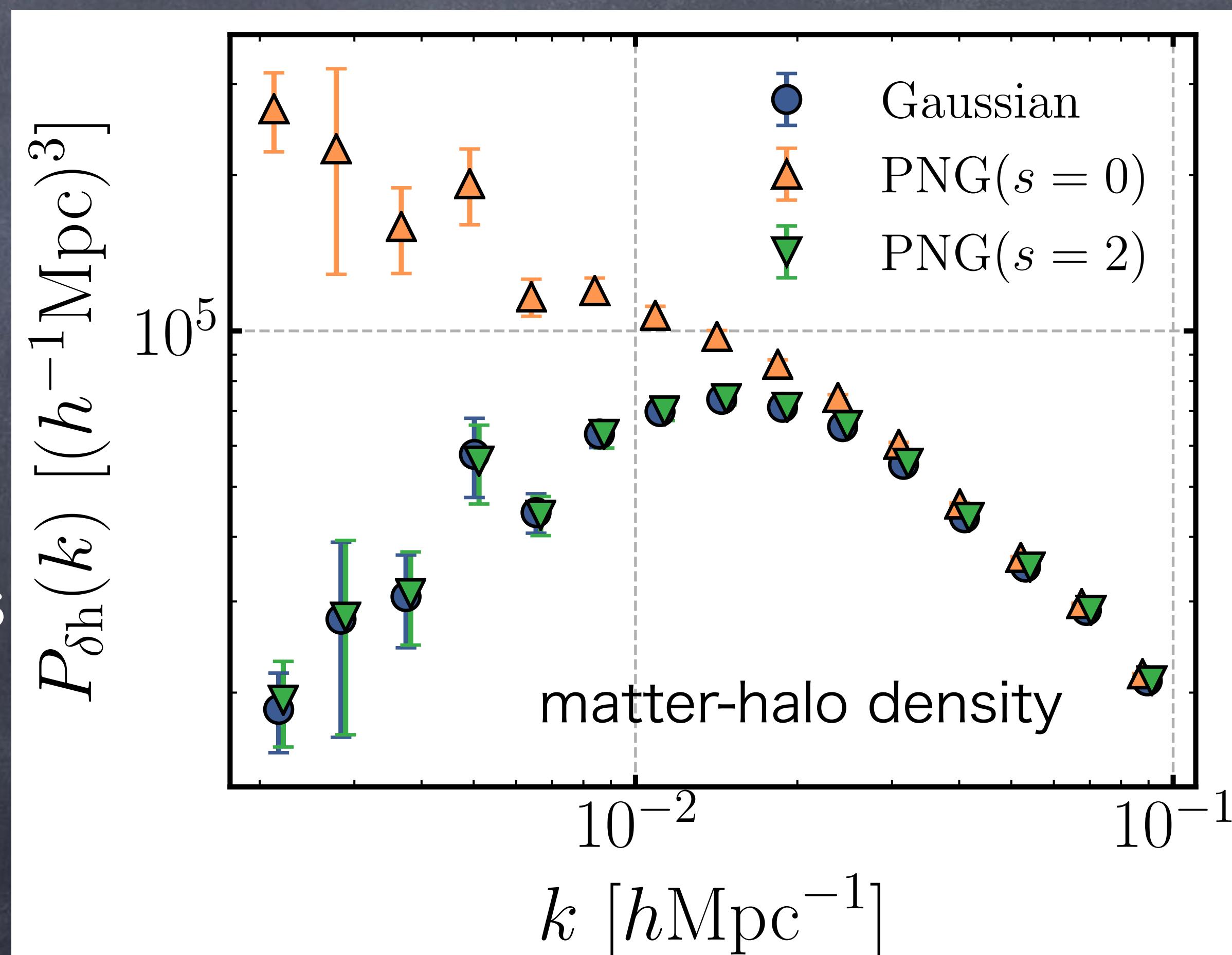
- ◀ $\delta_m(\mathbf{k}) \sim k^2 \phi(\mathbf{k})$ from Poisson eq.

- ▶ Constraints on f_{NL} from galaxy surveys

$-16 < f_{\text{NL}} < 26$ from BOSS T.Giannantonio+’14

$\sigma(f_{\text{NL}}) \sim \mathcal{O}(1)$ in the near future (SPHEREx)

- ▶ Note: there is no modulation in $P_m(k)$



Angular-dependent PNG

- ▶ The quadrupole local-type PNG: $B_\Phi(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) = 2f_{\text{NL}}^{s=2} [\mathcal{L}_2(\hat{\mathbf{k}}_1 \cdot \hat{\mathbf{k}}_2) P_\Phi(\mathbf{k}_1) P_\Phi(\mathbf{k}_2) + \text{2 perms.}]$
- ▶ cf. the usual local-type PNG: $B_\Phi(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) = 2f_{\text{NL}} [P_\Phi(\mathbf{k}_1) P_\Phi(\mathbf{k}_2) + \text{2 perms.}]$
- ▶ Solid inflation, Magnetic fields, Spin-2 particles during inflation
 - Endlich+’12
 - Shiraishi+’13
 - Arkani-Hamed&Maldacena’15
- ▶ The (small-scale) power spectrum becomes position-dependent&anisotropic
 - ▶ $P_m(\mathbf{k}_{\text{short}}|\mathbf{x}) = P_m(k_{\text{short}}) \left[1 + 4f_{\text{NL}}^{s=2} \sum_{ij} \psi_{ij}^{\text{long}}(\mathbf{x}) \hat{k}_{\text{short}}^i \hat{k}_{\text{short}}^j \right]$ with $\psi_{ij}^{\text{long}} \equiv \frac{3}{2} \left[\frac{\partial_i \partial_j}{\partial^2} - \frac{1}{3} \delta_{ij}^K \right] \phi^{\text{long}}$
 - ▶ cf. angular-independent case: $P_m(k_{\text{short}}|\mathbf{x}) = P_m(k_{\text{short}}) [1 + 4f_{\text{NL}} \phi^{\text{long}}(\mathbf{x})]$
 - ▶ $\hat{k}^i \hat{k}^j \delta_m \sim \frac{\partial^i \partial^j}{\partial^2} \delta_m \sim \partial^i \partial^j \phi$

Intrinsic alignments with angular-dependent PNG

Schmidt+’15, KA+’20

- ▶ Angular-dependent PNG \rightarrow small-scale tidal fluctuations are correlated

$$\blacktriangleright P_m(\mathbf{k}_{\text{short}} | \mathbf{x}) = P_m(k_{\text{short}}) \left[1 + 4f_{\text{NL}}^{s=2} \sum_{ij} \psi_{ij}^{\text{long}}(\mathbf{x}) \hat{k}_{\text{short}}^i \hat{k}_{\text{short}}^j \right] \text{ with } \psi_{ij}^{\text{long}} \equiv \frac{3}{2} \left[\frac{\partial_i \partial_j}{\partial^2} - \frac{1}{3} \delta_{ij}^K \right] \phi^{\text{long}}$$

$$\begin{aligned} \blacktriangleright \gamma_{ij}(\mathbf{k}_{\text{long}}) &= b_K K_{ij}(\mathbf{k}_{\text{long}}) + 4b_\psi f_{\text{NL}}^{s=2} \psi_{ij}(k_{\text{long}}) \\ &= [b_K + 6b_\psi f_{\text{NL}}^{s=2} \mathcal{M}^{-1}(k_{\text{long}})] K_{ij}(\mathbf{k}_{\text{long}}) \end{aligned}$$

$$\text{with } \delta_m(\mathbf{k}) = \mathcal{M}(k) \phi(\mathbf{k})$$

$$b_\psi = \frac{d\gamma_{ij}}{d(4f_{\text{NL}}^{s=2} \psi_{ij}^{\text{long}})}$$

$$\blacktriangleright \delta_g(\mathbf{k}_{\text{long}}) = b_1 \delta_m(\mathbf{k}_{\text{long}})$$

Angular-dependent PNG ICs & simulations

KA+'20a

► Generating initial condition with angular-dependent PNG

1. Generate random Gaussian fields $\phi(\mathbf{k})$ with the variance $P_\phi(k)$

2. Prepare auxiliary fields $\psi_{ij}(\mathbf{k}) = \frac{3}{2} \left[\hat{k}_i \hat{k}_j - \frac{1}{3} \delta_{ij}^K \right] \phi(\mathbf{k})$

3. FT to configuration space and construct non-Gaussian fields according to

$$\Phi(\mathbf{x}) = \phi(\mathbf{x}) + \frac{2}{3} f_{\text{NL}}^{s=2} \sum_{ij} \psi_{ij}^2(\mathbf{x}) \quad (\text{leading to } B_\Phi(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) = 2f_{\text{NL}}^{s=2} \left[\mathcal{L}_2(\hat{\mathbf{k}}_1 \cdot \hat{\mathbf{k}}_2) P_\phi(\mathbf{k}_1) P_\phi(\mathbf{k}_2) + \text{2 perms.} \right])$$

$$\text{cf. } \Phi(\mathbf{x}) = \phi(\mathbf{x}) + f_{\text{NL}}^{s=0} \phi^2(\mathbf{x}) \quad (\text{leading to } B_\Phi(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) = 2f_{\text{NL}}^{s=0} [P_\phi(\mathbf{k}_1) P_\phi(\mathbf{k}_2) + \text{2 perms.}])$$

4. FT back to Fourier space, then do the 2LPT

► Simulation: $L = 4.096 \text{ Gpc}/h$, $N_p = 2048^3$

► $(f_{\text{NL}}^{s=0}, f_{\text{NL}}^{s=2}) = (0,0), (500,0), (0,500)$

Scale-dependent bias in the IA power spectrum

KA+'20a

- ▶ There appears $1/k^2$ enhancement in galaxy/halo shape field on large-scales.

▶ $\gamma_{ij}(\mathbf{k}_{\text{long}}) = [b_K + 6b_\psi f_{\text{NL}}^{s=2} \mathcal{M}^{-1}(k_{\text{long}})] K_{ij}(\mathbf{k}_{\text{long}})$

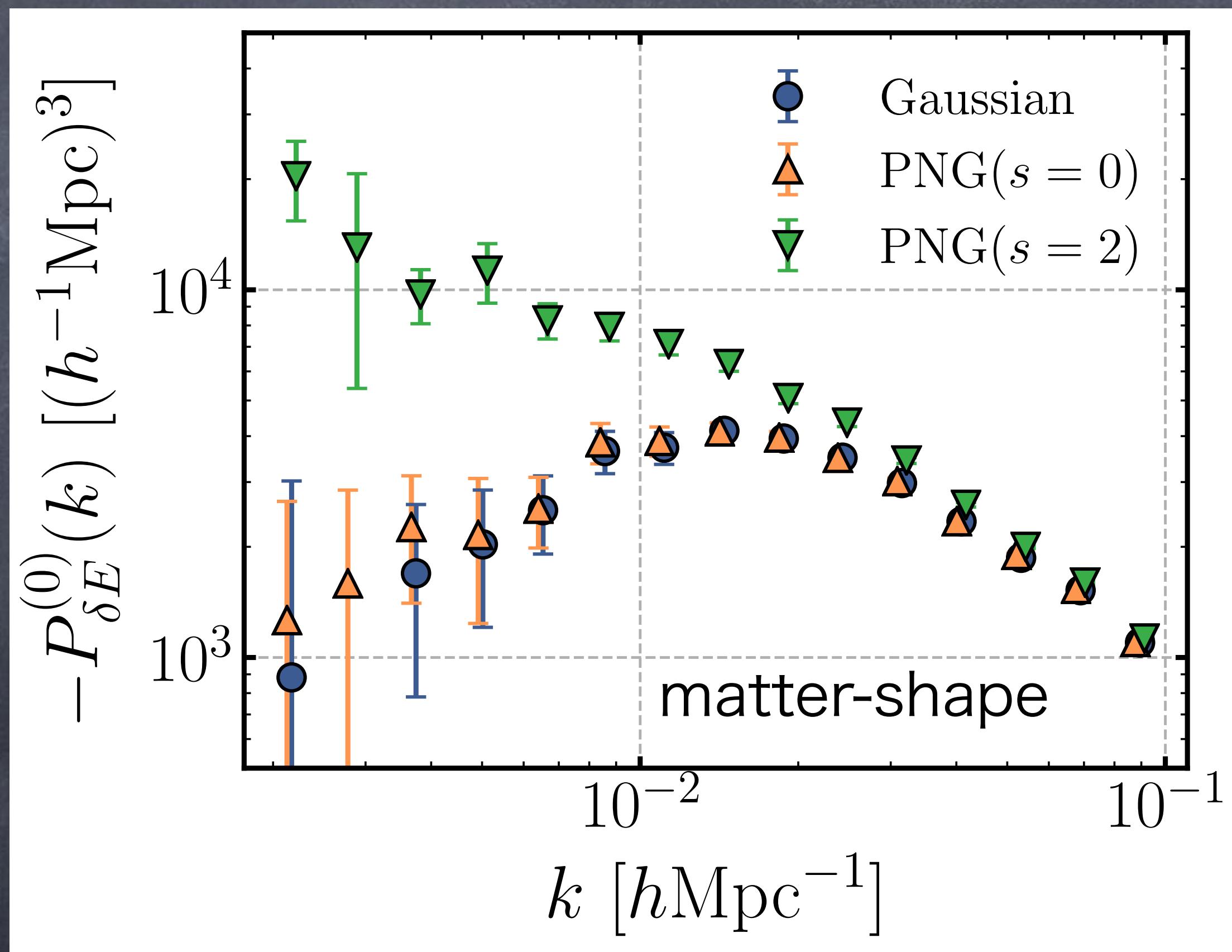
→ $P_{mE}(k) = [b_K + 6b_\psi f_{\text{NL}}^{s=2} \mathcal{M}^{-1}(k)] P_m(k)$

- ▶ $\mathcal{M}^{-1}(k) \propto 1/k^2$ on large-scales

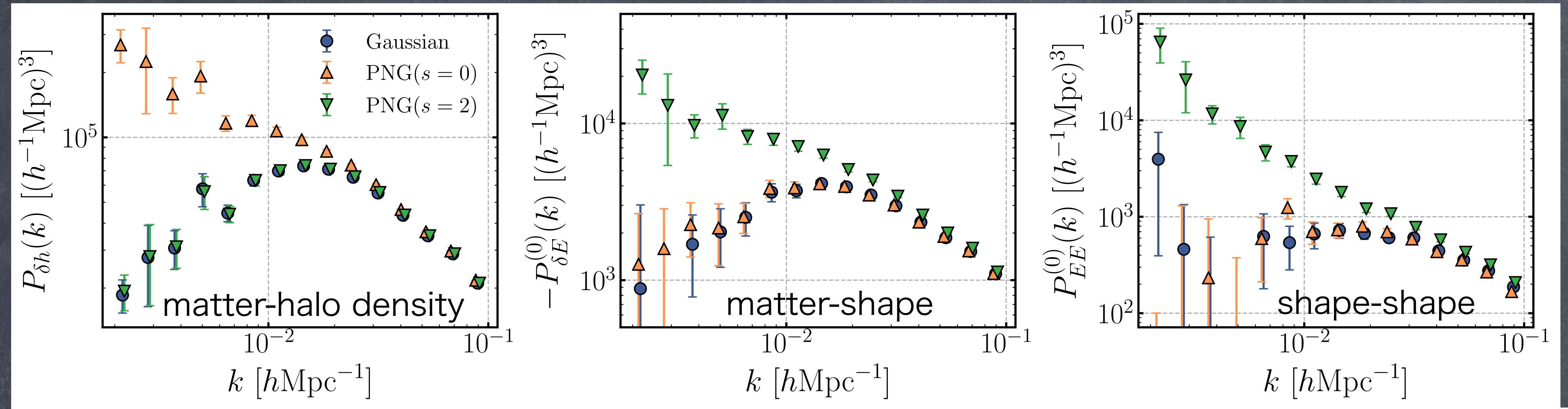
$\delta_m(\mathbf{k}) \sim k^2 \phi(\mathbf{k})$ from Poisson eq.

- ▶ The angular-independent PNG has no impact on shape field, i.e. P_{mE} & P_{EE}

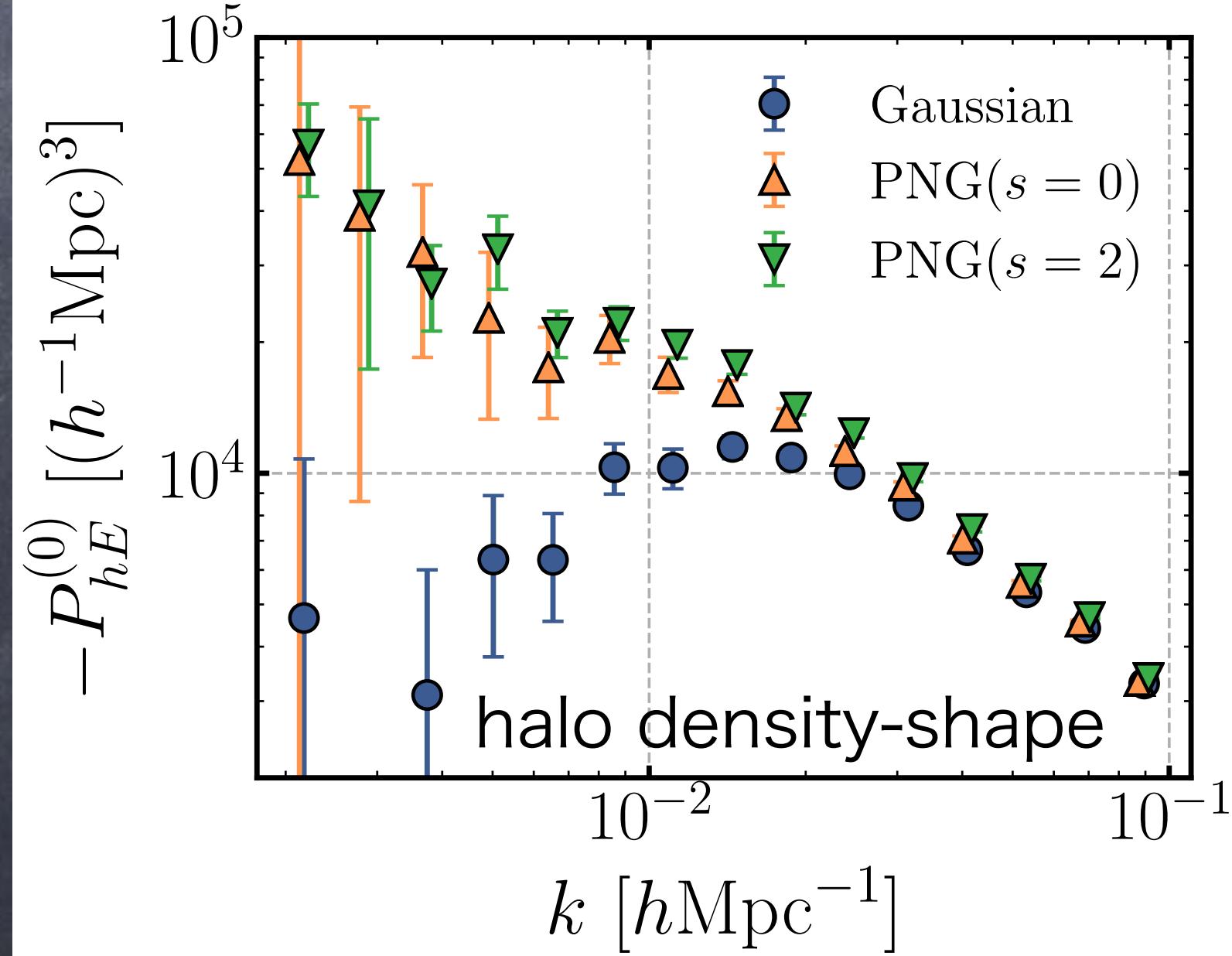
- ▶ The angular-dependent PNG has no impact on density field, i.e. P_{mh} & P_{hh}



Scale-dependent bias in various power spectrum



- ▶ The spin-0 and -2 observables only respond to the $s=0$ and $s=2$ PNGs, respectively
- ▶ The halo density-shape cross power spectrum P_{hE} is affected by both angular-independent-&-dependent PNGs
- ▶ P_{hh} responds to only the angular-independent PNG.



Summary of imprint of various PNGs

	# density tracer (spin-0 observable)	δ	shape tracer (spin-2 observable)	γ_{ij}
linear theory		$\delta_g = b_1 \delta_m$		$\gamma_{ij} = b_K K_{ij}$
s=0 PNG		$\Phi(\mathbf{x}) = \phi(\mathbf{x}) + f_{\text{NL}}^{s=0} \phi^2(\mathbf{x}), \quad P_m(\mathbf{k}; \mathbf{x}) = P_m(k) [1 + 4f_{\text{NL}}^{s=0} \phi^{\text{long}}(\mathbf{x})]$	scale-dependent bias	\times
s=2 PNG		$\Phi(\mathbf{x}) = \phi(\mathbf{x}) + \frac{2}{3} f_{\text{NL}}^{s=2} \sum_{ij} \psi_{ij}^2(\mathbf{x}), \quad P_m(\mathbf{k}; \mathbf{x}) = P_m(k) [1 + 4f_{\text{NL}}^{s=2} \psi_{ij}^{\text{long}}(\mathbf{x}) \hat{k}^i \hat{k}^j]$		scale-dependent bias
		$B_\Phi(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) = 2f_{\text{NL}}^{s=\ell} [\mathcal{L}_\ell(\hat{k}_1 \cdot \hat{k}_2) P_\phi(k_1) P_\phi(k_2) + 2 \text{ perms.}]$		

Forecast

- ▶ Using both P_{hh} & $P_{\text{h}E}$

- ▶ $V_{\text{survey}} = 69 \text{ (Gpc}/h)^3$

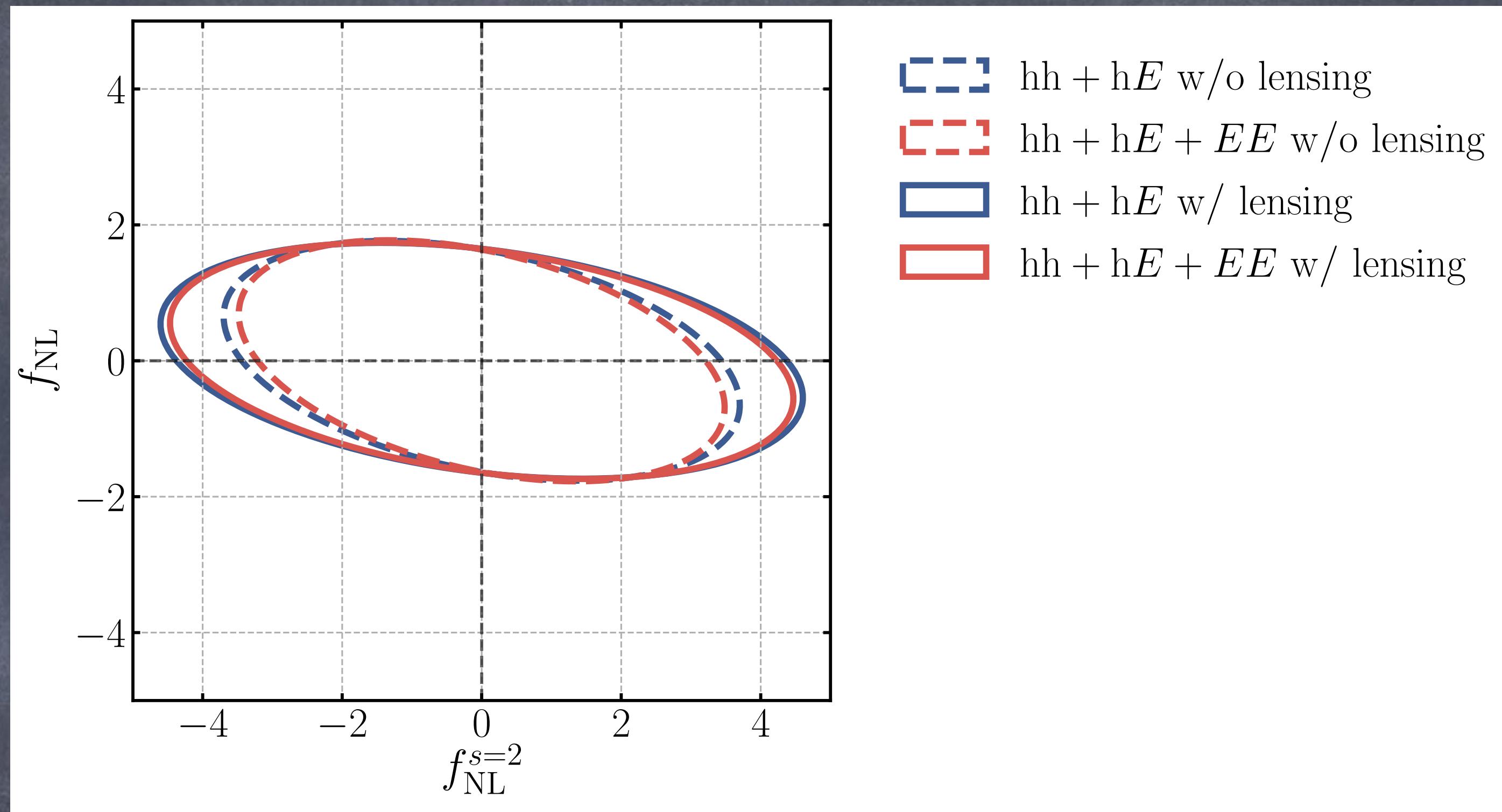
- ▶ $M_{\text{h}} > 10^{13} M_{\odot}/h, \bar{n}_{\text{h}} = 2.9 \times 10^{-4} \text{ (Mpc}/h)^3$

- ▶ The current CMB constraints:

$$\sigma(f_{\text{NL}}^{s=2}) \simeq 19$$

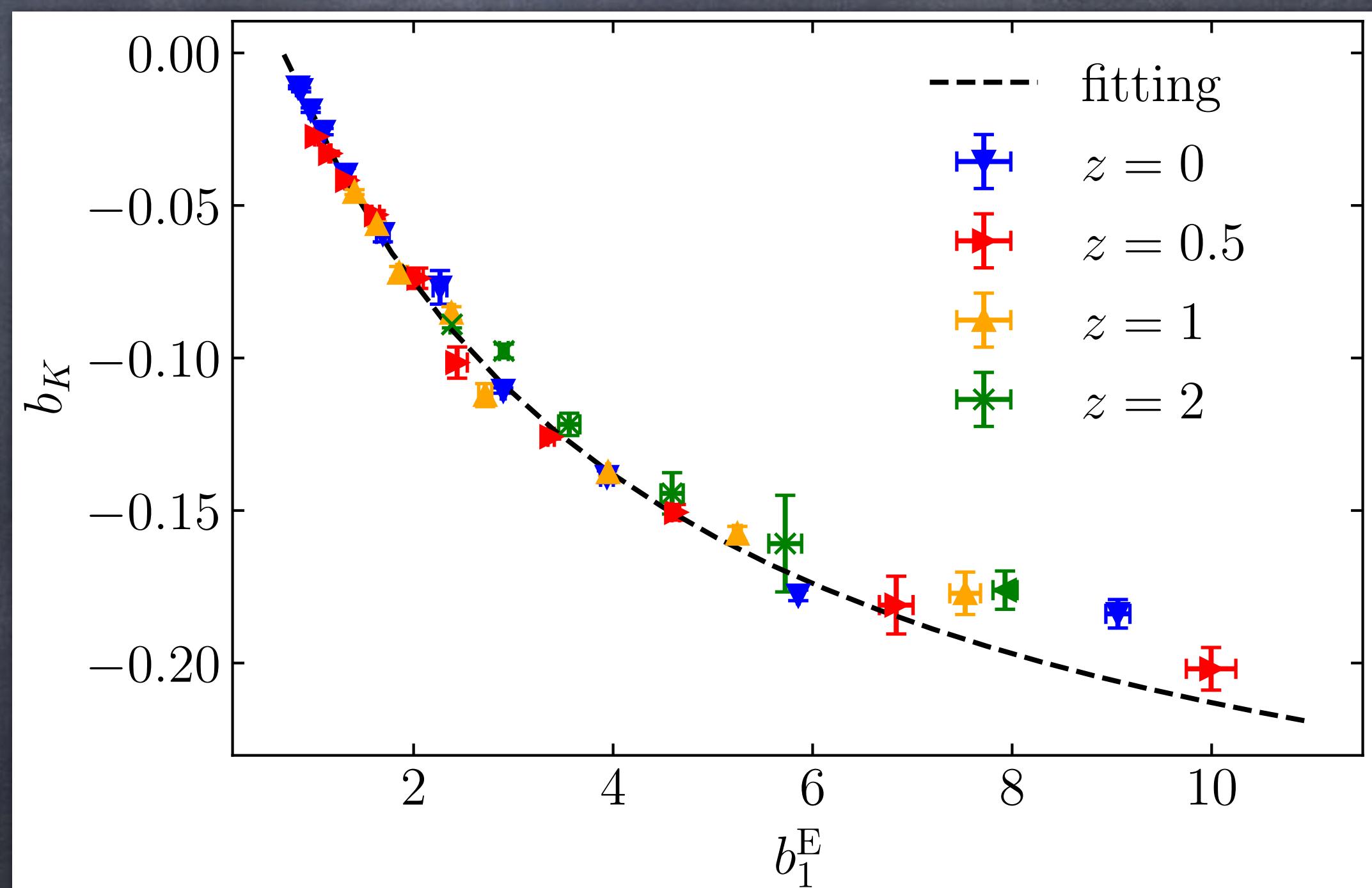
Planck2018

- ▶ We need both photo&spec surveys
- ▶ Projected (2D) shapes: photometric survey
- ▶ 3D position of galaxies: spectroscopic survey



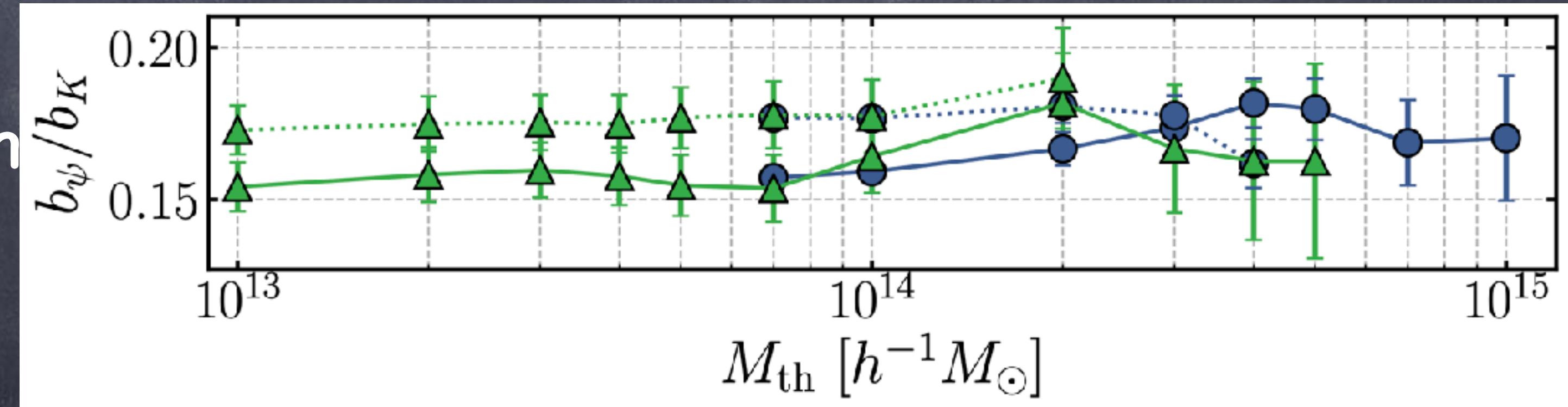
Challenge of IA cosmology

- ▶ Complete degeneracy between b_ψ and $f_{\text{NL}}^{s=2}$ $P_{\text{m}E}(k) = [b_K + 6b_\psi f_{\text{NL}}^{s=2} \mathcal{M}^{-1}(k)] P_{\text{m}}(k)$
- ▶ Density case: $P_{\text{mg}}(k) = [b_1 + 4b_\phi f_{\text{NL}} \mathcal{M}^{-1}(k)] P_{\text{m}}(k)$
- ▶ From peak theory: $b_\phi = 2\delta_{\text{cr}} b_1^{\text{L}} = 2\delta_{\text{cr}}(b_1^{\text{E}} - 1)$
- ▶ need to develop theory on shape bias
- ▶ Some hints:
 - ▶ universal relation between b_K and b_1
 - ▶ b_ψ/b_K looks constant



Challenge of IA cosmology

- ▶ Complete degeneracy between b_ψ and $f_{\text{NL}}^{s=2}$ $P_{\text{m}E}(k) = [b_K + 6b_\psi f_{\text{NL}}^{s=2} \mathcal{M}^{-1}(k)] P_{\text{m}}(k)$
- ▶ Density case: $P_{\text{mg}}(k) = [b_1 + 4b_\phi f_{\text{NL}} \mathcal{M}^{-1}(k)] P_{\text{m}}(k)$
- ▶ From peak theory: $b_\phi = 2\delta_{\text{cr}} b_1^L = 2\delta_{\text{cr}}(b_1^E - 1)$
- ▶ need to develop theory on shape bias
- ▶ Some hints:
 - ▶ universal relation between
 - ▶ b_ψ/b_K looks constant



Summary

- ▶ Intrinsic Alignment itself can be seen as new cosmological signal
- ▶ The angular-dependent PNG induces the scale-dependent bias in the IA power spectrum
- ▶ But no impact on number density tracers
- ▶ The angular-independent PNG has no impact on IA (while it affects number density tracers)
- ▶ Galaxy surveys (both photo&spec) can constrain $f_{\text{NL}}^{s=2}$ better than CMB
- ▶ Future: theory for the shape bias, bispectrum etc.